

# fat\_free\_calculation\_v01-02

February 14, 2025

## 1 Fat Free Simulation

### 1.1 Constantes (input)

```
[21]: import math

# Número pi
pi_number = math.pi

# Modulo de Elasticidade
young_modulus_steel = 207 * (10**9) # N/m2

# Coeficiente de expansão térmica
temperature_coefficient = 0.000017

# Coeficiente de Poisson
poisson_coefficient_steel = 0.3

# Constante Gravitacional
gravity = 9.80665 # m/s2
```

### 1.2 Densidades (input)

```
[22]: # Densidade
specific_mass_water = 1027 # Kg/m3

specific_mass_steel = 7850 # Kg/m3
specific_mass_concrete = 0 # Kg/m3
specific_mass_coating = 935 # kg/m3
specific_mass_content = 200 # Kg/m3
```

### 1.3 Dimensões do duto (input)

```
[23]: # Diametro
diameter = 0.2731 # metros

#Espessura do aço
```

```

steel_thickness = 0.0111 # metros

#Espessura do concreto
concrete_thickness = 0 # metros

# Espessura do revestimento
coating_thickness = 0.0027 # metros

# Diâmetro Interno
diameter_intern = diameter - 2*steel_thickness
area_intern = pi_number * ((diameter_intern/2) ** 2)

# Diametro Externo
diameter_outer = diameter + 2*concrete_thickness + 2*coating_thickness
area_outer = pi_number * ((diameter_outer/2) ** 2)

print('Diâmetro Externo(m) :' + str(diameter_outer))

```

Diâmetro Externo(m) :0.2785

## 1.4 Carregamentos Funcionais (input)

```

[24]: # Tensão Residual Efetiva
heff = 60000 # N

# Pressão interna no duto
pression_intern = 147.1 # bar
p = pression_intern * (10 ** 5) # 1 bar = 105 Pa

# Mudança de temperatura em relação à temperatura ambiente durante a instalação
delta_t = 0

```

## 1.5 Dados do Vão Livre (input)

```

[25]: # Comprimento da tubulação (em metros)
length = 17 # metros

# Profundidade da água
Water_depth = 200 # metros

# Distância entre o duto e o leito marinho (gap)
e_gap = 1 # metros

print('razão L/Ds :' + str(length/diameter))

```

razão L/Ds :62.2482607103625

## 1.6 Dados de Revestimento (input)

```
[26]: # Fator de rigidez do concreto
kc = 0

# Resistência normalizada de compressão
fcu = 42 # Mpa
```

## 1.7 Massa Efetiva (valores auxiliares)

```
[27]: # Cálculo da massa da estrutura
diameter_outer_steel = diameter
diameter_intern_steel = diameter_intern
area_steel_pipe = pi_number * (((diameter_outer_steel/2)**2) -
    ↳((diameter_intern_steel/2)**2))
mass_steel_pipe = specific_mass_steel * area_steel_pipe # mass of the pipe

diameter_outer_concrete = diameter_outer - 2*coating_thickness
diameter_intern_concrete = diameter_outer_steel
area_concrete_pipe = pi_number * (((diameter_outer_concrete/2)**2) -
    ↳((diameter_intern_concrete/2)**2))
mass_concrete_pipe = specific_mass_concrete* area_concrete_pipe # mass of the
    ↳pipe

diameter_outer_coating = diameter_outer
diameter_intern_coating = diameter_outer_concrete
area_coating_pipe = pi_number * (((diameter_outer_coating/2)**2) -
    ↳((diameter_intern_coating/2)**2))
mass_coating_pipe = specific_mass_coating* area_coating_pipe # mass of the
    ↳pipe

mass_structure_pipe = mass_steel_pipe + mass_concrete_pipe + mass_coating_pipe

area_water = pi_number * ((diameter_outer/2) ** 2)
mass_water_displaced = specific_mass_water * area_water # mass of the
    ↳displaced water

area_content = pi_number * ((diameter_intern/2) ** 2)
mass_content = specific_mass_content * area_content # mass of fluid

# Cálculo do coeficiente
if e_gap/diameter_outer < 0.8:
    coefficient_mass_added = 0.68 + (1.6/(1+5*(e_gap/diameter_outer)))
else:
```

```

    coefficient_mass_added = 1

# Calculo da massa adicionada
    mass_added = coefficient_mass_added * mass_water_displaced

    mass_effetive = mass_structure_pipe + mass_added + mass_content

    print('massa efetiva (kg/m): ' + str(mass_effetive))

```

massa efetiva (kg/m): 146.35824179397534

## 1.8 Rigidez (valores auxiliares)

```

[28]: # Rigidez à flexão do aço (EI_steel), dada em N.m²
    moment_inertia = (pi_number/4) * (((diameter/2) ** 4) - (((diameter/2) -
    ↳steel_thickness)**4))
    ei_steel = moment_inertia * young_modulus_steel

    print('rigidez do aço (N.m²) : ' + str(ei_steel))

```

rigidez do aço (N.m²) : 16256831.558693392

## 1.9 Contribuição adicional para a rigidez (valores auxiliares)

```

[29]: # Módulo de Young do Concreto
    young_modulus_concrete = 10000 * (fcn ** 0.3)
    moment_inertia_concrete = (pi_number/4) * (((diameter_outer_concrete/2) ** 4) -
    ↳(((diameter_intern_concrete/2)**4))
    ei_concrete = moment_inertia_concrete * young_modulus_concrete

# Contribuição da rigidez à flexão do concreto e revestimento expressa como
    ↳porcentagem de EI aço
    csf = kc * ((ei_concrete/ei_steel) ** 0.75)

    print('Momento de inércia do concreto(N.m²) : ' + str(ei_concrete))
    print('Contribuição da rigidez à flexão do concreto e revestimento expressa
    ↳como porcentagem de EI aço : ' + str(csf))

```

Momento de inércia do concreto(N.m²) :0.0

Contribuição da rigidez à flexão do concreto e revestimento expressa como  
porcentagem de EI aço :0.0

## 1.10 Força Axial Efetiva (valores auxiliares)

```
[30]: import math

# Tensão axial aplicada durante a instalação da tubulação (N)
effective_lay_tension = heff

# Diferença de pressão interna (assumida como zero neste caso)
internal_pressure_diff = p

# Diferença de temperatura entre a instalação e a operação (assumida como zero
↳ neste caso)
temperature_diff = delta_t

# **Cálculo da força axial efetiva**
effective_axial_force = (effective_lay_tension - # Tensão axial de instalação
                        internal_pressure_diff * area_intern * # Termo da
↳ pressão interna
                        (1 - 2 * poisson_coefficient_steel) - # Ajuste devido
↳ ao efeito de Poisson
                        area_outer * temperature_coefficient *
↳ temperature_diff) # Termo da variação térmica

print('Força Axial Efetiva (N): ' + str(effective_axial_force))
```

Força Axial Efetiva (N): -230913.4950855181

```
[31]: # tentar encontrar o valor de lambda

area_pipe_outer = pi_number * ((diameter_outer/2) ** 2)
lambda_max = effective_axial_force / area_pipe_outer

print(lambda_max/1000000)
```

-3.79060939253168

## 1.11 Parâmetros do solo (Clay Very Soft)

```
[32]: # Effetive Lenght
ms = mass_structure_pipe + mass_content
m = mass_water_displaced

ds_per_d = ms/m

user_defined = True

if user_defined == True:
```

```

kvs = 10 ** 5
kv = 10 ** 5
kl = 10 ** 5

else:

    poisson_coefficient_soil = 0.45

    cv = 600000 # boundary condition coefficient (vertical dynamic stiffness)
    cl = 500000 # boundary condition coefficient (lateral dynamic stiffness)

    # Definição dos parâmetros de rigidez do solo para argila muito mole (Clay
    ↪Very Soft)
    kvs = 75000 # N/m/m - Rigidez estática vertical do solo por unidade de
    ↪comprimento
    kv = (cv/(1-poisson_coefficient_soil))*((2/3)*(ds_per_d) + 1/3)*math.
    ↪sqrt(diameter_outer) # N/m/m - Rigidez dinâmica vertical do solo por unidade
    ↪de comprimento
    kl = (cl*(1+poisson_coefficient_soil))*((2/3)*(ds_per_d) + 1/3)*math.
    ↪sqrt(diameter_outer) # N/m/m - Rigidez dinâmica lateral do solo por unidade
    ↪de comprimento

print('Rigidez dinâmica vertical do solo: ' + str(kv))
print('Rigidez dinâmica lateral do solo: ' + str(kl))

```

Rigidez dinâmica vertical do solo: 100000

Rigidez dinâmica lateral do solo: 100000

## 1.12 Carga Crítica de Flambagem (dados de resposta)

```

[33]: import math
def effeitive_length(k: int, length: int, csf: int, stiffness: float):

    if k == kv:
        print('Rigidez dinâmica vertical do solo')

    elif k == kl:
        print('Rigidez dinâmica lateral do solo')

    else:
        print('Rigidez estática vertical do solo')

    # Cálculo do logaritmo do valor adimensional que influencia o comprimento
    ↪efetivo
    value_log = k * (length ** 4) / ((1 + csf) * stiffness)
    print('value_log: ' + str(value_log))

```

```

beta = math.log10(value_log) # Cálculo do logaritmo de base 10 do valor
↳obtido
print('beta: ' + str(beta)) # Exibe o valor de beta

# Cálculo da razão entre o comprimento efetivo e o comprimento total da
↳tubulação
ratio_length_eff = 4.73 / ((-0.066 * (beta ** 2)) + (1.02 * beta) + 0.63)

# Cálculo do comprimento efetivo da tubulação
length_eff = ratio_length_eff * length

print('Comprimento Efetivo: ' + str(length_eff)) # Exibe o comprimento
↳efetivo da tubulação

# Coeficiente de condição de contorno
c2 = 4

# Cálculo da carga crítica de flambagem (Pcr)
pcr = (1 + csf) * c2 * (pi_number ** 2) * stiffness / (length_eff ** 2)

print('Carga Crítica de Flambagem: ' + str(pcr)) # Exibe o valor da carga
↳crítica de flambagem

# Razão entre uma carga específica (90000 N) e a carga crítica de flambagem
print('Razão entre Força Axial Efetiva e Carga Crítica de Flambagem: ' +
↳str(effective_axial_force / pcr)) # Exibe a relação entre a carga axial
↳efetiva e a carga crítica de flambagem
print('')

return length_eff, pcr

length_eff_vertical_dynamic, pcr_vertical_dynamic = effective_length(k=kv,
↳length=length, csf=csf, stiffness=ei_steel)
length_eff_lateral_dynamic, pcr_lateral_dynamic = effective_length(k=kl,
↳length=length, csf=csf, stiffness=ei_steel)
length_eff_vertical_static, pcr_vertical_static = effective_length(k=kvs,
↳length=length, csf=csf, stiffness=ei_steel)

pcr = min([pcr_vertical_dynamic, pcr_lateral_dynamic, pcr_vertical_static])

```

Rigidez dinâmica vertical do solo

value\_log: 513.7593983086875

beta: 2.710759779597058

Comprimento Efetivo: 27.63237316021189

Carga Crítica de Flambagem: 840541.7159652793

Razão entre Força Axial Efetiva e Carga Crítica de Flambagem:

-0.2747198511383064

Rigidez dinâmica vertical do solo

value\_log: 513.7593983086875

beta: 2.710759779597058

Comprimento Efetivo: 27.63237316021189

Carga Crítica de Flambagem: 840541.7159652793

Razão entre Força Axial Efetiva e Carga Crítica de Flambagem:

-0.2747198511383064

Rigidez dinâmica vertical do solo

value\_log: 513.7593983086875

beta: 2.710759779597058

Comprimento Efetivo: 27.63237316021189

Carga Crítica de Flambagem: 840541.7159652793

Razão entre Força Axial Efetiva e Carga Crítica de Flambagem:

-0.2747198511383064

### 1.13 Deflexão Estática (dados de resposta)

```
[34]: # Coeficiente c6 de condição de contorno
c6 = 1/384

# Peso do tubo por unidade de comprimento
pipe_structure_weight = (mass_structure_pipe + mass_content) * gravity

# Cálculo do Empuxo
empuxo = mass_water_displaced * gravity

# Peso Submerso por Unidade de Comprimento
q = pipe_structure_weight - empuxo

# Solicitacao Axial Efetiva
seff = effective_axial_force

# Cálculo da Deflexão Estática
deflection = c6 * ((q * (length_eff_vertical_static**4))/(ei_steel * (1 +
↪csf))) * (1 / (1 + seff/pcr_vertical_static))
deflection_vertical_dynamic = c6 * ((q * (length_eff_vertical_dynamic**4))/
↪(ei_steel * (1 + csf))) * (1 / (1 + seff/pcr_vertical_dynamic))

print('Peso Submerso(N/L): ' + str(q))
print('Deflexão: ' + str(deflection))
print('Razão entre deflexão e diâmetro: '+ str(deflection/diameter_outer))
```

Peso Submerso(N/L): 208.23649458580167



Deflexão: 0.026813694927538767

Razão entre deflexão e diâmetro: 0.09627897640049826

### 1.14 Amplitude máxima de tensão (dados de resposta)

```
[35]: length_eff_dic = {'vertical' : length_eff_vertical_dynamic, 'lateral' :  
    ↪length_eff_lateral_dynamic}  
  
print(length_eff_dic['vertical'])
```

27.63237316021189

```
[36]: # Coeficiente C4 de condição de contorno  
  
length_eff_dic = {'vertical' : length_eff_vertical_dynamic, 'lateral' :  
    ↪length_eff_lateral_dynamic}  
length_eff_list = [length_eff_vertical_dynamic, length_eff_lateral_dynamic]  
  
amplitude_dic = {'vertical' : [], 'lateral': []}  
  
for key, length_eff in length_eff_dic.items():  
  
    c4_midspan = 8.6  
    c4_shoulder = 14.1 * ((length/length_eff)**2)  
    c4 = [c4_midspan, c4_shoulder]  
  
    if key == 'vertical':  
        name_length_eff = 'Rigidez dinâmica vertical do solo'  
  
    elif key == 'lateral':  
        name_length_eff = 'Rigidez dinâmica lateral do solo'  
  
    for c in c4:  
  
        if c == c4_midspan:  
            name_c = 'midspan'  
  
        else:  
            name_c = 'shouder'  
  
        # Distância à linha neutra  
        middle_line = (diameter_outer - 1*steel_thickness)/2  
  
        print(name_length_eff + ', ' + name_c + ', ' + 'linha média')  
  
        # Cálculo seguindo a fórmula do manual da fatfree
```

```

    amplitude_max = 2 * c * (1 + csf) * diameter * young_modulus_steel *
    ↪middle_line / (length_eff ** 2)

    amplitude_dic[key].append(amplitude_max/1000000)

    print('Amplitude (MPa): ' + str(amplitude_max/1000000))
    print('')

print('Amplitude máx. in-line (Mpa) :'+ str(max(amplitude_dic['lateral'])))
print('Amplitude máx. cross-flow (Mpa) :'+ str(max(amplitude_dic['vertical'])))

```

Rigidez dinâmica vertical do solo, midspan, linha média  
 Amplitude (MPa): 170.26113705593167

Rigidez dinâmica vertical do solo, shouder, linha média  
 Amplitude (MPa): 105.6568511019522

Rigidez dinâmica lateral do solo, midspan, linha média  
 Amplitude (MPa): 170.26113705593167

Rigidez dinâmica lateral do solo, shouder, linha média  
 Amplitude (MPa): 105.6568511019522

Amplitude máx. in-line (Mpa) :170.26113705593167  
 Amplitude máx. cross-flow (Mpa) :170.26113705593167

## 1.15 Frequência Natural Fundamental (dados de resposta)

```

[37]: # Boundary condition coefficients
c1_inline, c1_crossflow = 3.56, 3.56
c3_inline, c3_crossflow = 0, 0.4

# Massa efetiva
me = mass_effetive

# Cálculo das Frequências
f_inline = c1_inline * math.sqrt(1 + csf) * math.sqrt(ei_steel/(me *
    ↪(length_eff_lateral_dynamic ** 4)) * (1 + (seff/pcr_lateral_dynamic) +
    ↪c3_inline * (deflection/diameter_outer) ** 2))
f_crossflow = c1_crossflow * math.sqrt(1 + csf) * math.sqrt(ei_steel/(me *
    ↪(length_eff_vertical_dynamic ** 4)) * (1 + (seff/pcr_vertical_dynamic) +
    ↪c3_crossflow * (deflection/diameter_outer) ** 2))

print('Frequência na direção in-line (Hz) :'+ str(f_inline))
print('Frequência na direção cross-flow (Hz) :'+ str(f_crossflow))

```

Frequência na direção in-line (Hz) :1.3233535421939862  
Frequência na direção cross-flow (Hz) :1.326731926235356

## 2 Resumo dos resultados

```
[38]: print('-----MAIN-----')
print('STRUCTURAL MODELLING')
print('coating data')
print('kc : ' + str(kc))
print('fcu : ' + str(fcu))
#print('k[m] : ' + str())
print('')

print('Functional Loads')
print('Heff: ' + str(effective_lay_tension))
print('p[bar] : ' + str(pression_intern))
print('delta_T[°C] : ' + str(delta_t))
print('')

print('Pipe Dimensions')
print('Ds: ' + str(diameter))
print('t_steel: ' + str(steel_thickness))
print('t_concrete: ' + str(concrete_thickness))
print('t_coating: ' + str(coating_thickness))
print('')

print('Constants')
print('v: ' + str(poisson_coefficient_steel))
print('alfa_exp_term: ' + str(temperature_coefficient))
print('E(N/m): ' + str(young_modulus_steel))
print('')

print('Densities: ')
print('d_steel: ' + str(specific_mass_steel))
print('d_concrete: ' + str(specific_mass_concrete))
print('d_coating: ' + str(specific_mass_coating))
print('d_cont: ' + str(specific_mass_content))
print('')

print('FREE SPAN SCENÁRIO')
#print('h[m] : ' + str(Water_depth))
print('L[m] : ' + str(length))
print('e[m] : ' + str(e_gap))
print('D[m] : ' + str(diameter_outer))
print('L/Ds : ' + str(length/diameter))
print('')
```

```

print('RESPONSE DATA')
print('f1 (in-line) : ' + str(f_inline))
print('f1 (cr-flow) : ' + str(f_crossflow))
print('A1 (in-line) : ' + str(max(amplitude_dic['lateral'])))
print('A1 (cr-flow) : ' + str(max(amplitude_dic['vertical'])))
print('delta/D : ' + str(deflection/diameter_outer))
print('Seff/Pe : ' + str(effective_axial_force / pcr))
print('')

print('SOIL PROPERTIES')
print('Kv : ' + str(kv))
print('Kl : ' + str(kl))
print('Kv,s : ' + str(kvs))
print('')

print('-----ABA-----')
print('STRUCTURAL MODELLING INTERMEDIATE RESULTS')
print('Transfer Values')
print('EI_steel : ' + str(ei_steel))
print('me : ' + str(me))
print('q : ' + str(q))
print('Seff : ' + str(effective_axial_force))
print('Ca : ' + str(coefficient_mass_added))
print('CSF : ' + str(csf))
print('ds/d : ' + str(ds_per_d))
print('')

print('Areas [m²]')
print('Ai : ' + str(area_intern))
print('A_steel : ' + str(area_steel_pipe))
print('A_concrete : ' + str(area_concrete_pipe))
print('A_coating : ' + str(area_coating_pipe))
print('Ae : ' + str(area_outer))

```

-----MAIN-----

STRUCTURAL MODELLING

coating data

kc : 0

fcu : 42

Functional Loads

Heff: 60000

p[bar] : 147.1

delta\_T[°C] : 0

Pipe Dimensions

Ds: 0.2731  
t\_steel: 0.0111  
t\_concrete: 0  
t\_coating: 0.0027

#### Constants

v: 0.3  
alfa\_exp\_term: 1.7e-05  
E(N/m): 207000000000

#### Densities:

d\_steel: 7850  
d\_concrete: 0  
d\_coating: 935  
d\_cont: 200

#### FREE SPAN SCENÁRIO

L[m] : 17  
e[m] : 1  
D[m] : 0.2785  
L/Ds : 62.2482607103625

#### RESPONSE DATA

f1 (in-line) : 1.3233535421939862  
f1 (cr-flow) : 1.326731926235356  
A1 (in-line) : 170.26113705593167  
A1 (cr-flow) : 170.26113705593167  
delta/D : 0.09627897640049826  
Seff/Pe : -0.2747198511383064

#### SOIL PROPERTIES

Kv : 100000  
Kl : 100000  
Kv,s : 100000

-----ABA-----

#### STRUCTURAL MODELLING INTERMEDIATE RESULTS

##### Transfer Values

EI\_steel : 16256831.558693392  
me : 146.35824179397534  
q : 208.23649458580167  
Seff : -230913.4950855181  
Ca : 1  
CSF : 0.0  
ds/d : 1.3394106338363645

##### Areas [m<sup>2</sup>]

Ai : 0.04944145055838173

```
A_steel : 0.009136379755169835
A_concrete : 0.0
A_coating : 0.0023394183854221788
Ae : 0.06091724869897374
```

### 3 Exporting to PDF

```
[39]: !sudo apt-get install texlive-xetex texlive-fonts-recommended_
↳texlive-plain-generic
```

```
Reading package lists... Done
Building dependency tree... Done
Reading state information... Done
texlive-fonts-recommended is already the newest version (2021.20220204-1).
texlive-plain-generic is already the newest version (2021.20220204-1).
texlive-xetex is already the newest version (2021.20220204-1).
0 upgraded, 0 newly installed, 0 to remove and 20 not upgraded.
```

```
[40]: from google.colab import drive
drive.mount('/content/drive')
```

```
Mounted at /content/drive
```

```
[41]: !apt-get install pandoc
```

```
Reading package lists... Done
Building dependency tree... Done
Reading state information... Done
The following additional packages will be installed:
  libcmark-gfm-extensions0.29.0.gfm.3 libcmark-gfm0.29.0.gfm.3 pandoc-data
Suggested packages:
  texlive-luatex pandoc-citeproc context wkhtmltopdf librsvg2-bin groff ghc
nodejs php python
  libjs-mathjax libjs-katex citation-style-language-styles
The following NEW packages will be installed:
  libcmark-gfm-extensions0.29.0.gfm.3 libcmark-gfm0.29.0.gfm.3 pandoc pandoc-
data
0 upgraded, 4 newly installed, 0 to remove and 20 not upgraded.
Need to get 20.6 MB of archives.
After this operation, 156 MB of additional disk space will be used.
Get:1 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libcmark-
gfm0.29.0.gfm.3 amd64 0.29.0.gfm.3-3 [115 kB]
Get:2 http://archive.ubuntu.com/ubuntu jammy/universe amd64 libcmark-gfm-
extensions0.29.0.gfm.3 amd64 0.29.0.gfm.3-3 [25.1 kB]
Get:3 http://archive.ubuntu.com/ubuntu jammy/universe amd64 pandoc-data all
2.9.2.1-3ubuntu2 [81.8 kB]
Get:4 http://archive.ubuntu.com/ubuntu jammy/universe amd64 pandoc amd64
```

```
2.9.2.1-3ubuntu2 [20.3 MB]
Fetched 20.6 MB in 1s (28.8 MB/s)
Selecting previously unselected package libcmark-gfm0.29.0.gfm.3:amd64.
(Reading database ... 161755 files and directories currently installed.)
Preparing to unpack .../libcmark-gfm0.29.0.gfm.3_0.29.0.gfm.3-3_amd64.deb ...
Unpacking libcmark-gfm0.29.0.gfm.3:amd64 (0.29.0.gfm.3-3) ...
Selecting previously unselected package libcmark-gfm-
extensions0.29.0.gfm.3:amd64.
Preparing to unpack .../libcmark-gfm-
extensions0.29.0.gfm.3_0.29.0.gfm.3-3_amd64.deb ...
Unpacking libcmark-gfm-extensions0.29.0.gfm.3:amd64 (0.29.0.gfm.3-3) ...
Selecting previously unselected package pandoc-data.
Preparing to unpack .../pandoc-data_2.9.2.1-3ubuntu2_all.deb ...
Unpacking pandoc-data (2.9.2.1-3ubuntu2) ...
Selecting previously unselected package pandoc.
Preparing to unpack .../pandoc_2.9.2.1-3ubuntu2_amd64.deb ...
Unpacking pandoc (2.9.2.1-3ubuntu2) ...
Setting up libcmark-gfm0.29.0.gfm.3:amd64 (0.29.0.gfm.3-3) ...
Setting up libcmark-gfm-extensions0.29.0.gfm.3:amd64 (0.29.0.gfm.3-3) ...
Setting up pandoc-data (2.9.2.1-3ubuntu2) ...
Setting up pandoc (2.9.2.1-3ubuntu2) ...
Processing triggers for man-db (2.10.2-1) ...
Processing triggers for libc-bin (2.35-0ubuntu3.8) ...
/sbin/ldconfig.real: /usr/local/lib/libtcm_debug.so.1 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libhwloc.so.15 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libtbbbind.so.3 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libur_loader.so.0 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libur_adapter_level_zero.so.0 is not a
symbolic link

/sbin/ldconfig.real: /usr/local/lib/libtbbmalloc.so.2 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libumf.so.0 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libur_adapter_opencl.so.0 is not a symbolic
link

/sbin/ldconfig.real: /usr/local/lib/libtcm.so.1 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libtbb.so.12 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libtbbbind_2_5.so.3 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libtbbbind_2_0.so.3 is not a symbolic link
```

```
/sbin/ldconfig.real: /usr/local/lib/libtbbmalloc_proxy.so.2 is not a symbolic  
link
```

```
[42]: !jupyter nbconvert --to pdf '/content/drive/MyDrive/fat_free_calculation_v01-02.  
↪ipynb'
```

```
[NbConvertApp] Converting notebook  
/content/drive/MyDrive/fat_free_calculation_v01-02.ipynb to pdf  
[NbConvertApp] Writing 73658 bytes to notebook.tex  
[NbConvertApp] Building PDF  
[NbConvertApp] Running xelatex 3 times: ['xelatex', 'notebook.tex', '-quiet']  
[NbConvertApp] Running bibtex 1 time: ['bibtex', 'notebook']  
[NbConvertApp] WARNING | bibtex had problems, most likely because there were no  
citations  
[NbConvertApp] PDF successfully created  
[NbConvertApp] Writing 73177 bytes to  
/content/drive/MyDrive/fat_free_calculation_v01-02.pdf
```