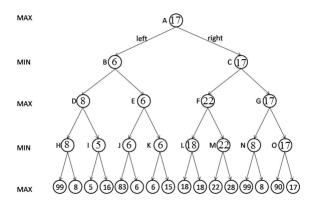
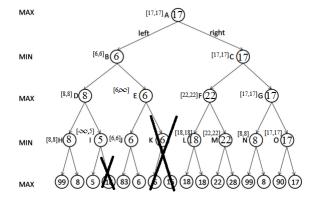
## Problem 1

# Problem 2

• A.



• B.



We cut off the subtree at node K since node B is a MIN and will only accept a value less than 8 we know that we wont get a value greater than 6 down said subtree. The same also occurs below node I. The terminal node 15 is pruned because node D will accept any number greater than 8 however, node I is a MIN and the left terminal node being 5 allows us to denote that the right terminal node cannot be less than 5.

- C. The max player will choose 17 at the root state by using the exhaustive Minimax Algorithm. The same result will occur when using alpha-beta pruning and the max player will again choose 17. The most optimal move is guaranteed using either the exhaustive Minimax algorithm or the alpha-beta pruning algorithm. This is accomplished by alpha-beta pruning ignoring subtrees that are irrelevant while exhaustive Minimax algorithm checks every node regardless of relevance. The outcome is the same however, since alpha-beta pruning ignores irrelevant subtrees it is more efficient.
- D.
- E.

## Problem 3

A. Variables: Defined as  $n_{i,j}$  where  $i \in \{\text{set of all row numbers}\}$  and  $j \in \{\text{set of all column numbers}\}$  for each cell n on the board. Essentially, each square on the sudoku board will be a variable, for a total of 81 variables.

**Domain:** Defined as the set of possible values in sudoku. Here, this set is defined as  $\{1, 2, ..., 9\}$  Constraints:

- 1. All variables in any row must be assigned distinct values.
- 2. All variables in any column must be assigned distinct values.
- 3. All variables in any 3x3 region must be assigned distinct values.
- 4. The assignments given to variables in the start state cannot be changed.
- B. **Start State:** The start state is a given board that has variables assigned with certain values. These values are the basis for the constraints for the rest of the problem and may not be changed. Below is an example start state.

	1		4	2				5
		2		7	1		3	9
							4	
2		7	1					6
				4				
6					7	4		3
	7							
1	2		7	3		5		
3				8	2		7	

#### **Successor Function:**

- 1. Select a random unassigned variable
- 2. Assign a value to this variable that does not violate any constraints
- 3. The resulting state is the successor

Goal Test: A state is considered to a valid goal state if it is both consistent and complete.

Path Cost Function: The path cost from any one state to its successor state will be 1.

C. Sudoku problems that are easy compared to ones that are hard can be determined based on the relative usefulness of applying the minimum remaining values heuristic to their search states.

Consider a Sudoku board for which there are an equal number of remaining values for each variable based on their constraints. Here, the heuristic will not be of much use to us since it will not help us narrow our search and we will have to backtrack from many more states to find a satisfiable goal state than if we were faced with an easier Sudoku board.

An easier Sudoku board can be defined as one for which there is a varied range of minimum remaining values for each variable. This will be an easier game because the minimum remaining values heuristic will direct us to expand states with the least minimum remaining values first. Since the distribution of minimum remaining values for an easy board is more varied, there will always be a good estimate of what state to expand next and this will lead us more directly to the goal state.

#### Algorithm 1 Sudoku Local Search Algorithm

```
1: procedure SUDOKUSOLVER(Board board)
2: board ← randomizeCompleteState(board)
3: while !completeAndSatisfied(board) do
4: nextBoard ← updateState(board)
5: if evaluateSatisfiability(nextBoard) > evaluateSatisfiability(board) then
6: board ← nextBoard
7: return board
```

Due to its random nature this problem will perform worse on easier problems and better on hard problems than its incremental formulation counterpart.

When local search using incremental formulation is used with a good heuristic it will be able to solve easier problems much faster because the heuristic will be very good at directing the search to the goal state. Compared to complete state formulation, which randomizes one variable in a complete state as a successor state, the incremental method will be much more directed and be able to find a solution much faster. Whereas because of the randomness of complete state it will most likely take longer to find a solution.

With harder Sudoku problems however, the incremental formulation will not find a solution as fast as the complete state formulation. The heuristic that the incremental formulation uses will not be very useful for hard problems because it will still have to search a lot of the search tree to make up for what cannot be informed by the heuristic. The complete state formulation however, since it changes states randomly, will not have this problem, and will probabilistically complete the algorithm in faster time than the incremental formulation.

### Problem 4

For Superman to be defeated, it has to be that he is facing an opponent alone and his opponent is carrying Kryptonite. Acquiring Kryptonite, however, means that Batman has to coordinate with Lex Luthor and acquire it from him. If, however, Batman coordinates with Lex Luthor, this upsets Wonder Woman, who will intervene and fight on the side of Superman.

• A.

Superman defeated = S Facing Opponent Alone = A Opponent carrying Kryptonite = K Batman coordinates with Lex Luther = B Wonder Woman Upset = W

• B. Superman being defeated implies that not only did his opponent have Kryptonite but that Superman was also fighting alone. This is equivalent to Superman not being defeated or his opponent has Kryponite and Superman is fighting alone. This all equates to:

$$(\neg S \lor K) \land (\neg S \lor A)$$

Superman fighting alone implies that Superman was defeated.

$$(\neg K \lor B)$$

Batman coordinating with Lex Luther implies that Wonder Woman will be upset and will team up with Superman.

$$(\neg B \lor W)$$

Wonder Woman being upset implies that she will team up with Superman and he will not be fighting alone.

$$(\neg W \lor \neg A)$$

C. Based off the knowledge presented above we can prove that Batman cannot defeat Superman.

$$(\neg S \lor K) \land (\neg S \lor A) \land (\neg K \lor B) \land (\neg B \lor W) \land (\neg W \lor \neg A)$$

$$(\neg S \lor \neg S) \land (\neg A \lor A) \land (\neg K \lor K) \land (\neg B \lor B) \land (\neg W \lor W)$$

$$\neg S$$

### Problem 5

• A.

### Problem 6

• A. Using the minimum value of  $h_1(n)$  and  $h_2(n)$  for each state:

Given that 
$$h_1(n) \leq h^*(n)$$
 is always true,  $Min(h_1(n), \infty) \leq h^*(n)$   
Therefore  $h_1(n) = minimum(h_1(n), h_2(n))$  is admissible. consistent?

• B. Using the maximum value of  $h_1(n)$  and  $h_2(n)$  for each state:

Given that 
$$h_1(n) \leq h^*(n)$$
 
$$h_2(n) \leq h^*(n)$$
 
$$Max(h_1(n), h_2(n)) \leq h^*(n)$$
 Therefore  $h_4(n) = maximum(h_1(n), h_2(n))$  is admissible. consistent?

• C. The defined heuristic function

$$h_3(n) = w \times h_1(n) + (1-w)h_2(n)$$
, where  $0 \le w \le 1$ 

is admissible only when w is a value less than 0.5, any value larger than 0.5 will cause  $h_1(n)$  to be multiplied by a value larger than  $h_2(n)$ . Since the bounds are from 0 to 1 the heuristic is NOT admissible.

consistent?

• D. Considering the informed, best-first search algorithm with an object function of  $f(n) = (2-w) \times g(n) + w \times h(n)$ . It is guaranteed to work for  $0 \le w \le 1$  since being multiplied by g(n) which is a constant implies no effect on which order chosen paths are arranged. However, if w > 1, then the goal state may have an overestimated distance which will make the heuristic not admissible and so not optimal.

Given the information above we can assess the function for when the values of w are 0, 1, and 2.

w = 0

When w=0 it will make f(n)=2g(n) and causes the algorithm to perform like a Uniform Cost Search since there is no weight assigned it will find the most optimal path however, it will not be efficient.

w = 1:

When w = 1 it will make f(n) = g(n) + h(n) which causes the algorithm to perform like  $A^*$  and as with w = 0 is guaranteed to find the optimal path however, is more efficient.

w=2

When w=2 it will make f(n)=2h(n) which causes the algorithm to perform like Greedy Best first search.