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1 import numpy as np
2 import matplotlib.pyplot as plt
3 from scipy.interpolate import interp1d
4 from scipy.interpolate import make_interp_spline
5
6 # Function definitions remain the same
7
8 def myFactorial(n):
9     factorialValue = 1
10    for i in range(1, n+1):
11        factorialValue = i * factorialValue
12    return factorialValue
13
14 def binomialCoef(f, b):
15     return myFactorial(f+b) / (myFactorial(f) * myFactorial(b))
16
17 def likelihood(m, f, b):
18     bfResult = binomialCoef(f, b)
19     for x in range(len(likelihoodArr)):
20         likelihoodArr[x] = bfResult * (m[x] ** f) * ((1 - m[x]) ** b)
21     return likelihoodArr
22
23 def posterior(p, pT):
24     for x in range(len(p)):
25         posteriorProb[x] = p[x] / pT
26     return posteriorProb
27
28 # Model and prior initialization
29 model = np.arange(0.0, 1.1, 0.1) # Model values: probability of success in each jump
30
31 mound_shaped = np.array([0.05, 0.10, 0.16, 0.19, 0.18, 0.15, 0.09, 0.05, 0.2, 0.01, 0.00]) #mound-shaped
32 bimodal = np.array([0.8, 0.7, 0.3, 0.05, 0.05, 0.05, 0.05, 0.05, 0.3, 0.5, 0.8]) #bimodal
33 right_skewed = np.array([0.8, 0.6, 0.4, 0.3, 0.2, 0.1, 0.05, 0.01, 0.001, 0.001, 0.0]) #right-skewed
34 uniform = np.full([11], 0.5) #uniform prior
35
36 priorProb = [mound_shaped,
37              bimodal,
38              right_skewed,
39              uniform]
40 linespecs = ['--', ':', '-']
41

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41
42 # Initialize arrays for likelihood and posterior
43 likelihoodArr = np.zeros((len(model)))
44 posteriorProb = np.zeros((len(model)))
45
46 #senarios for 3/5, 15/25, and 75/125
47 floor = [3, 15, 75]
48 back = [2, 10, 50]
49
50 figure, axis = plt.subplots(2, 2)
51
52 # Mound Shaped
53 for i in range(3):
54     # Cubic interpolation for prior
55     xArr = np.array([x for x in range(len(model))])
56     X_Y_Spline = interp1d(xArr, priorProb[0], kind='cubic')
57     priorProbX = np.linspace(xArr.min(), xArr.max(), 1000)
58     priorProbY = X_Y_Spline(priorProbX)
59
60     axis[0, 0].plot(priorProbX, priorProbY, color = 'r')
61
62     likelihoodArr = likelihood(model, floor[i], back[i])
63     probTemp = priorProb[0] * likelihoodArr
64     probTempSum = sum(probTemp)
65     posteriorProb = posterior(probTemp, probTempSum)
66
67     # Spline interpolation for posterior
68     X_Y_Spline2 = make_interp_spline(xArr, posteriorProb)
69     posteriorProbY = X_Y_Spline2(priorProbX)
70     axis[0, 0].plot(priorProbX, posteriorProbY, color= 'b', ls = linespecs[i])
71
72
73 axis[0, 0].set_title("Mound Shaped prior distribution")
74
75 # Bimodal
76 for i in range(3):
77     # Cubic interpolation for prior
78     xArr = np.array([x for x in range(len(model))])
79     X_Y_Spline = interp1d(xArr, priorProb[1], kind='cubic')
80     priorProbX = np.linspace(xArr.min(), xArr.max(), 1000)
81     priorProbY = X_Y_Spline(priorProbX)

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83     axis[0, 1].plot(priorProbX, priorProbY, color = 'r')
84
85     likelihoodArr = likelihood(model, floor[i], back[i])
86     probTemp = priorProb[1] * likelihoodArr
87     probTempSum = sum(probTemp)
88     posteriorProb = posterior(probTemp, probTempSum)
89
90     # Spline interpolation for posterior
91     X_Y_Spline2 = make_interp_spline(xArr, posteriorProb)
92     posteriorProbY = X_Y_Spline2(priorProbX)
93     axis[0, 1].plot(priorProbX, posteriorProbY, color= 'b', ls = linespecs[i])
94
95     axis[0, 1].set_title("Bimodal prior distribution")
96
97     # Right-skewed
98     for i in range(3):
99         # Cubic interpolation for prior
100         xArr = np.array([x for x in range(len(model))])
101         X_Y_Spline = interp1d(xArr, priorProb[2], kind='cubic')
102         priorProbX = np.linspace(xArr.min(), xArr.max(), 1000)
103         priorProbY = X_Y_Spline(priorProbX)
104
105         axis[1, 0].plot(priorProbX, priorProbY, color = 'r')
106
107         likelihoodArr = likelihood(model, floor[i], back[i])
108         probTemp = priorProb[2] * likelihoodArr
109         probTempSum = sum(probTemp)
110         posteriorProb = posterior(probTemp, probTempSum)
111
112         # Spline interpolation for posterior
113         X_Y_Spline2 = make_interp_spline(xArr, posteriorProb)
114         posteriorProbY = X_Y_Spline2(priorProbX)
115         axis[1, 0].plot(priorProbX, posteriorProbY, color= 'b', ls = linespecs[i])
116
117     axis[1, 0].set_title("Right-skewed prior distribution")

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118
119     # Uniform
120     for i in range(3):
121         # Cubic interpolation for prior
122         xArr = np.array([x for x in range(len(model))])
123         X_Y_Spline = interp1d(xArr, priorProb[3], kind='cubic')
124         priorProbX = np.linspace(xArr.min(), xArr.max(), 1000)
125         priorProbY = X_Y_Spline(priorProbX)
126
127         # to avoid excess labels in legend
128         if i == 0:
129             axis[1, 1].plot(priorProbX, priorProbY, color = 'r', label='Prior')
130         else:
131             axis[1, 1].plot(priorProbX, priorProbY, color = 'r')
132         # Likelihood and posterior
133         likelihoodArr = likelihood(model, floor[i], back[i])
134         probTemp = priorProb[3] * likelihoodArr
135         probTempSum = sum(probTemp)
136         posteriorProb = posterior(probTemp, probTempSum)
137
138         # Spline interpolation for posterior
139         X_Y_Spline2 = make_interp_spline(xArr, posteriorProb)
140         posteriorProbY = X_Y_Spline2(priorProbX)
141         axis[1, 1].plot(priorProbX, posteriorProbY, color= 'b', ls = linespecs[i], label=f'Posterior, {floor[i]}/{floor[i]+back[i]} data')
142
143     axis[1, 1].set_title("Uniform prior distribution")
144
145     plt.legend()
146     plt.show()
147

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