

Lagrangian

$$\begin{aligned}
\mathcal{L} = & \frac{m\omega_y}{2} (-r_1^2(t) + r_2^2(t)) \frac{d}{dt}q(t) + \frac{m}{8} (r_1^2(t) + r_2^2(t)) \frac{d}{dt}q(t)^2 + \frac{m}{2} \frac{d}{dt}r_1(t)^2 \\
& + \frac{m}{2} \frac{d}{dt}r_2(t)^2 + \omega_x \left(\frac{\omega_x}{2} \left(mr_1^2(t) \sin^2 \left(\frac{1}{2}q(t) \right) + mr_2^2(t) \sin^2 \left(\frac{1}{2}q(t) \right) \right) \right. \\
& \quad \left. + \frac{\omega_z}{2} \left(-mr_1^2(t) \sin \left(\frac{1}{2}q(t) \right) \cos \left(\frac{1}{2}q(t) \right) \right. \right. \\
& \quad \left. \left. + mr_2^2(t) \sin \left(\frac{1}{2}q(t) \right) \cos \left(\frac{1}{2}q(t) \right) \right) \right) \\
& + \frac{\omega_y^2}{2} \left(m \left(r_1^2(t) \sin^2 \left(\frac{1}{2}q(t) \right) + r_1^2(t) \cos^2 \left(\frac{1}{2}q(t) \right) \right) \right. \\
& \quad \left. + m \left(r_2^2(t) \sin^2 \left(\frac{1}{2}q(t) \right) + r_2^2(t) \cos^2 \left(\frac{1}{2}q(t) \right) \right) \right) \\
& + \omega_z \left(\frac{\omega_x}{2} \left(-mr_1^2(t) \sin \left(\frac{1}{2}q(t) \right) \cos \left(\frac{1}{2}q(t) \right) \right. \right. \\
& \quad \left. \left. + mr_2^2(t) \sin \left(\frac{1}{2}q(t) \right) \cos \left(\frac{1}{2}q(t) \right) \right) \right. \\
& \quad \left. + \frac{\omega_z}{2} \left(mr_1^2(t) \cos^2 \left(\frac{1}{2}q(t) \right) + mr_2^2(t) \cos^2 \left(\frac{1}{2}q(t) \right) \right) \right)
\end{aligned} \tag{1}$$

Hamiltonian

$$\begin{aligned}
\mathcal{H} = & J_x \left(\frac{J_x}{2} \left(\frac{(-r_1^2(t) + r_2^2(t))^2 \sin^2(q(t))}{8m(r_1^2(t) + r_2^2(t))(\cos(q(t)) + 1)r_1^2(t)r_2^2(t)\sin^4(\frac{1}{2}q(t))} \right. \right. \\
& \quad \left. \left. + \frac{2}{m(r_1^2(t) + r_2^2(t))(-\cos(q(t)) + 1)} \right) - \frac{J_z(-r_1^2(t) + r_2^2(t))}{4mr_1^2(t)r_2^2(t)\sin(q(t))} \right) \\
& + \frac{J_y^2(r_1^2(t) + r_2^2(t))}{2m(-(r_1^2(t) - r_2^2(t))^2 + (r_1^2(t) + r_2^2(t))^2)} + \frac{J_y p(t)}{2mr_2^2(t)} - \frac{J_y p(t)}{2mr_1^2(t)} \\
& + J_z \left(-\frac{J_x(-r_1^2(t) + r_2^2(t))}{4mr_1^2(t)r_2^2(t)\sin(q(t))} + \frac{J_z(r_1^2(t) + r_2^2(t))}{4m(\cos(q(t)) + 1)r_1^2(t)r_2^2(t)} \right) \\
& + \frac{p^2(t)}{2mr_2^2(t)} + \frac{p^2(t)}{2mr_1^2(t)} + \frac{p_1^2(t)}{2m} + \frac{p_2^2(t)}{2m}
\end{aligned} \tag{2}$$