### **Knowledge Tracing**

Machine Learning for Behavioral Data March 28, 2022



# **Today's Topic**

Week	Lecture/Lab
1	Introduction
2	Data Exploration
3	Regression
4	Classification
5	Model Evaluation
6	Knowledge Tracing
7	Knowledge Tracing
8	Time Series Prediction

**Supervised learning on time series:** 

- Probabilistic graphical models
- Neural networks: LSTM, GRU, etc.

### Getting ready for today's lecture...

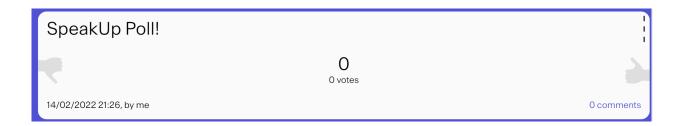
- If not done yet: clone the repository containing the Jupyter notebook and data for today's lecture into your Noto workspace
- SpeakUp room for today's lecture:

https://go.epfl.ch/mlbd-lecture

### Short quiz about the past...

[Model Evaluation] Given a data set {1,2,3,4}, one possible bootstrap set is {1,1,1,1}:

- a) True
- b) False



### Short quiz about the past...

[Model Evaluation] Which of the following statements about k-fold cross validation are wrong? N denotes the number of samples in the data set, k the number of folds:

- a) k must always be smaller than N.
- b) The smaller k is, the more expensive it is to compute the error.
- c) Cross validation can be used to tune model hyperparameters.
- d) Cross validation is not a valid method for computing the generalization error of a model.



# **Today's Topic**

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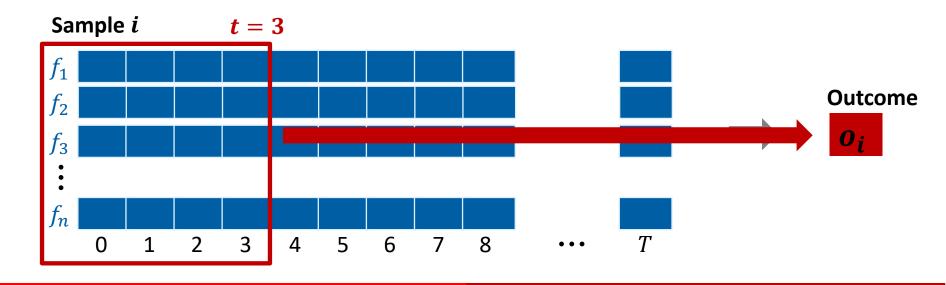
6	Knowledge Tracing
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8	Time Series Prediction

**Supervised learning on time series:** 

- Probabilistic graphical models
- Neural networks: LSTM, GRU, etc.

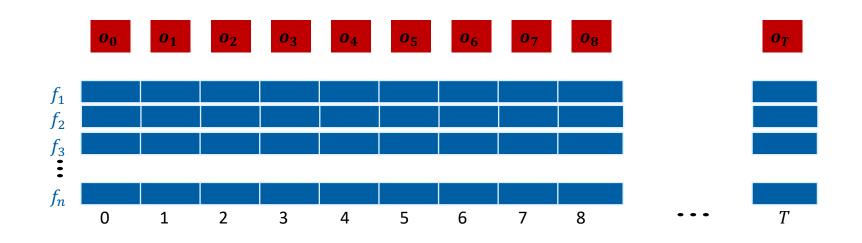
#### **Time Series – Prediction Task**

• Prediction of a target variable after t < T time steps, where T is the total number of time steps



### **Time Series – Tracing Task**

- Prediction of a target variable after t < T time steps, where T is the total number of time steps
- Prediction of a variable in time step t+1, based on time steps  $0, \dots, t$



### **Today: Tracing Student Knowledge**

- Is the student learning?
  - Measure what the student knows at a specific time t
  - More specifically: knowledge of the student about relevant knowledge components (skills)



Task:

50 - 23 = ? 75 - 12 = ?

38 - 14 = ?

Answer:

27

61

24

### Tracing Knowledge – why is it useful?

- Is the student learning?
  - Measure what the student knows at a specific time t
  - More specifically: knowledge of the student about relevant knowledge components (skills)

- Choose the next appropriate activity
- Know which activities support learning

### **Today's Use Case**

- ASSISTments is a free tool for assigning and assessing math problems and homework
- All math problems (tasks/items) are associated to a specific skill/knowledge component
- 4,217 middle-school students
- 525,534 observations

### **Today: Tracing Student Knowledge**

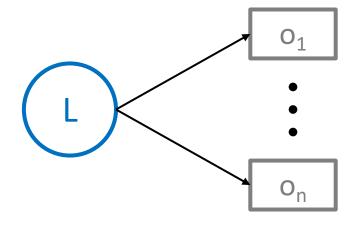
- Bayesian Knowledge Tracing (BKT)
- Learning Curves

#### What is a latent variable?



#### What is a latent variable?

- A latent variable L is a variable which is not directly observable/cannot be measured
- It is assumed to affect the outcome of other variables o, which can be observed (directly measured)

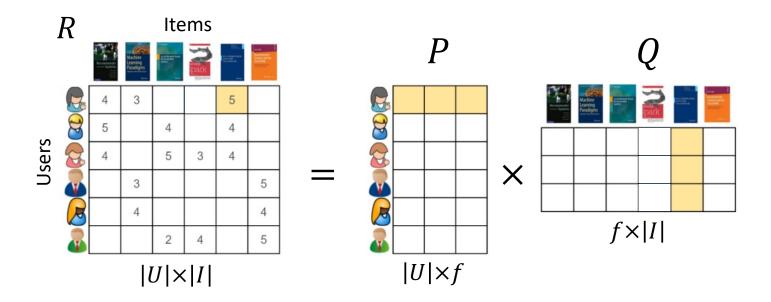


### Why should we use latent variables?

- In many scientific fields, we are interested in concepts/factors that cannot directly be measured/observed:
  - Political sciences: leadership, political competence, etc.
  - Psychology: stress, self-worth, personality characteristics, talent, etc.
  - Education: memory, spatial ability, cognitive abilities, etc.
- We represent underlying concepts/factors by latent variables and infer them from the observed variables

### **Example 1: Recommender Systems**

• Given: ratings of users u for items i (e.g., books)



### **Example 2: Education**

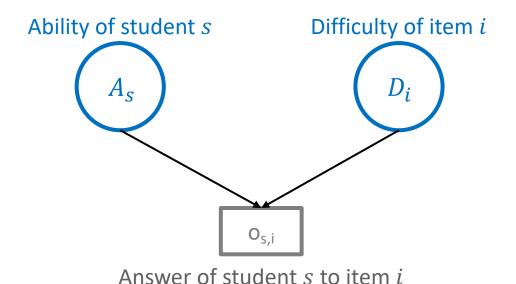
 Observations: binary answers (correct/wrong) of students to items (tasks)

O<sub>s,i</sub>

Answer of student s to item i

### **Example 2: Education**

 Observations: binary answers (correct/wrong) of students to items (tasks)



### Is the student learning?





Task:

$$50 - 23 = ?$$

$$75 - 12 = ?$$

$$50 - 23 = ?$$
  $75 - 12 = ?$   $38 - 14 = ?$ 

Answer:

### What are we measuring?





Task:

$$50 - 23 = ?$$

$$50 - 23 = ?$$
  $75 - 12 = ?$   $38 - 14 = ?$ 

$$38 - 14 = 3$$

Answer:



### Binary observations of student answers



**Subtraction 0-100** 

1 2 ••• r

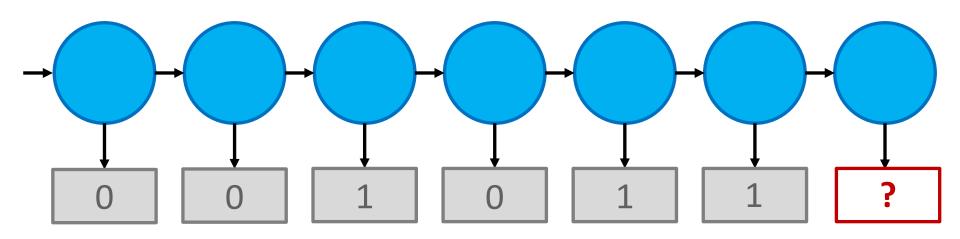
### **Predicting future performance**



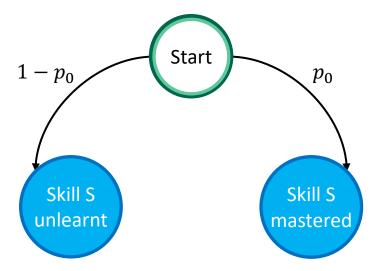
#### **Subtraction 0-100**

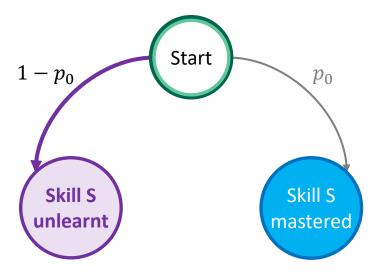
1 2 ··· n n+1
0 0 1 0 1 ?

Latent variable Observed variable

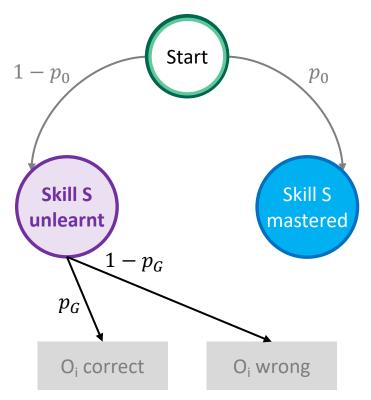




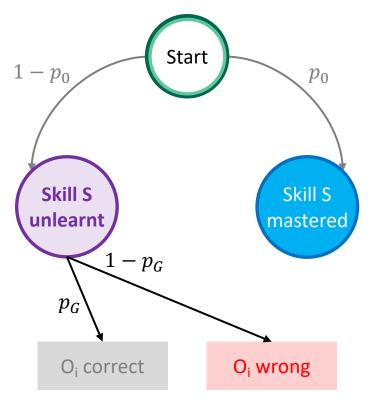




$$t = 0$$
:

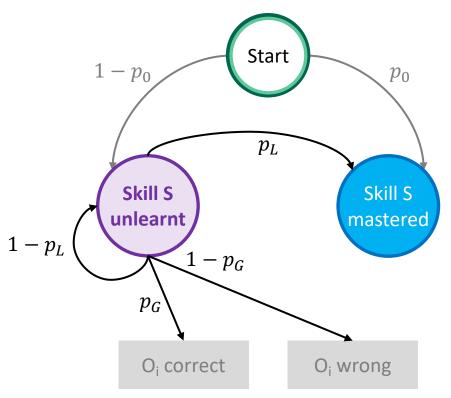


$$t = 0$$
:



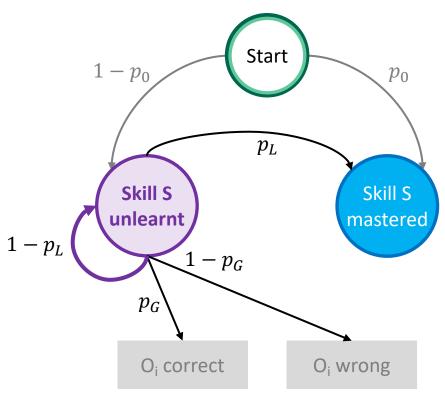
Observations for student s:

t = 0:0



Observations for student s:

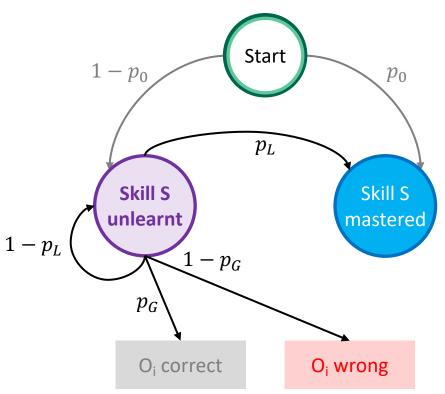
t = 0: 0



Observations for student *s*:

t = 0: 0

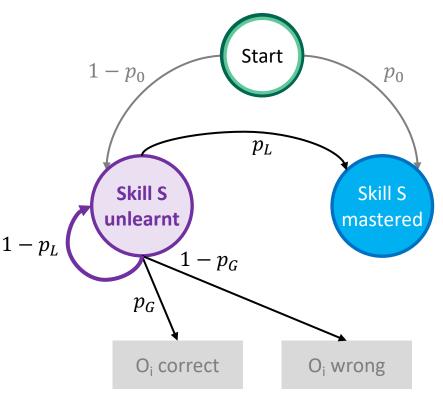
t = 1:



Observations for student s:

t = 0: 0

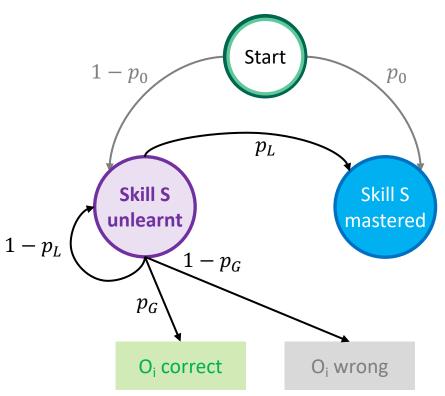
t = 1:0



$$t = 0: 0$$

$$t = 1:0$$

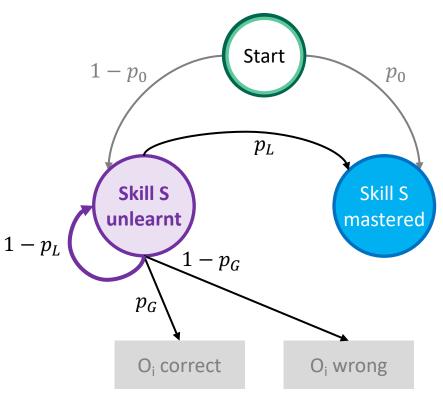
$$t = 2$$
:



$$t = 0: 0$$

$$t = 1:0$$

$$t = 2:1$$

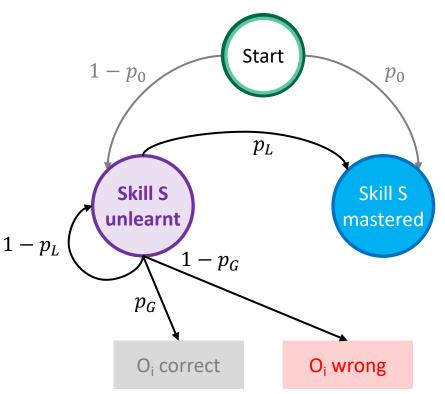


$$t = 0: 0$$

$$t = 1:0$$

$$t = 2:1$$

$$t = 3$$
:

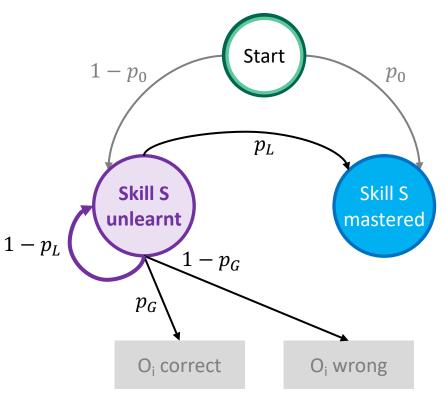


$$t = 0: 0$$

$$t = 1:0$$

$$t = 2:1$$

$$t = 3:0$$



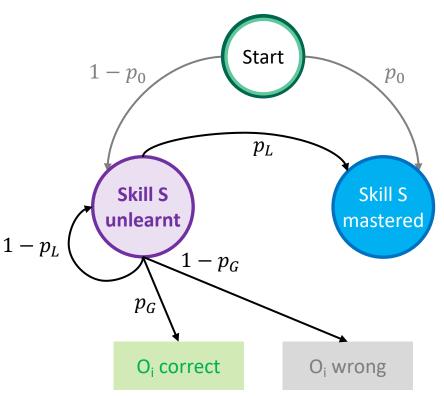
$$t = 0: 0$$

$$t = 1:0$$

$$t = 2:1$$

$$t = 3:0$$

$$t = 4$$
:



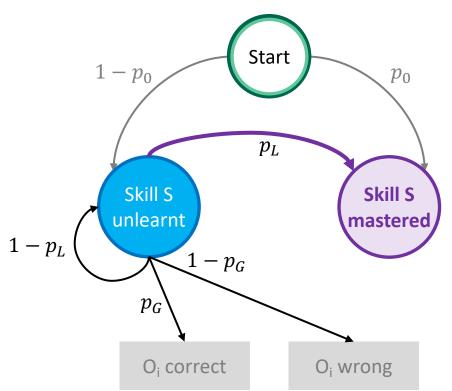
$$t = 0: 0$$

$$t = 1:0$$

$$t = 2:1$$

$$t = 3:0$$

$$t = 4:1$$



$$t = 0: 0$$

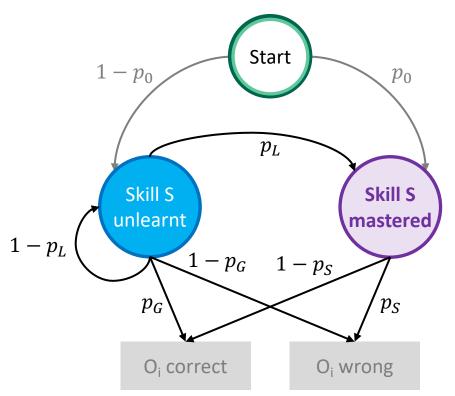
$$t = 1:0$$

$$t = 2:1$$

$$t = 3:0$$

$$t = 4:1$$

$$t = 5$$
:



$$t = 0: 0$$

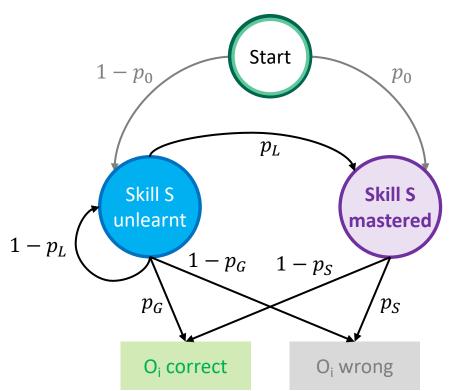
$$t = 1:0$$

$$t = 2:1$$

$$t = 3:0$$

$$t = 4:1$$

$$t = 5$$
:



$$t = 0: 0$$

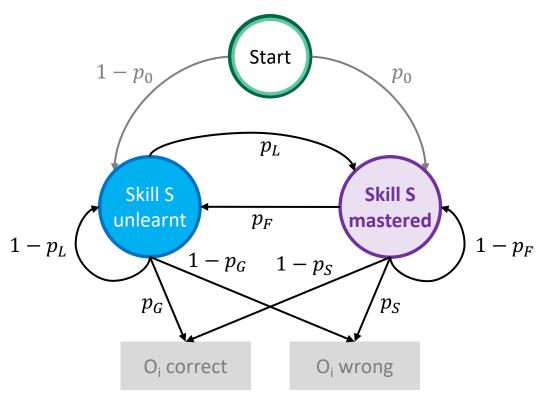
$$t = 1:0$$

$$t = 2:1$$

$$t = 3:0$$

$$t = 4:1$$

$$t = 5:1$$



$$t = 0: 0$$

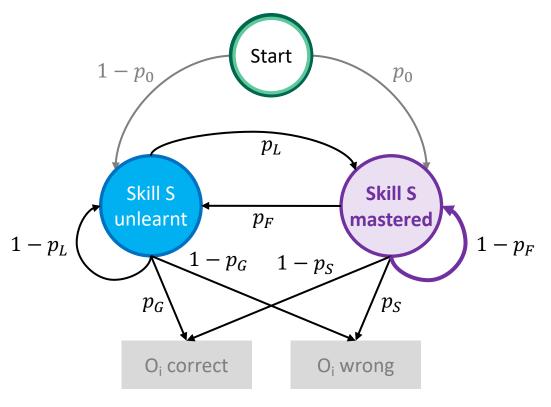
$$t = 1:0$$

$$t = 2:1$$

$$t = 3:0$$

$$t = 4:1$$

$$t = 5:1$$



$$t = 0: 0$$

$$t = 1:0$$

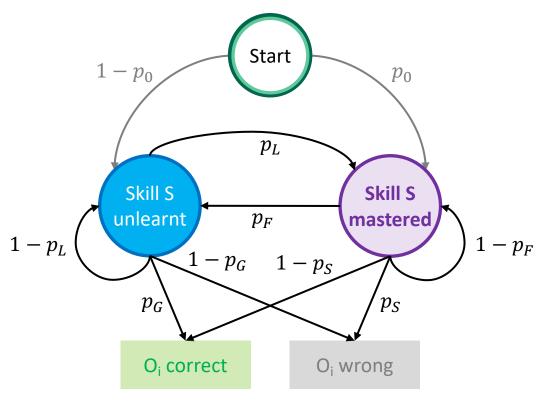
$$t = 2:1$$

$$t = 3:0$$

$$t = 4:1$$

$$t = 5:1$$

$$t = 6$$
:



$$t = 0: 0$$

$$t = 1:0$$

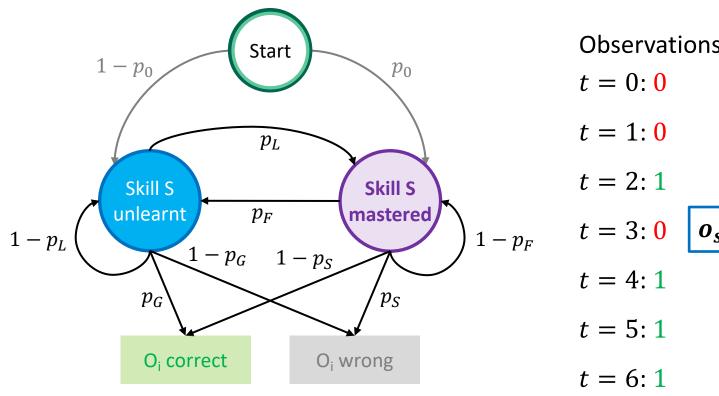
$$t = 2:1$$

$$t = 3:0$$

$$t = 4:1$$

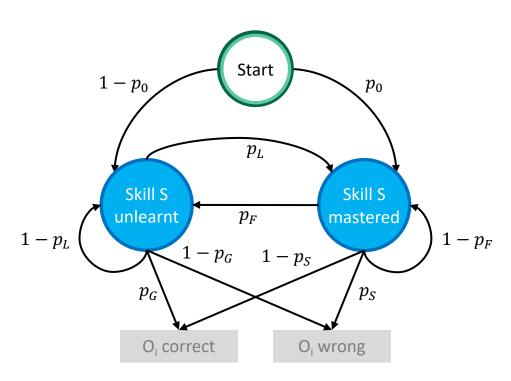
$$t = 5:1$$

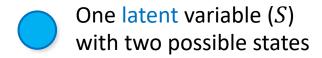
$$t = 6:1$$



$$o_s = [0,0,1,0,1,1,1]$$

## **BKT - Terminology**

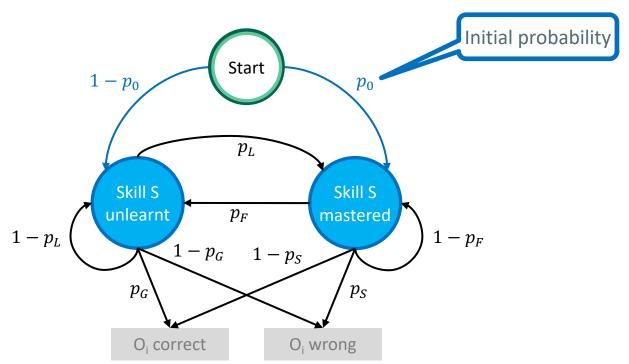




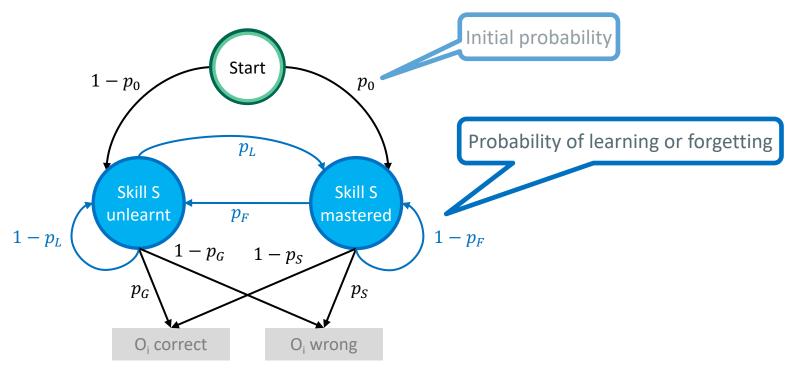
Observations (also binary)

Five parameters: probabilities 
$$\theta = \{p_0, p_L, p_F, p_S, p_G\}$$
 Transition probabilities

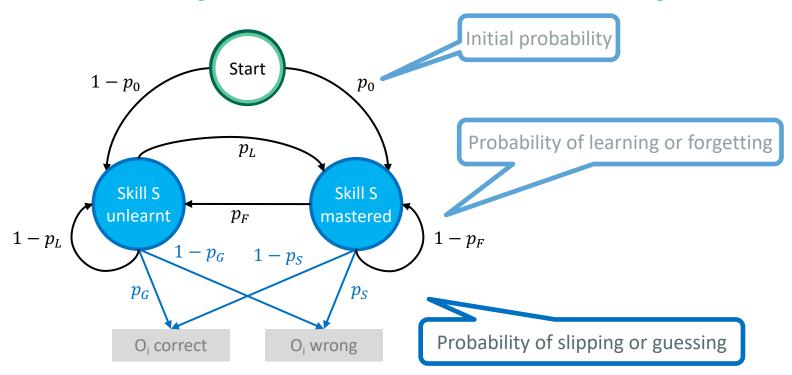
## BKT parameters are interpretable



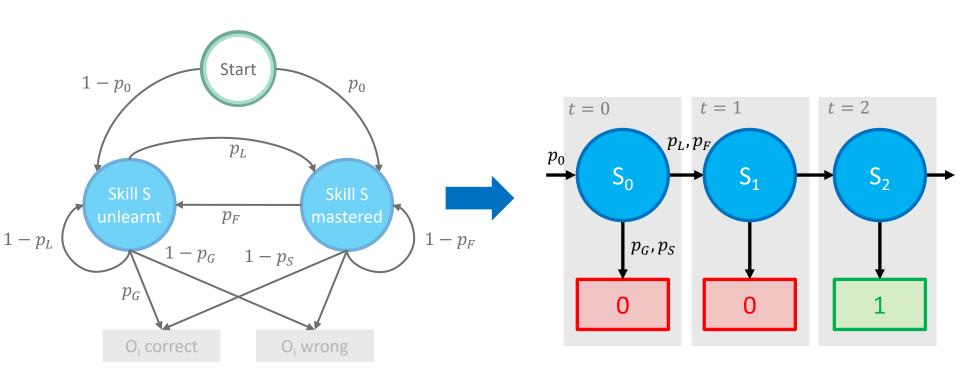
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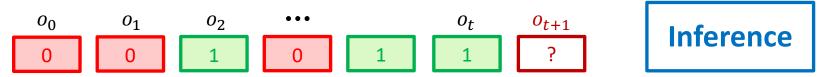


### BKT – unrolled over time

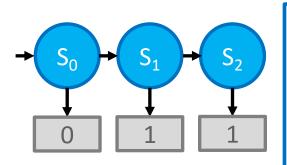


## Two tasks need to be solved in practice

• Given a model with parameters  $\theta = \{p_0, p_L, p_F, p_S, p_G\}$  and a sequence of observations  $\mathbf{o} = [o_0, \dots, o_t]$  from a student s, predict  $o_{t+1}$ 



## **Inference Example**



```
p_0 = 0.5

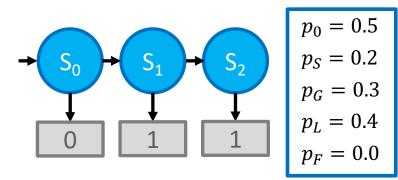
p_S = 0.2

p_G = 0.3

p_L = 0.4

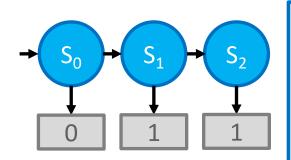
p_F = 0.0
```

## Inference Example - Your Turn



•  $p(s_0 = 1)$ ? •  $p(o_0 = 1)$ ? •  $p(s_1 = 1|o_0 = 0)$ ? •  $p(o_1 = 1|o_0 = 0)$ ? •  $p(s_2 = 1|o_0 = 0, o_1 = 1)$ ?

## Inference Example - Your Turn



22		0 E
$p_0$	_	0.5
$p_{\mathcal{S}}$	=	0.2
$p_G$	=	0.3
$p_L$	=	0.4
$p_F$	=	0.0

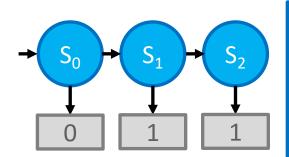
$S_0$	$p(S_0)$
1	$p_0$
0	1- $p_0$

S <sub>t</sub>	$S_{t+1}$	$p(S_{t+1} S_t)$
0	0	$1-p_L$
0	1	$p_L$
1	0	$p_F$
1	1	$1-p_F$

S <sub>t</sub>	O <sub>t</sub>	$p(O_t S_t)$
0	0	$1-p_G$
0	1	$p_G$
1	0	$p_S$
1	1	$1-p_S$

- $p(s_0 = 1)$ ?
- $p(o_0 = 1)$ ?
- $p(s_1 = 1 | o_0 = 0)$ ?
- $p(o_1 = 1 | o_0 = 0)$ ?
- $p(s_2 = 1 | o_0 = 0, o_1 = 1)$ ?

## Inference Example - Your Turn



$p_0$	=	0.5
$p_{\mathcal{S}}$	=	0.2
$p_G$	=	0.3
$p_L$	=	0.4
$p_F$	=	0.0

S <sub>0</sub>	p(S <sub>0</sub> )
1	$p_0$
0	1- $p_0$

S <sub>t</sub>	$S_{t+1}$	$p(S_{t+1} S_t)$
0	0	$1-p_L$
0	1	$p_L$
1	0	$p_F$
1	1	$1-p_F$

S <sub>t</sub>	O <sub>t</sub>	$p(O_t S_t)$
0	0	$1-p_G$
0	1	$p_G$
1	0	$p_S$
1	1	$1-p_S$

#### Some useful rules:

$$p(A,B) = p(A|B) \cdot p(B)$$

$$p(A|B) = \frac{p(B|A) \cdot p(A)}{p(B)}$$

$$p(A = 1) = p(A = 1, B = 1)$$

$$+ p(A = 1, B = 0)$$

• 
$$p(s_0 = 1)$$
?

• 
$$p(o_0 = 1)$$
?

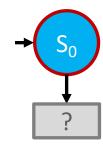
• 
$$p(s_1 = 1 | o_0 = 0)$$
?

• 
$$p(o_1 = 1 | o_0 = 0)$$
?

• 
$$p(s_2 = 1 | o_0 = 0, o_1 = 1)$$
?

#### **Equations for time step 0:**

$$p(s_0 = 1) = p_0$$
  
 $p(s_0 = 0) = 1 - p_0$ 

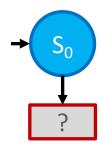


#### **Equations for time step 0:**

$$p(s_0 = 1) = p_0$$
  
 $p(s_0 = 0) = 1 - p_0$ 

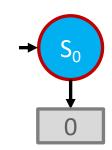
$$p(o_0 = 1) = p(o_0 = 1, s_0 = 1) + p(o_0 = 1, s_0 = 0)$$
  
=  $(1 - p_s) \cdot p_0 + p_G \cdot (1 - p_0)$ 

$$p(o_0 = 0) = p_S \cdot p_0 + (1 - p_G) \cdot (1 - p_0)$$



$$p(s_0 = 1 | o_0 = 0) = \frac{p(o_0 = 0 | s_0 = 1) \cdot p(s_0 = 1)}{p(o_0 = 0)}$$

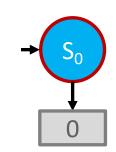
$$= \frac{p_S \cdot p_0}{p_S \cdot p_0 + (1 - p_G) \cdot (1 - p_0)}$$



$$p(s_0 = 0 | o_0 = 0) = 1 - p_{s_0|0}$$

$$p(s_0 = 1 | o_0 = 1) = \frac{p(o_0 = 1 | s_0 = 1) \cdot p(s_0 = 1)}{p(o_0 = 1)}$$

$$= \frac{(1 - p_S) \cdot p_0}{(1 - p_S) \cdot p_0 + p_G \cdot (1 - p_0)}$$



$$p(s_0 = 0 | o_0 = 1) = 1 - p_{s_0|1}$$

#### **Equations for time step 1:**

$$p(s_1 = 1 | o_0 = 0) = \frac{p(s_1 = 1, o_0 = 0)}{p(o_0 = 0)}$$

$$= \frac{p(s_1 = 1, s_0 = 1, o_0 = 0)}{p(o_0 = 0)} + \frac{p(s_1 = 1, s_0 = 0, o_0 = 0)}{p(o_0 = 0)}$$

$$= \frac{p(s_1 = 1 | s_0 = 1) \cdot p(o_0 = 0 | s_0 = 1) \cdot p(s_0 = 1)}{p(o_0 = 0)}$$

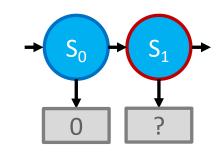
$$+ \frac{p(s_1 = 1 | s_0 = 0) \cdot p(o_0 = 0 | s_0 = 0) \cdot p(s_0 = 0)}{p(o_0 = 0)}$$

$$p(s_1 = 1 | o_0 = 0) = (1 - p_F) \cdot p_{s_0|0} + p_L \cdot (1 - p_{s_0|0})$$

$$p(s_1 = 1|o_0 = 1) = (1 - p_F) \cdot p_{s_0|1} + p_L \cdot (1 - p_{s_0|1})$$

$$p(s_1 = 1|o_0 = 0) = (1 - p_F) \cdot p_{s_0|0} + p_L \cdot (1 - p_{s_0|0})$$

$$p_{s_1|o_0} = (1 - p_F) \cdot p_{s_0|o_0} + p_L \cdot (1 - p_{s_0|o_0})$$



$$\begin{split} p(o_1 = 1 | o_0 = 0) &= \frac{p(o_1 = 1, o_0 = 0)}{p(o_0 = 0)} \\ &+ \frac{p(o_1 = 1, s_1 = 1, s_0 = 1, o_0 = 0)}{p(o_0 = 0)} \\ &+ \frac{p(o_1 = 1, s_1 = 1, s_0 = 0, o_0 = 0)}{p(o_0 = 0)} \\ &+ \frac{p(o_1 = 1, s_1 = 0, s_0 = 1, o_0 = 0)}{p(o_0 = 0)} + \frac{p(o_1 = 1, s_1 = 0, s_0 = 0, o_0 = 0)}{p(o_0 = 0)} \\ &= p(o_1 = 1 | s_1 = 1) \cdot (p(s_1 = 1 | s_0 = 1) \cdot p(o_0 = 0 | s_0 = 1) \cdot p(s_0 = 1)/p(o_0 = 0)) \\ &+ p(o_1 = 1 | s_1 = 1) \cdot (p(s_1 = 1 | s_0 = 0) \cdot p(o_0 = 0 | s_0 = 0) \cdot p(s_0 = 0)/p(o_0 = 0)) \\ &+ p(o_1 = 1 | s_1 = 0) \cdot (p(s_1 = 0 | s_0 = 1) \cdot p(o_0 = 0 | s_0 = 1) \cdot p(s_0 = 1)/p(o_0 = 0)) \\ &+ p(o_1 = 1 | s_1 = 0) \cdot (p(s_1 = 0 | s_0 = 0) \cdot p(o_0 = 0 | s_0 = 0) \cdot p(s_0 = 0)/p(o_0 = 0)) \end{split}$$

 $p(o_1 = 1 | o_0 = 0) = (1 - p_S) \cdot p_{s_1 | o_0 = 0} + p_G \cdot (1 - p_{s_1 | o_0 = 0})$ 

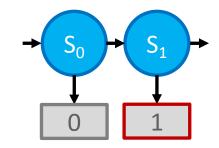
$$p(o_1 = 1 | o_0 = 1) = (1 - p_S) \cdot p_{s_1 | o_0 = 1} + p_G \cdot (1 - p_{s_1 | o_0 = 1})$$

$$p(o_1 = 0 | o_0 = 1) = p_S \cdot p_{s_1 | o_0 = 1} + (1 - p_G) \cdot (1 - p_{s_1 | o_0 = 1})$$



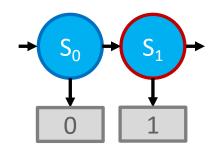
$$p(o_1 = 1|o_0) = (1 - p_S) \cdot p_{s_1|o_0} + p_G \cdot (1 - p_{s_1|o_0})$$

$$p(o_1 = 0|o_0) = p_S \cdot p_{s_1|o_0} + (1 - p_G) \cdot (1 - p_{s_1|o_0})$$



$$p(s_1 = 1 | o_1 = 1, o_0) = \frac{p(s_1 = 1, o_1 = 1, o_0)}{p(o_1 = 1, o_0)}$$

$$p(o_1 = 1, o_0) = p(o_1 = 1|o_0) \cdot p(o_0)$$
  
=  $((1 - p_S) \cdot p_{s_1|o_0} + p_G \cdot (1 - p_{s_1|o_0})) \cdot p(o_0)$ 



$$p(s_1 = 1, o_1 = 1, o_0) = p(o_1 = 1 | s_1 = 1) \cdot p(s_1 = 1 | s_0 = 1) \cdot p(o_0 | s_0 = 1) \cdot p(s_0 = 1)$$

$$+ p(o_1 = 1 | s_1 = 1) \cdot p(s_1 = 1 | s_0 = 0) \cdot p(o_0 | s_0 = 0) \cdot p(s_0 = 0)$$

$$= (1 - p_s) \cdot p_{s_1 | o_0} \cdot p(o_0)$$

$$p(s_1 = 1 | o_1 = 1, o_0) = \frac{(1 - p_s) \cdot p_{s_1 | o_0}}{((1 - p_s) \cdot p_{s_1 | o_0} + p_G \cdot (1 - p_{s_1 | o_0}))}$$

## Inference in BKT models $o_{t-1} = [o_0, ..., o_{t-1}]$

$$\boldsymbol{o_{t-1}} = [o_0, \dots, o_{t-1}]$$

#### Equations for time t=0:

#### Equations for time steps t = 1, ..., T:

Belief about latent state before observation

$$p(s_0 = 1) = p_0$$

$$p_{s_t|o_{t-1}} = (1 - p_F) \cdot p_{s_{t-1}|o_{t-1}} + p_L \cdot (1 - p_{s_{t-1}|o_{t-1}})$$

#### Predicted observation at time t

$$p(o_0 = 1) = (1 - p_s) \cdot p_0 + p_G \cdot (1 - p_0)$$

$$p(o_0 = 0) = p_S \cdot p_0 + (1 - p_G) \cdot (1 - p_0)$$

$$p(o_t = 1 | o_{t-1}) = (1 - p_S) \cdot p_{s_t | o_{t-1}} + p_G \cdot (1 - p_{s_t | o_{t-1}})$$

$$p(o_t = 0 | o_{t-1}) = p_S \cdot p_{s_t | o_{t-1}} + (1 - p_G) \cdot (1 - p_{s_t | o_{t-1}})$$

#### Posterior: belief about latent state after observation

$$p_{s_0|1} = \frac{(1 - p_S) \cdot p_0}{(1 - p_S) \cdot p_0 + p_G \cdot (1 - p_0)}$$

$$p_{s_0|0} = \frac{p_S \cdot p_0}{p_S \cdot p_0 + (1 - p_G) \cdot (1 - p_0)}$$

$$p_{s_{t}|1,o_{t-1}} = \frac{(1 - p_{s}) \cdot p_{s_{t}|o_{t-1}}}{(1 - p_{s}) \cdot p_{s_{t}|o_{t-1}} + p_{G} \cdot (1 - p_{s_{t}|o_{t-1}})} p_{s_{t}|o_{t}}$$

$$p_{s_{t}|0,o_{t-1}} = \frac{p_{s} \cdot p_{s_{t}|o_{t-1}}}{(1 - p_{s}) \cdot p_{s_{t}|o_{t-1}} + p_{G} \cdot (1 - p_{s_{t}|o_{t-1}})}$$

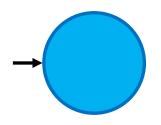
 $p_0 = 0.5$ 

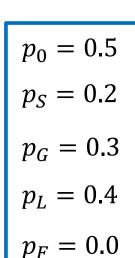
 $p_S = 0.2$ 

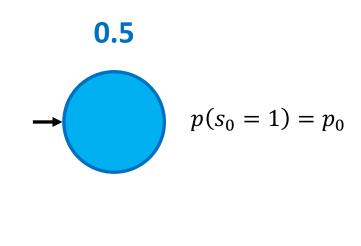
 $p_G = 0.3$ 

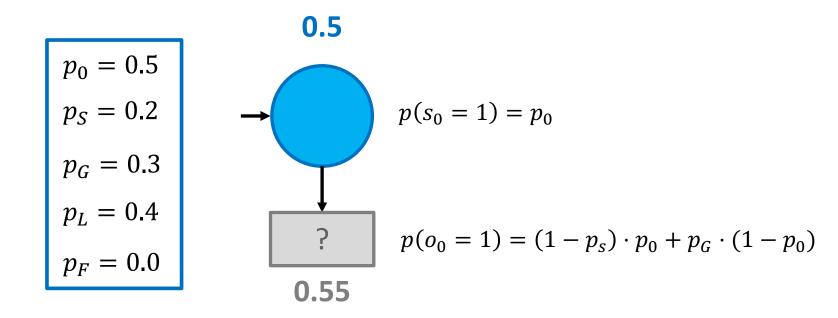
 $p_L = 0.4$ 

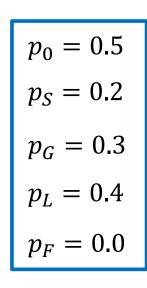
 $p_F = 0.0$ 

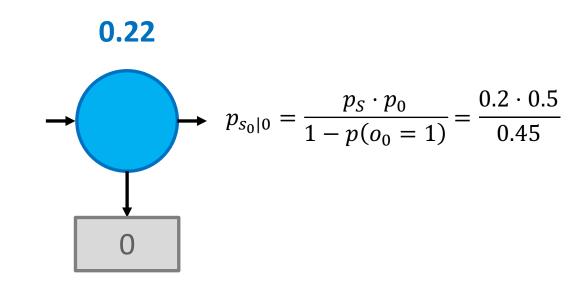


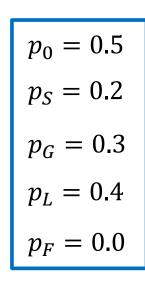


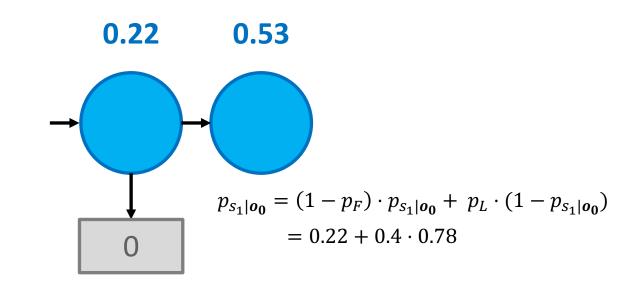


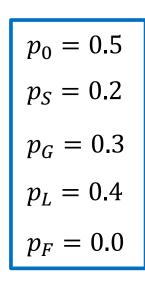


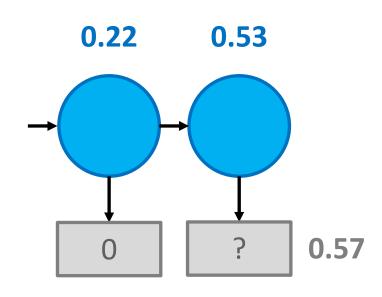




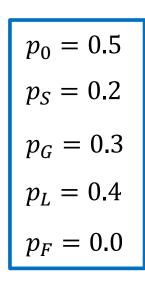


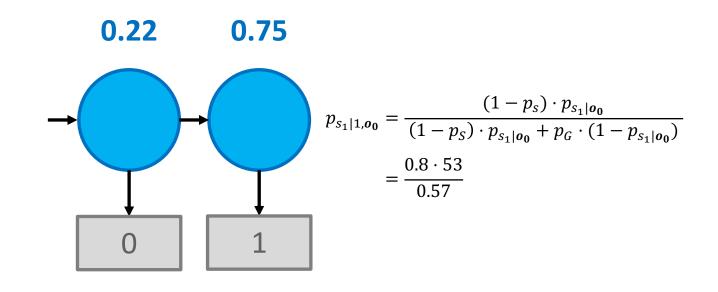


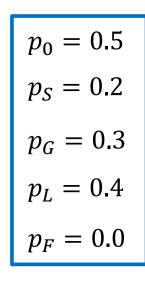


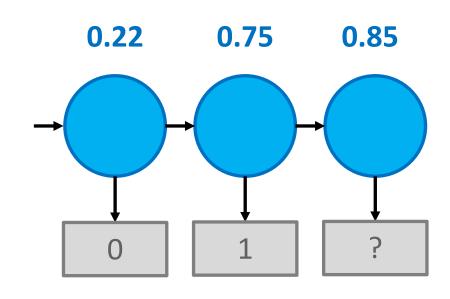


$$p(o_1 = 1 | \mathbf{o_0}) = (1 - p_S) \cdot p_{s_1 | \mathbf{o_0}} + p_G \cdot (1 - p_{s_1 | \mathbf{o_0}})$$
$$= 0.8 \cdot 0.53 + 0.3 \cdot 0.47$$

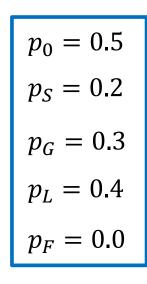


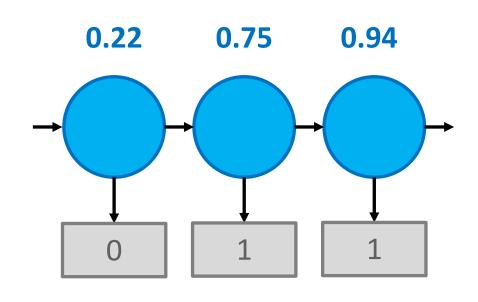




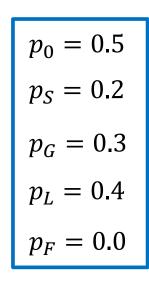


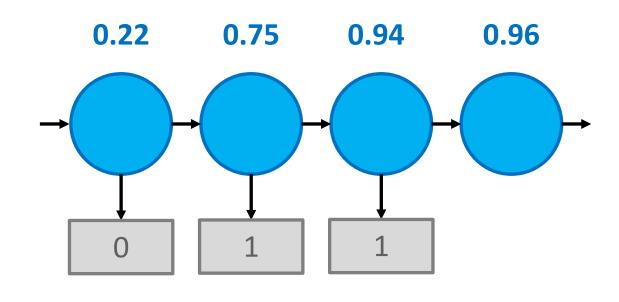
# Making predictions using a BKT model



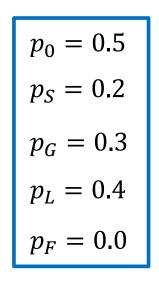


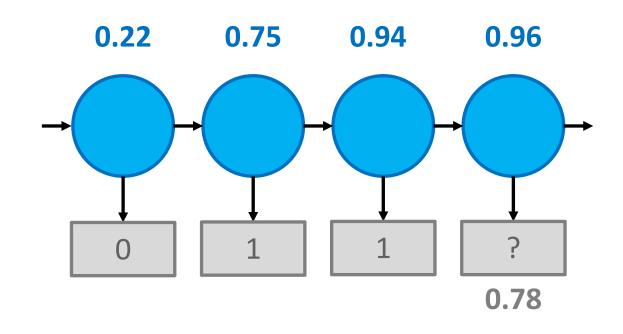
# Making predictions using a BKT model





# Making predictions using a BKT model



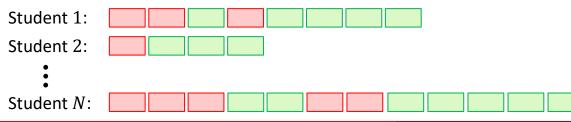


# Two tasks need to be solved in practice

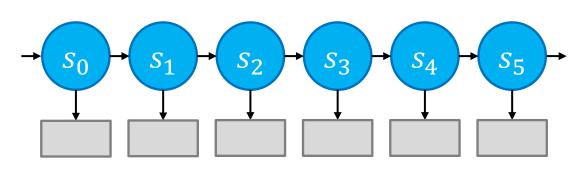
• Given a model with parameters  $\theta = \{p_0, p_L, p_F, p_S, p_G\}$  and a sequence of observations  $\mathbf{o} = [o_0, \dots, o_t]$  from a student s, predict  $o_{t+1}$ 



• Given sequences of observations  $\mathbf{o}=[o_0,\dots,o_T]$  of N students, learn the parameters  $\theta=\{p_0,p_L,p_F,p_S,p_G\}$  that maximize the likelihood of the observed data



Parameter Learning



$$\theta = \{p_0, p_L, p_F, p_S, p_G\}$$

Student  $l_0$ :

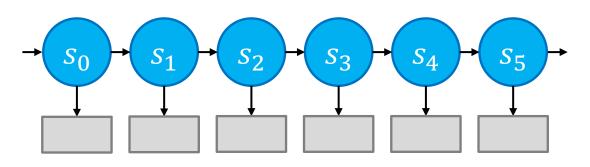
$$\mathbf{o}_{l_0} = [0,1,1]$$

•

Student 
$$l_{N-1}$$
:  $\mathbf{o}_{l_{N-1}} = [1,0,1,1,1,0,0,1,1,1]$ 

Student 
$$l_N$$
:  $\mathbf{o}_{l_N} = [0,1,0,1]$ 

$$\max_{\theta} p(o_{l_0}, \dots, o_{l_{N-1}}, o_{l_N})$$



$$\theta = \{p_0, p_L, p_F, p_S, p_G\}$$

Student  $l_0$ :

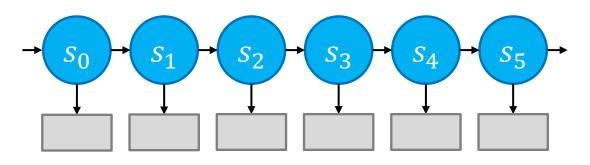
$$\mathbf{o}_{l_0} = [0,1,1]$$

•

Student 
$$l_{N-1}$$
:  $\mathbf{o}_{l_{N-1}} = [1,0,1,1,1,0,0,1,1,1]$ 

Student 
$$l_N$$
:  $\mathbf{o}_{l_N} = [0,1,0,1]$ 

$$\max_{\theta} \ \prod_{i=1}^{N} p(\boldsymbol{o_{l_i}})$$



$$\theta = \{p_0, p_L, p_F, p_S, p_G\}$$

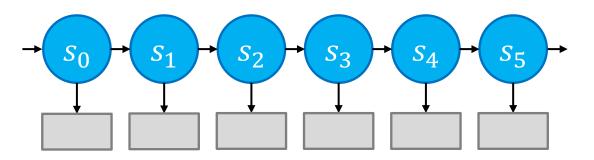
Student 
$$l_0$$
:  $p(\mathbf{o}_{l_0}) = \sum_{s} p(\mathbf{o}_{l_0}, s)$ 

•

Student 
$$l_{N-1}$$
:  $p(\mathbf{o}_{l_0}) = \sum_{s} p(\mathbf{o}_{l_0}, s)$ 

Student 
$$l_N$$
:  $p(\mathbf{o}_{l_0}) = \sum_{s} p(\mathbf{o}_{l_0}, s)$ 

$$\max_{\theta} \prod_{i=1}^{N} \sum_{s_{l_i}} p(\mathbf{o}_{l_i}, s_{l_i})$$



$$\theta = \{p_0, p_L, p_F, p_S, p_G\}$$

$$\max_{\theta} \prod_{i=1}^{N} \sum_{s_{l_i}} p(\mathbf{o}_{l_i}, s_{l_i}) \quad \Longrightarrow \quad \min_{\theta} -\sum_{i=1}^{N} \log \left( \sum_{s_{l_i}} p(\mathbf{o}_{l_i}, s_{l_i}) \right)$$

- Brute-Force Grid Search
- Expectation Maximization
- Gradient Descent
- Nelder-Mead Optimization

## Your Turn – Evaluating a BKT model

- In the student notebook, you have:
  - A trained BKT model for six selected skills
  - A data frame containing the predictions of the BKT model for each observation in the test set

#### Your task:

- Compute the RMSE or AUC separately for each skill
- Provide a visualization of the mean RMSE (or AUC) + standard deviation over all skills as well as the per skill RMSE (or AUC)

### **Assumptions behind BKT**

- Knowledge can be divided into different skills
- Definition of skills is accurate/detailed enough
- Each task corresponds to a single skill (original)
- There is no connection between the skills
- Mastery can be achieved through practice
- There is no forgetting:  $p_F = 0$  (original)

# **Today: Tracing Student Knowledge**

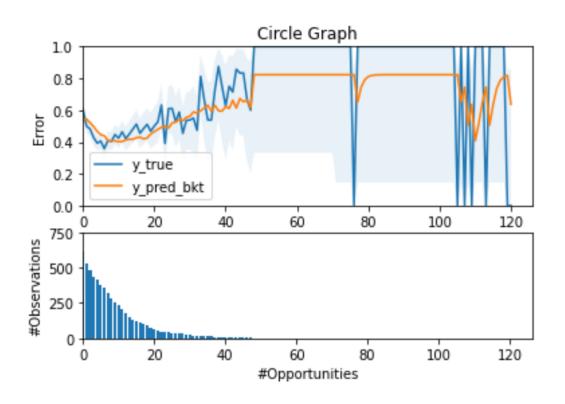
- Bayesian Knowledge Tracing (BKT)
- Learning Curves

# Tracing Knowledge – why is it useful?

- Is the student learning?
  - Measure what the student knows at a specific time t
  - More specifically: knowledge of the student about relevant knowledge components (skills)

- Choose the next appropriate activity
- Know which activities support learning

### What could this curve indicate?



### **Your Turn – Learning Curves**

- In the student notebook, you have:
  - BKT model trained on all skills and students
  - List of available skills
  - Function for plotting learning curves and student numbers for a specific skill
- Your task:
  - Pick 1-2 skills, generate the learning curves for them, and interpret them
  - Send us your plots and interpretations

# Tracing Knowledge – why is it useful?

- Is the student learning?
  - Measure what the student knows at a specific time t
  - More specifically: knowledge of the student about relevant knowledge components (skills)

- Choose the next appropriate activity
- Know which activities support learning

## If you want additional practice...

- You can solve tasks from last year's homework
  - independently
  - during the tutorial sessions on Wednesday morning, the
     TAs will be happy to help and answer questions
- For this lecture: Knowledge Tracing Exercise
- We are happy to provide feedback on your solution:

Upload your Jupyter Notebook here:

https://go.epfl.ch/mlbd-activities