

# Classical trajectory simulation of the CO<sub>2</sub> collision-induced band profile in the far IR spectral range

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## Introduction

There is a growing demand to improve existing methods of collision-induced absorption (CIA) spectra simulation [1]. From the one hand, the impetus to refine presently available theories is due to anticipation of future observations concerning a multitude of exoplanetary atmospheres. From the other hand, there is a remarkable progress in computer facilities that opens access to unprecedented timescale and accuracy of computations.

The use of computationally heavy pure quantum [2] and molecular dynamics [3, 4] methods of CIA simulation is still infrequent and can hardly satisfy near future practical requirements in terms of variety of molecular constituents and range of temperature. In contrast, the method based on consideration of classical scattering trajectories seems to have good perspective for extensive CIA simulation. Recent analysis [5] of the classical scattering dynamics in laboratory frame of reference permitted satisfactory simulation of the CO<sub>2</sub>–Rg (Rg = Ar, Xe) rototranslational CIA band profiles.

An alternative trajectory based approach is being developed in our research group. Salient features and some preliminary results of it were recently reported elsewhere [6]. Excellent agreement was demonstrated among our calculated trajectory based rototranslational profiles in N<sub>2</sub>–N<sub>2</sub> and those computed quantum mechanically in [2] or obtained experimentally (see [1] and references therein). We use body-fixed frame in which classical dynamics of a collision as well as quantum chemical electronic energy (PES) and induced dipole (IDS) surfaces are rigorously examined. Present paper shows results concerning CO<sub>2</sub>–Ar and CO<sub>2</sub>–CO<sub>2</sub> systems. We discuss both strengths and weaknesses of our trajectory based approach.

## Main features of calculation

Absorption coefficient  $\alpha$  normalized to the product of densities is known to be written as

$$\frac{\alpha(\nu, T)}{\rho_1 \rho_2} = \frac{(2\pi)^2 N_L^2}{3\hbar} \nu \left[ 1 - \exp\left(-\frac{h\nu}{k_B T}\right) \right] V J(\nu, T), \quad (1)$$

where spectral function  $J(\nu, T)$  can be found as Fourier transform of the dipole autocorrelation function

$$J(\nu, T) = \frac{1}{4\pi\epsilon_0 2\pi} \int_{-\infty}^{+\infty} \langle \mathbf{d}(0) \cdot \mathbf{d}(t) \rangle e^{-2\pi i \nu t} dt. \quad (2)$$

As a result of change of variables that greatly improves the convergence properties of the integral for the free states, we obtained the following expression for spectral function

$$J(\nu, T) = \frac{1}{4\pi\epsilon_0 2\pi\Gamma_0} \int \cdots \int \frac{p_R}{\mu} dp_R \exp\left(-\frac{H}{k_B T}\right) d\mathbf{q}' d\mathbf{p}' \left| \int_{-\infty}^{+\infty} \mathbf{d}(t; \mathbf{q}', p_R, \mathbf{p}') e^{-2\pi i \nu t} dt \right|^2. \quad (3)$$

Here  $\mu$  is the reduced mass of a molecule pair,  $\Gamma_0 = \int \cdots \int \exp\left(-\frac{H}{k_B T}\right) d\mathbf{q} d\mathbf{p}$  is the normalization factor, differential  $d\mathbf{q}'$  only angular degrees of freedom of the each monomer and the complex as whole.

## Spectral moments

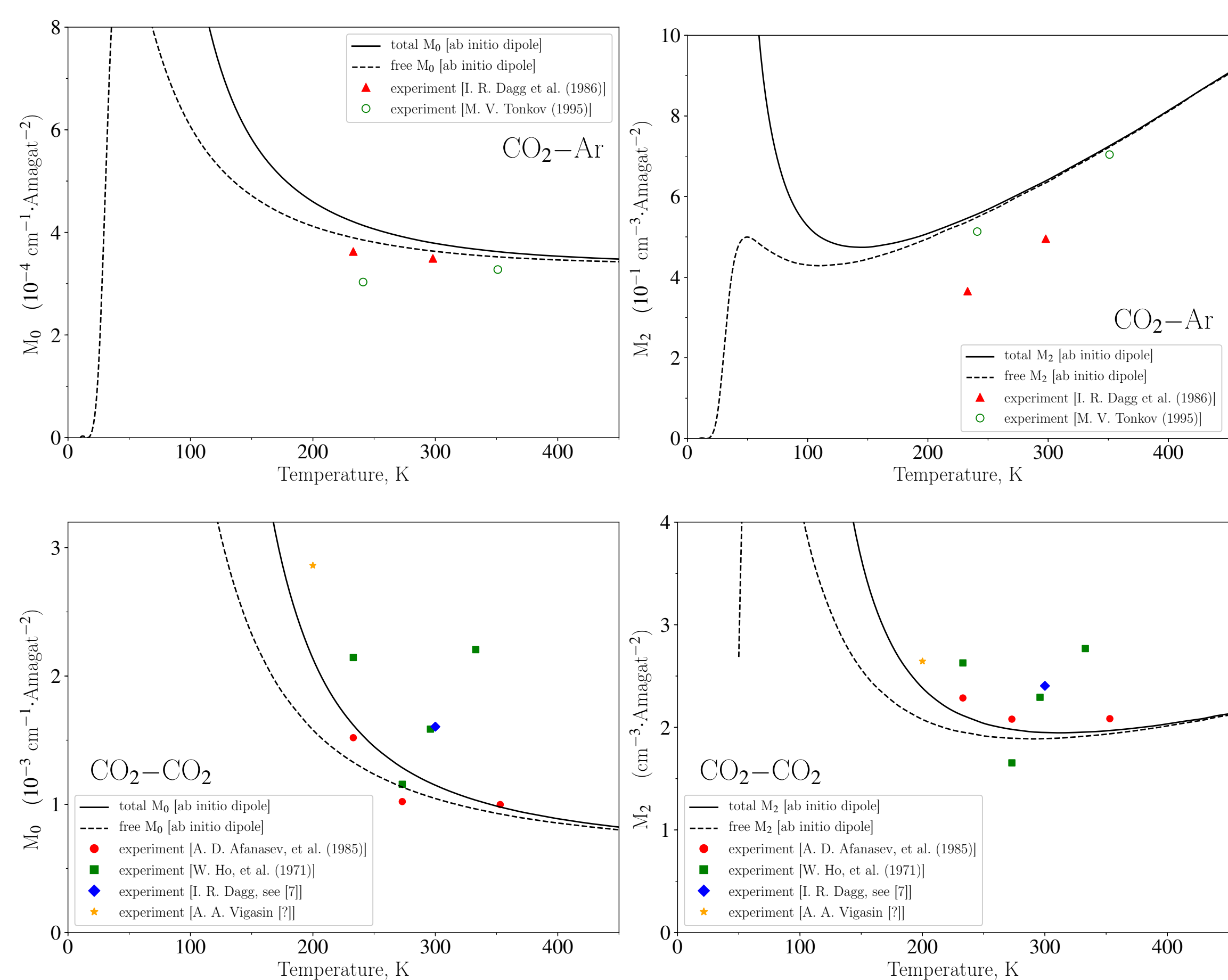
Spectral moments are integral values, which are widely used to characterise CIA spectra. The usage of spectral moments is justified by the possibility to represent them either in terms of integrals over experimentally measured spectral profiles or in terms of Boltzmann weighted functions of induced dipole.

**Calculation of spectral moments as phase space integrals**

$$M_0 = \frac{\int d^2 \exp[-H(\mathbf{q}, \mathbf{p}, \mathbf{J})/k_B T] d\mathbf{q} d\mathbf{p} d\mathbf{J}}{\int \exp[-H(\mathbf{q}, \mathbf{p}, \mathbf{J})/k_B T] d\mathbf{q} d\mathbf{p} d\mathbf{J}} \quad M_2 = \frac{\int d^2 \exp[-H(\mathbf{q}, \mathbf{p}, \mathbf{J})/k_B T] d\mathbf{q} d\mathbf{p} d\mathbf{J}}{\int \exp[-H(\mathbf{q}, \mathbf{p}, \mathbf{J})/k_B T] d\mathbf{q} d\mathbf{p} d\mathbf{J}} \quad (4)$$

**Calculation of spectral moments from spectral profile**

$$M_0 = 2 \int_0^\infty \left[ 1 - \exp\left(-\frac{h\nu}{k_B T}\right) \right]^{-1} \frac{\alpha(\nu)}{\nu} d\nu \quad M_2 = 2 \int_0^\infty \left[ 1 - \exp\left(-\frac{h\nu}{k_B T}\right) \right]^{-1} \nu \alpha(\nu) d\nu \quad (5)$$

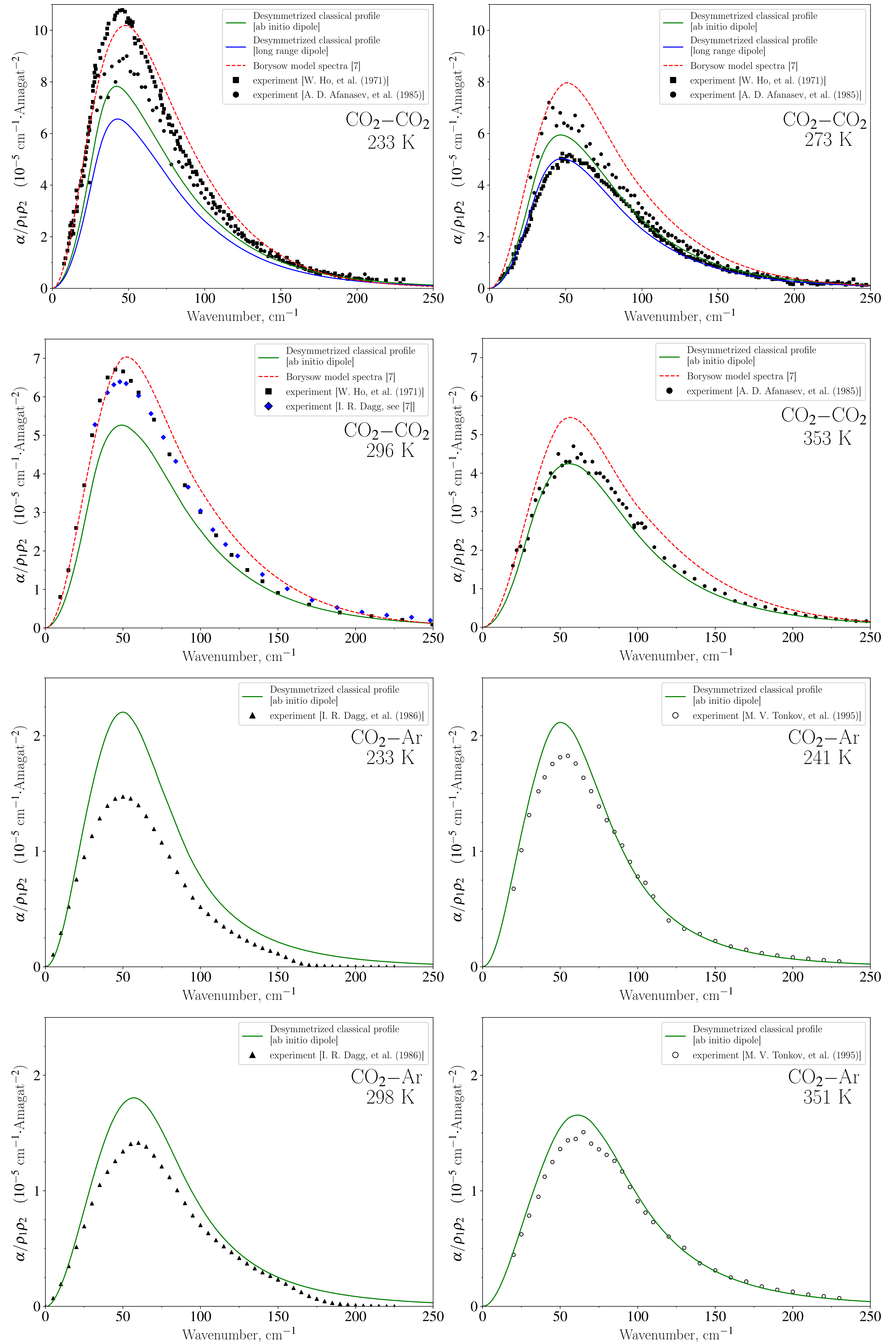


## Discussion

Currently in our calculation we disregard the following contributions and factors

- quadrupole absorption in an individual CO<sub>2</sub> molecule: varies linearly against pure gas pressure and produces different bandshape
- absorption belonging to isotopically substituted CO<sub>2</sub> molecule,
- true bound dimer absorption: amounts up to 10% of total intensity at near room temperature and is more pronounced at lower temperatures,
- fraction of CO<sub>2</sub> molecules occupies (010) bending state: expected to increase at elevated temperature, however, the regular mismatch between calculated and measured spectra is not currently observed.

## Collision-induced absorption of CO<sub>2</sub>–Ar and CO<sub>2</sub>–CO<sub>2</sub> in rototranslational band



## Conclusions

The results reported here show encouraging perspective for our trajectory based method to be employed in extensive CIA simulation. To the best of our knowledge, trajectory based calculation of CIA spectra for various pairs of linear molecules is performed for the first time. Moreover, we extended calculations to CO<sub>2</sub>–CO<sub>2</sub> pair which is known to possess strong anisotropy of intermolecular interaction. We admit that ensemble of available experimental data for CO<sub>2</sub>–CO<sub>2</sub> is yet not perfectly reproduced by our trajectory based calculations. Nevertheless, overall agreement is quite reasonable bearing in mind an appreciable uncertainty, which characteristic to experimental data issuing from different laboratories. Moreover, in contrast to some series of experimental data our spectra vary regularly as a function of temperature. These calculated variations are strongly supported by our independent computations of the zeroth and the second spectral moments as integrals over phase space.

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