

Expression Trees

XML Serialisation & Deserialisation, Evaluation, Postfix

This assignment will give you practical experience with serialisation topics and lambda-based expression trees.

For a general view on **.NET Serialization**, see this doc:

<https://docs.microsoft.com/en-us/dotnet/standard/serialization/>

> **Serialization** is the process of converting the state of an object into a form that can be persisted or transported. The complement of serialization is **deserialization**, which converts a stream into an object. Together, these processes allow data to be **stored** and **transferred**.

These topics are very important for distributed applications. Here we use **XML** serialisation. The **appendix** shows basic code for basic serialisation and deserialization.

Linq expression trees are essential for the versatility of **Linq**, allowing the **targeted translation** of **higher-order functions involving lambda expressions**, to a wide variety of formats, e.g. to methods, to SQL, or to URL.

These trees have been briefly discussed in the **lectures**. For their **detailed** structure, see these docs:

<https://docs.microsoft.com/en-us/dotnet/api/system.linq.expressions.expression?view=netframework-4.8>

<https://docs.microsoft.com/en-us/dotnet/api/system.linq.expressions.lambdaexpression?view=netframework-4.8>

These are the latest versions, but for our purposes there are no critical differences.

Linqpad is also great in **visualising** the structure of expression trees. The **Appendix** shows a Linqpad dump of such a tree structure.

This assignment has a required part (**A#6**) and a bonus part (**A#6B**), both in **C#**. There will be an additional bonus part for a somehow similar **F#** version (**A#6C**), with a separate handout and other time limits.

Each part carries the same weight: **1 course mark**, thus the total can be 2 marks (including the C# bonus) or 3 marks (also including the F# bonus).

A#6 "what to do" description

At each run, your program reads a text from stdin, representing one single XML serialisation of a simple lambda expression of this format:

Expression<Func<int, int, ... int>>

Our simple lambdas use only int parameters, int constants, and the four basic int binary operators (+, -, *, /). No free variables, no closures, nothing else.

Your task is to recreate the original lambda expression and evaluate it in one of the following ways, and print the result on one single line:

- If the lambda has no parameters, then just evaluate it.
- If the lambda has one parameter, then evaluate it with the argument (1).
- If the lambda has two parameters, then evaluate it with the arguments (1, 2).
- If the lambda has three parameters, then evaluate it with the arguments (1,2,3).
- Otherwise, print a question mark (?), w/o any surrounding spaces.

A#6B "what to do" description

Your program reads the same XML serialisations as above (**A#6**)

However, the output must be an equivalent postfix (aka reverse Polish) expression for the tree body (the body is the expression after the equal sign).

The postfix notation must only consist of: parameter names (e.g. x), int constants (e.g. 2, -3), operator symbols (+, -, *, /) - not the enumeration names appearing in the tree, Add, Subtract, Multiply, Divide - separated by single spaces and nothing else.

Caveat

Standard Linq expressions trees cannot be directly serialised and deserialised. There are several reasons for this, but we do not go into details.

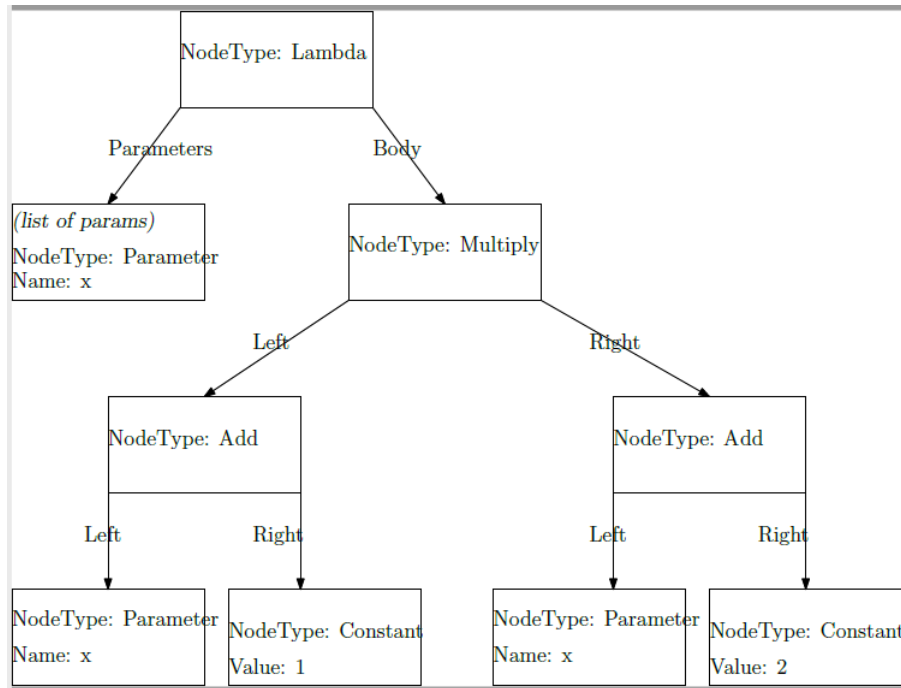
The workaround is to convert Linq expressions trees to an isomorphic third party format, called MetaLinq editable expressions, that allows serialisation, deserialisation, and editing (under some constraints). We use a library called MetaLinq.dll, which we have recompiled as MetaLinqUoA.dll, to match the software that we currently use.

This MetaLinqUoA.dll library will be given to you in the A#6 samples folder, and is also present on the automaker, so you'll be able to use it w/o worries.

An **A#6** scenario (and how to do hints). Assume that, before compiling and running your programs, the **automarker** (AM) starts with this lambda:

Expression<Func<int, int>> **lambda1** = x => (x + 1) * (x + 2);

It is useful to consider its **abstract syntax tree** (AST), here annotated with attributes close to those used by the **Linq** (and **MetaLinq**) expression trees:



Then, AM will convert this to an isomorphic **MetaLinq** editable expression tree, that will be serialised and sent to **stdin**. All this is done by AM, w/o your help.

Your task starts now, by reading the XML sent to your **stdin**:

- **deserialise** the XML into a **MetaLinq** editable expression (see **Appendix**),
- **convert** this to a standard **Linq** expression,
- **compile** this to method, and
- **invoke** this with the right number of parameters (you need to find this)
- **print** the result

Recall that, when invoking this method, the 1st parameter takes value 1, the 2nd value 3, the 3rd value 3. In our scenario, print one line with the number **6**, b/c:

lambda1 (1) = (1 + 1) * (1 + 2) = 6

You could, if you wish, obtain the result directly from parsing and interpreting the XML text, w/o deserialisation etc – there is no penalty for this, but this could be a longer way. Up to you.

The **Appendix** show a (bit simplified) XML serialisation of the **MetaLinq** editable expression created from our **lambda1**.

A#6B scenario (and how to do hints). Consider the same lambda as above:

```
Expression<Func<int, int>> lambda1 = x => (x + 1) * (x + 2);
```

You will get the same XML text and, by **visiting** the highlighted **body** of the expression tree in **postfix** order (see 105 or a good basic book on algorithms), you can write the following output line (equivalent reverse Polish):

```
x 1 + x 2 + *
```

You can obtain this postfix notation by other means, but these alternatives may prove longer. There is no penalty though, up to you again.

Testing before submission

Besides the given **lambda1**, please test your programs **extensively**, **locally**, with many other lambda expressions of the expected type:

```
Expression<Func<int, int, ... int>>
```

The **assignment support folder**, **03-A6-Samples**, contains code for both serialisation and deserialisation, so you can serialise yourself as many other test lambdas as necessary for a reasonable test coverage. You can also adapt and reuse the testing harness (**batch**) given for A#5.

Programs:

(A#5) a **C#** solution (**required**).

(A#5b) a **C#** solution (**optionally, bonus**).

Essentially, each program must be totally contained in one single file and use only standard libraries extant in the labs, plus **MetaLinqUoA.dll**

These programs will run on **automarker**:

- The input xml must be read from **stdin**, i.e. **Console.In** in C#.
- The output must be written to **stdout**, i.e. **Console[.Out]** in C#.

Submission

Please submit to the **automarker**

(<https://www.automarker.cs.auckland.ac.nz/student.php>):

APPENDIX

Visualise the actual **Linq expression tree** of our sample **lambda1** - Linqpad dump!

Top, **Parameters**, and **Body** / **Left** :

lambda1

^ Expression<Func<Int32,Int32>>																																																																																																													
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Left	<div>^ SimpleBinaryExpression</div>																																																																																																												

Body / Right, bottom :

		NodeType	Add
		Type	typeof(Int32)
	Left	SimpleBinaryExpression	
		(x + 1)	
		CanReduce	False
		Right	ConstantExpression
			1
		CanReduce	False
		Type	typeof(Int32)
		NodeType	Constant
		Value	1
		Left	PrimitiveParameterExpression<Int32>
			x
		CanReduce	False
		Type	typeof(Int32)
		NodeType	Parameter
		Name	x
IsByRef	False		
	Method	<i>null</i>	
	Conversion	<i>null</i>	
	IsLifted	False	
	IsLiftedToNull	False	
	NodeType	Add	
	Type	typeof(Int32)	
	Method	<i>null</i>	
	Conversion	<i>null</i>	
	IsLifted	False	
	IsLiftedToNull	False	
	NodeType	Multiply	
	Type	typeof(Int32)	
ReturnType	typeof(Int32)		
TailCall	False		

Method

null

Conversion

null

IsLifted

False

IsLiftedToNull

False

NodeType

Add

Type

[typeof\(Int32\)](#)

The next page shows a (bit simplified) version of the **XML serialisation** of the equivalent **MetaLinq** editable expression.

```
<?xml version="1.0" encoding="utf-16"?>
<EditableLambdaExpression xmlns:xsi="..." xmlns:xsd="...">
  <NodeType>Lambda</NodeType>
  <Parameters>
    <EditableExpression xsi:type="EditableParameterExpression">
      <NodeType>Parameter</NodeType>
      <Name>x</Name>
    </EditableExpression>
    <EditableExpression xsi:type="EditableParameterExpression">
      <NodeType>Parameter</NodeType>
      <Name>y</Name>
    </EditableExpression>
  </Parameters>
  <Body xsi:type="EditableBinaryExpression">
    <NodeType>Multiply</NodeType>
    <Left xsi:type="EditableBinaryExpression">
      <NodeType>Add</NodeType>
      <Left xsi:type="EditableParameterExpression">
        <NodeType>Parameter</NodeType>
        <Name>x</Name>
      </Left>
      <Right xsi:type="EditableConstantExpression">
        <NodeType>Constant</NodeType>
        <Value xsi:type="xsd:int">3</Value>
      </Right>
    </Left>
    <Right xsi:type="EditableBinaryExpression">
      <NodeType>Add</NodeType>
      <Left xsi:type="EditableParameterExpression">
        <NodeType>Parameter</NodeType>
        <Name>y</Name>
      </Left>
      <Right xsi:type="EditableConstantExpression">
        <NodeType>Constant</NodeType>
        <Value xsi:type="xsd:int">7</Value>
      </Right>
    </Right>
  </Body>
</EditableLambdaExpression>
```

Sample serialisation code, using **MetaLinq** as intermediary:

```
Expression<Func<int, int>> lambda1 = x => (x + 1) * (x + 2);  
var exp = lambda1 as Expression  
var metexp =  
    MetaLinq.EditableExpression.CreateEditableExpression (exp);  
  
var serializer = new XmlSerializer (typeof(EditableLambdaExpression));  
var sw = new StringWriter ();  
serializer.Serialize (sw, metexp);  
var xml = sw.ToString ();
```

Sample deserialisation code, using **MetaLinq** as intermediary:

```
var sr = new StringReader (xml);  
var serializer = new XmlSerializer (typeof(EditableLambdaExpression));  
var metexp = serializer.Deserialize (sr) as EditableLambdaExpression;  
var exp = metexp.ToExpression () as LambdaExpression;  
if (exp is Expression<Func<int, int>>) ...
```

The lecture handouts show **how to internally compile and then evaluate** an expression tree.

To **compile with CSC**, include the external **MetaLinqUoA.dll**, here assumed in the current folder (source file name irrelevant):

```
csc -r:MetaLinqUoA.dll jbon007.cs
```

Your sources will probably need to reference these namespaces:

```
System; System.IO; System.Linq;  
System.Linq.Expressions; System.Xml.Serialization;  
MetaLinq.Expressions;
```