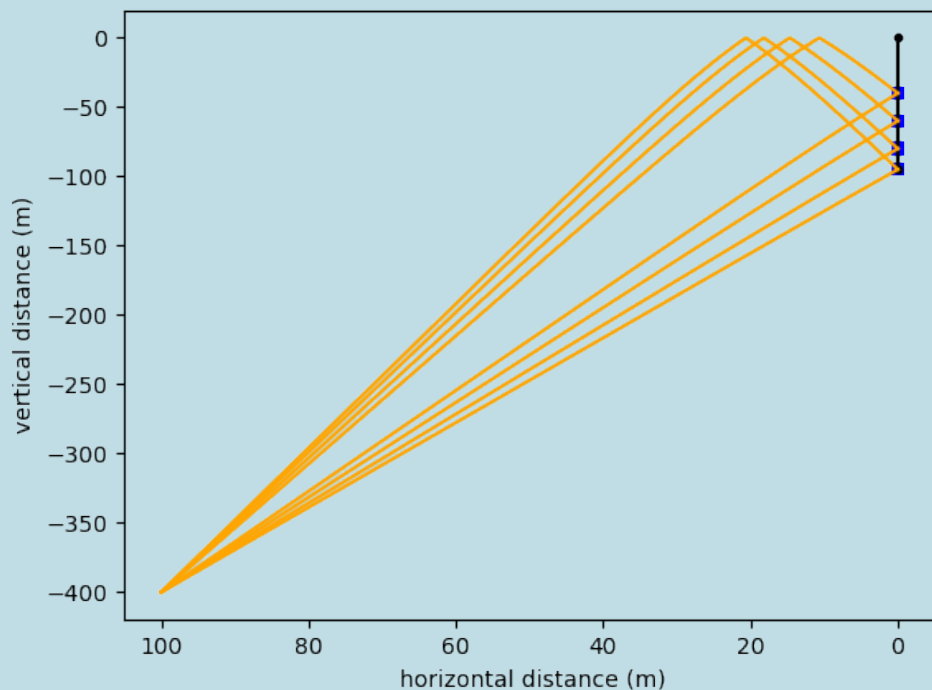


Radio detection of high energy neutrinos in the Greenland icecap

Arthur Adriaens



Department of Physics and Astronomy

Promotor: Prof. dr. Dirk Ryckbosch Dirk.Ryckbosch@ugent.be

Accompanist: Bob Oeyen Bob.Oeyen@ugent.be

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CHAPTER

1

FOREWORD

1.1 Abstract: English

The Radio Neutrino Observatory - RNO-G - is under construction at Summit Station in Greenland to search for neutrinos of several PeV energy up to the Eev range. It's a mid-scale, discovery phase, extremely high-energy neutrino telescope that will probe the astrophysical neutrino flux at energies beyond the reach of IceCube. More particularly it will make it possible to reach the next major milestone in astroparticle physics: the discovery of cosmogenic neutrinos. All

simulations carried out within this work were made with the three programs

- NuRadioMC
- radiotools
- RadioPropa

whom are free to download on [github](#)

1.2 Abstract: Nederlands

CHAPTER

2

BACKGROUND

2.1 Electroweak interaction

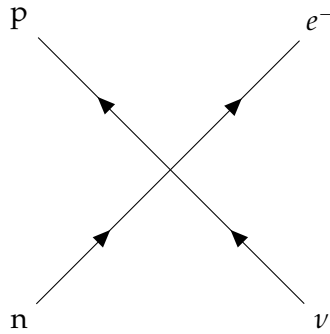
$$\begin{aligned}
 \mathcal{L}_{SM} = & -\frac{1}{4}F_{\mu\nu}^a F^{\mu\nu a} - \frac{1}{4}G_{\mu\nu}^a G^{\mu\nu a} - \frac{1}{4}B_{\mu\nu}^a B^{\mu\nu a} \\
 & + \sum_q \bar{\psi}_{q,L}(i\mathcal{D})\psi_{q,L} + \sum_l \bar{\psi}_{l,L}(i\mathcal{D})\psi_{l,L} + \sum_l \bar{\psi}_{q,R}(i\mathcal{D})\psi_{q,R} + \sum_l \bar{\psi}_{l,R}(i\mathcal{D})\psi_{l,R} \\
 & + \mathcal{D}_\mu \phi (\mathcal{D}^\mu \phi)^\dagger - u^2 \phi \phi^\dagger - \lambda (\phi \phi^\dagger)^2 \\
 & + g_Y^{(e)} \bar{\psi}_{e,L} \phi e_R + g_Y^{(u)} \bar{\psi}_{q,L} \tilde{\phi} u_R + g_Y^{(d)} \bar{\psi}_{q,L} \phi d_R + h.c
 \end{aligned}$$

2.1.1 History

Fermi realised a quantitatively good local field theory for the β -decay in 1934 based on the idea of the following interaction:

$$n \rightarrow p + e^- + \bar{\nu} \quad (2.1)$$

i.e



This 4-fermion interaction is however not renormalizable, meaning that it will be incorrect for sufficiently high energies. As the lagrangian would look like

$$\mathcal{L}_{int}^F = -G_F (\bar{\psi}_p \gamma_\mu \psi_n) (\bar{\psi}_e \gamma^\mu \psi_{\bar{\nu}}) + h.c \quad (2.2)$$

And indeed, from dimensionality analysis we see that, as $[\psi] = [L]^{-3/2}$, we get that from $[\mathcal{L}_{int}] = [L]^{-4}$, $[G_F] = [L]^2 = [\Lambda]^{-2}$

This interaction lagrangian also doesn't explain how this weak interaction violates parity as it couples only to the left handed part of lepton- and baryon fields. Everything was finally ex

2.1.2 $SU(2) \rightarrow SU(2)_L \times U(1)_Y$

We'll only concern ourselves with leptons and lepton decay, defining the operators

$$P_R = \frac{1}{2}(1 + \gamma_5) \quad P_L = \frac{1}{2}(1 - \gamma_5) \quad (2.3)$$

with

$$\gamma_5 = i\gamma_0\gamma_1\gamma_2\gamma_3 \quad (2.4)$$

And with this defining

$$\psi_R := P_R\psi \quad \psi_L := P_L\psi \quad (2.5)$$

2.2 Discovery

2.2.1 See-saw mechanism

Given a spinor ψ with the following Lagrange density:

$$\mathcal{L} = i\bar{\psi}\not{\partial}\psi - m\bar{\psi}\psi - \frac{M}{2}(\bar{\psi}_R\psi_{Rc} + \bar{\psi}_{Rc}\psi_R) \quad (2.6)$$

We can re-write this Lagrangian in terms of

$$\chi := \frac{1}{\sqrt{2}}(\psi_R + \psi_{Rc}) \quad (2.7)$$

$$\omega := \frac{1}{\sqrt{2}}(\psi_L + \psi_{Lc}) \quad (2.8)$$

by first identifying that

$$-\frac{M}{2}(\bar{\psi}_R\psi_{Rc} + \bar{\psi}_{Rc}\psi_R) \quad (2.9)$$

is equal to

$$-M\bar{\chi}\chi = -\frac{M}{2}(\bar{\psi}_R + \bar{\psi}_{Rc})(\psi_R + \psi_{Rc}) = -\frac{M}{2}(\bar{\psi}_R\psi_{Rc} + \bar{\psi}_{Rc}\psi_R) \quad (2.10)$$

Where we've used

$$\bar{\psi}_R\psi_R \equiv \psi_R^\dagger\gamma^0\psi_R \equiv P_R\psi^\dagger\gamma^0P_R\psi = P_RP_L\psi^\dagger\gamma^0\psi = 0 \quad (2.11)$$

And next that in

$$i\bar{\psi}\not{\partial}\psi - m\bar{\psi}\psi = i\bar{\psi}_R\not{\partial}\psi_R + i\bar{\psi}_L\not{\partial}\psi_L - m\bar{\psi}_R\psi_L - m\bar{\psi}_L\psi_R \quad (2.12)$$

We can identify that

$$\bar{\chi}\not{\partial}\chi = \frac{1}{2}(\bar{\psi}_R\not{\partial}\psi_R + \bar{\psi}_{Rc}\not{\partial}\psi_{Rc}) = \bar{\psi}_R\not{\partial}\psi_R \quad (2.13)$$

$$\bar{\omega}\not{\partial}\omega = \bar{\psi}_L\not{\partial}\psi_L \quad (2.14)$$

Where we've done an integration by parts and used $\bar{\psi}_c \gamma_\mu \chi_c = -\bar{\chi} \gamma_\mu \psi$. We thus get:

$$\mathcal{L} = i\bar{\chi}\not{\partial}\chi + i\bar{\omega}\not{\partial}\omega - m\bar{\psi}_R\psi_L - m\bar{\psi}_L\psi_R - M\bar{\chi}\chi \quad (2.15)$$

And finally we notice that

$$\bar{\chi}\omega = \frac{1}{2}(\bar{\psi}_R\psi_L + \bar{\psi}_R\psi_{Lc} + \bar{\psi}_{Rc}\psi_L + \bar{\psi}_{Rc}\psi_{Lc}) \quad (2.16)$$

$$= \frac{1}{2}(\bar{\psi}_R\psi_L + \bar{\psi}_R\psi_{Lc} + \bar{\psi}_{Rc}\psi_L + \bar{\psi}_L\psi_R) \quad (2.17)$$

$$\bar{\omega}\chi = \frac{1}{2}(\bar{\psi}_L\psi_R + \bar{\psi}_{Lc}\psi_R + \bar{\psi}_L\psi_{Rc} + \bar{\psi}_{Lc}\psi_{Rc}) \quad (2.18)$$

$$= \frac{1}{2}(\bar{\psi}_L\psi_R + \bar{\psi}_{Lc}\psi_R + \bar{\psi}_L\psi_{Rc} + \bar{\psi}_R\psi_L) \quad (2.19)$$

As $\bar{\psi}_c\chi_c = \bar{\chi}\psi$. Summing these, we get:

$$\bar{\chi}\omega + \bar{\omega}\chi = \bar{\psi}_L\psi_R + \bar{\psi}_R\psi_L \quad (2.20)$$

$$+ \frac{1}{2}(\bar{\psi}_R\psi_{Lc} + \bar{\psi}_{Rc}\psi_L + \bar{\psi}_{Lc}\psi_R + \bar{\psi}_L\psi_{Rc}) \quad (2.21)$$

$$= \bar{\psi}_L\psi_R + \bar{\psi}_R\psi_L \quad (2.22)$$

Where we've used the handedness flips a charge conjugation entails, at last we now have:

$$\mathcal{L} = i\bar{\chi}\not{\partial}\chi + i\bar{\omega}\not{\partial}\omega - m(\bar{\chi}\omega + \bar{\omega}\chi) - M\bar{\chi}\chi \quad (2.23)$$

Now to determine the mass eigenstates we'll re-write this equation into the form

$$\mathcal{L} = i\bar{\chi}\not{\partial}\chi + i\bar{\omega}\not{\partial}\omega - \begin{pmatrix} \bar{\chi} & \bar{\omega} \end{pmatrix} \cdot \begin{pmatrix} M & m \\ m & 0 \end{pmatrix} \cdot \begin{pmatrix} \chi \\ \omega \end{pmatrix} \quad (2.24)$$

lets now find the eigenvalues:

$$\begin{vmatrix} M - \lambda & m \\ m & -\lambda \end{vmatrix} = (\lambda - M)\lambda - m^2 = 0 \implies \lambda_{\pm} = \frac{M \pm \sqrt{M^2 + 4m^2}}{2} \quad (2.25)$$

i.e

$$\lambda_{\pm} = \frac{M}{2} \left(1 \pm \sqrt{1 + 4m^2/M^2} \right) \quad (2.26)$$

Now we'll determine the eigenvectors:

$$\begin{bmatrix} M - \lambda_{\pm} & m \\ m & -\lambda_{\pm} \end{bmatrix} \begin{pmatrix} x_{\pm} \\ y_{\pm} \end{pmatrix} = \vec{0} \quad (2.27)$$

this gives

$$Mx_{\pm} - \lambda_{\pm}x_{\pm} + my_{\pm} = 0 \quad (2.28)$$

$$mx_{\pm} - \lambda_{\pm}y_{\pm} = 0 \implies \frac{mx_{\pm}}{\lambda_{\pm}} = y_{\pm} \quad (2.29)$$

inserting the second equation in the first we get:

$$Mx_{\pm} - \lambda_{\pm}x_{\pm} + m\frac{mx_{\pm}}{\lambda_{\pm}} = 0 = M\lambda_{\pm}x_{\pm} - \lambda_{\pm}^2x_{\pm} + m^2x_{\pm} \quad (2.30)$$

$$= x_{\pm}(\lambda_{\pm}^2 - M\lambda_{\pm} + m^2) \quad (2.31)$$

which is true for every x_{\pm} (see equation 2.25) i.e we can freely choose x_{\pm} so let's opt for $x_{\pm}^2 + y_{\pm}^2 = 1$:

$$x_{\pm}^2 \left(1 + \frac{m^2}{\lambda_{\pm}^2}\right) = 1 \implies x_{\pm}^2 = \frac{1}{1 + \frac{m^2}{\lambda_{\pm}^2}} \implies x_{\pm} = \frac{\lambda_{\pm}}{\sqrt{\lambda_{\pm}^2 + m^2}} \quad (2.32)$$

$$\& \quad y_{\pm} = \frac{m}{\sqrt{\lambda_{\pm}^2 + m^2}} \quad (2.33)$$

And thus, summing up, we get the eigenvectors ϕ_{\pm} with eigenvalues m_{\pm} :

$$\phi_{\pm} := \begin{pmatrix} x_{\pm} \\ y_{\pm} \end{pmatrix} = \begin{pmatrix} \frac{\lambda_{\pm}}{\sqrt{\lambda_{\pm}^2 + m^2}} \\ \frac{m}{\sqrt{\lambda_{\pm}^2 + m^2}} \end{pmatrix} \quad \text{and} \quad m_{\pm} := \lambda_{\pm} = \frac{M}{2} \left(1 \pm \sqrt{1 + 4m^2/M^2}\right) \quad (2.34)$$

Now we'll consider the limit $M \gg m$:

$$m_{\pm} = \frac{M}{2} \left(1 \pm \sqrt{1 + 4m^2/M^2}\right) \approx \frac{M}{2} \left(1 \pm 1 \pm \frac{2m^2}{M^2}\right) \quad (2.35)$$

Which gives:

$$m_{+} \approx M \quad (2.36)$$

$$m_{-} \approx -\frac{m^2}{M} \quad (2.37)$$

and:

$$\phi_{+} \approx \begin{pmatrix} \frac{M}{M} \\ \frac{m}{M} \end{pmatrix} = \begin{pmatrix} 1 \\ m/M \end{pmatrix} \quad (2.38)$$

$$\phi_{-} \approx \begin{pmatrix} -\frac{m}{M} \\ \frac{m}{m} \end{pmatrix} = \begin{pmatrix} -m/M \\ 1 \end{pmatrix} \quad (2.39)$$

i.e, in the χ, ω basis:

$$m_{+} \approx M \quad \text{with eigenstate} \quad \chi + \frac{m}{M}\omega \quad (2.40)$$

$$m_{-} \approx -\frac{m^2}{M} \quad \text{with eigenstate} \quad \omega - \frac{m}{M}\chi \quad (2.41)$$

$$(2.42)$$

Here we can clearly see the See-Saw mechanism at work, for a certain m if we choose a big M we'll get a big m_{+} and small m_{-} (and vice versa). We also see that there's only a very small mixing of states, i.e the m_{-} mass state is almost purely ω (and m_{+} almost purely χ). The parameter m in the original matrix is forbidden by electroweak gauge symmetry, and can only appear after the symmetry has been spontaneous broken by a Higgs mechanism; for this reason a good estimate of the order of m is the vacuum expectation energy: $m \approx v = 246 \approx 10^2 \text{GeV}$. In grand unified theories it's theorised that $M \approx 10^{15} \text{GeV}$ after symmetry breaking, using these values we get

$$m_{-} \approx 10^{-11} \text{GeV} \approx 10^{-2} \text{eV} \quad (2.43)$$

which is an appropriate mass size for the observed neutrinos

2.3 Why?

Neutrinos are ideal messengers to identify the UHE (Ultra High Energy) sources in the universe. Unlike cosmic rays, which are deflected by magnetic fields and interact with matter and radiation on their way to us, neutrinos point back to sources and can reach Earth unperturbed from the most distant corners of the universe. Neutrinos can be generated in 2 ways: either they're generated in interactions at the sources, termed *astrophysical neutrinos*. Or they're created through the interaction of ultra-high energy cosmic rays during propagation with the cosmic microwave or other photon backgrounds termed *cosmogenic neutrinos*. Supernovae are a source for *astrophysical neutrinos*:

2.3.1 Supernovae

A star starts its life as a ball of pure hydrogen, at the core due to the gravitational pressure of the outside plasma fusion of hydrogen into deuterium and helium happens, converting mass into energy. The pressure of this energy counteracts the pressure of gravity and the star is stable.

When the hydrogen at the core runs out no more hydrogen can be fused and the fusion of heavier elements starts, this can't keep going on however as at some point the star starts to form the most stable element: iron. It costs energy to both make lighter elements than iron and heavier ones. As the iron core builds up the outside pressure from the core starts to decrease as no new energy is released. This goes on until the inwards pressure becomes too large and the electrons surrounding the iron core fuse with the protons, creating neutrons and neutrino's.

This last part happens in a split second, creating a very dense neutron star and up to 10^{52} ultra-relativistic neutrinos. As the density has suddenly increased so much there's a huge distance of pure vacuum between the plasma outer layer and the (now) neutron star, this plasma starts falling in as these neutrinos carrying tremendous amounts of energy start going outwards the neutron stars core.

These then collide resulting in what we observe as a "supernova", wrongly thought of by Kepler as being a "new (nova) star" rather being a violent death of an old star.

Not all the neutrinos collide with matter of course as neutrinos rarely interact, it's only as the incoming plasma is so dense and due to the tremendous amount of neutrinos that collisions happen at all. The ones that escape, however, will be visible on earth in our neutrino detectors, far before the light escapes the exploding star.

Neutrino observatories are thus useful to know where to point our various telescopes before the supernova is actually visible in the night sky.

2.3.2 Oscillations

2.3.3 Majorana

2.4 Outside sources

The radio detection of neutrinos targets the energy range 10PeV to 100EeV [1], here we'll see diffuse neutrino fluxes both directly from sources (*astrophysical neutrinos*) i.e created directly in (or very close to) the sources of ultra-high energy cosmic rays (UHECRs), as well as from the interaction of UHECRs with photon backgrounds (e.g the CMB) (*cosmogenic neutrinos*).

2.4.1 primordial neutrinos

To estimate the temperature of the neutrinos who decoupled at the start of the universe, we can take a look at conservation of entropy [3] (...) The entropy before and after decoupling are:

$$s(a_1) = \frac{2\pi^2}{45} \left(2 + \frac{7}{8}(2 + 2 + 3 + 3)\right) T_1^3 \quad (2.44)$$

$$= \frac{2\pi^2}{45} \frac{86}{8} T_1^3 \quad (2.45)$$

$$s(a_2) = \frac{2\pi^2}{45} (2T_\gamma^3 + \frac{7}{8}(6)T_\nu^3) \quad (2.46)$$

$$(2.47)$$

Conservation of entropy:

$$s(a_1)a_1^3 = s(a_2)a_2^3 \quad (2.48)$$

$$\frac{86}{8}(T_1 a_1)^3 = \left(2 \left(\frac{T_\gamma}{T_\nu}\right)^3 + \frac{42}{8}\right) (T_\nu a_2)^3 \quad (2.49)$$

$$\frac{86}{8} = 2 \left(\frac{T_\gamma}{T_\nu}\right)^3 + \frac{42}{8} \quad (2.50)$$

$$\frac{44}{16} = \left(\frac{T_\gamma}{T_\nu}\right)^3 \quad (2.51)$$

$$\left(\frac{T_\gamma}{T_\nu}\right) = \left(\frac{11}{4}\right)^{1/3} \quad (2.52)$$

i.e

$$T_\nu = \left(\frac{4}{11}\right)^{1/3} T_\gamma \quad (2.53)$$

2.5 Why look for them?

The origin of the most energetic cosmic rays is still not conclusively identified. One approach to solving this problem is *multi-messenger astrophysics*, where several types of cosmic particles are used to identify the sources of these ultra-high energy cosmic rays (UHECRs). E.g we simultaneously measure gravitational waves (gravitons?) with the Einstein telescope, neutrino's with IceCube (or eventually RNO-G) and muons with a muon detector.

CHAPTER

3

RADIO DETECTION

For a particle shower to emit strong radio signals, two conditions have to be met:

- There needs to be a separation of positive and negative charges in the shower front
- The signals produced over the length of the shower profile need to overlap coherently.

The first item, separation of positive and negative charges, can be caused by 2 mechanisms: The *Askaryan* effect [2], also known as Askaryan radiation. This is the phenomenon whereby a particle traveling faster than the phase velocity of light in a dense dielectric (such as ice) produces a shower of secondary charged particles which contains a charge anisotropy (net negative charge), this charge imbalance is a result of medium electrons either Compton scattering into the advancing shower or annihilating with shower positrons. You thus get moving charges which move faster than the light speed in the medium, creating Cherenkov radiation. The other effect, called *geomagnetic emission* is the separation of charges by the Lorentz force from the geomagnetic field, however, because of its relatively high density, in ice the Askaryan effect is dominant. It's possible to distinguish between the two with polarization as with Askaryan emission, the light is polarized in the radial direction towards the shower axis contrary to geomagnetic emission where it's polarized in the Lorentz force direction.

In the following two sections I'll quickly give a short overview of the equations of Cherenkov radiation to determine the viewing angle of an incoming neutrino particle, this is relevant to the second condition which I'll explain afterwards. The reader who wants a thorough explanation and derivation is advised to check out *Chapter 14: Radiation by Moving Charges* from the book *Classical Electrodynamics* by Jackson.

3.1 Spectral distribution of radiation

We wish to know the emitted energy per elementary unit solid angle over a certain frequency interval for a moving charge far away from the source. For this we have that the vectorpotential \mathbf{A} , defined as

$$\mathbf{B} = \nabla \times \mathbf{A} \quad (3.1)$$

takes the form

$$\mathbf{A}(\omega) = \frac{q}{4\pi\sqrt{2\pi}} \sqrt{\frac{\mu}{\epsilon}} \frac{e^{ikr}}{r} \boldsymbol{\alpha} \quad (3.2)$$

with q the charge, r the distance from the charge to the observer and

$$\boldsymbol{\alpha} = \int_{-\infty}^{\infty} \boldsymbol{\beta}(t) e^{i\omega(t - \mathbf{e}_r \cdot \mathbf{r}_0(t)/c')} dt \quad (3.3)$$

With $\boldsymbol{\beta} := \mathbf{u}/c'$ wherein \mathbf{u} is the speed of the particle, c' is the local speed of light and the integration is along the path of the moving charged particle. The energy emitted per unit solid angle is given by

$$\frac{d\mathcal{P}}{d\Omega} = R'^2 \mathbf{S}(t) \cdot \mathbf{n}' \quad (3.4)$$

Defining \mathcal{E} to be the time integral of this, we can reformulate this into (standard practice to integrate over the frequencies)

$$\frac{d\mathcal{E}}{d\Omega} = r^2 \int_{-\infty}^{\infty} d\omega (\mathbf{E}(\omega) \times \mathbf{H}(-\omega)) \cdot \mathbf{e}_r = \int_0^{\infty} \frac{d^2 \mathcal{J}(\omega)}{d\omega d\Omega} \quad (3.5)$$

i.e. $\frac{d^2 \mathcal{J}}{d\omega d\Omega}$ is the energy radiated per elementary unit solid angle and per elementary unit frequency interval, re-writing gives

$$\frac{d^2 \mathcal{J}(\omega)}{d\omega d\Omega} = 2r^2 \Re\{\mathbf{E}(\omega) \times \mathbf{H}^*(\omega)\} \cdot \mathbf{e}_r \quad (3.6)$$

up to $\mathcal{O}(r^{-2})$ we get

$$\frac{d^2 \mathcal{J}(\omega)}{d\omega d\Omega} = \frac{q^2 \omega^2}{16\pi^3} \sqrt{\frac{\mu}{\epsilon}} |\mathbf{e}_r \times (\mathbf{e}_r \times \boldsymbol{\alpha})|^2 \quad (3.7)$$

3.2 Cherenkov radiation

Cherenkov radiation is like the elektromagnetic equivalent of a sonic boom, a sonic boom happens when something goes faster than the sounds speed in the medium; A particle emits Cherenkov radiation if it goes faster than the light speed in the medium. Choosing the particle trajectory to lie along the z axis we can approximate equation 3.7 as

$$\frac{d^2 \mathcal{J}(\omega)}{d\omega d\Omega} = \frac{q^2}{4\pi} \sqrt{\frac{\mu}{\epsilon}} \beta^2 \omega^2 \delta^2[\omega(1 - \beta \mathbf{e}_r \cdot \mathbf{e}_z)] |\mathbf{e}_r \times \mathbf{e}_z|^2 \quad (3.8)$$

or, in spherical coordinates, $1 - \beta \mathbf{e}_r \cdot \mathbf{e}_z = 1 - \beta \cos(\theta_c)$ in the delta function. We thus only expect radiation if

$$\cos(\theta_c) = \frac{1}{\beta} = \frac{c'}{u} = \frac{c}{n} \cdot \frac{1}{u} \quad (3.9)$$

I.e if $u > \frac{c}{n}$ with n the index of refraction, Cherenkov radiation will be emitted along a cone surface with half angle $\frac{\pi}{2} - \theta_c$ as illustrated in figure 3.2. Integrating equation 3.8 over the solid angle and formally deviding by the time interval we get:

$$\frac{d^2 \mathcal{J}}{d\omega dt} = \frac{q^2}{4\pi} \sqrt{\frac{\mu}{\epsilon}} \beta \omega \left(1 - \frac{1}{\beta^2}\right) \quad (3.10)$$

We see that the energy is proportional to ω , so we expect that most radiation will be emitted "in blue", as seen in figure 3.1. For ice the index of refraction is roughly 1.75, so we expect an ultra-relativistic particle to produce the most radiation at around 55° opening as $\cos\left(\frac{1}{1.75}\right) \approx 55^\circ$ (generally we take 56°). Now if an observer is positioned at this Cherenkov angle all radio emission produced during the shower development reaches him/it at the same time, leading to constructive interference, hence the second condition is satisfied in ice for signals of ≈ 56

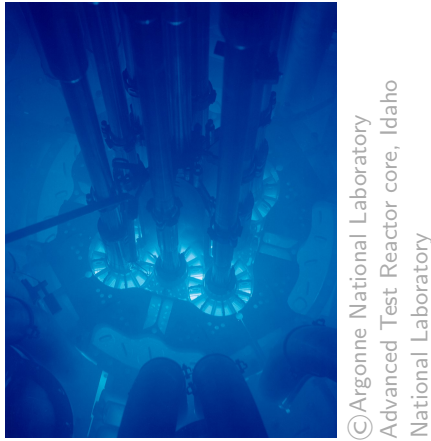


Figure 3.1: Cherenkov radiation in a nuclear reactor

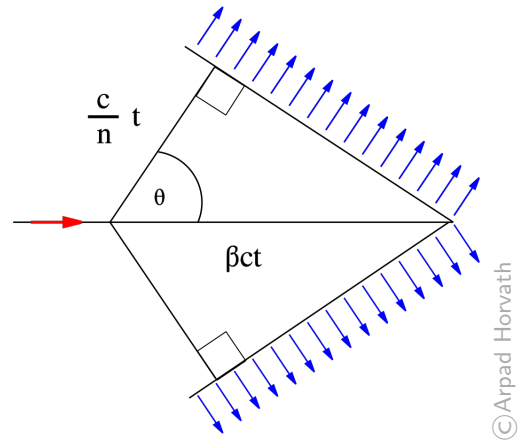


Figure 3.2: Diagrammatic representation of Cherenkov radiation

3.3 Reconstruction

It can pose a challenge to reconstruct the radio signals produced by the Cherenkov radiation as they are often obscured by background noise. A solution used in RadioReco is Information Field Theory (IFT) implemented in RadioReco by Welling et al. [6] which uses Bayesian inference to calculate the most likely radio signal, given recorded data.

CHAPTER

4

THE DETECTOR

Both cosmic ray and neutrino detectors face the same main problem at the highest energies: the steeply falling flux requires large effective areas, which leads to the construction of neutrino detectors with volumes on the cubic kilometer scale: IceCube. As we wish to detect neutrinos with even higher energies we turn to look at an array of detectors spanning multiple cubic kilometers: RNO-G.

One such detector is illustrated in figure 4.1.

The deep component of the detector can be split up in three parts: Two *helper strings*, one *power string* and the surface components. The helper strings are the 2 vertical cables shown on the right of the figure and each house 2 vertically polarized antennas (Vpols), one quadslot antenna for the horizontal polarization component (Hpol) and one radio pulser on each helper string which can be used to generate calibration signals.

The power string (the leftmost vertical cable) is more densely instrumented: At the bottom it houses a set of four Vpol and two Hpol antennas with a spacing of 1m and further up the string, with a spacing of 20m are three more Vpol antennas.

The signal from each of these antennae are fed into a low-noise amplifier directly above it, from there the signal is sent to the data acquisition (DAQ) system at the surface via a Radio Frequency over Fiber (RFoF) cable. There it's again amplified, digitized and saved onto an SD card. This data is then transmitted via a Long Term Evolution (LTE) telecommunications network to a local server¹, from where it is sent via a satellite link.

There are solar panels as a power source who charge up battery banks, but as there isn't enough light during the Greenland winters, there're plans to build wind turbines (with the problem being the possibly detectable RF noise the 'engine' produces)

¹There is additionally a Long Range Wide Area Network (LoRaWAN) antenna as backup in case of problems with the LTE network

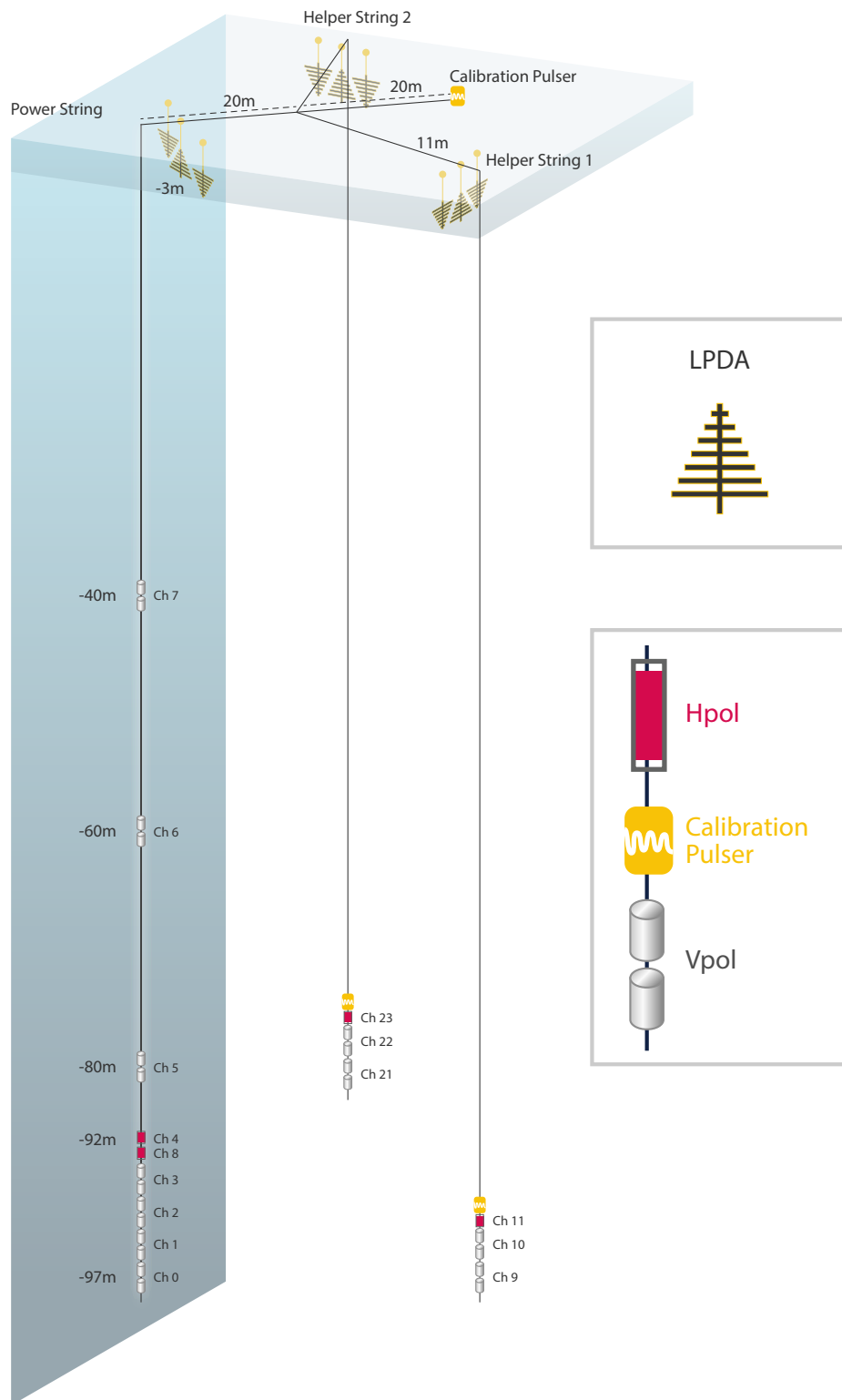


Figure 4.1: illustration of the detector

The radio signal from a neutrino often travels along both direct and refracted paths (designated DnR) to the deep array, this happens because the upper ice layer is a non-uniform medium where the signal trajectory is bent, as illustrated by a simulation in figure 4.2.

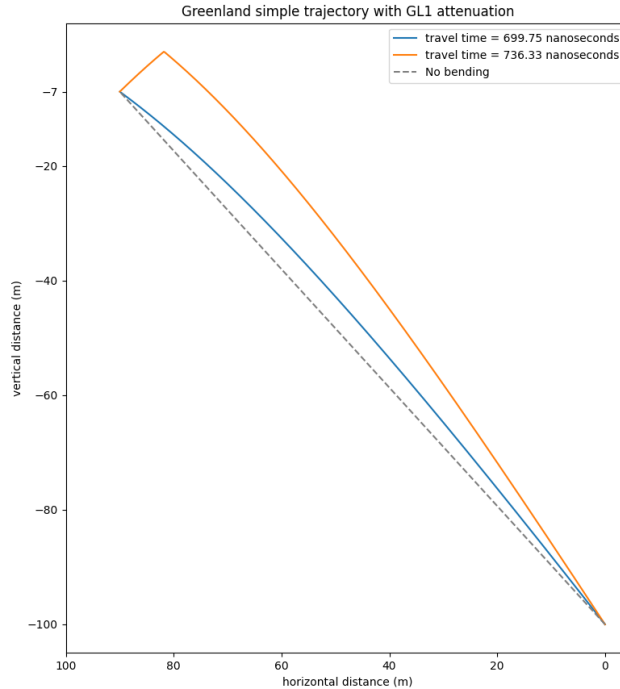
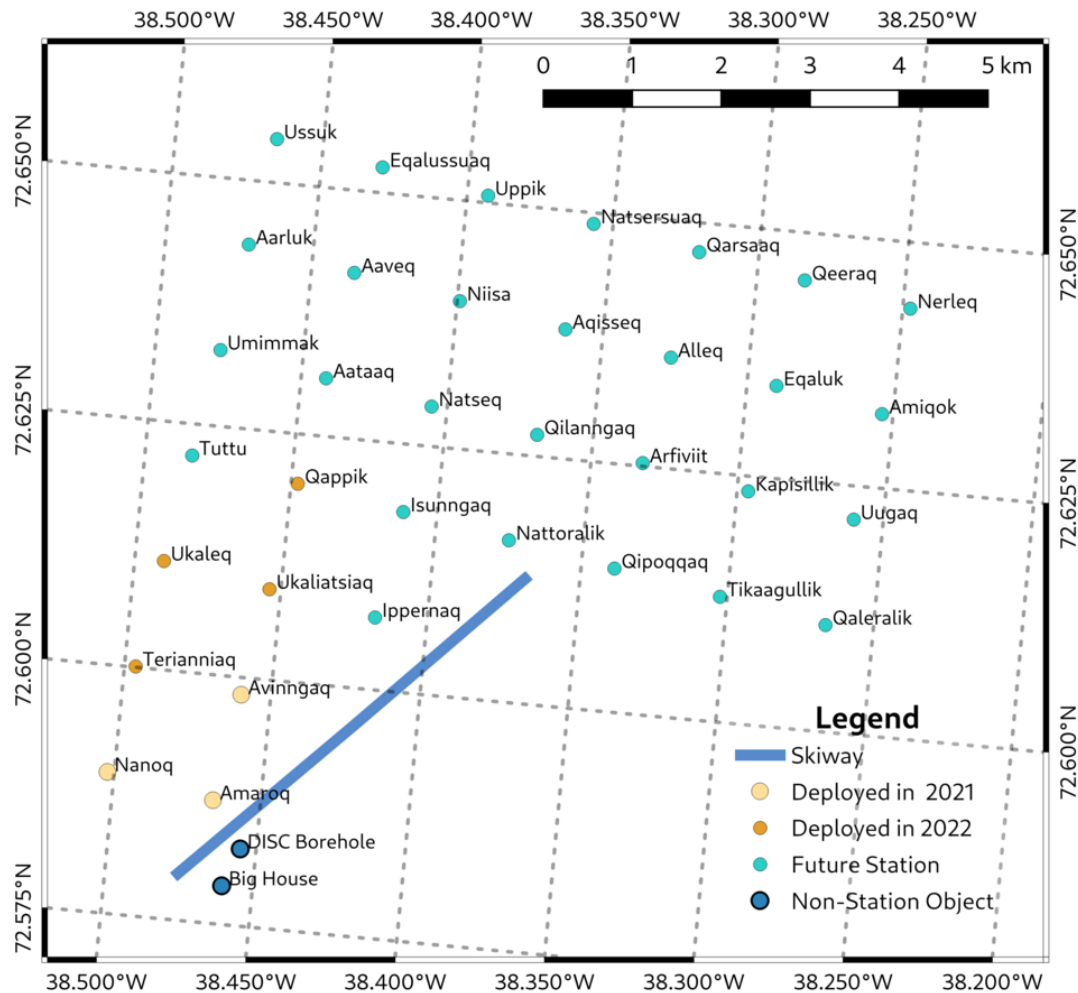


Figure 4.2: illustration of a neutrino signal path

This double pulse characteristic would be a smoking-gun signature of an in-ice source. The two helper strings are needed for a full direction reconstruction. Three independent measurements are needed for azimuthal information, which is provided by the Vpol (Vertical polarization) antennas and placing the Hpol (Horizontal polarization) antennas at different depths on every string, both zenith and azimuth information will be provided for those signals. The helper strings' calibration pulsers, as well as one on the surface, will ensure regular monitoring of the performance of the station and provide information useful for precise calibration of the antenna geometry.

Christoph Welling did an investigation into energy reconstruction from the received signals [7] for air showers in one single station (as the RNO-G stations are so far apart this is the case here aswell) and he noticed that it is necessary to know if the detector who observes an event falls inside or outside the Cherenkov cone to accurately reconstruct the primary particle energy as most over-estimated energies in his simulations are caused by events viewed from within the Cherenkov ring being mistaken for events outside of it. He went on to show that, if we somehow know if the shower was seen from inside or outside the ring from some extra source, that most outliers in the energy disappeared. It is shown by Hiller et al. [4] that the combination of a muon detector with the radio detector might make the issue of confusion between being within or outside of the Cherenkov-ring disappear. Because of this the RNO-G stations are fitted with surface Log Periodic Dipole Antennas (LPDA), capable of detecting muons. Note that this is for air showers, the radio signal from neutrinos show additional complexities.

RNO-G Planned Layout



Notes:

- Station numbering follows a grid, where the first numeral is in increasing W-E and the second numeral is in increasing S-N, skipping non-existent stations (the Seckel method).
- Station spacing is 1.25 km in map coordinates (but really 1.23 km due to projection, which creates a 2% scale difference.)
- Projection is Greenland Polar Stereographic (EPSG:5938). True north indicated by Rose, offset from grid north by 5.37°.
- Magnetic Declination, for August 1 2022, is -25.2° according to the WMM.
- In list below, all future stations labeled as 2023.



v 0.5.1
2022-08-26
68000:1
Greenland Polar Stereographic Projection (EPSG:5938)

Figure 4.3: map of the station

CHAPTER

5

HYBRID RAY TRACER

5.1 Introduction

It has become apparent [citation needed] that complex ice models will be necessary moving forward as the exponential ice model fails to fit the density curve. The ideal software for radio wave propagation through ice is radioprop [8], but due to the way it works you'll have to know the start point, the end point and the launch angle of your ray to work out the path. With the exponential model the launch angle is known from solving a simple equation. However for a more difficult ice model the launch angle can't be known a priori. Work has been done on this by B. Oeyen et al. [5], where they created a ray tracer which iteratively finds the solution, called the "iterative ray tracer". The full explanation of how their algorithm works can be found in the mentioned paper. This is however a sub-optimal solution in python as an optimisation library will generally work faster, work had been done on trying to implement such an algorithm but this attempt failed. As I saw this work I had an idea to combine the iterative ray tracer and the code using the optimisation libraries (a so called "minimizer"), to come up with the algorithm that will be discussed in this chapter: The hybrid ray tracer, in the source code called the "hybrid minimizer".

It succeeds in more rapidly tracing the path from the event to the detector, is more accurate and also arrives closer to the detector as the final result is not limited by the final drawn sphere size but by a given tolerance.

5.2 How it works

The hybrid minimizer can be seen as an extension of the iterative raytracer, it checks after the first loop (as explained in the paper by B. Oeyen et al. [5]) if there are 2 distinct launch regions, if this is the case it breaks out of the loop as is visually explained using a modified version of B. Oeyen et al. their figure in the top part of figure 5.1. It then goes on to use the `scipy.optimize.minimize` module to find the solutions in the respective angle intervals as shown in the bottom part of figure 5.1 (minimizing Δz). If it doesn't find 2 distinct regions after the first loop, it falls back on the iterative ray tracer.

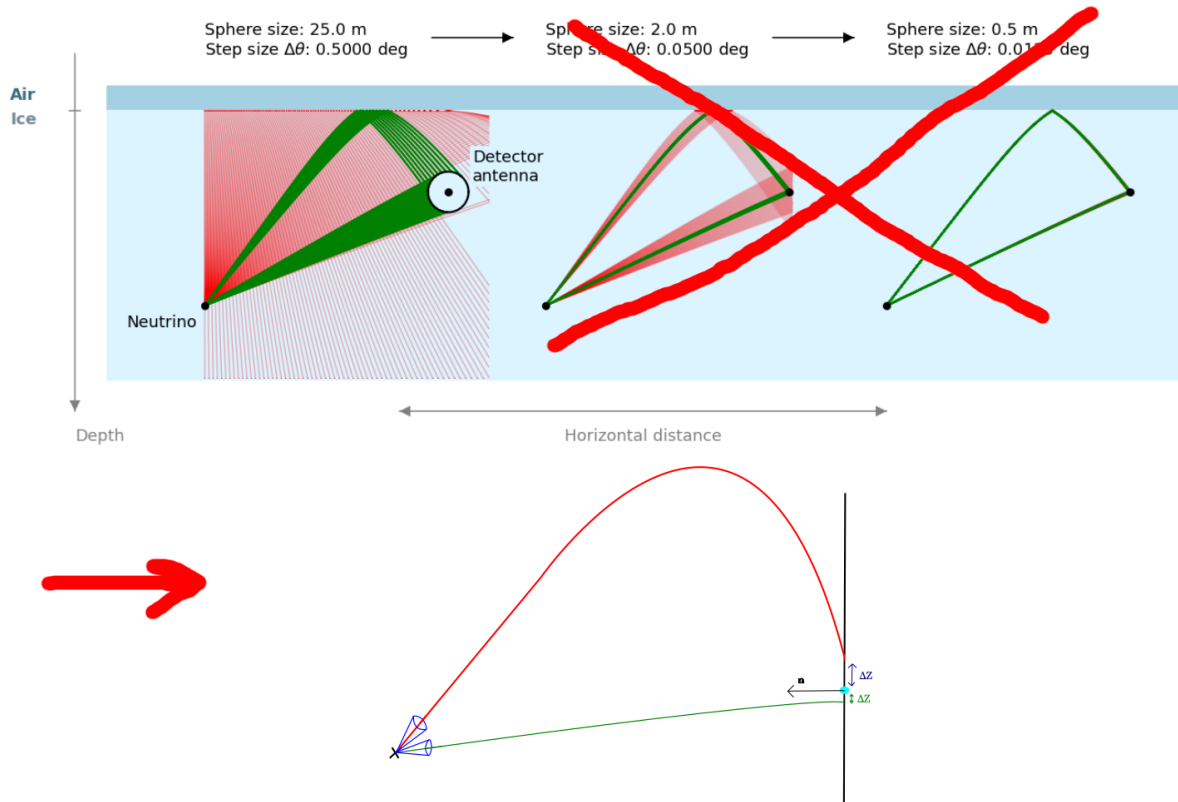


Figure 5.1: explanation of the hybrid method

5.3 random number generator

To test the hybrid minimizer the numpy random module was used to generate random coördinates, the considered square (as there is only a z component to the ice model the 3D problem is essentially only a 2D problem) is $x:0.1\text{km}, 4\text{km}$ and $z:-0.1\text{km}, -3\text{km}$.¹

5.4 Performance Optimalisation

5.4.1 Length of the normal vector

As visually explained in figure 5.2, the size of the normal vector seems to influence how big the ray tracer's step size is taken close to the detector. This thus influences the convergence and time taken. The results of varying this are shown in figures 5.5 and 5.6. Looking at these figures the first optimization conclusion is as expected: take the normal vector length to be 1 meter.

5.4.2 ztol

We'll now change the tolerance on the vertical distance away from the detector which is deemed accepted i.e in figure 5.2 if Δz is below this threshold it's accepted. The results are shown in figures 5.7 and 5.8. From which we can conclude the second optimization conclusion: take ztol to be 0.05 m.

¹This start at 100m depth was to get around issues concerning events that won't even trigger in a full simulation

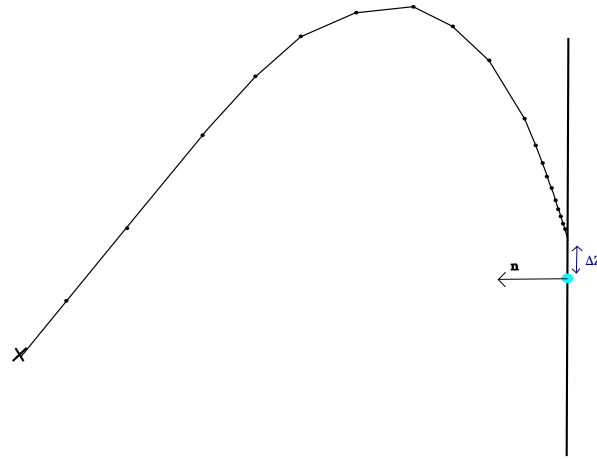


Figure 5.2: how normal vector size influences the stepsize

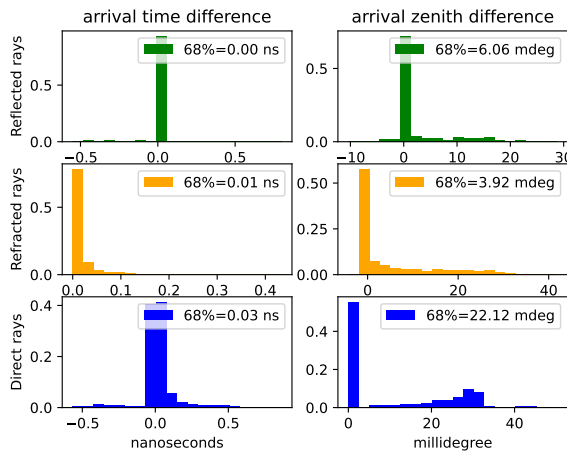


Figure 5.3: Hybrid

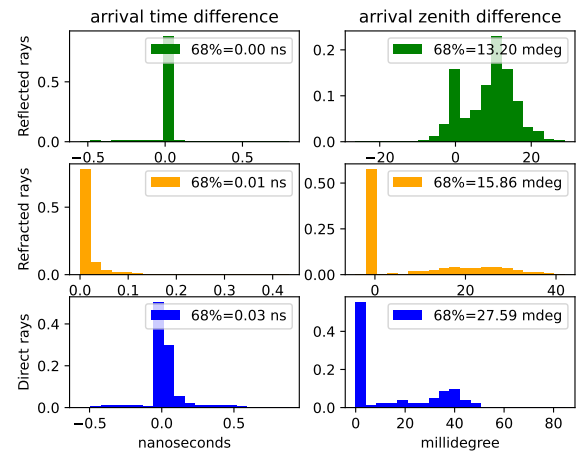


Figure 5.4: Iterative

5.4.3 Sphere Size & Step Size

As explained in Oeyen et al.'s work, the initial rays are sent out in steps of a certain angle and with a sphere around the detector (as can also be seen at the top of figure 5.1, but for clarification I again refer to their paper). The sphere size and step size weren't yet optimized. But as this is the slowest step in the hybrid ray tracer this was optimized here (only the initial sphere and step size as those are relevant for the hybrid raytracer) as seen in figures 5.9 and 5.10.

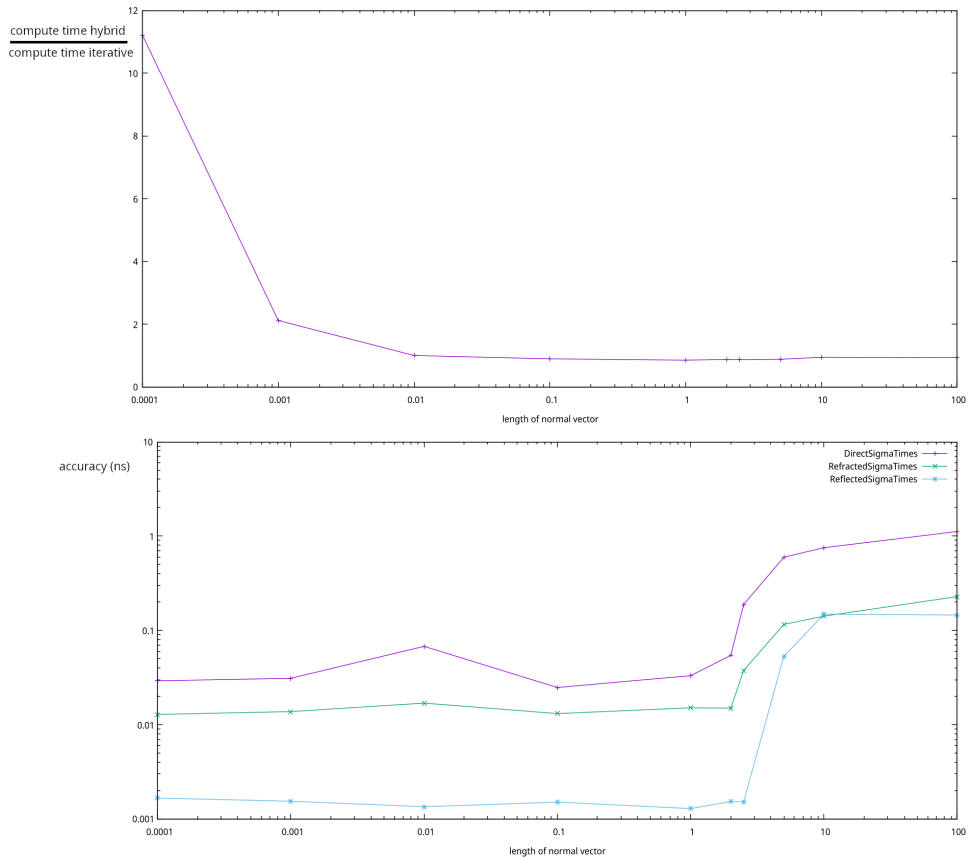


Figure 5.5: influence of the length of the normal vector

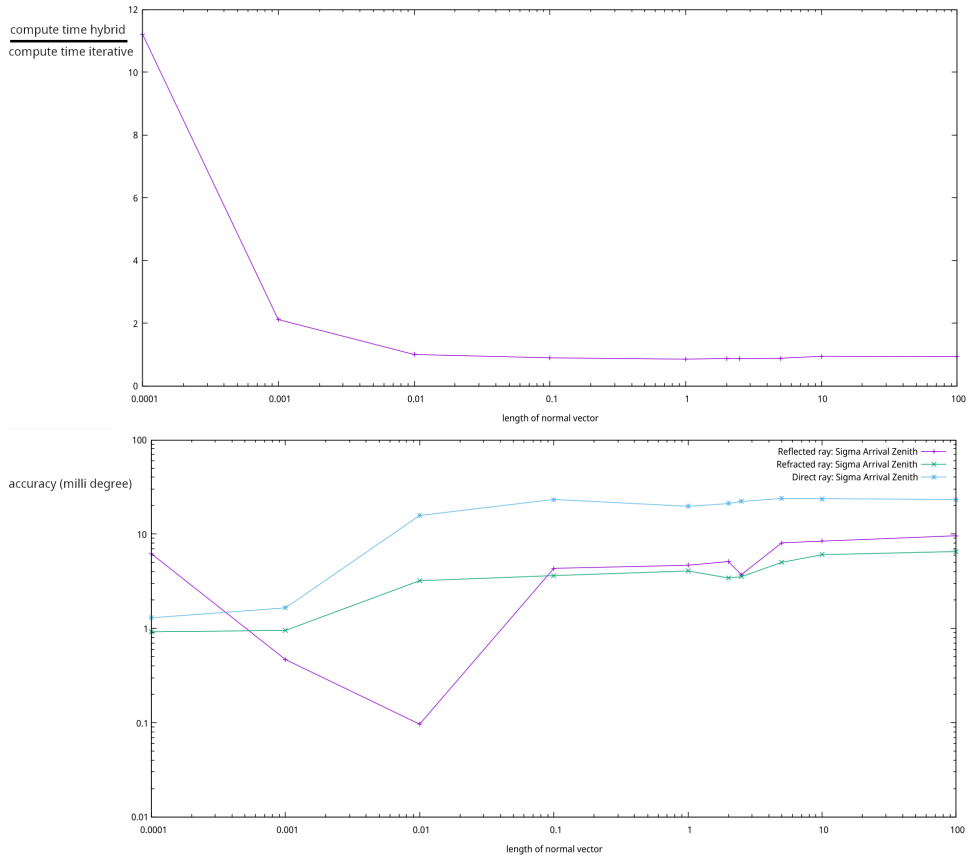


Figure 5.6: influence of the length of the normal vector

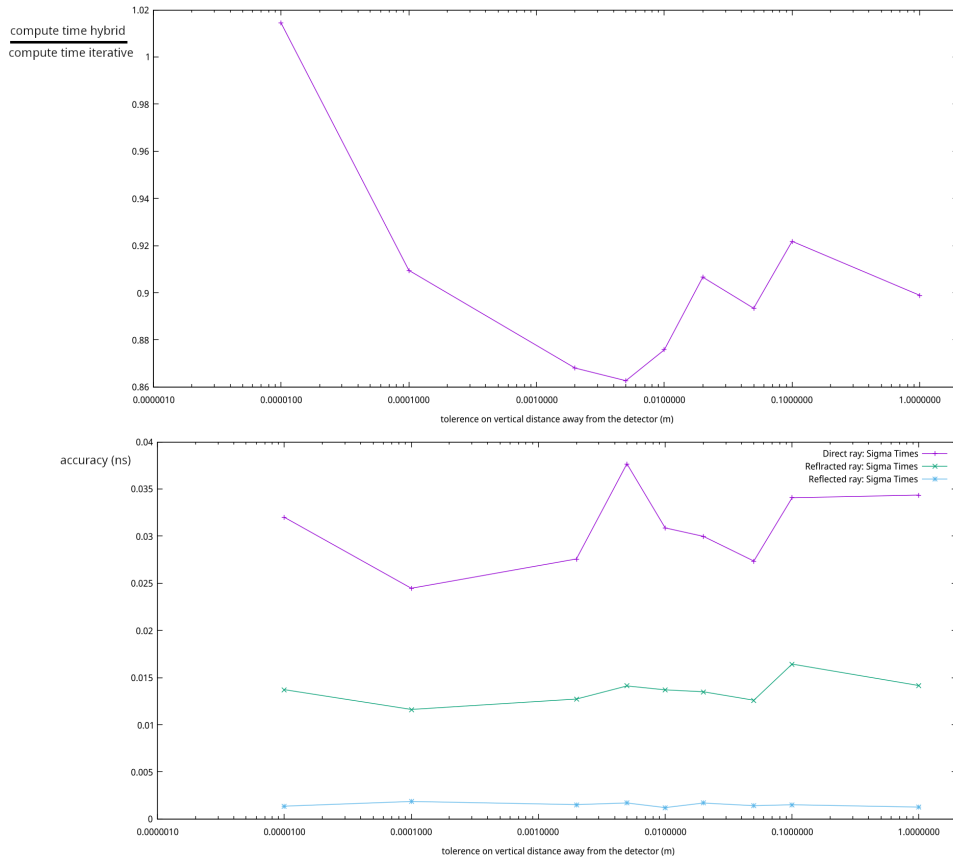


Figure 5.7: influence of the tolerance on vertical distance

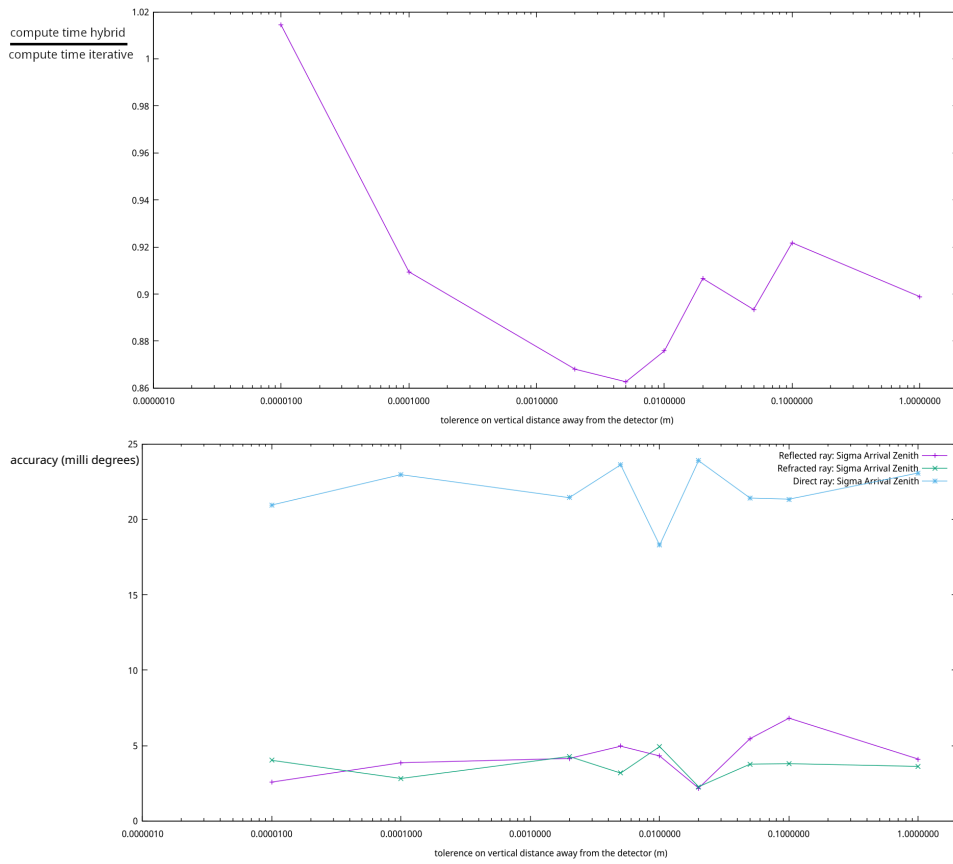


Figure 5.8: influence of the tolerance on vertical distance

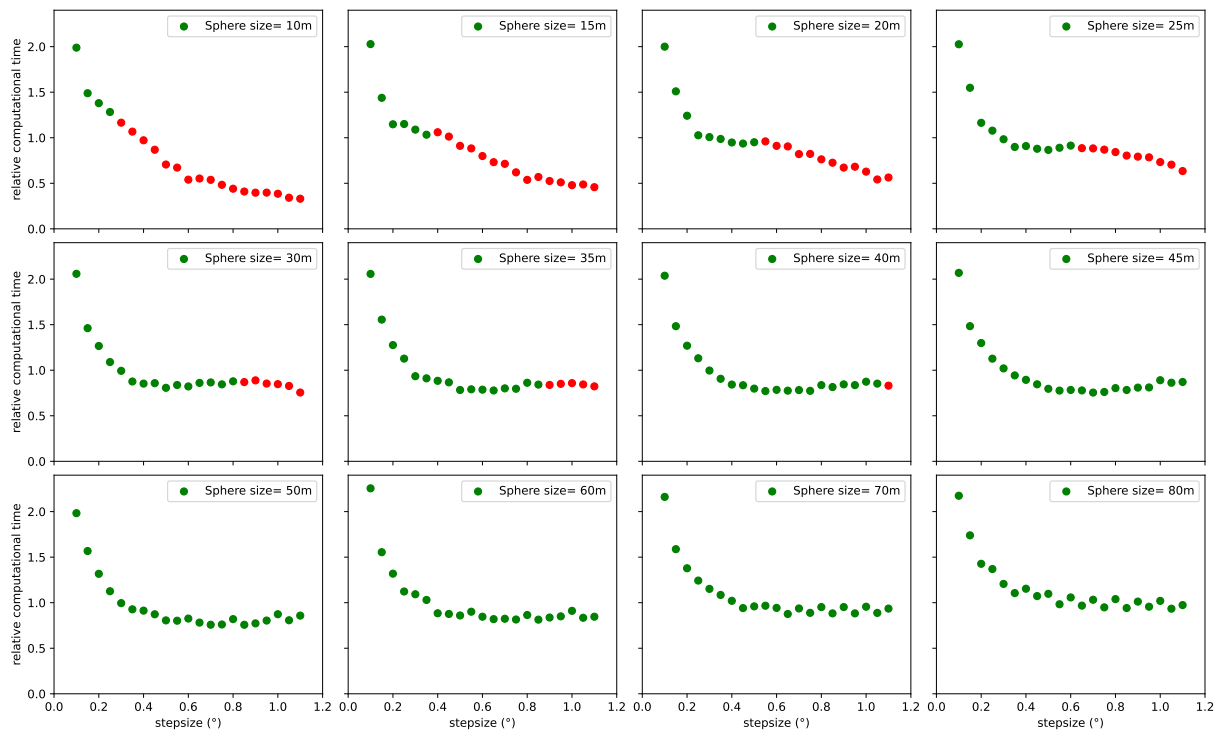


Figure 5.9: Variation in Sphere and angle step size with report on relative time.

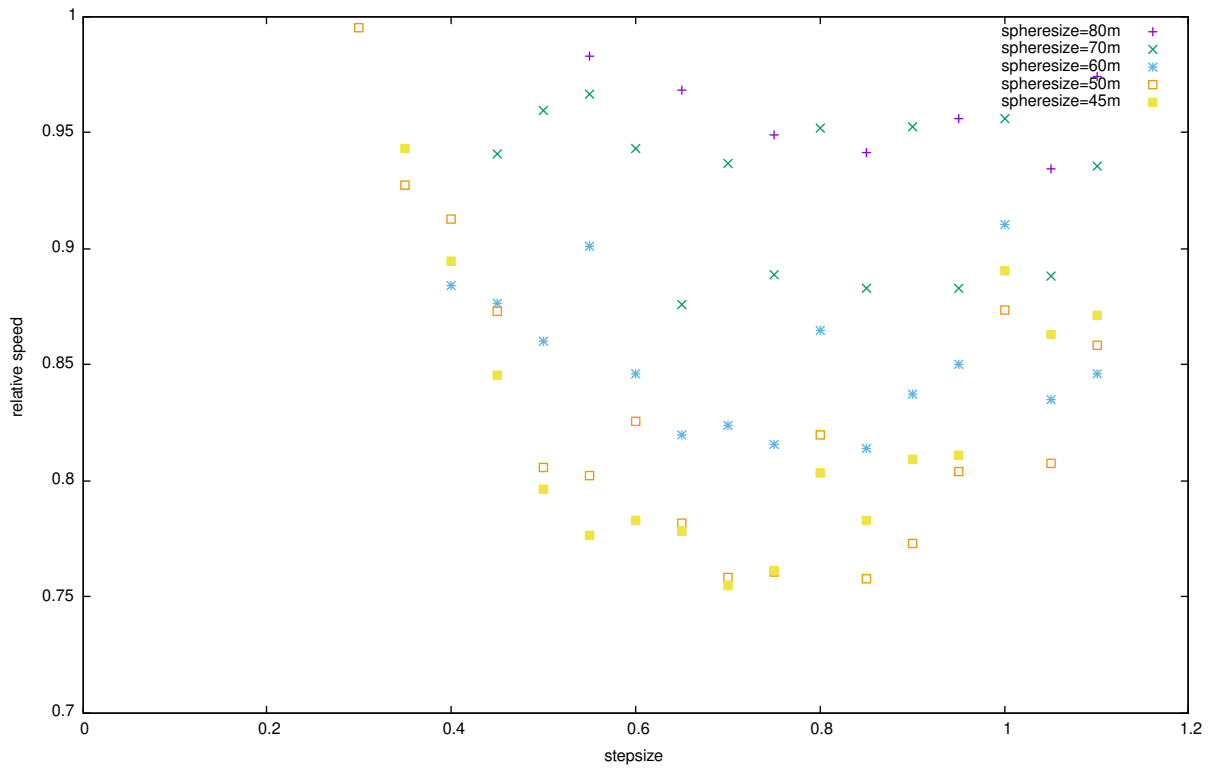


Figure 5.10: Green values in variation in sphere and angle step size with report on relative time.

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