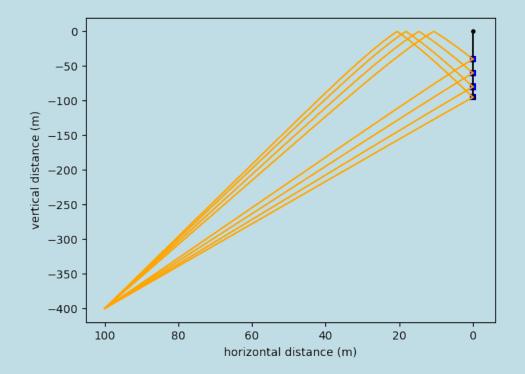


Radio detection of high energy neutrinos in the Greenland icecap

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1

FOREWORD

1.1 Abstract: English

The Radio Neutrino Observatory in Greenland - RNO-G - is under construction at Summit Station in Greenland to search for neutrinos of several PeV energy up to the Eev range. It's a mid-scale, discovery phase, extremely high-energy neutrino telescope that will probe the astrophysical neutrino flux at energies beyond the reach of IceCube. More particularly if will make it possible to reach the next major milestone in astroparticle physics: the discovery of cosmogenic neutrinos. All simulations carried out within this work were made with the three

programs

- NuRadioMC
- radiotools
- RadioPropa

whom are free to download on github. The projects built over the course of this thesis were the "Hybrid minimizer": a new algorithm for finding the path of a neutrino interaction to the detector in complex ice models and (...)

1.2 Abstract: Nederlands

De Radio Neutrino Observatory in Greenland - RNO-G - is een detector die momenteel onder constructie is in Groenland. Deze detector heeft als doel het vinden van neutrino's met energieën van enkele PeV tot in het EeV gebied. Deze extreem hoge energy neutrino telescoop zal astrofysische neutrinos zoeken op energieën waar icecube te klein voor is. Het zal ook het vinden van cosmogenische neutrinos mogelijk maken. Alle simulaties werden mogelijk gemaakt door de volgende programmas:

• NuRadioMC

- ullet radiotools
- RadioPropa

Dewelke te downloaden zijn op github De projecten die tot completie zijn gebracht over deze master thesis waren de *Hybrid minimizer*: een algoritme gemaakt met als doel het snel vinden van een pad vanuit de interactievertex tot de detector in complexe ijsmodellen en (...)

2

NEUTRINOS

When looking outside into the night sky you might see various stars, but invisible to the naked eye various kinds of particles are also transversing light-years to end up where you stand.

When looking at phenomena outside our earth the astronomer will turn to electromagnetic radiation, as a lot of the most interesting events emit photons in some kind of way this is very useful but he's missing out on a big part of the full picture. That's where the astroparticle physicist comes in who takes a look at muons, nuclei,... and even neutrinos.

Neutrinos are ideal messengers to identify sources of ultra high energy (UHE) cosmic rays in the universe. They also interact very weakly making it possible for them to traverse large distances unhindered. To fully grasp how little they interact consider that on average 100 trillion neutrinos pass through your body per second, none of them having any effect. You'd also need a light year of lead to give you a 50% chance of stopping a neutrino.

2.1 Discovery

When researching beta decay, the decay of a neutron, researcher detected a proton and an electron coming from the neutron. However on closer inspection it became apparent that energy was lost somewhere in violation with the conservation law of energy, and angular momentum wasn't conserved. The solution postulated by Wolfgang Pauli was to introduce a new, really hard to detect particle: the neutrino. The neutrino comes in three flavours: electron, muon and tau neutrinos, each corresponding to their respective lepton and each again having an antiparticle as to make it possible to conserve lepton number. Now with the introduction of the neutrino the full beta decay becomes

$$n \to p^+ + e^- + \nu_e$$
 (2.1)

2.2 Neutrino sources

2.3 Do neutrinos have mass?

Neutrinos get produced through the following ways in the nucleus of our star: $\mathbf{pp} - \mathbf{cycle}$

$$p + p \to D + e^+ + \nu_e \tag{2.2}$$

$$D + p \to {}^{3}He + \gamma \tag{2.3}$$

$${}^{3}\text{He} + {}^{3}\text{He} \rightarrow {}^{4}\text{He} + p + p$$
 (2.4)

boron - cycle

$$^{4}\text{He} + ^{3}\text{He} \rightarrow ^{7}\text{Be} + \gamma$$
 (2.5)

$$^{7}\text{Be} + p \rightarrow ^{8}\text{B} + \gamma$$
 (2.6)

$$^{8}\text{B} \to {}^{8}\text{Be}^{*} + e^{+} + \nu_{e}$$
 (2.7)

$${}^{8}\text{Be}^{*} \rightarrow {}^{4}\text{He} + {}^{4}\text{He}$$
 (2.8)

Be-capture

$$^{7}\text{Be} + e^{-} \rightarrow ^{7}\text{Li} + \nu_{e} \tag{2.9}$$

pep

$$p + e^- + p \to D + \nu_e \tag{2.10}$$

Now with this and some information about the sun like the pressure and mass, the so-called "standard solar model" was made. This model predicted a certain amount of neutrinos to be hitting the earth from the previously mentioned thermonuclear fusion, it was however 3 times higher than the observed amount of neutrinos back at our planet. Through various experiments it became apparent that this was due to the various kind of neutrinos oscillating into each other, i.e 2/3 of the original electron neutrinos had oscillated into mu and tau neutrinos but for them to oscillate into eachother, they require mass:

2.3.1 neutrino oscillations

So the transition probability is

$$P(\nu_e \to \nu_\mu) = |\langle \nu_\mu | \psi(L, T) \rangle|^2 = c_\mu c_\mu^* = \sin^2(2\theta) \sin^2\left(\frac{\Delta \phi_{12}}{2}\right)$$
 (2.11)

with

$$\Delta\phi_{12} \approx \frac{m_1^2 - m_2^2}{2p}L\tag{2.12}$$

I.e not only mass but difference in mass of the eigenstates is a requirement for oscillations to occur. In general

$$|\nu_{\alpha}\rangle = \sum_{i} U_{\alpha i} |\nu_{i}\rangle \tag{2.13}$$

With $U_{\alpha i}$ e.g the Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix. This phenomenon has been observed e.g from the descrepency from the observed and expected neutrino events coming from a nuclear reactor [5]. Now the question remains, how do neutrinos get their mass (theoretically)?

2.3.2 See-saw mechanism

We can give neutrino's mass as with any other spinor throught Yukawa couplings and an extra term:

$$\mathcal{L} = i\bar{\nu}\partial \!\!\!/ \nu - m\bar{\psi}\nu - \frac{M}{2}(\bar{\nu}_R \nu_{Rc} + \bar{\nu}_{Rc}\nu_R)$$
 (2.14)

More general, given a spinor ψ with the following Lagrange density:

$$\mathcal{L} = i\bar{\psi}\partial\psi - m\bar{\psi}\psi - \frac{M}{2}(\bar{\psi}_R\psi_{Rc} + \bar{\psi}_{Rc}\psi_R)$$
(2.15)

We can re-write this Lagrangian in terms of

$$\chi := \frac{1}{\sqrt{2}}(\psi_R + \psi_{Rc}) \tag{2.16}$$

$$\omega := \frac{1}{\sqrt{2}}(\psi_L + \psi_{Lc}) \tag{2.17}$$

by first identifying that

$$-\frac{M}{2}(\bar{\psi}_R\psi_{Rc} + \bar{\psi}_{Rc}\psi_R) \tag{2.18}$$

is equal to

$$-M\bar{\chi}\chi = -\frac{M}{2}(\bar{\psi}_R + \bar{\psi}_{Rc})(\psi_R + \psi_{Rc}) = -\frac{M}{2}(\bar{\psi}_R\psi_{Rc} + \bar{\psi}_{Rc}\psi_R)$$
(2.19)

Where we've used

$$\bar{\psi}_R \psi_R \equiv \psi_R^{\dagger} \gamma^0 \psi_R \equiv P_R \psi^{\dagger} \gamma^0 P_R \psi = P_R P_L \psi^{\dagger} \gamma^0 \psi = 0 \tag{2.20}$$

And next that in

$$i\bar{\psi}\partial\psi - m\bar{\psi}\psi = i\bar{\psi}_R\partial\psi_R + i\bar{\psi}_L\partial\psi_L - m\bar{\psi}_R\psi_L - m\bar{\psi}_L\psi_R \tag{2.21}$$

We can identify that

$$\bar{\chi}\partial \chi = \frac{1}{2}(\bar{\psi}_R \partial \psi_R + \bar{\psi}_{Rc} \partial \psi_{Rc}) = \bar{\psi}_R \partial \psi_R$$
 (2.22)

$$\bar{\omega}\partial\omega = \bar{\psi}_L\partial\psi_L \tag{2.23}$$

Where we've done an integration by parts and used $\bar{\psi}_c \gamma_\mu \chi_c = -\bar{\chi} \gamma_\mu \psi$. We thus get:

$$\mathcal{L} = i\bar{\chi}\partial \chi + i\bar{\omega}\partial \omega - m\bar{\psi}_R\psi_L - m\bar{\psi}_L\psi_R - M\bar{\chi}\chi$$
 (2.24)

And finally we notice that

$$\bar{\chi}\omega = \frac{1}{2} \left(\bar{\psi}_R \psi_L + \bar{\psi}_R \psi_{Lc} + \bar{\psi}_{Rc} \psi_L + \bar{\psi}_{Rc} \psi_{Lc} \right)$$
 (2.25)

$$= \frac{1}{2} \left(\bar{\psi}_R \psi_L + \bar{\psi}_R \psi_{Lc} + \bar{\psi}_{Rc} \psi_L + \bar{\psi}_L \psi_R \right)$$
 (2.26)

$$\bar{\omega}\chi = \frac{1}{2} \left(\bar{\psi}_L \psi_R + \bar{\psi}_{Lc} \psi_R + \bar{\psi}_L \psi_{Rc} + \bar{\psi}_{Lc} \psi_{Rc} \right) \tag{2.27}$$

$$=\frac{1}{2}\left(\bar{\psi}_L\psi_R + \bar{\psi}_{Lc}\psi_R + \bar{\psi}_L\psi_{Rc} + \bar{\psi}_R\psi_L\right) \tag{2.28}$$

As $\bar{\psi}_c \chi_c = \bar{\chi} \psi$. Summing these, we get:

$$\bar{\chi}\omega + \bar{\omega}\chi = \bar{\psi}_L\psi_R + \bar{\psi}_R\psi_L \tag{2.29}$$

$$+\frac{1}{2}\left(\bar{\psi}_R\psi_{Lc} + \bar{\psi}_{Rc}\psi_L + \bar{\psi}_{Lc}\psi_R + \bar{\psi}_L\psi_{Rc}\right) \tag{2.30}$$

$$= \bar{\psi}_L \psi_R + \bar{\psi}_R \psi_L \tag{2.31}$$

Where we've used the handedness flips a charge conjugation entails, at last we now have:

$$\mathcal{L} = i\bar{\chi}\partial \chi + i\bar{\omega}\partial \omega - m(\bar{\chi}\omega + \bar{\omega}\chi) - M\bar{\chi}\chi \tag{2.32}$$

Now to determine the mass eigenstates we'll re-write this equation into the form

$$\mathcal{L} = i\bar{\chi}\partial \!\!\!/ \chi + i\bar{\omega}\partial \!\!\!/ \omega - \left(\begin{array}{cc} \bar{\chi} & \bar{\omega} \end{array}\right) \cdot \left(\begin{array}{cc} M & m \\ m & 0 \end{array}\right) \cdot \left(\begin{array}{cc} \chi \\ \omega \end{array}\right)$$
 (2.33)

lets now find the eigenvalues:

$$\begin{vmatrix} M - \lambda & m \\ m & -\lambda \end{vmatrix} = (\lambda - M)\lambda - m^2 = 0 \implies \lambda_{\pm} = \frac{M \pm \sqrt{M^2 + 4m^2}}{2}$$
 (2.34)

i.e

$$\lambda_{\pm} = \frac{M}{2} \left(1 \pm \sqrt{1 + 4m^2/M^2} \right) \tag{2.35}$$

Now we'll determine the eigenvectors:

$$\begin{bmatrix} M - \lambda_{\pm} & m \\ m & -\lambda_{\pm} \end{bmatrix} \begin{pmatrix} x_{\pm} \\ y_{\pm} \end{pmatrix} = \vec{0}$$
 (2.36)

this gives

$$Mx_{\pm} - \lambda_{\pm}x_{\pm} + my_{\pm} = 0 \tag{2.37}$$

$$mx_{\pm} - \lambda_{\pm}y_{\pm} = 0 \implies \frac{mx_{\pm}}{\lambda_{+}} = y_{\pm} \tag{2.38}$$

inserting the second equation in the first we get:

$$Mx_{\pm} - \lambda_{\pm}x_{\pm} + m\frac{mx_{\pm}}{\lambda_{+}} = 0 = M\lambda_{\pm}x_{\pm} - \lambda_{\pm}^{2}x_{\pm} + m^{2}x_{\pm}$$
 (2.39)

$$= x_{\pm}(\lambda_{\pm}^2 - M\lambda_{\pm} + m^2) \tag{2.40}$$

which is true for every x_{\pm} (see equation 2.34) i.e we can freely choose x_{\pm} so let's opt for $x_{\pm}^2 + y_{\pm}^2 = 1$:

$$x_{\pm}^{2}(1+\frac{m^{2}}{\lambda_{\pm}^{2}}) = 1 \implies x_{\pm}^{2} = \frac{1}{1+\frac{m^{2}}{\lambda_{+}^{2}}} \implies x_{\pm} = \frac{\lambda_{\pm}}{\sqrt{\lambda_{\pm}^{2}+m^{2}}}$$
 (2.41)

$$\& y_{\pm} = \frac{m}{\sqrt{\lambda_{\pm}^2 + m^2}} \tag{2.42}$$

And thus, summing up, we get the eigenvectors ϕ_{\pm} with eigenvalues m_{\pm} :

$$\phi_{\pm} := \begin{pmatrix} x_{\pm} \\ y_{\pm} \end{pmatrix} = \begin{pmatrix} \frac{\lambda_{\pm}}{\sqrt{\lambda_{\pm}^2 + m^2}} \\ \frac{m}{\sqrt{\lambda_{+}^2 + m^2}} \end{pmatrix} \quad \text{and} \quad m_{\pm} := \lambda_{\pm} = \frac{M}{2} \left(1 \pm \sqrt{1 + 4m^2/M^2} \right)$$
 (2.43)

Now we'll consider the limit $M \gg m$:

$$m_{\pm} = \frac{M}{2} \left(1 \pm \sqrt{1 + 4m^2/M^2} \right) \approx \frac{M}{2} \left(1 \pm 1 \pm \frac{2m^2}{M^2} \right)$$
 (2.44)

Which gives:

$$m_{+} \approx M \tag{2.45}$$

$$m_{-} \approx -\frac{m^2}{M} \tag{2.46}$$

and:

$$\phi_{+} \approx \begin{pmatrix} \frac{M}{M} \\ \frac{m}{M} \end{pmatrix} = \begin{pmatrix} 1 \\ m/M \end{pmatrix} \tag{2.47}$$

$$\phi_{-} \approx \begin{pmatrix} -\frac{m}{M} \\ \frac{m}{m} \end{pmatrix} = \begin{pmatrix} -m/M \\ 1 \end{pmatrix} \tag{2.48}$$

i.e, in the χ, ω basis:

$$m_{+} \approx M$$
 with eigenstate $\chi + \frac{m}{M}\omega$ (2.49)

$$m_{-} \approx -\frac{m^2}{M}$$
 with eigenstate $\omega - \frac{m}{M}\chi$ (2.50)

(2.51)

This is what's called the See-Saw mechanism, it's both a theory of giving mass to neutrinos and explaining their small mass. For a certain m if we choose a big M we'll get a big m_+ and small m_- (and vice versa). We also see that there's only a very small mixing of states, i.e the m_- mass state is almost purely ω (and m_+ almost purely χ). The parameter m in the original matrix is forbidden by electroweak gauge symmetry, and can only appear after the symmetry has been spontaneous broken by a Higgs mechanism; for this reason a good estimate of the order of m is the vaccuum expectation energy: $m \approx v = 246 \approx 10^2 \text{GeV}$. In grand unified theories it's theorised that $M \approx 10^{15} \text{GeV}$ after symmetry breaking, using these values we get

$$m_{-} \approx 10^{-11} \text{GeV} \approx 10^{-2} \text{eV}$$
 (2.52)

which seems [2] to be a reasonable order of magnitude estimate for the observed neutrino mass. This mechanism would also lead to supermassive neutrinos, which are a possible dark matter candidate.

2.3.3 Majorana fermions

A theory that's also quite interesting is that neutrinos are majorana, a dirac fermion has the following density:

$$\mathcal{L} = i\bar{\psi}\partial \psi - m\bar{\psi}\psi \tag{2.53}$$

$$= i\bar{\psi}_L \partial \psi_L + i\bar{\psi}_R \partial \psi_R - m\bar{\psi}_R \psi_L - m\bar{\psi}_L \psi_R \tag{2.54}$$

Now assume that we only have right-handed particles:

$$\mathcal{L} = i\bar{\psi}_R \partial \psi_R - \frac{M}{2}\bar{\psi}_R \psi_{Rc} - \frac{M}{2}\bar{\psi}_{Rc}\psi_R \tag{2.55}$$

A majorana fermion is a fermion which is it's own anti-particle, i.e:

$$\chi = \frac{1}{\sqrt{2}} \left(\psi_R + \psi_{Rc} \right) = \chi_c \tag{2.56}$$

With this we have that

$$\bar{\chi}\chi = \frac{1}{2} \left(\bar{\psi}_R \psi_{Rc} + \bar{\psi}_{Rc} \psi_R \right) \tag{2.57}$$

Which we can recognize in 2.55 and

$$\bar{\chi}\partial \chi = \frac{1}{2}(\bar{\psi}_R + \bar{\psi}_{Rc})\partial (\psi_R + \psi_{Rc})$$
(2.58)

$$= \frac{1}{2}\bar{\psi}_R \partial \psi_R + \frac{1}{2}\bar{\psi}_{Rc} \partial \psi_{Rc} \tag{2.59}$$

$$= \bar{\psi}_R \partial \psi_R \tag{2.60}$$

where we've used integration by parts at the end, with these we can re-write 2.55 as:

$$\mathcal{L} = i\bar{\chi}\partial \chi - M\bar{\chi}\chi \tag{2.61}$$

Thus arriving at a density for Majorana fermions with mass M, a possible detection mechanism to find out if neutrinos are Majorana is "Neutrinoless double beta decay":



Figure 2.1: normal and neutrinoless double beta decay

This is (at the time of writing) actively investigated.

2.4 Why study neutrinos?

Neutrinos are ideal messengers to identify the UHE (Ultra High Energy) sources in the universe. Unlike cosmic rays, which are deflected by magnetic fields and interact with matter and radiation on their way to us, neutrinos point back to sources and can reach Earth unperturbed from the most distant corners of the universe. Neutrinos can be generated in 2 ways: either they're generated in interactions at the sources, termed astrophysical neutrinos. Or they're created through the interaction of ultra-high energy cosmic rays during propagation with the cosmic microwave or other photon backgrounds termed cosmogenic neutrinos.

2.4.1 astrophysical neutrinos: general

As cosmic rays get accelerated they will occasionally interact with matter and photon fields near the source. These will then produce new particles, of which the most common is pions due to their low mass (a lot of available phase space). As seen in chapter ?? pions can decay into neutrino's as follows:

$$\pi^- \to \mu^- + \bar{\nu}_{\mu} \to e^- + \bar{\nu}_e + \nu_{\mu} + \bar{\nu}_{\mu}$$
 (2.62)

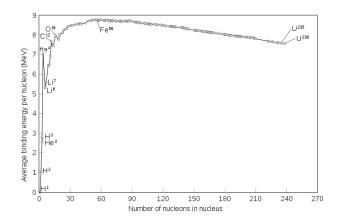
$$\pi^+ \to \mu^+ + \nu_\mu \to e^+ + \nu_e + \bar{\nu}_\mu + \nu_\mu$$
 (2.63)

Another possibility is direct production of neutrino's at the source, of which Supernovae are a prime example:

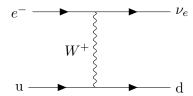
2.4.2 Supernovae

A star starts its life as a ball of pure hydrogen. At the core, due to the gravitational pressure of the outside plasma, fusion of hydrogen into deuterium and helium happens. Thus converting mass into energy. The pressure of this energy counteracts the pressure of gravity and the star is stable.

When the hydrogen at the core runs out no more hydrogen can be fused. For stars with masses between $8M_{\odot}$ and $30M_{\odot}$ the fusion of heavier elements starts, this can't keep going on however



as at some point the star starts to form the most stable element: iron. It costs energy to both make lighter elements than iron and heavier ones. As the iron core builds up the outside pressure from the core starts to decrease as no new energy is released. This goes on until the treshold of an iron core with a mass of $1.4M_{\odot}$ known as the Chandrasekhar limit and the the inwards pressure becomes too large, making the electrons surrounding the iron core fuse with the protons (uud), creating neutrons (udd) and neutrino's, diagramatically:



This last part happens in a split second as the collapse goes at 25% the speed of light, creating a very dense neutron star (3000km in diameter iron core to 30km in diameter neutron star) and up to 10⁵² ultra-relativistic neutrinos, carrying up to 99% of the released energy [11]¹. As the density has suddenly increased so much there's a huge distance of pure vaccuum between the plasma outer layer and the (now) neutron star, this plasma starts free-falling inwards, also at 25% the speed of light whilst the neutrinos carrying tremendous amounts of energy start going outwards from the neutron stars core.

The neutrinos then collide with the plasma resulting in what we observe as a "supernova", wrongly thought of by Kepler as being a "new (nova) star" rather being a violent death of an old star.

This is quite unexpected as neutrinos rarely interact, they only do becouse the incoming plasma is so dense and due to the tremendous amount of neutrinos that collissions happen at all. Some, however, escape and will be visible on earth in our neutrino detectors \approx 18h before the light escapes the exploding star.

Neutrino observatories are thus useful to know where to point our various telescopes before the supernova is actually visible in the night sky.

2.4.3 primordial neutrinos

Aside from all the previously mentioned sources, there's also a less spectacular source of neutrinos: the neutrino version of the CMB. We can estimate the temperature of the neutrinos

¹1% is released as kinetic energy, only 0.001% as electromagnetic radiation

who decoupled at the start of the universe, for this we can take a look at conservation of entropy [4]

$$T_{\nu} = \left(\frac{4}{11}\right)^{1/3} T_{\gamma} \tag{2.64}$$

2.4.4 How do they fit into the full detector spectrum?

The origin of the most energetic cosmic rays is still not conclusively identified. One approach to solving this problem is *multi-messenger astrophysics*, where several types of cosmic particles are used to identify the sources of these ultra-high energy cosmic rays (UHECRs). E.g we simultaneously measure gravitational waves (gravitons?) with the Einstein telescope, neutrino's with IceCube (or eventually RNO-G), photons with various telescopes and muons with a muon detector.

3

RADIO DETECTION OF NEUTRINOS

3.1 Neutrino interactions in ice

As neutrinos propagate through ice they can interact with nuclei in the following ways [6]:



Figure 3.1: Most prominent ways of neutrino-nucleus interaction

With the produced leptons in the W boson mediated interaction being either electrons, resulting in an electromagnetic shower, muons wich typically go undetected as they live too long or tauons wich will decay via

$$\tau^- \to e^- + \bar{\nu}_e + \nu_\tau \tag{3.1}$$

or, less ideally

$$\tau^- \to \mu^- + \bar{\nu}_\mu + \nu_\tau \tag{3.2}$$

In both of the possible interactions the resulting nucleus will result in a hadronic shower, for the neutral current interaction (mediated by the Z boson) the fraction of the neutrino energy that gets transferred to the nucleon is described by the inelasticity y and is heavily shifted towards small values of y [1]. This causes a big, irreducable uncertainty when trying to estimate the original neutrino energy from these kinds of events. With the charged current interaction (mediated by the W^{\pm} bosons) this isn't a problem however as the full neutrino energy ends up in the resulting cascades.

3.2 Askaryan effect

For a particle shower to emit strong radio signals, two conditions have to be met:

- There needs to be a speration of positive and negative charges in the shower front
- The signals produced over the length of the shower profile need to overlap coherently.

The Askaryan [3] effect, also known as Askaryan radiation describes the effect at radio frequencies which abides by both of these conditions, in general it's a quite difficult effect but we'll give a crude overview. The above described interactions create a shower of secondary charged particles containing a charge anisotropy, this charge imbalance is a result of medium electrons either Compton scattering into the advancing shower or annihilating with shower positrons. In the end you have a moving charge anisotropy, propagating faster than the speed of light in the medium, creating Cherenkov radiation. Cherenkov radiation is like the elektromagnetic equivalent of a sonic boom, a sonic boom happens when something goes faster than the sounds speed in the medium; A particle emits Cherenkov radiation if it goes faster than the light speed in the medium¹. Choosing the particle trajectory to lie along the z axis we can approximately find an equation for $\frac{\mathrm{d}^2 \mathscr{J}}{\mathrm{d}\omega \mathrm{d}\Omega}$: the energy radiated per elementary unit solid angle and per elementary unit frequency interval

$$\frac{\mathrm{d}^2 \mathscr{J}(\omega)}{\mathrm{d}\omega \mathrm{d}\Omega} = \frac{q^2}{4\pi} \sqrt{\frac{\mu}{\epsilon}} \beta^2 \omega^2 \delta^2 [\omega (1 - \beta \mathbf{e}_r \cdot \mathbf{e}_z)] |\mathbf{e}_r \times \mathbf{e}_z|^2$$
(3.3)

Now we can re-write this equation in spherical coordinates, which gives $1 - \beta \mathbf{e}_r \cdot \mathbf{e}_z = 1 - \beta \cos(\theta_c)$ in the delta function. We thus only expect radiation if

$$\cos(\theta_c) = \frac{1}{\beta} = \frac{c'}{u} = \frac{c}{n} \cdot \frac{1}{u}$$
(3.4)

I.e if $u > \frac{c}{n}$ with n the index of refraction, Cherenkov radiation will be emitted along a cone surface with half angle $\frac{\pi}{2} - \theta_c$ as illustrated in figure 3.3. Integrating equation 3.3 over the solid angle and formally deviding by the time interval we get:

$$\frac{\mathrm{d}^2 \mathscr{J}}{\mathrm{d}\omega \mathrm{d}t} = \frac{q^2}{4\pi} \sqrt{\frac{\mu}{\epsilon}} \beta \omega \left(1 - \frac{1}{\beta^2} \right) \tag{3.5}$$

We see that the energy is proportional to ω , so we expect that most radiation will be emitted "in blue", as seen in figure 3.2. For ice the index of refraction is roughly 1.78 in deep ice, so we expect an ultra-relativistic particle to produce the most radiation at around 56° opening as

$$\cos(\theta_c) \approx \frac{1}{n} \implies \cos^{-1}\left(\frac{1}{1.78}\right) \approx 56^{\circ}$$
 (3.6)

Of course this is just an estimate, as the actual index of refraction is depth-dependent which we'll get to in section (...). Now this explains how the signals get generated but logically, from only knowing this we'd expect radio waves to almost be non-existent due to the "in blue" nature of Cherenkov radiation. This isn't the full story however as we'll need to talk about coherent overlap to fully understand the Askaryan effect. This can be intuitively explained as follows: generally the shower is of length $\mathcal{O}(10\text{cm})$ [10], over this length the radiation gets emitted, most frequencies decoherently interfering, but radio waves with wavelengths of $\approx 10\text{cm}$ coherently interfere, and it's these waves we then wish to detect.

¹The reader who wants a thorough explanation and derivation is advised to check out *Chapter 14: Radiation by Moving Charges* from the book *Classical Electrodynamics* by Jackson.

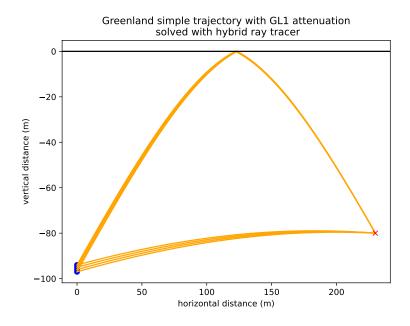


Figure 3.2: Cherenkov radiation in a nuclear reactor

Figure 3.3: Diagrammatic representation of Cherenkov radiation

3.3 Wave propagation

Waves propagating through ice to a detector generally looks something like this:



Here the interaction of the neutrino happens somewhere in the neighbourhood of the red cross, the orange rays represent the resulting radio wave paths to the detectors which are signaled by the blue dot. Notice that reflection at the surface is also a possible path to the detector. In a homogeneous dielectric medium a ray propagates straight with it's signal wave-speed determined by the local index of refraction as v = c/n, the dependence of the index of refraction on density for ice is given by the Schytt equation:

$$n(x, y, z) \approx 1 + 0.78\rho(x, y, z)/\rho_0$$
 (3.7)

Where $\rho(x, y, z)$ is the local ice density and ρ_0 is the density for solid ice (917 kg/m³). This isn't the only part of the index of refraction with which we'll need to concern ourselves however. If a ray propagates towards a boundary dividing 2 media with different indexes of refraction, the

ray will refract and the refracted angle can be found from Snell's law:

$$n_1 \sin \theta_1 = n_2 \sin \theta_2 \tag{3.8}$$

Where n is the index of refraction and θ is the angle with respect to the surface. The system we'll consider however, isn't homogeneous with some specified boundary, it's continuous: ice in greenland has a continuously varying density. Because of this we can't work with Snell's law but we'll have to take a look at the continuous version to figure out how these rays propagate. The "continuous version of Snell's law" is the eikonal equation: a path of a ray $\mathbf{r}(s)$ with path parameter s in a medium with index of refraction $\mathbf{n}(\mathbf{r})$ is described by:

$$\frac{d}{ds}\left(n(\mathbf{r})\frac{d\mathbf{r}}{ds}\right) = \nabla n\tag{3.9}$$

The software we'll be using for ray reconstruction is called "radiopropa" [15] and in radiopropa the local paraxial approximation is used, i.e. if we assume that in any individual step of the algorithm the change of the refractive index along the path ds is small it's possible to re-write the equation as:

$$n(\mathbf{r})\frac{d^2\mathbf{r}}{ds^2} \approx \nabla n$$
 (3.10)

Which is then easily iteratively solved. If there are boundaries (such as defects or the surface) these are treated seperately using Snell's law.

3.4 Ice model

Equation 3.10, and thus the path, depends on the index of refraction on a given location. Purely from classical gravity and density considerations it can be derived that the index of refraction abides by

$$n(z) = n_{ice} - \Delta n e^{z/z_0} \tag{3.11}$$

with n_{ice} the refractive index of solid ice and $\Delta n = n_{ice} - n_s$ with n_s the index of refraction of snow. This is called "the exponential model".

From the measured density with depth variation this seems to roughly hold but it could be better (as will be explained in chapter (TBC)). This exponential model has a huge advantage as it's analytically solvable, meaning that we don't have to iteratively search for the path to the detector but know it instantly after the location of the neutrino interaction and the detector are specified, this "model" is called the *analytic ray tracer*.

3.5 Reconstruction

It can pose a challenge to reconstruct the radio signals produced by the Cherenkov radiation as they are often obscured by background noise. A solution used in RadioReco is Information Field Theory (IFT) implemented in RadioReco by Welling et al. [13] which uses Bayesian inference to calculate the most likely radio signal, given recorded data. The full reconstruction will then work as follows: events and their propagation are generated in a monte-carlo simulation using NuRadioMC [8] [7], how the detector signals would look like is then simulated with RadioReco and saved in a database. If we then detect a neutrino event in the real detector it can be compared to the database, thus finding the origin.

4

THE DETECTOR

Both cosmic ray and neutrino detectors face the same main problem at the highest energies: the steeply falling flux (as can be seen on figure 4.1) requires large effective areas, which leads to the construction of neutrino detectors with volumes on the cubic kilometer scale: IceCube. As we wish to detect neutrino's with even higher energies we turn to look at an array of detectors spanning multiple cubic kilometers: RNO-G.

One such detector is illustrated in figure 4.2.

The deep component of the detector can be split up in three parts: Two *helper strings*, one *power string* and the surface components. The helper strings are the 2 vertical cables shown on the right of the figure and each one houses 2 vertically polarized antennas (Vpols), one quadslot antenna for the horizontal polarization component (Hpol) and one radio pulser on each helper string which can be used to generate calibration signals.

The power string (the leftmost vertical cable) is more densely instrumented: At the bottom it houses a set of four Vpol and two Hpol antennas with a spacing of 1m and further up the string, with a spacing of 20m are three more Vpol antennas.

The signal from each of these antennae are fed into a low-noise amplifier directly above it, from there the signal is send to the data acquisition (DAQ) system at the surface via a Radio Frequency over Fiber (RFoF) cable. There it's again amplified, digitized and saved onto an SD card. This data is then transmitted via a Long Term Evolution (LTE) telecommunications network to a local server¹, from where it is sent via a sattelite link.

There are solar panels as a power source who charge up battery banks, but as there is't enough light during the Greenland winters, there're plans to build wind turbines (with the problem being the possibly detectable RF noise the 'engine' produces)

¹There is additionally a Long Range Wide Area Network (LoRaWAN) antenna as backup in case of problems with the LTE network

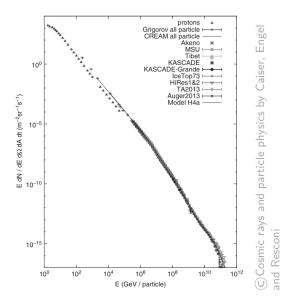


Figure 4.1: Falling cosmic ray flux with energy

The radio signal from a neutrino often travels along both direct and refracted paths (designated DnR) to the deep array, this happens because the upper ice layer is a non-uniform medium where the signal trajectory is bent, as illustrated by a simulation in figure 4.3.

This double pulse characteristic would be a smoking-gun signature of an in-ice source. The two helper strings are needed for a full direction reconstruction. Three independent measurements are needed for azimuthal information, which is provided by the Vpol (Vertical polarization) antennas and placing the Hpol (Horizontal polarization) antennas at different depths on every string, both zentih and azimuth information will be provided for those signals. The helper strings' calibration pulsers, as well as one on the surface, will ensure regular monitoring of the performance of the station and provide information useful for precise calibration of the antenna geometry.

The plan is to construct these detectors in an array as shown in figure 4.4, note that all the individual detectors are named after various species living in greenland (in the native tongue).

Christoph Welling did an investigation into energy reconstruction from the received signals [14] for air showers in one single station (as the RNO-G stations are so far apart this is the case here aswell) and he noticed that it is nescessary to know if the detector who observes an event falls inside or outside the Cherenkov cone to accurately reconstruct the primary particle energy as most over-estimated energies in his simulations are caused by events viewed from within the Cherenkov ring being mistaken for events outside of it. He went on to show that, if we somehow know if the shower was seen from inside or outside the ring from some extra source, that most outliers in the energy disappeared. It is shown by Hiller et al. [9] that the combination of a muon detector with the radio detector might make the issue of confusion between being within or outside of the Cherenkov-ring disappear. Because of this the RNO-G stations are fitted with surface Log Periodic Dipole Antennas (LPDA), capable of detecting muons. Note that this is for air showers, the radio signal from neutrinos show additional complexities.

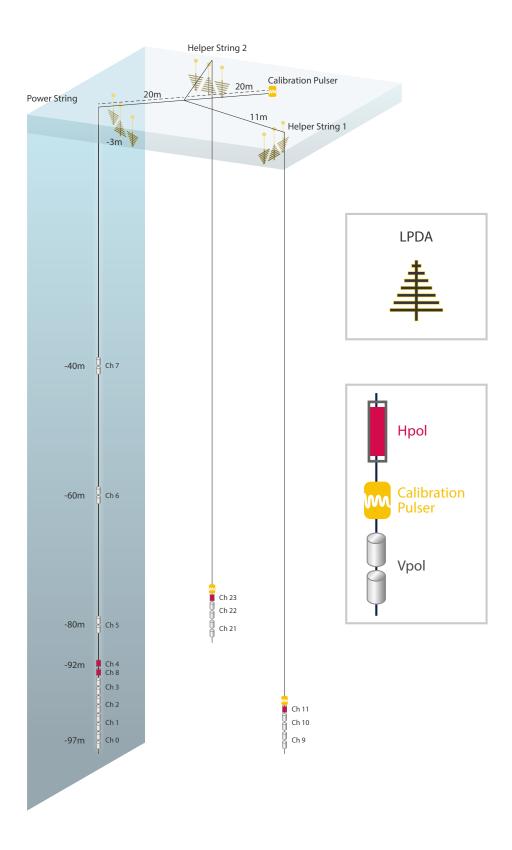


Figure 4.2: illustration of the detector

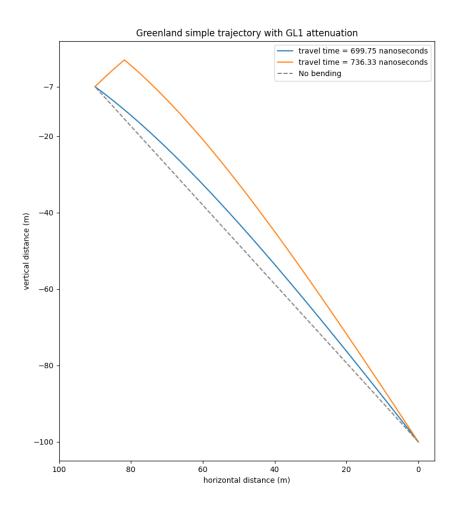
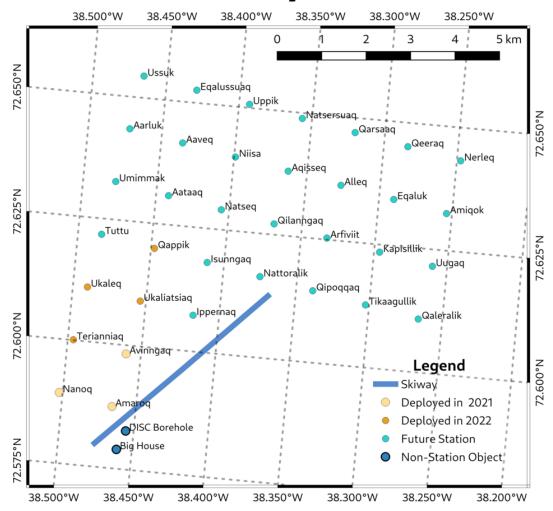


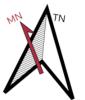
Figure 4.3: illustration of a neutrino signal path, the neutrino interaction being located at (0,-100) and the detector at (90,-7)

RNO-G Planned Layout



Notes:

- Station numbering follows a grid, where the first numeral is in increasing W-E and the second numeral is in increasing S-N, skipping non-existent stations (the Seckel method).
- Station spacing is 1.25 km in map coordinates (but really 1.23 km due to projection, which creates a 2% scale difference.)
- Projection is Greenland Polar Stereographic (EPSG:5938). True north indicated by Rose, offset from grid north by 5.37°.
- Magnetic Declination, for August 1 2022, is -25.2° according to the WMM
- In list below, all future stations labeled as 2023.



v 0.5.1 2022-08-26 68000:1

Greenland Polar Stereographic Projection (EPSG:5938)

Figure 4.4: map of the station

5

HYBRID RAY TRACER

5.1 Shortcomings of the exponential ice model

It has become apparent (TBC) that complex ice models will be nescessary moving forward as the exponential ice model fails to fit the density curve. The ideal software for radio wave propagation through ice is radiopropa [15], but due to the way it works you'll have to know the start point, the end point and the launch angle of your ray to work out the path. This isn't difficult for the analytic model as it's exactly solvable but for a general ice model you'll somehow have to find where to shoot the ray. Work has been done on finding the launch angle in the case of complex ice models by B. Oeyen et al. [12], where they created a ray tracer which iteratively finds the solution, called the "iterative ray tracer". The full explanation of how their algorithm works can be found in the mentioned paper. This is however a sub-optimal solution in python as an optimalisation library will generally work faster, work had been done on trying to implement such an algorithm but this attempt failed. As we saw this work the idea came to mind to combine the iterative ray tracer and the code using the optimisation libraries (a so called "minimizer"), to come up with the algorithm that will be discussed in this chapter: The hybrid ray tracer, in the source code called the "hybrid minimizer".

It succeeds in more rapidly tracing the path from the event to the detector, is more accurate and also arrives closer to the detector as the final result is not limited by the final drawn sphere size but by a given tolerence.

5.2 How it works

The full code can be found in appendix A, here we'll walk you through the algorithm. The hybrid minimizer can be seen as an extension of the iterative raytracer [12] as it starts out the same way: Say our source of radiation is at position \mathbf{X}_1 and our detector is located at position \mathbf{X}_2 , we start by defining the vector $\mathbf{v} = \mathbf{X}_2 - \mathbf{X}_1$, then we clone it as a new vector u and set u's z coordinate to 0, making it a normal vector of a plane parallel to the z direction. we now wish to know where we'd actually be able to find possible paths, looking at figure 4.3 we see that no solutions below the direct path are possible as there would need to be upwards reflection,

so we convert our vector \mathbf{v} representing the path from the source to the detector to spherical coordinates, giving us a polar angle (zenith angle) "theta-direct". With this we know that the, at the source, the ray should propagate with an initial zenith angle within the angle interval 0° to theta-direct° := Ω .

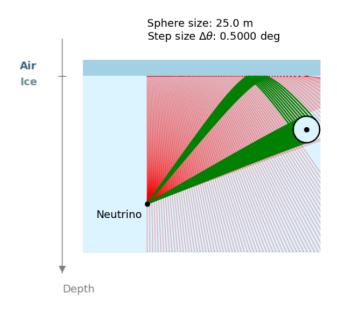
Next we need to define our "observers", if you shoot a ray with the radiopropa module from a certain point at a certain angle the ray path will get simulated until it interacts with this "observer". Ideally we would like to a priori know where to shoot our ray and have the detector be an infinitesimally small observer in our simulation, but as we'll be working with general ice models this can't be done.

The algorithm of finding the possible paths is then as follows: We define a spherical observer at the location of the detector, with a radius of fair size. We place an observer plane directly behind the detector (with normal vector \mathbf{u} , no rays can propagate back after crossing) and an observer above the surface (as no rays could make it back after escaping the ice) our full setup is then what's illustrated in the figure below

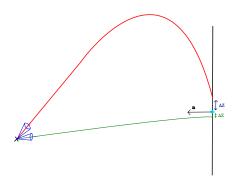


Here the red cross is the radio source, the blue horizontal line is the ice-air boundary surface, the blue dot to the right is the detector and the green Ω indicates the range over which solutions to the problem are possible.

We start off by just iteratively guessing: given a certain angle stepsize $\Delta\theta$ shoot rays at the angles $\{0, \Delta\theta, 2\Delta\theta, ..., \Omega\}$ And see which ones get detected at the sphere around the detector, this process is illustrated in a modified version of B. Oeyen et al. their figure below



if there are 2 distinct launch regions, it will start the so called "minimization", using scipy's module optimize minimize. First we get rid of the spherical observer and place the vertical observer exactly at the detector, now to be able to use the minimize module we'll need a function to minimize, for this reason we define the function $delta_z$ as, given a certain launch angle, returning the distance from the point where it lands on the plane to the detector as illustrated below



The function we'll minimize is then detla_z_squared which is just the square of delta_z as we wish it to be as close as possible to 0, it gets minimized within the angle boundaries found from the previous step. With this our algorithm is done, it does have a fail-safe as well for if the first step, finding the launch regions, doesn't work namely it reverts back to being the iterative ray tracer.

5.3 Performance Optimalisation

To test the hybrid minimizer the numpy random module was used to generate random coördinates, the considered square (as there is only a z component to the ice model the 3D problem is essentially only a 2D problem) is x:0.1km,4km and z:-0.1km,-3km.¹ Every test point shown in the following subsections consists of at least 500 random initial positions. As the speed of the algorithm is computer dependent the algorithm's speed is always plotted relative to the iterative ray tracer's speed, simulated with the same coordinates at the same time.

5.3.1 Length of the normal vector

As visually explained in figure 5.1, the size of the normal vector seems to influence how big the ray tracer's step size is taken close to the detector. This thus influences the convergence and time taken. The results of varying this are shown in figures 5.4 and 5.5. Looking at these figures the first optimization conclusion is as expected: take the normal vector length to be 1 meter.

5.3.2 ztol

We'll now change the tolerence on the vertical distance away from the detector which is deemed accepted i.e in figure 5.1 if Δz is below this threshold it's accepted. The results are shown in figures 5.6 and 5.7. From which we can conclude the second optimization conclusion: take ztol to be 0.05 m.

¹This start at 100m depth was to get around issues concerning events that won't even trigger in a full simulation

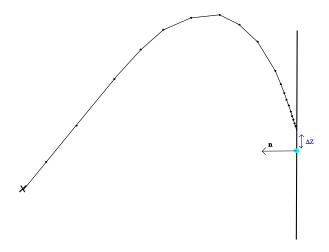


Figure 5.1: how normal vector size influences the stepsize

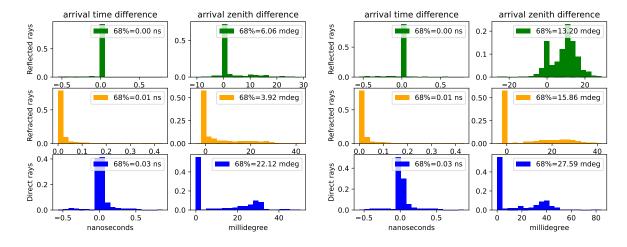


Figure 5.2: Hybrid

Figure 5.3: Iterative

5.3.3 Sphere Size & Step Size

The initial rays are sent out in steps of a certain angle and with a sphere around the detector of a certain size. As this initial search for launch angle regions is the slowest step in the hybrid ray tracer it's imperative to optimize this. The procedure was: change the sphere size and loop over various step sizes, recording the speed. The results are shown in figure 5.8 the lower on the chart the better, zooming in onto the lowest point as is shown in a combined plot on figure 5.9, we see that an optimum seems to be around a spheresize of 45m and a stepsize of 0.7°.

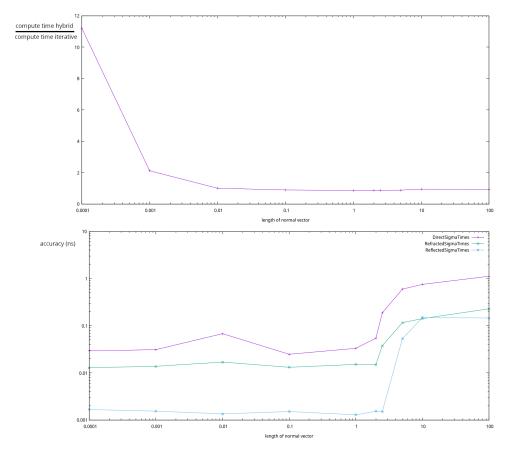


Figure 5.4: influence of the length of the normal vector

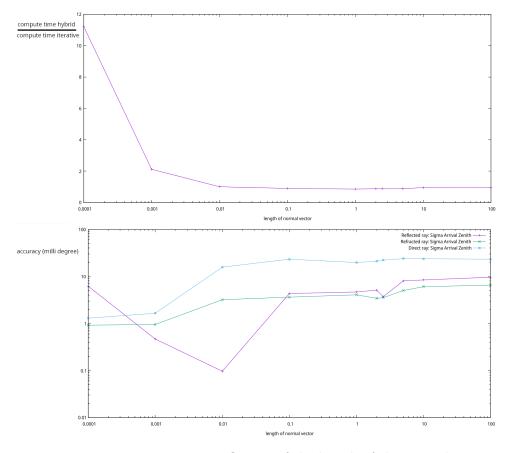


Figure 5.5: influence of the length of the normal vector

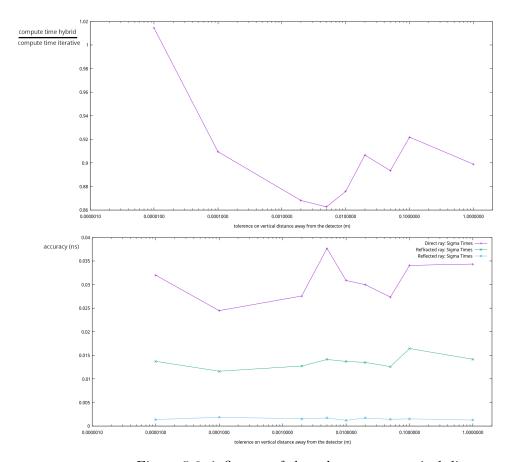


Figure 5.6: influence of the tolerence on vertical distance

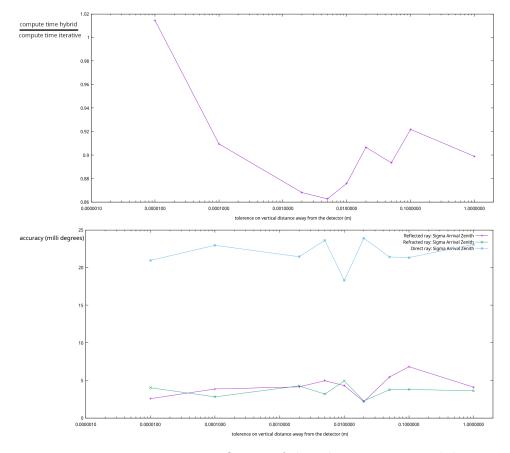


Figure 5.7: influence of the tolerence on vertical distance

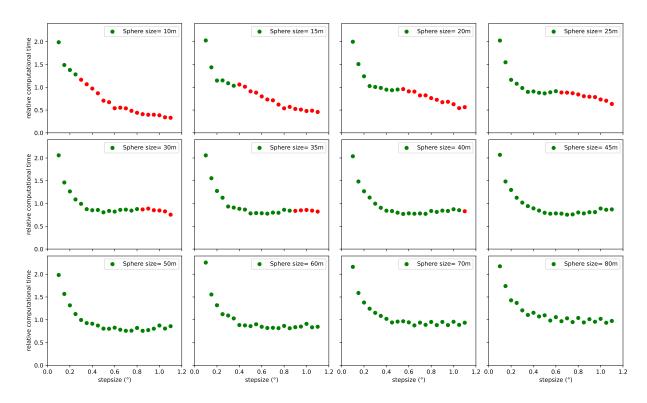


Figure 5.8: Variation in Sphere and angle step size with report on relative time.

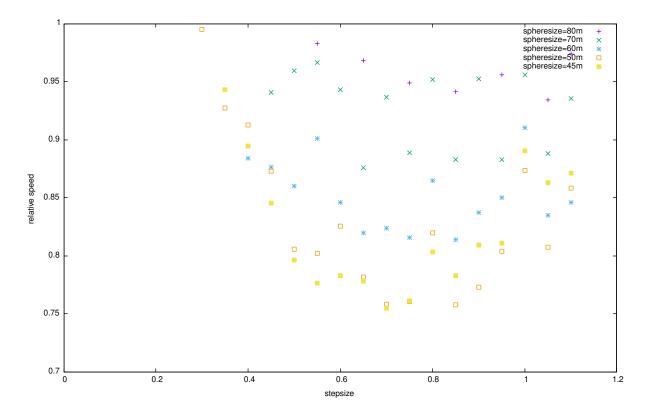


Figure 5.9: Green values in variation in sphere and angle step size with report on relative time.

6

WEATHER BALLOON

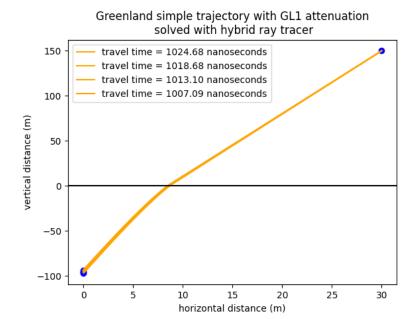
There are some changes that need to be made to the established hybrid minimizer, first off the air observer needs to be hard removed as to make the simulation possible, second off the extra air observer needs to be removed that's additionally defined for some reason and thirdly, the boundary behind the detector is now no longer vertical but horizontal.

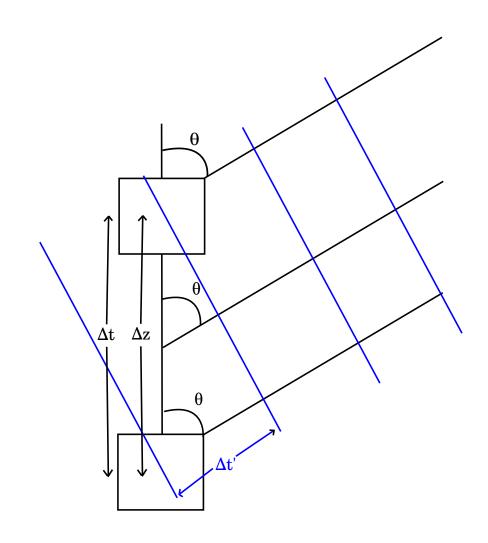
Now having established this the first problem we'll consider is plane wave reconstruction of the original position, an example path to some of the sensors is given in figure (...)

$$\Delta t' = \frac{m}{(m/s)} = (s/m) * m = v^{-1} * m = \frac{c}{n} \cos \theta \Delta z$$
 (6.1)

We take n to be 1.78 as

$$Correlation = \Delta t - \frac{\cos \theta \Delta z}{v} \tag{6.2}$$







APPENDIX

Α

HYBRID MINIMIZER CODE

```
def raytracer_hybrid_minimizer(self,n_reflections=0):
1
2
           Uses RadioPropa to first find all the numerical ray tracing solutions
3
       between sphere x1
           and sphere x2 for a big sphere. After which it uses the scipy
       optimize.minimize module
           to find the best path in these angle intervals.
5
           Tracer does not work for reflective bottoms or secondary creation at the
6
       moment
           11 11 11
7
8
           try:
9
               X1 = self._X1 * (radiopropa.meter/units.meter)
10
               X2 = self._X2 * (radiopropa.meter/units.meter)
11
           except TypeError:
               self.__logger.error('NoneType: start or endpoint not initialized')
13
               raise TypeError('NoneType: start or endpoint not initialized')
15
           def get_ray(theta,phi):
               ray_dir = hp.spherical_to_cartesian(theta,phi)
17
               if ray_dir.shape==(3,1): ray_dir = ray_dir.T[0] #doesn't always give
               → the right shape
               source = radiopropa.Source()
19
               source.add(radiopropa.SourcePosition(radiopropa.Vector3d(*X1)))
20
               source.add(radiopropa.SourceDirection(radiopropa.Vector3d(*ray_dir)))
^{21}
               ray = source.getCandidate()
               return ray
23
           def shoot_ray(theta):
25
               ray = get_ray(theta,phi_direct)
               sim.run(ray, True)
27
               return ray
29
```

```
def cot(x):
              return 1/np.tan(x)
31
          def arccot(x):
33
              return np.arctan(-x) + np.pi/2
35
          def delta_z(cot_theta):
              theta = arccot(cot_theta)
37
              ray = shoot_ray(theta)
              ray_endpoint = self.get_path_candidate(ray)[-1]
39
              return (ray_endpoint-self._X2)[2]
40
41
          def delta_z_squared(cot_theta):
42
              return delta_z(cot_theta)**2
43
44
          def MinimizeAble(lower, upper):
45
               #This checks if there are 2 distinct regions, takes about 10^-6% of
               \hookrightarrow the total time
              if ((len(lower) == 2) and (len(upper)==2)):
47
                  return ((lower[1] > upper[0]) and (lower[0] < upper[0]) and
                   else:
                  return False
50
51
          LetsMinimize = False
52
          v = (self._X2 - self._X1)
54
          u = copy.deepcopy(v)
55
          \mathbf{u}[2] = 0
56
          theta_direct, phi_direct = hp.cartesian_to_spherical(*v) # zenith and
57
           → azimuth for the direct linear ray solution (radians)
          cherenkov_angle = np.arccos(1. /

→ self._medium.get_index_of_refraction(self._X1))
59
           if np.linalg.norm(u) != 0:
60
              delta_theta =
61
               else:
62
63
               delta_theta = self._step_sizes[0]/units.radian
64
           ## regions of theta with posible solutions (radians)
          launch_lower = [0]
66
          launch_upper = [theta_direct + delta_theta] # below theta_direct no
           → solutions are possible without upward reflections
          if n_reflections > 0:
69
              if self.medium.reflection is None:
                   self.__logger.error("a solution for {:d} reflection(s) off the
71
                   → bottom reflective layer is requested,"
                                      +"but ice model does not specify a reflective
72
                                       → layer".format(n_reflections))
                  raise AttributeError("a solution for {:d} reflection(s) off the
73
                   \hookrightarrow bottom reflective layer is requested,"
```

```
+"but ice model does not specify a reflective
                                                                                   → layer".format(n_reflections))
                                else:
                                        z_refl = self._medium.reflection
 76
                                        rho_channel = np.linalg.norm(u)
                                        if self._X2[2] > self._X1[2]:
 78
                                                 z_{up} = self._X2[2]
 79
                                                 z_{down} = self._X1[2]
 80
                                        else.
                                                 z_{up} = self._X1[2]
 82
                                                 z_{down} = self._X2[2]
 83
                                        rho_bottom = (rho_channel * (z_refl - z_down)) / (2*z_refl - z_up
                                         \rightarrow - z_down)
                                         alpha = np.arctan((z_down - z_refl)/rho_bottom)
 85
                                         ## when reflection on the bottom are allowed, a initial region
 86
                                         → for theta from 180-alpha to 180 degrees is added
                                        launch_lower.append(((np.pi/2 + alpha) -
 87
                                         \ \hookrightarrow \ 2*abs(self.delta\_theta\_bottom(dz=self.\_sphere\_sizes[0]\,,

    z_refl=z_refl) / units.radian)))
                                        launch_upper.append(np.pi)
                        #we first do the same as in the iterative solver
 89
                        for s,sphere_size in enumerate(self._sphere_sizes):
 91
                                sphere_size = sphere_size * (radiopropa.meter/units.meter)
                                detected_rays = []
 93
                                results = []
 95
                                ##define module list for simulation
 96
                                sim = radiopropa.ModuleList()
 97
                                sim.add(radiopropa.PropagationCK(self._ice_model.get_scalar_field(),
 98
                                 \rightarrow 1E-8, .001, 1.)) ## add propagation to module list
                                for module in self._ice_model.get_modules().values():
 99
                                        sim.add(module)
100
                                sim.add(radiopropa.MaximumTrajectoryLength(self._max_traj_length *
101
                                 102
                                ## define observer for detection (channel)
                                obs = radiopropa.Observer()
104
                                obs.setDeactivateOnDetection(True)
106

¬ radiopropa.ObserverSurface(radiopropa.Sphere(radiopropa.Vector3d(*X2),
                                 → sphere_size)) ## when making the radius larger than 2 meters,
                                       sometimes three solution times are found
107
                                obs.add(channel)
                                sim.add(obs)
109
                                ## define observer for stopping simulation (boundaries)
111
                                obs2 = radiopropa.Observer()
112
                                obs2.setDeactivateOnDetection(True)
113
                                w = (u / np.linalg.norm(u)) * 2*sphere_size
114
                                boundary_behind_channel =

¬ radiopropa.ObserverSurface(radiopropa.Plane(radiopropa.Vector3d(*(X2)))

¬ radiopropa.Vector3d(*(X2))

¬ radiopropa.Vec
                                 → + w)), radiopropa.Vector3d(*w)))
```

```
obs2.add(boundary_behind_channel)
116
                boundary_above_surface =
117

¬ radiopropa.ObserverSurface(radiopropa.Plane(radiopropa.Vector3d(0,

→ 0, 1*radiopropa.meter), radiopropa.Vector3d(0, 0, 1)))

                obs2.add(boundary_above_surface)
118
                sim.add(obs2)
119
120
                #create total scanning range from the upper and lower thetas of the
121
                \hookrightarrow bundles
                step = self._step_zeniths[s] / units.radian
                theta_scanning_range = np.array([])
123
                for iL in range(len(launch_lower)):
                    new_scanning_range = np.arange(launch_lower[iL],
125
                     → launch_upper[iL]+step, step)
                    theta_scanning_range = np.concatenate((theta_scanning_range,
126
                     → new_scanning_range))
127
                for theta in theta_scanning_range:
                    ray_dir = hp.spherical_to_cartesian(theta, phi_direct)
129
                    def delta(ray_dir,shower_dir):
131
                         viewing = np.arccos(np.dot(shower_dir, ray_dir)) *
                         \hookrightarrow units.radian
                         return viewing - cherenkov_angle
133
134
                    if (self._shower_axis is None) or
                        (abs(delta(ray_dir,self._shower_axis)) <</pre>
                       self._cut_viewing_angle):
                         source = radiopropa.Source()
136
137
                             source.add(radiopropa.SourcePosition(radiopropa.Vector3d(*X1)))
138

→ source.add(radiopropa.SourceDirection(radiopropa.Vector3d(*ray_dir))))

                         sim.setShowProgress(True)
139
                         ray = source.getCandidate()
140
                         sim.run(ray, True)
141
                         current_rays = [ray]
143
                         while len(current_rays) > 0:
                             next_rays = []
145
                             for ray in current_rays:
                                 if channel.checkDetection(ray.get()) ==
147

→ radiopropa.DETECTED:

                                     detected_rays.append(ray)
148
                                     result = {}
149
                                     if n_reflections == 0:
150
                                          result['reflection']=0
                                          result['reflection_case']=1
152
                                     elif self._ice_model.get_modules()["bottom")
153
                                      → reflection"].get_times_reflectedoff(ray.get())
                                         <= n_reflections:
                                          → result['reflection']=self._ice_model.get_modules()["t
                                          → reflection"].get_times_reflectedoff(ray.get())
```

```
155
                                          → result['reflection_case']=int(np.ceil(theta/np.deg2ra
                                     results.append(result)
156
                                 for secondary in ray.secondaries:
157
                                     next_rays.append(secondary)
                             current_rays = next_rays
159
                #loop over previous rays to find the upper and lower theta of each

→ bundle of rays

                #uses step, but because step is initialized after this loop this ios
161
                 → the previous step size as intented
                if len(detected_rays) > 0:
162
                    launch_lower.clear()
163
                    launch_upper.clear()
164
165
                    launch_theta_prev = None
                    for iDC,DC in enumerate(detected_rays):
166
                         launch_theta = DC.getLaunchVector().getTheta()/radiopropa.rad
                         if iDC == (len(detected_rays)-1) or iDC == 0:
168
                             if iDC == 0:
                                 launch_lower.append(launch_theta-step)
170
                             if iDC == (len(detected_rays)-1):
                                 launch_upper.append(launch_theta+step)
172
                         elif abs(launch_theta - launch_theta_prev) > 1.1*step: ##take
173
                         → 1.1 times the step to be sure the next ray is not in the
                         → bundle of the previous one
                             launch_upper.append(launch_theta_prev+step)
174
                             launch_lower.append(launch_theta-step)
175
                         else:
176
                             pass
                         launch_theta_prev = launch_theta
178
                    isMinimizeAble = MinimizeAble(launch_lower,launch_upper)
179
                     #check if we have two distinct launch regions so we can minimize
180
                    #accuracy is chosen above time duration, so this will take a
181
                     \hookrightarrow while
                    if isMinimizeAble and (s == 0): # speed hack: Only check on first
182
                     \rightarrow iteration
                         LetsMinimize = True
183
                         break
185
                else:
                     #if detected_rays is empty, no solutions where found and the
187
                     \hookrightarrow tracer is terminated
                    break
188
            if LetsMinimize:
190
                iterative = False
191
                ##define module list for simulation, this needs to be redone to get
192
                \rightarrow rid of the spherical observer
                sim = radiopropa.ModuleList()
193
                sim.add(radiopropa.PropagationCK(self._ice_model.get_scalar_field(),
194
                \rightarrow 1E-8, .001, 1.)) ## add propagation to module list
                for module in self._ice_model.get_modules().values():
195
                    sim.add(module)
197
                   sim.add(radiopropa.MaximumTrajectoryLength(self._max_traj_length*(radiopropa.
```

```
198
                ## define observer for detection (channel)
199
                obs = radiopropa.Observer()
                obs.setDeactivateOnDetection(True)
201
                #a bigger normal value makes the calculation faster, a smaller one

→ more precise

                #NormalScale = 2.5
203
               w = (u / np.linalg.norm(u)) #* NormalScale
204
               plane_channel =
205

¬ radiopropa.ObserverSurface(radiopropa.Plane(radiopropa.Vector3d(*X2),
                → radiopropa.Vector3d(*w)))
                obs.add(plane_channel)
206
               sim.add(obs)
207
                # handy?
209
               boundary_above_surface =
210

¬ radiopropa.ObserverSurface(radiopropa.Plane(radiopropa.Vector3d(0,

→ 0, 1*radiopropa.meter), radiopropa.Vector3d(0, 0, 1)))

                obs2.add(boundary_above_surface)
211
                sim.add(obs2)
213
               detected_rays = []
               detected_theta = []
215
                #we minimize the cotangens of the zenith to reflect the same
                → resolution in z to the different angles (vertical vs horizontal)
217
               for i in range(len(launch_lower)):
218
                   11 = launch_lower[i]
219
                   lu = launch_upper[i]
220
                   cotll = cot(11)
221
                    cotlu = cot(lu)
222
                   InitGuess = cot((11+lu)/2)
223
                   if cotlu > cotll:
224
                        bounds = scipy.optimize.Bounds(lb=cotll, ub=cotlu,
225

    keep_feasible=False)

                   else:
226
                        bounds = scipy.optimize.Bounds(lb=cotlu, ub=cotll,
227
                        \rightarrow keep_feasible=False)
                   root =
229
                    theta = arccot(root.x)
230
                   detected_theta.append(theta)
                   detected_rays.append(shoot_ray(theta))
232
                self._rays = detected_rays
234
                self._results = [{'reflection':0,'reflection_case':1} for ray in
235

    detected_rays]

               launch_bundles = None
236
237
                self.__used_method = 'hybrid minimizer'
               return launch_bundles, iterative
238
           else:
240
241
               iterative = True
```

```
self._rays = detected_rays

self._results = results

self._used_method = 'iterator'

launch_bundles = np.transpose([launch_lower, launch_upper])

return launch_bundles,iterative
```

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