## Problem Set 2

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1. (10 points) Estimate the MSE of the model using the traditional approach. That is, fit the linear regression model using the entire dataset and calculate the mean squared error for the entire dataset. Present and discuss your results at a simple, high level.

```
# load libraries
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
      filter, lag
## The following objects are masked from 'package:base':
##
      intersect, setdiff, setequal, union
library(tidyverse)
## -- Attaching packages --
                     v purrr
## v ggplot2 3.2.1
                             0.3.3
                    v stringr 1.4.0
## v tibble 2.1.3
## v tidyr
          1.0.0
                     v forcats 0.4.0
## v readr
           1.3.1
## -- Conflicts -------
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                   masks stats::lag()
library(ISLR)
library(broom)
library(rsample)
library(rcfss)
library(yardstick)
## For binary classification, the first factor level is assumed to be the event.
```

## Set the global option `yardstick.event\_first` to `FALSE` to change this.

```
##
## Attaching package: 'yardstick'
## The following object is masked from 'package:readr':
##
##
       spec
library(skimr)
# import data
setwd("/Users/artemisyang/Dropbox/MACS33002 Introduction to Machine Learning/problem-set-2")
nes data <- read.csv(file="nes2008.csv")</pre>
# estimate MSE
lm1 <- lm(biden ~ female+age+educ+dem+rep, data=nes_data)</pre>
out <- summary(lm1)</pre>
(mse <- augment(lm1, newdata = nes_data) %>%
    mse(truth = biden, estimate = .fitted))
## # A tibble: 1 x 3
##
     .metric .estimator .estimate
     <chr>
             <chr>
                             <dbl>
##
## 1 mse
             standard
                              395.
```

The MSE of the fitted model is 395.2702. This is the average of the squared errors, which is commonly used to evaluate the performance of a model for regression problems. The smaller the MSE, the closer we are to finding the line of best fit.

- 2. (30 points) Calculate the test MSE of the model using the simple holdout validation approach.
- (5 points) Split the sample set into a training set (50%) and a holdout set (50%). Be sure to set your seed prior to this part of your code to guarantee reproducibility of results.

• (5 points) Fit the linear regression model using only the training observations.

```
lm2 <- lm(biden ~ female+age+educ+dem+rep, data=train)
summary(lm2)</pre>
```

```
##
## Call:
## lm(formula = biden ~ female + age + educ + dem + rep, data = train)
##
## Residuals:
## Min    1Q Median    3Q    Max
## -75.880 -11.950    1.929    11.899    46.124
```

```
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 58.68937
                          4.30323 13.638 < 2e-16 ***
## female
                4.41344
                           1.28889
                                    3.424 0.000644 ***
                           0.03858
                                   1.156 0.247980
                0.04460
## age
                           0.26831 -0.681 0.496251
## educ
               -0.18263
## dem
               13.63872
                           1.45353
                                    9.383 < 2e-16 ***
## rep
              -18.76842
                           1.78349 -10.523 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 19.11 on 898 degrees of freedom
## Multiple R-squared: 0.3085, Adjusted R-squared: 0.3046
## F-statistic: 80.12 on 5 and 898 DF, p-value: < 2.2e-16
```

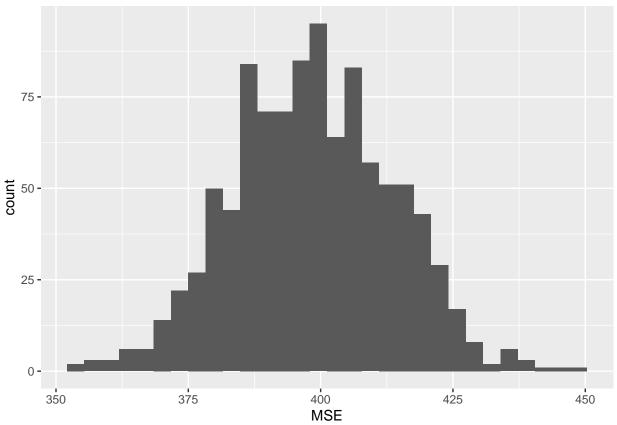
• (10 points) Calculate the MSE using only the test set observations.

- (10 points) How does this value compare to the training MSE from question 1? Present numeric comparison and discuss a bit. The MSE of the test set using the model fitted from the training set is 431.6, which is larger than the MSE from question 1. This means that the model does not fit the test observations very well.
  - 3. (30 points) Repeat the simple validation set approach from the previous question 1000 times, using 1000 different splits of the observations into a training set and a test/validation set. Visualize your results as a sampling distribution ( hint: think histogram or density plots). Comment on the results obtained.

```
if (x == 1001){
    break
}

# graph the distribution of MSE values
ggplot(sv_mse) + geom_histogram(aes(x = MSE))
```

## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



The distribution of the 1000 MSEs follows a normal distribution, with is consistent with the random sampling process. The median is about 400, which is close to the MSE obtained from question 1. However, we can see that the MSE from question 2 is beyond 425, which is at the far right side of the distribution. This tells us that cross validation is very important in ensuring the accuracy of a model, as there is too much randomness using just one split.

4. (30 points) Compare the estimated parameters and standard errors from the original model in question 1 (the model estimated using all of the available data) to parameters and standard errors estimated using the bootstrap (B = 1000). Comparison should include, at a minimum, both numeric output as well as discussion on differences, similarities, etc. Talk also about the conceptual use and impact of bootstrapping.

```
# parameter estimates and standard errors from question 1
lm <- lm(biden ~ female+age+educ+dem+rep, data=nes_data)
tidy(lm)</pre>
```

```
## # A tibble: 6 x 5
##
     term
                 estimate std.error statistic p.value
                                         <dbl>
##
     <chr>>
                    <dbl>
                               <dbl>
## 1 (Intercept) 58.8
                              3.12
                                         18.8 2.69e-72
## 2 female
                   4.10
                              0.948
                                          4.33 1.59e- 5
                   0.0483
                              0.0282
                                          1.71 8.77e- 2
## 3 age
## 4 educ
                  -0.345
                              0.195
                                         -1.77 7.64e- 2
## 5 dem
                  15.4
                              1.07
                                         14.4 8.14e-45
## 6 rep
                 -15.8
                              1.31
                                        -12.1 2.16e-32
```

```
## # A tibble: 6 x 3
##
     term
                  .estimate
##
     <chr>>
                      <dbl>
                            <dbl>
## 1 (Intercept)
                    58.9
                            2.97
## 2 age
                     0.0468 0.0297
## 3 dem
                    15.4
                            1.03
## 4 educ
                    -0.347
                            0.187
## 5 female
                     4.12
                            0.920
## 6 rep
                   -15.8
                            1.41
```

The estimated parameters from the original model are generally the same as from the bootstrapped estimates. Other than for female, bootstrapped standard errors for the other 4 variables are slightly larger than original standard errors. This is because bootstrapped estimates do not rely on any distributional assumptions, whereas the traditional estimates do. Conceptually, we would prefer to use bootstrap method when our data cannot meet the distributional assumptions, where the bootstrap estimator will give more accurate results. Another possible situation to use bootstrap is when our data is not large enough. In this case, bootstrap can potentially increase the robustness of our estimate. Also, even if the distributional assumptions are met and the data is large, we can still use bootstrap as a robustness check, as the bootstrap method is not biased by distributional assumptions.