

3. a. (A, B)
 b. No, not in BCNF.
 Violating relation: $D \rightarrow C$

c. $R: (DC)$ $R: (ABD)$
 $FD: D \rightarrow C$ $AB \rightarrow D$

- d. No, $D \rightarrow C$ does not satisfy the requirements.

$\begin{pmatrix} DC \\ ABC \end{pmatrix}$ same as BCNF

4. (1) A has to be part of any candidate key.
 Trying out AB, AD and AE we see that all of them are candidate keys.
 AC is not a candidate key so that's all.

(2) $E \rightarrow B$ violates BCNF

(3) (i) Split on $E \rightarrow B$ to get $\{BE, ACDE\}$
 (ii) Split $\{BE, ACDE\}$ according to $D \rightarrow E$ gives

$\{BE, DE, ACD\}$

(iii) Split $\{BE, DE, ACD\}$ using $A \rightarrow C$ gives 4 relations

$\{BE, DE, AC, D\}$

(4) No, not in BCNF

(5) Already a canonical cover

BCD
 DE
 AC
 EB
 AB

5. $R(A, B, C, D, E)$

$A \rightarrow B$
 $BC \rightarrow D$

decomposes into

$R(AB)$

$A \rightarrow B$

and $R(BCD)$

$BC \rightarrow D$