



03OAIQW

## **Dynamic Design of Machines**

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Mechanical Engineering

Prof. Nicola Amati

Dipartimento di Ingegneria Meccanica ed Aerospaziale

[nicola.amati@polito.it](mailto:nicola.amati@polito.it)

[angelo.bonfitto@polito.it](mailto:angelo.bonfitto@polito.it)

## **Tutorial 4 – Controlled systems**

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## Exercise 1

In the linear system with a single degree of freedom in Figure 1, an active control action is provided by an actuator working on the spring with stiffness  $K_1$ .

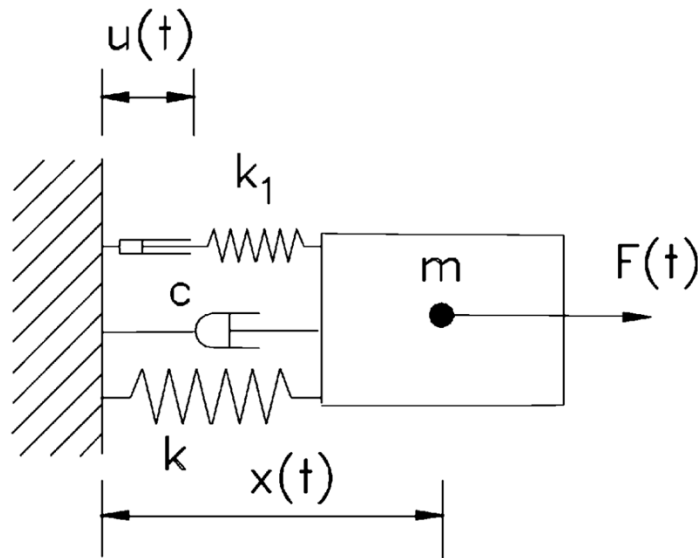


Figure 1 - Exercise 1.

It is requested to:

- Compute the equation of motion of the system
- Obtain the equivalent block diagram of the system
- Considering that the controlled variable is the displacement of the mass  $m$ , write the closed loop transfer function  $G_1(s) = x(s)/x_{ref}(s)$ , considering a PID control action ( $G_{PID} = K_P + K_D s + K_I/s$ )
- Write the closed loop transfer function  $G_2(s) = x(s)/F(s)$ , considering a PID control action ( $G_{PID} = K_P + K_D s + K_I/s$ )
- Use the Matlab script and the Simulink model in the folder to design the PID control and evaluate the behaviour of the controlled system.

## Exercise 2

In the linear system with a single degree of freedom in Figure 2, an active control action is provided by an actuator working on the dashpot with damping  $C_1$ .

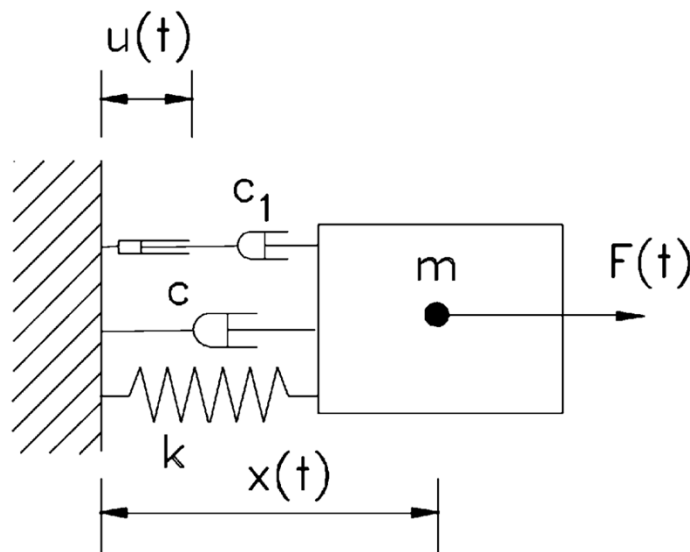


Figure 2 - Exercise 2.

It is requested to:

- Compute the equation of motion of the system
- Obtain the equivalent block diagram of the system
- Considering that the controlled variable is the displacement of the mass  $m$ , write the closed loop transfer function  $G_1(s) = x(s)/x_{ref}(s)$ , considering a PID control action ( $G_{PID} = K_P + K_D s + K_I/s$ )
- Write the closed loop transfer function  $G_2(s) = x(s)/F(s)$ , considering a PID control action ( $G_{PID} = K_P + K_D s + K_I/s$ )
- Adapt the Matlab script and the Simulink model in the folder to design the PID control and evaluate the behaviour of the controlled system.

### Exercise 3

In the linear system with a single degree of freedom in Figure 3, an active control action is provided by an actuator working on an auxiliary mass  $m_1$ .

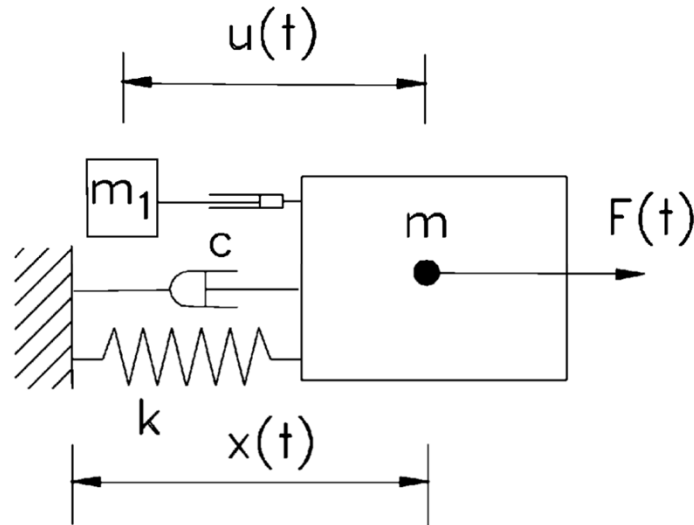


Figure 3 - Exercise 3.

It is requested to:

- f) Compute the equation of motion of the system
- g) Obtain the equivalent block diagram of the system
- h) Considering that the controlled variable is the displacement of the mass  $m$ , write the closed loop transfer function  $G_1(s) = x(s)/x_{ref}(s)$ , considering a PID control action ( $G_{PID} = K_P + K_D s + K_I/s$ )
- i) Write the closed loop transfer function  $G_2(s) = x(s)/F(s)$ , considering a PID control action ( $G_{PID} = K_P + K_D s + K_I/s$ )
- j) Adapt the Matlab script and the Simulink model in the folder to design the PID control and evaluate the behaviour of the controlled system.

