## **WAYNE BISHOP**

# **SWIFT ALGORITHMS & DATA STRUCTURES**



A practical guide to concepts, theory and code



## **SWIFT ALGORITHMS** & DATA STRUCTURES

**BY WAYNE BISHOP** 



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## **SOURCE CODE & GITHUB**



This series is available through Github as an adjunct to the book. In the spirit of collaborative effort, I welcome ongoing feedback and contribution from others. The source code and unit tests are optimized for Swift 1.2 or later and can be obtained from the following repository:

http://github.com/waynewbishop/SwiftStructures

#### **USAGE**

Individuals are welcome to use code for commercial and open-source projects. As a courtesy, please provide attribution to "waynewbishop.com". For more information, review the complete Github license agreement.

## **FOREWORD**

I was sitting in the third row on stage right during the keynote of Apple's annual Worldwide Developers Conference in 2014 (WWDC). There were a lot of exciting announcements. Then came the last announcement. Apple is releasing a brand new programming language - Swift. "It's like Objective-C, without the C," said Craig Federighi, Apple's senior vice president of Software Engineering.

None of us expected that. In fact, it was a surprise to many of Apple's own software engineers. So, at the moment when Swift was announced, there was a tiny pause before awkward, indecisive clapping ensued.

At first glance, Swift looked very familiar and easy to any programmer who's ever programmed in another language besides Objective-C. On social media, there were memes circulating that all JavaScript developers were now iOS developers. Coming from a Ruby background, it looked like Ruby to me. Python developers saw Python in it. Haskell developers said it was most like Haskell - although, at the time, I didn't know anything about Haskell. Everyone immediately felt familiar with Swift, even though we all just learned about it that day.

Swift is a language on a mission. One of its goals is to help us write safe and robust code. By adding specific language features such as optionals and generics, it forces us, as programmers, to handle error-prone scenarios that we often forget to address.

This combination of familiarity and fun has made Swift the most loved language within only the first few months of its release, according to StackOverflow's 2015 Developer Survey.

This is just the beginning for Swift. As I sat in the second row on stage right during the keynote at WWDC 2015, I was witness to the excitement and energy that swept the crowd as it was announced that Swift will be open-sourced. This time the clapping was immediate - without a moment of hesitation.

#### Natasha Murashev

-NatashaTheRobot

## INTRODUCTION

This series provides an introduction to commonly used data structures and algorithms written in a new iOS development language called Swift. While details of many algorithms exist on Wikipedia, these implementations are often written as pseudocode or are expressed in C or C++. With Swift now officially released, its general syntax should be familiar enough for most programmers to understand.

#### **AUDIENCE**

As a reader, you should already be familiar with the basics of programming. Beyond common algorithms, this guide also provides an alternative source for learning the basics of Swift. This includes implementations of many Swift-specific features such as optionals and generics. Beyond Swift, you should be familiar with factory design patterns along with sets, arrays and dictionaries.

#### WHY ALGORITHMS?

When creating modern apps, much of the theory inherent to algorithms is often overlooked. For solutions that consume relatively small amounts of data, decisions about specific techniques or design patterns may not be as important as just getting things to work. However, as your audience grows, so will your data. Much of what makes big tech companies successful is their ability to interpret vast amounts of data. Making sense of data allows users to connect, share, complete transactions and make decisions.

In the startup community, investors often fund companies that use data to create unique insights - something that can't be duplicated by just connecting an app to a simple database. These implementations often boil down to creating unique (often patentable) algorithms like Google PageRank or The Facebook Graph. Other categories include social networking (e.g. LinkedIn), predictive analysis (e.g Uber.com) or machine learning (e.g. Amazon.com).

## **BIG O NOTATION**

Building an app that finds information quickly could mean the difference between success and failure. For example, much of Google's success comes from algorithms that allow people to search vast amounts of data with great efficiency.

There are numerous ways to search and sort data. As a result, computer scientists have devised a way for us to compare the efficiency of software algorithms regardless of computing device, memory or hard disk space. Asymptotic analysis is the process of describing the efficiency of algorithms as their input size (n) grows. In computer science, asymptotics are usually expressed in a common format known as Big O Notation.

#### MAKING COMPARISONS

To understand Big O Notation, one only needs to start comparing algorithms. In this example, we compare two techniques for searching values in a sorted array.

```
//array of sorted integers
let numberList : Array<Int> = [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]
```

#### **LINEAR TIME**

Our first approach employs a common "brute force" technique that involves looping through the entire array until we find a match. In Swift, this can be achieved with the following;

```
func linearSearch(key: Int) {
    //check all possible values
    for number in numberlist {
            if number == key {
                println("value at \((key)) found..")
                break
            }
     }
}
```

While this approach achieves our goal, each item in the array must be evaluated. A function like this is said to run in "linear time" because its speed is dependent on its input size. In other words, the algorithm becomes less efficient as its input size (n) grows.

#### **LOGARITHMIC TIME**

Our next approach uses a technique called binary search. With this method, we apply our knowledge about the data to help reduce our search criteria.

```
func binarySearch(key: Int, imin: Int, imax: Int) {
   var midIndex : Double = round(Double((imin + imax) / 2))
   var midNumber = numberList[Int(midIndex)]

   //reduce the range
   if midNumber > key {
        binarySearch(key, imin, Int(midIndex) - 1)
   }

   //increase the range
   else if (midNumber < key ) {
        binarySearch(key, Int(midIndex) + 1, imax)
   }

   else {
        println("value \((key)\) found..")
   }
}</pre>
```

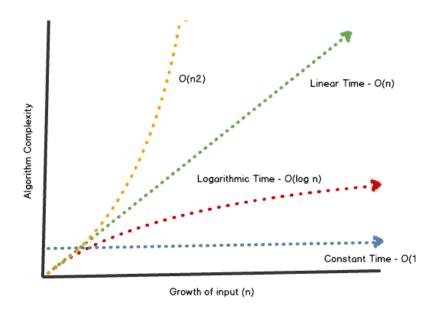
To recap, we know we're searching a sorted array to find a specific value. By applying our understanding of data, we assume there is no need to search values less than the key. For example, to find the value at index 8, it would be impossible to find that value at array index 0 - 7.

By applying this logic we substantially reduce the amount of times the array is checked. This type of search is said to work in *logarithmic time* and is represented with the symbol O(log n). Overall, its complexity is minimized when the size of its inputs (n) grows. Here's a table that compares the different techniques;

Array Size (n)	Search Key	O(n) - No of Checks	O(log n) - No of Checks
10	8	8	2
20	12	12	3
50	23	23	5
75	48	48	6
100	64	64	7
500	235	235	9

Big O Notation ///17

Plotted on a graph, it's easy to compare the running time of popular search and sorting techniques. Here, we can see how most algorithms have relatively equal performance with small datasets. It's only when we apply large datasets that we're able to see clear differences.



#### **FURTHER READING**

- » Asymptotic Analysis http://en.wikipedia.org/wiki/Asymptotic\_analysis
- » Big O Notation http://en.wikipedia.org/wiki/Big\_O\_notation
- » Binary Search http://en.wikipedia.org/wiki/Binary\_search\_algorithm
- » Graphing Logarithms http://www.khanacademy.org

## **SORTING**

Sorting is an essential task when managing data. As we saw with Big O Notation, sorted data allows us to implement efficient algorithms. Our goal with sorting is to move from disarray to order. This is done by arranging data in a logical sequence so we'll know where to find information. Sequences can be easily implemented with integers, but can also be achieved with characters (e.g., alphabets), and other sets like binary and hexadecimal numbers. To start, we'll use various techniques to sort the following array:

```
//a simple array of unsorted integers
var numberList : Array<Int> = [8, 2, 10, 9, 11, 1, 7, 3, 4]
```

With a small list, it's easy to visualize the problem and how things should be organized. To arrange our set into an ordered sequence, we can implement an invariant. In computer science, invariants represent assumptions that remain unchanged throughout execution. To see how this works, consider the *insertion sort* algorithm.

#### **INSERTION SORT**

One of the more basic algorithms in computer science, insertion sort works by evaluating a constant set of numbers with a secondary set of changing numbers. The outer loop acts as the invariant, assuring all array values are checked. The inner loop acts as a secondary engine, reviewing which numbers get compared. Completed enough times, this process eventually sorts all items in the list.

```
//insert the number at the key position
    numberList.insert(key, atIndex: y)
}

} //end for

return numberList
} //end function
```

#### **BUBBLE SORT**

Another common sorting technique is the bubble sort. Like insertion sort, this algorithm combines a series of steps with an invariant. The function works by evaluating pairs of values. Once compared, the position of the largest value is swapped with the smaller value. Completed enough times, this "bubbling" effect eventually sorts all items in the list.

```
func bubbleSort(var numberList: Array<Int>) ->Array<Int> {
        var x, y, z, passes, key: Int
        //track iterations
        for x in 0..<numberList.count {</pre>
             passes = (numberList.count - 1) - x
             for y in 0..<passes {
                 key = numberList[y]
                 println("comparing \((key) and \((numberList[y + 1])"))
                 //compare and rank values
                 if (key > numberList[y + 1]) {
                     z = numberList[y + 1]
                     numberList[y + 1] = key
                     numberList[y] = z
                 }
             }
        }
        return numberList
    } //end function
```

Sorting //21

#### **EFFICIENCY**

Besides insertion sort and bubble sort, there are many other sorting algorithms. Because both insertion and bubble sort combine a variant and invariant, their average performance is  $n \times n$  or  $O(n^2)$ . Other techniques (like Merge Sort) apply different methods and can improve average performance to  $O(n \log n)$ .

See additional sorting algorithms for Quick Sort and Merge Sort on Github.

#### **FURTHER READING**

- » Binary Numbers http://en.wikipedia.org/wiki/Binary\_number
- » Hexadecimal Numbers http://en.wikipedia.org/wiki/Hexadecimal
- » Invariant http://en.wikipedia.org/wiki/Invariant\_(computer\_science)
- » Insertion Sort http://en.wikipedia.org/wiki/Insertion\_sort
- » Bubble Sort http://en.wikipedia.org/wiki/Bubble\_sort
- » Quick Sort http://en.wikipedia.org/wiki/Quicksort
- » Merge Sort http://en.wikipedia.org/wiki/Merge\_sort
- » Selection Sort http://en.wikipedia.org/wiki/Selection\_sort

### LINKED LISTS

A linked list is a basic data structure that provides a way to associate related content. At a basic level, linked lists provide the same functionality as an array. That is, the ability to insert, retrieve, update and remove related items. However, if properly implemented, linked lists can provide additional flexibility. Since objects are managed independently (instead of contiguously - as with an array), lists can prove useful when dealing with large datasets.

#### **HOW IT WORKS**

In its basic form, a linked list is comprised of a key and an indicator. The key represents the data you would like to store such as a string or scalar value. Typically represented by a pointer, the indicator stores the location (also called the address) of where the next item can be found. Using this technique, you can chain seemingly independent objects together.



A linked list with three keys and three indicators.

#### THE DATA STRUCTURE

Here's an example of a "doubly" linked list structure written in Swift. In addition to storing a key, the structure also provides pointers to the next and previous items. Using generics, the structure can also store any type of object and supports nil values. The concept of combining keys and pointers to create structures not only applies to linked lists, but to other objects like tries, queues and graphs.

```
//generic doubly linked list structure

class LLNode<T> {
    var key: T!
    var next: LLNode?
    var previous: LLNode?
}
```

#### **USING OPTIONALS**

When creating algorithms its good practice to set your class properties to nil before they are used. Like with app development, nil can be used to determine missing values or to predict the end of a list. Swift helps enforce this best-practice at compile time through a paradigm called *optionals*. For example, the function printAllKeys employs an implicit unwrapped optional (e.g., current) to iterate through linked list items.

```
//print all keys for the class

func printAllKeys() {

   var current: LLNode! = head

   //assign the next instance
   while (current != nil) {
       println("link item is: \(current.key)")
       current = current.next
   }
}
```

#### **ADDING LINKS**

Here's a function that builds a doubly linked list. The method addLink creates a new item and appends it to the list. The Swift generic type constraint <T: Equatable> is also defined to ensure link instances conform to a specific protocol.

```
class LinkedList<T: Equatable> {
  var head: LLNode<T> = LLNode<T>()

//append a new item
  func addLink(key: T) {
    if (head.key == nil) {
        head.key = key
        return
    }

    //establish loop variables
    var current: LLNode? = head

    while (current != nil) {
        if (current?.next == nil) {
            var childToUse: LLNode = LLNode<T>()
            childToUse.key = key
            childToUse.previous = current
```

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Linked Lists //25

#### **REMOVING LINKS**

Conversely, here's an example of removing items from a list. Removing links not only involves reclaiming memory (for the deleted item), but also reassigning links so the chain remains unbroken.

```
//remove at specific index
func removeLinkAtIndex(index: Int) {
    //check for nil conditions
    if ((index < 0) || (index > (self.count - 1)) || (head.key == nil)) {
        println("link index does not exist..")
        return
    }
    var current: LLNode<T>? = head
    var trailer: LLNode<T>?
    var listIndex: Int = 0
    //determine if the removal is at the head
    if (index == 0) {
        current = current?.next
        head = current!
        return
    }
    //iterate through the remaining items
    while (current != nil) {
        if (listIndex == index) {
            //redirect the trailer and next pointers
            trailer!.next = current?.next
            current = nil
            break
        }
```

```
//update the assignments
    trailer = current

    current = current?.next
    listIndex++
    } //end while
} //end function
```

#### **COUNTING LINKS**

It can also be convenient to count link items. In Swift, this can be expressed as a *computed property*. For example, the following technique will allow a linked list instance to use a dot notation. (e.g., someList.count).

```
//the number of items
var count: Int {
        if head.key == nil {
            return 0
        }
        else {
            var current: LLNode = head
            var x: Int = 1
            //cycle through the list of items
            while current.next != nil {
                current = current.next!
                χ++
            }
            return x
        }
}
```

#### **EFFICIENCY**

Linked lists typically provide O(n) for storage and lookup. As we'll see, linked lists are often used with other structures to create new models. Algorithms with an efficiency of O(n) are said to run in linear time.

## **GENERICS**

The introduction of Swift brings a new series of tools that make coding more friendly and expressive. Along with its simplified syntax, Swift borrows from the success of other languages to prevent common programming errors like null pointer exceptions and memory leaks.

To contrast, Objective-C has often been referred to as 'the wild west' of code. While extensive and powerful, many errors in Objective-C apps are discovered at runtime. This delay in error discovery is usually due to programming mistakes with memory management and type cast operations. For this essay, we'll review a new design technique with Swift called *generics* and will explore how this allows data structures to be more expressive and type-safe.

#### **BUILDING FRAMEWORKS**

As we've seen, data structures are the building blocks for organizing data. For example, linked lists, binary trees and queues provide a blueprint for data processing and analysis. Just like any well-designed program, data structures should also be designed for extensibility and reuse.

To illustrate, assume you're building a simple app that lists a group of students. The data could be easily organized with a linked list and represented in the following manner:

```
//student linked list structure

class StudentNode {
   var key: Student?
   var next: StudentNode?
}
```

#### THE CHALLENGE

While this structure is descriptive and organized, it's not reusable. In other words, the structure is valid for listing students but is unable to manage any other type of data (e.g. teachers). The property Student is an object that may include specific properties such as name, class schedule and grades. If you attempted to reuse the same StudentNode class to manage Teachers, this would cause a complier type mismatch.

The problem could be solved through inheritance, but it still wouldn't meet our primary goal of class reuse. This is where generics helps. Generics allows us to build generic versions of data structures so they can be used in different ways.

#### **APPLYING GENERICS**

If you've reviewed the other topics in this series, you've already seen generics in action. In addition to data structures and algorithms, core Swift functions like arrays and dictionaries also make use of generics. Let's refactor the StudentNode to be resuable:

```
//refactored linked list structure

class LLNode<T> {
   var key: T?
   var next: LLNode<T>?
}
```

With this revised structure we see several changes. The class name StudentNode has been changed to something more general (e.g., LLNode). The syntax <T> seen after the classname is called a *place-holder*. With generics, values seen inside angled brackets (e.g., T) are declared variables. Once the placeholder T is established, it can be reused anywhere a class reference would be expected. In this example, we've replaced the class type Student with the generic placeholder T.

#### THE IMPLEMENTATION

The power of generics can be now be seen through its implementation. With the class refactored, LLNode can now manage lists of Students, Teachers, or any other type we decide.

```
//a new list of students
var studentList = LLNode<Student>()

//a new list of teachers
var teacherList = LLNode<Teacher>()
```

Here's an expanded view of a linked list implementation using generics. The method addLinkAtIndex adds generic LLNodes at a specified index. Since portions of our code evaluate generic types, the type constraint Equatable is appended to the generic T placeholder. Native to Swift, Equatable is a simple protocol that ensures various object types conform to the equatable specification.

Generics //29

```
//insert at specific index
func addLinkAtIndex(key: T, index: Int) {
    //check for nil conditions
    if ((index < 0) \mid | (index > (self.count - 1))) {
        println("link index does not exist..")
    }
    //establish the head node
    if (head.key == nil) {
        head.key = key
        return
    }
    //establish the trailer, current and new items
    var current: LLNode<T>? = head
    var trailer: LLNode<T>?
    var listIndex: Int = 0
    //iterate through the list to find the insertion point
    while (current != nil) {
        if (index == listIndex) {
            var childToUse: LLNode = LLNode<T>()
            //create the new node
            childToUse.key = key
            //connect the node in front of the current node
            childToUse.next = current
            childToUse.previous = trailer
            //use optional binding when using the trailer
            if let linktrailer = trailer {
                linktrailer.next = childToUse
                childToUse.previous = linktrailer
            }
            //point new node to the current / previous
            current!.previous = childToUse
            //replace the head node if required
            if (index == 0) {
                head = childToUse
            break
        } //end if
```

```
//iterate through to the next item
    trailer = current
    current = current?.next
    listIndex += 1
} //end while
}
```

## **BINARY SEARCH TREES**

A binary search tree is a data structure that stores information in a logical hierarchy. As demonstrated with Big O Notation, algorithms provide the best results with sorted data. Binary Search Trees extend this idea by using specific rules. A binary search tree (BST) should not be mistaken for a binary tree or trie. Those structures also store information in a hierarchy, but employ different rules.

#### **HOW IT WORKS**

A binary search tree is comprised of a key and two indicators. The key represents the data you would like to store, such as a string or scalar value. Typically represented with pointers, the indicators store the location (also called the address) of its two children. The left child contains a value that is smaller than its parent. Conversely, the right child contains a value greater than its parent.

#### THE DATA STRUCTURE

Here's an example of a BST written in Swift. Using generics, the structure also stores any type of object and supports nil values. The concept of combining keys and pointers to create hierarchies not only applies to binary search trees, but to other structures like tries and binary trees.

```
/* an AVL tree is another name for a balanced binary search tree*/
public class AVLTree <T: Comparable> {
   var key: T?
   var left: AVLTree?
   var right: AVLTree?
}
```

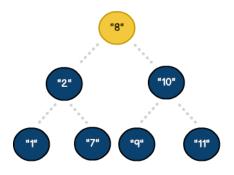
When creating algorithms, it is good practice to set your class properties to nil before they are used. Swift helps to enforce this best-practice at compile time through a new paradigm called *optionals*. Along with our class declaration, the generic type constraint <T: Comparable> is also defined to ensure instances conform to a specific protocol.

#### THE LOGIC

Here's an example of a simple array written in Swift. We'll use this data to build our binary search tree:

```
//a simple array of unsorted integers
let numberList : Array<Int> = [8, 2, 10, 9, 11, 1, 7]
```

Here's the same list visualized as a balanced binary search tree. It does not matter that the values are unsorted. Rules governing the BST will place each node in its "correct" position accordingly.



Balanced binary search tree - O (log n)

#### **BUILDING THE HIERARCHY**

Here's the class used for creating the BST. Written in Swift, the method addNode employs the rules to position each array value.

```
//add item based on its value
func addNode(key: T) {
    //check for the head node
    if (self.key == nil) {
        self.key = key
        return
    }
    //check the left side
    if (key < self.key) {</pre>
        if (self.left != nil) {
            left?.addNode(key)
        else {
             //create a new left node
            var leftChild : AVLTree = AVLTree()
            leftChild.key = key
            self.left = leftChild
        }
```

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Binary Search Trees ///33

```
} //end if

//check the right side
if (key > self.key) {
    if (self.right != nil) {
        right?.addNode(key)
    }
    else {

        //create a new right node
        var rightChild : AVLTree = AVLTree()
        rightChild.key = key
        self.right = rightChild
    }

} //end if
} //end function
```

The method addNode uses recursion to determine where data is added. While not required, recursion is a powerful enabler as each child becomes another instance of a BST. As a result, inserting data becomes a straightforward process of iterating through the array.

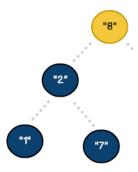
```
//a simple array of unsorted integers
let numberList : Array<Int> = [8, 2, 10, 9, 11, 1, 7]

//create a new BST instance
var root = AVLTree<Int>()

//sort each item in the list
for number in numberList {
    root.addNode(number)
}
```

#### **EFFICIENCY**

BSTs are powerful due to their consistent rules. However, their greatest advantage is speed. Since data is organized at the time of insertion, a clear pattern emerges. Values less than the root node (e.g 8) will naturally filter to the left. Conversely, all values greater than the root will filter to the right.



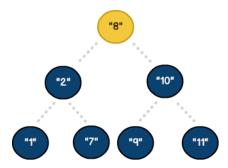
As we saw with Big O Notation, our understanding of the data allows us to create an effective algorithm. So, for example, if we were searching for the value 7, it's only required that we traverse the left side of the BST. This is due to our search value being smaller than our root node (e.g 8). Binary Search Trees typically provide O(log n) for insertion and lookup. Algorithms with an efficiency of O(log n) are said to run in logarithmic time.

## TREE BALANCING

In the previous chapter, we saw how binary search trees (BST) are used to manage data. With basic logic, an algorithm can easily traverse a model, searching data in O(log n) time. However, there are occasions when navigating a tree becomes inefficient - in some cases working at O(n) time. In this essay, we will review those scenarios and introduce the concept of tree balancing.

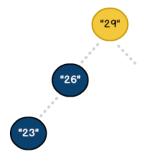
#### **NEW MODELS**

To start, let's revisit our original example. Array values from numberList were used to build a tree. As shown, all nodes had either one or two children - otherwise called leaf nodes. This is known as a balanced binary search tree.

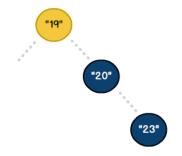


A balanced BST with 7 nodes - O (log n)

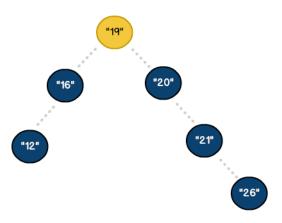
Our model achieved balance not only through usage of the addWord algorithm, but also by the way keys were inserted. In reality, there could be numerous ways to populate a tree. Without considering other factors, this can produce unexpected results:



An unbalanced "left-heavy" BST with 3 nodes - O(n)



An unbalanced "right-heavy" BST with 3 nodes - O(n)

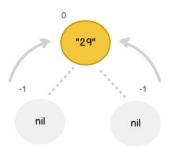


A 6-node BST with left and right imbalances - O(n)

#### **NEW HEIGHTS**

To compensate for these imbalances, we need to expand the scope of our algorithm. In addition to left / right logic, we'll add a new property called height. Coupled with specific rules, we can use height to detect tree imbalances. To see how this works, let's create a new BST:

```
//a simple array of unsorted integers
let balanceList : Array<Int> = [29, 26, 23]
```



Tree Balancing ///37

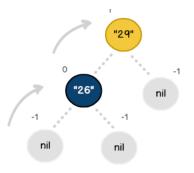
To start, we add the root node. As the first item, left / right leaves don't yet exist so they are initialized to nil. Arrows point from the leaf nodes to the root because they are used to calculate its height. For math purposes, the height of non-existent leaves are set to -1.

With a model in place, we can calculate the node's height. This is done by comparing the height of each leaf, finding the largest value, then increasing that value by +1. For the root node this equates to 0. In Swift, these rules can be represented as follows:

```
//retrieve the height of a node
func getNodeHeight(aNode: AVLTree!) -> Int {
    if (aNode == nil) {
        return -1
    }
    else {
       return aNode.height
}
//calculate the height of a node
func setNodeHeight() -> Bool {
    //check for a nil condition
    if (self.key == nil) {
        println("no key provided..")
        return false
    }
    //initialize leaf variables
    var nodeHeight: Int = 0
    //do comparision and calculate node height
    nodeHeight = max(getNodeHeight(self.left), getNodeHeight(self.right)) + 1
    self.height = nodeHeight
    return true
}
```

#### MEASURING BALANCE

With the root node established, we can proceed to add the next value. Upon implementing standard BST logic, item 26 is positioned as the left leaf node. As a new item, its height is also calculated (i.e., 0). However, since our model is a hierarchy, we traverse upwards to recalculate its parent height value.



Step two: 26 is added to the BST

With multiple nodes present, we run an additional check to see if the BST is balanced. In computer science, a tree is considered balanced if the height difference between its leaf nodes is less than 2. As shown below, even though no right-side items exist, our model is still valid.

```
//example math for tree balance check

var rootVal: Int!
var leafVal: Int!

leafVal = abs((-1) - (-1)) //equals 0 (balanced)
rootVal = abs((0) - (-1)) //equals 1 (balanced)
```

In Swift, these nodes can be checked with the isTreeBalanced method.

```
//determine if the tree is "balanced"

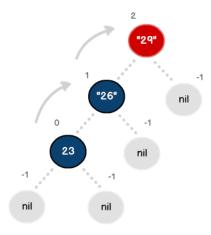
func isTreeBalanced() -> Bool {
    //check for a nil condition
    if (self.key == nil) {
        println("no key provided..")
        return false
    }

    //use absolute values to manage right and left imbalances
    if (abs(getNodeHeight(self.left) - getNodeHeight(self.right)) <= 1) {
        return true
    }
    else {
        return false
    }
} //end function</pre>
```

Tree Balancing //39

#### **ADJUSTING THE MODEL**

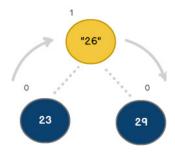
With 29 and 26 added we can proceed to insert the final value (i.e., 23). Like before, we continue to traverse the left side of the tree. However, upon insertion, the math reveals node 29 violates the BST property. In other words, its subtree is no longer balanced.



Step three: 23 is added to the BST

```
//example math for tree balance check
var rootVal: Int!
rootVal = abs((1) - (-1)) //equals 2 (unbalanced)
```

For the tree to maintain its BST property, we need to change its performance from O(n) to O(log n). This can be achieved through a process called *rotation*. Since the model has more nodes to the left, we'll balance it by performing a right rotation sequence. Once complete, the new model will appear as follows:



Step four: right rotation on node 29

```
//right rotation sequence

var childToUse : AVLTree = AVLTree()
childToUse.height = 0
childToUse.key = self.key

if (getNodeHeight(self.left) - getNodeHeight(self.right) > 1) {
    //reset the root node
    self.key = self.left?.key
    self.height = getNodeHeight(self.left)

    //assign the new right node
    self.right = childToUse

//adjust the left node
    self.left?.left
    self.left?.height = 0
    return true
}
```

Even though we undergo a series of steps, the process occurs in O(1) time. Meaning, its performance is unaffected by other factors such as number of leaf nodes, descendants or tree height. In addition, even though we've completed a right rotation, similar steps could be implemented to resolve both left and right imbalances.

#### THE RESULTS

With tree balancing, it is important to note that techniques like rotations improve performance, but do not change tree output. For example, even though a right rotation changes the connections between nodes, the overall BST sort order is preserved. As a test, one can traverse a balanced and unbalanced BST (comparing the same values) and receive the same results. In our case, a simple depth-first search will produce the following:

```
//sorted values from a traversal 23, 26, 29
```

See p.69 to learn more about traversals and Depth-First Search.

## **TRIES**

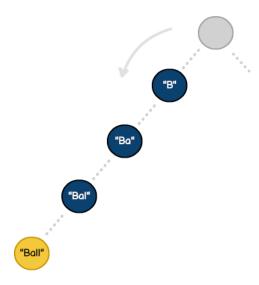
Similar to binary search trees, trie data structures also organize information in a logical hierarchy. Often pronounced "try", the term comes from the English language verb to retrieve. While most algorithms are designed to manipulate generic data, tries are commonly used with strings. In this chapter, we'll review trie structures and will implement our own trie model with Swift.

#### **HOW IT WORKS**

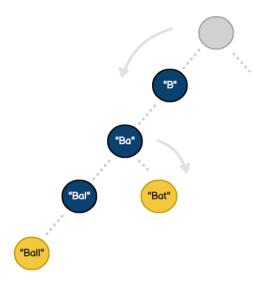
As discussed, tries organize data in a hierarchy. To see how they work, let's build a dictionary that contains the following words:

Ball Balls Ballard Bat Bar Cat Dog

At first glance, we see words prefixed with the phrase "Ba", while entries like "Ballard" combine words and phrases (e.g., "Ball" and "Ballard"). Even though our dictionary contains a limited quantity of words, a thousand-item list would have the same properties. As with any algorithm, we'll apply our knowledge to build an efficient model. To start, let's create a new trie for the word "Ball":



Tries involve building hierarchies, storing phrases along the way until a word is created (seen in yellow). With so many permutations, it's important to know what qualifies as an actual word. For example, even though we've stored the phrase "Ba", it's not identified as a word. To see the significance, consider the next example:



#### THE DATA STRUCTURE

Here's an example of a trie data structure written in Swift. In addition to storing a key, the structure also includes an Array for identifying its children. Unlike a binary search tree, a trie can store an unlimited number of leaf nodes. The boolean value isFinal will allow us to distinguish words and phrases. Finally, the level will indicate the node's level in a hierarchy.

```
//basic trie data structure

public class TrieNode {

  var key: String!
  var children: Array<TrieNode>
  var isFinal: Bool
  var level: Int

  init() {
     self.children = Array<TrieNode>()
     self.isFinal = false
     self.level = 0
  }
}
```

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#### **ADDING WORDS**

Here's an algorithm that adds words to a trie. Although most tries are recursive structures, our example employs an iterative technique. The while loop compares the keyword length with the current node's level. If no match occurs, it indicates additional keyword phases remain to be added.

```
//builds a iterative tree of dictionary content
func addWord(keyword: String) {
    if (keyword.length == 0){
        return
    var current: TrieNode = root
    var searchKey: String!
    while(keyword.length != current.level) {
        var childToUse: TrieNode!
        var searchKey: String = keyword.substringToIndex(current.level + 1)
        //iterate through the node children
        for child in current.children {
            if (child.key == searchKey) {
                childToUse = child
                break
            }
        }
        //create a new node
        if (childToUse == nil) {
            childToUse = TrieNode()
            childToUse.key = searchKey
            childToUse.level = current.level + 1
            current.children.append(childToUse)
        }
        current = childToUse
    } //end while
    //add final end of word check
    if (keyword.length == current.level) {
        current.isFinal = true
```

```
println("end of word reached!")
    return
}
//end function
```

A final check confirms our keyword after completing the while loop. As part of this final check, we update the current node with the isFinal indicator. As mentioned, this step will allow us to distinguish words from phrases.

#### **FINDING WORDS**

The algorithm for finding words is similar to adding content. Again, we establish a while loop to navigate the trie hierarchy. Since the goal will be to return a list of possible words, these will be tracked using an Array.

```
//finds all words based on the prefix
func findWord(keyword: String) -> Array<String>! {
    if (keyword.length == 0){
        return nil;
    }
    var current: TrieNode = root
    var searchKey: String!
    var wordList: Array<String>! = Array<String>()
    while(keyword.length != current.level) {
        var childToUse: TrieNode!
        var searchKey: String = keyword.substringToIndex(current.level + 1)
        //iterate through any children
        for child in current.children {
            if (child.key == searchKey) {
                childToUse = child
                current = childToUse
                break
        }
        if (childToUse == nil) {
            return nil
    } //end while
```

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Tries //45

```
//retrieve the keyword and any descendants
if ((current.key == keyword) && (current.isFinal)) {
    wordList.append(current.key)
}

//include only children that are words
for child in current.children {
    if (child.isFinal == true) {
        wordList.append(child.key)
    }
}

return wordList
}
```

The findWord function checks to ensure keyword phrase permutations are found. Once the entire keyword is identified, we start the process of building our word list. In addition to returning keys identified as words (e.g., "Bat", "Ball"), we account for the possibility of returning nil by returning an implicit unwrapped optional.

#### **EXTENDING SWIFT**

Even though we've written our trie in Swift, we've extended some language features to make things work. Commonly known as *categories* in Objective-C, our algorithms employ two additional Swift extensions. The following class extends the functionality of the native String class:

```
extension String {
    //compute the length of string
    var length: Int {
        return count(self)
    }

    //returns characters range to a specified index
    func substringToIndex(to: Int) -> String {
        return self.substringToIndex(advance(self.startIndex, to))
    }

    //return a character at a specific index
    func characterAtIndex(position: Int) -> String {
        return String(Array(self)[position])
    }
}
```

- » Trie Data Structure http://en.wikipedia.org/wiki/Trie
- » Recursion https://en.wikipedia.org/wiki/Recursion\_(computer\_science)

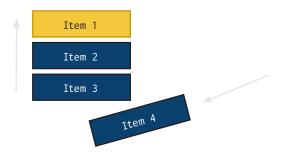
# **STACKS & QUEUES**

Stacks and queues are structures that help organize data in a particular order. Their concept is based on the idea that information can be organized similar to how things interact in the real world. For example, a stack of dinner plates can be represented by placing a single plate on a group of existing plates. Similarly, a queue can be easily understood by observing groups of people waiting in a line at a concert or grand opening.

In computer science, the idea of stacks and queues can be seen in numerous ways. Any app that makes use of a shopping cart, waiting list or playlist employs a stack or queue. In programming, a call stack is often used as an essential debugging and analytics tool. For this essay, we'll discuss the idea of stacks and queues and will review how to implement a queue in code.

#### **HOW IT WORKS**

Queues are based on the concept of "first-in, first-out". When new objects are created, they are added to the bottom of the queue. Items in the queue are preserved in order until requested. When a request is made, the top level item is removed and is sent to the client.



In their basic form, stacks and queues employ the same structure and only vary in their use. The data structure common to both forms is the linked list. Using generics, we'll build a queue to hold any type of object. In addition, the class will also support nil values.

```
//generic queue node

class QNode<T> {

   var key: T?
   var next: QNode?
}
```

#### **ENQUEUING OBJECTS**

The process of adding items is often referred to as "enqueuing". Here, we define the method used to enqueue objects and identify the property top that will serve as our starting point.

```
//enqueue the specified object
func enQueue(key: T) {
    //check for the instance
    if (top == nil) {
        top = QNode<T>()
    //establish the top node
    if (top.key == nil) {
        top.key = key;
        return
    }
    var childToUse: QNode<T> = QNode<T>()
    var current: QNode = top
    //cycle through the list of items
    while (current.next != nil) {
        current = current.next!
    }
    //append a new item
    childToUse.key = key;
    current.next = childToUse;
}
```

The process to enqueue items is similar to building a generic linked list. However, since queued items can be removed as well as added, we must ensure that our structure supports the absence of values (e.g. nil). As a result, the class property top is defined as an implicit unwrapped optional.

To keep the queue generic, the enQueue method signature also has a parameter that is declared as type T. With Swift, generics usage not only preserves type information, but also ensures objects conform to various protocols.

#### **DEQUEUEING OBJECTS**

Removing items from the queue is called dequeuing. As shown, dequeueing is a two-step process that involves returning the top-level item and reorganizing the queue.

Stacks and Queues //49

```
//retrieve items from the top level in O(1) constant time
func deQueue() -> T? {
     //determine if the key or instance exist
     let topitem: T? = self.top?.key
     if (topitem == nil) {
         return nil
     }
     //retrieve and queue the next item
     var queueitem: T? = top.key!
     //use optional binding
     if let nextitem = top.next {
       top = nextitem
     else {
         top = nil
     }
     return queueitem
 }
```

When dequeuing, it is vital to know when values are absent. With deQueue, we account for the potential absence of a key in addition to an empty queue. In Swift, one must use specific techniques like optional chaining to check for nil values.

#### SUPPORTING FUNCTIONS

Along with adding and removing items, supporting functions also include checking for an empty queue as well as retrieving the top level item.

```
//check for queue
func isEmpty() -> Bool {

    //check for key instance
    if let topitem: T = self.top?.key {
        return false
    }

    else {
        return true
    }
}
```

```
//retrieve the top most item
func peek() -> T? {
    return top.key!
}
```

#### **EFFICIENCY**

In this example, our queue provides O(n) for insertion and O(1) for lookup. As noted, stacks support the same basic structure and generally provide O(1) for both storage and lookup. Similar to linked lists, stacks and queues play an important role when managing other data structures and algorithms.

- » Stacks http://en.wikipedia.org/wiki/Stack\_(abstract\_data\_type)
- » Queues http://en.wikipedia.org/wiki/Queue\_(abstract\_data\_type)
- » Call Stack http://en.wikipedia.org/wiki/Call\_stack

### **GRAPHS**

A graph is a data structure that shows a relationship (e.g., connection) between two or more objects. Because of their flexibility, graphs are one of the most widely used structures in modern computing. Popular tools and services like online maps, social networks, and even the Internet as a whole are based on how objects relate to one another. In this chapter, we'll highlight the key features of graphs and will demonstrate how to create a basic graph with Swift.

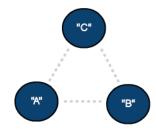
#### THE BASICS

As discussed, a graph is a model that shows how objects relate to one another. Graph objects are usually referred to as nodes or vertices. While it would be possible to build and graph a single node, models that contain multiple vertices better represent real-world applications.

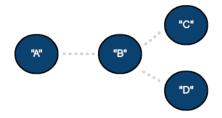
Graph objects relate to one another through connections called edges. Depending on your requirements, a vertex could be linked to one or more objects through a series of edges. It's also possible to create a vertex without edges. Here are some basic graph configurations:



An undirected graph with two vertices and one edge.



An undirected graph with three vertices and three edges.



An undirected graph with four vertices and three edges.

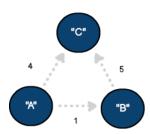
#### **DIRECTED VS. UNDIRECTED**

As shown above, there are many ways to configure a graph. An additional option is to set the model to be either directed or undirected. The examples above represent undirected graphs. In other words, the connection between vertices A and B is equivalent to the connection between vertices B and A. Social networks are a great example of undirected graphs. Once a request is accepted, both parties (e.g. the sender and recipient) share a mutual connection.

A service like *Google Maps* is a great example of a directed graph. Unlike an undirected graph, directed graphs only support a one-way connection between source vertices and their destinations. So, for example, vertex A could be connected to B, but A wouldn't necessarily be reachable through B. To show the varying relationship between vertices, directed graphs are drawn with lines and arrows.

#### **EDGES & WEIGHTS**

Regardless of graph type, it's common to represent the level of connectedness between vertices. Normally associated with an edge, the weight is a numerical value tracked for this purpose. As we'll see, modeling of graphs with edge weights can be used to solve a variety of problems.



A directed graph with three vertices and three weighted edges.

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#### THE VERTEX

With our understanding of graphs in place, let's build a basic directed graph with edge weights. To start, here's a data structure that represents a vertex:

```
public class Vertex {
    var key: String?
    var neighbors: Array<Edge>
    init() {
        self.neighbors = Array<Edge>()
    }
}
```

As we've seen with other structures, the key represents the data to be associated with a class instance. To keep things straightforward, our key is declared as a string. In a production app, the key type would be replaced with a generic placeholder, <T>. This would allow the key to store any object like an integer, account or profile.

#### **ADJACENCY LISTS**

The neighbors property is an array that represents connections a vertex may have with other vertices. As discussed, a vertex can be associated with one or more items. This list of neighboring items is sometimes called an adjacency list and can be used to solve a variety of problems. Here's a basic data structure that represents an edge:

```
public class Edge {
    var neighbor: Vertex
    var weight: Int

    init() {
        weight = 0
        self.neighbor = Vertex()
    }
}
```

#### **BUILDING THE GRAPH**

With our vertex and edge objects built, we can use these structures to construct a graph. To keep things straightforward, we'll focus on the essential operations of adding and configuring vertices.

A graph canvas could also be implemented with a Swift "Set" collection type.

```
public class SwiftGraph {
    //declare a default directed graph canvas
    private var canvas: Array<Vertex>
    public var isDirected: Bool
    init() {
        canvas = Array<Vertex>()
        isDirected = true
    }
    //create a new vertex
    func addVertex(#key: String) -> Vertex {
        //set the key
        var childVertex: Vertex = Vertex()
        childVertex.key = key
        //add the vertex to the graph canvas
        canvas.append(childVertex)
        return childVertex
    }
}
```

The function addVertex accepts a string which is used to create a new vertex. The SwiftGraph class also has a private property named canvas which is used to manage all vertices. While not required, the canvas can be used to track and manage vertices with or without edges.

#### MAKING CONNECTIONS

Once a vertex is added, it can be connected to other vertices. Here's the process of establishing an edge:

```
//add edge to source vertex
func addEdge(#source: Vertex, neighbor: Vertex, weight: Int) {
    //create a new edge
    var newEdge = Edge()

    //establish the default properties
    newEdge.neighbor = neighbor
    newEdge.weight = weight
    source.neighbors.append(newEdge)

//check condition for an undirected graph
    if (isDirected == false) {
```

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```
//create a new reversed edge
var reverseEdge = Edge()

//establish the reversed properties
reverseEdge.neighbor = source
reverseEdge.weight = weight
neighbor.neighbors.append(reverseEdge)
}
```

The function addEdge receives two vertices, identifying them as source and neighbor. Since our model defaults to a directed graph, a new edge is created and is added to the adjacency list of the source vertex. For an undirected graph, an additional edge is created and added to the neighbor vertex.

As we've seen, there are many components to graph theory. In the next section, we'll examine a popular problem (and solution) with graphs known as *shortest paths*.

- » Graph Theory http://en.wikipedia.org/wiki/Graph\_theory
- » Google Maps https://www.google.com/maps
- » Adjacency Lists http://en.wikipedia.org/wiki/Adjacency\_list

### SHORTEST PATHS

In the previous chapter, we saw how graphs show the relationship between two or more objects. Because of their flexibility, graphs are used in a wide range of applications including map-based services, networking and social media. Popular models may include roads, traffic, people and locations. In this chapter, we'll review how to search a graph and will implement a popular algorithm called *Dijkstra's shortest path*.

#### MAKING CONNECTIONS

The challenge with graphs is knowing how a vertex relates to other objects. Consider the social networking website, LinkedIn. With LinkedIn, each profile can be thought of as a single vertex that may be connected with other vertices.

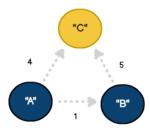
One feature of LinkedIn is the ability to introduce yourself to new people. Under this scenario, LinkedIn will suggest routing your message through a shared connection. In graph theory, the most efficient way to deliver your message is called the *shortest path*.



The shortest path from vertex A to C is through vertex B

#### FINDING YOUR WAY

Shortest paths can also be seen with map-based services like *Google Maps*. Users frequently use Google Maps to ascertain driving directions between two points. As we know, there are often multiple ways to get to any destination. The shortest route will often depend on various factors such traffic, road conditions, accidents and time of day. In graph theory, these external factors represent edge weights.

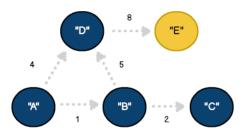


The shortest path from vertex A to C is through vertex A.

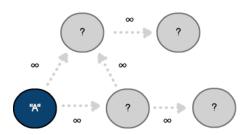
This example illustrates some key points we'll see in Dijkstra's algorithm. In addition to there being multiple ways to arrive at vertex C from A, the shortest path is assumed to be through vertex B. It's only when we arrive to vertex C from B, we adjust our interpretation of the shortest path and change direction (e.g. 4 < (1 + 5)). This change in direction is known as the *greedy approach* and is used in similar problems like the *traveling salesman*.

#### INTRODUCING DIJKSTRA

Edsger Dijkstra's algorithm was published in 1959 and is designed to find the shortest path between two vertices in a directed graph with non-negative edge weights. Let's review how to implement this in Swift.



Even though our model is labeled with key values and edge weights, our algorithm can only see a subset of this information. Starting at the source vertex, our goal will be to traverse the graph.



#### **USING PATHS**

Throughout our journey, we'll track each node visit in a custom data structure called Path. The total will manage the cumulative edge weight to reach a particular destination. The previous property will represent the Path taken to reach that vertex.

```
//the path class maintains objects that comprise the "frontier"

class Path {
   var total: Int!
   var destination: Vertex
   var previous: Path!
```

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Shortest Paths //59

```
//object initialization
init() {
    destination = Vertex()
}
```

#### **DECONSTRUCTING DIJKSTRA**

With all the graph components in place, let's see how it works. The method processDijkstra accepts the vertices source and destination as parameters. It also returns a Path. Since it may not be possible to find the destination, the return value is declared as a Swift optional.

```
//process Dijkstra's shortest path algorithm
func processDijkstra(source: Vertex, destination: Vertex) -> Path? {
    ...
}
```

#### **BUILDING THE FRONTIER**

As discussed, the key to understanding Dijkstra's algorithm is knowing how to traverse the graph. To help, we'll introduce a few rules and a new concept called the frontier.

```
var frontier = Array<Path>()
var finalPaths = Array<Path>()

//create the frontier
for e in source.neighbors {

   var newPath: Path = Path()

   newPath.destination = e.neighbor
   newPath.previous = nil
   newPath.total = e.weight

   //add the new path to the frontier
   frontier.append(newPath)
}
```

The algorithm starts by examining the source vertex and iterating through its list of neighbors. Recall from the previous chapter, each neighbor is represented as an edge. For each iteration, information about the neighboring edge is used to construct a new Path. Finally, each Path is added to the frontier.

Total Weight	Destination Vertex	Previous Vertices
4	D	A (nil)
1	В	A (nil)

The frontier visualized as a list

With our frontier established, the next step involves traversing the Path with the smallest total weight (e.g, B). Identifying the bestPath is accomplished using this linear approach:

```
//construct the best path
var bestPath: Path = Path()

while frontier.count != 0 {
    //the greedy approach
    bestPath = Path()
    var pathIndex: Int = 0

for x in 0..<frontier.count {
    var itemPath: Path = frontier[x]

    if (bestPath.total == nil) || (itemPath.total < bestPath.total) {
        bestPath = itemPath
        pathIndex = x
    }
}</pre>
```

An important section to note is the while loop condition. As we traverse the graph, Path objects will be added and removed from the frontier. Once a Path is removed, we assume the shortest path to that destination as been found. As a result, we know we've traversed all possible paths when the frontier reaches zero.

```
//enumerate the bestPath edges
for e in bestPath.destination.neighbors {
   var newPath: Path = Path()
   newPath.destination = e.neighbor
   newPath.previous = bestPath
   newPath.total = bestPath.total + e.weight
```

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Shortest Paths //61

```
//add the new path to the frontier
    frontier.append(newPath)

}

//preserve the bestPath
    finalPaths.append(bestPath)

//remove the bestPath from the frontier
    frontier.removeAtIndex(pathIndex)

} //end while
```

As shown, we've used the bestPath to build a new series of Paths. We've also preserved our visit history with each new object. With this section completed, let's review our changes to the frontier:

Total Weight	Destination Vertex	Previous Vertices
4	D	A (nil)
6	D	B - A (nil)
3	С	B - A (nil)

The frontier after visiting two additional vertices.

At this point, we've learned a little more about our graph. There are now two possible paths to vertex D. The shortest path has also changed to arrive at vertex C. Finally, the Path through route A-B has been removed and has been added to a new structure named finalPaths.

#### A SINGLE SOURCE

Dijkstra's algorithm can be described as "single source" because it calculates the path to every vertex. In our example, we've preserved this information in the finalPaths array.

Total Weight	Destination Vertex	Previous Vertices
1	В	A (nil)
3	С	B - A (nil)
4	D	A (nil)
6	D	B - A (nil)
12	E	D - A (nil)
14	E	D - B - A (nil)

The finalPaths once the frontier reaches zero. As shown, every permutation from vertex A is calculated.

Based on this data, we can see the shortest path to vertex E from A is A-D-E. The bonus is that in addition to obtaining information for a single route, we've also calculated the shortest path to each node in the graph.

See the complete algorithm for Dijkstra's Shortest Path on Github.

#### **ASYMPTOTICS**

Dijkstra's algorithm is an elegant solution to a complex problem. Even though we've used it effectively, we can improve its performance by making a few adjustments. We'll analyze those details in the next chapter.

- » Graph Theory http://en.wikipedia.org/wiki/Graph\_theory
- » Greedy Approach http://en.wikipedia.org/wiki/Greedy\_algorithm
- » Traveling Salesman http://en.wikipedia.org/wiki/Travelling\_salesman\_problem
- » Edsger Dijkstra http://en.wikipedia.org/wiki/Edsger\_W.\_Dijkstra
- » Dijkstra's Algorithm http://en.wikipedia.org/wiki/Dijkstra%27s\_algorithm

## **HEAPS**

In the previous chapter, we reviewed Dijkstra's algorithm for searching a graph. Originally published in 1959, this popular technique for finding the shortest path is an elegant solution to a complex problem. The design involved many parts including graph traversal, custom data structures and the greedy approach.

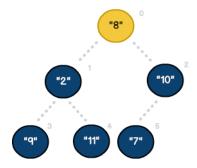
When designing programs, it's great to see them work. With Dijkstra, the algorithm did allow us to find the shortest path between a source vertex and destination. However, our approach could be refined to be more efficient. In this essay, we'll enhance the algorithm with the addition of binary heaps.

#### **HOW IT WORKS**

In its basic form, a heap is just an Array. However, unlike an Array, we *visualize* it as a tree. The term "*visualize*" implies we use processing techniques normally associated with recursive data structures. This shift in thinking has numerous advantages. Consider the following:

```
//a simple array of unsorted integers
let numberList : Array<Int> = [8, 2, 10, 9, 11, 7]
```

As shown, numberList can be easily represented as a heap. Starting at index 0, items fill a corresponding spot as a parent or child node. Each parent also has two children with the exception of index 2.



An array visualized as a "nearly complete" tree

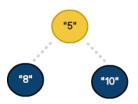
Since the arrangement of values is sequential, a simple pattern emerges. For any node, we can accurately predict its position using these formulas:

$$parent = floor(\frac{i-1}{2})$$
 
$$left = 2i + 1 \qquad right = 2i + 2$$

Formulas to calculate heap indices

#### **SORTING HEAPS**

An interesting feature of heaps is their ability to sort data. As we've seen, many algorithms are designed to sort entire datasets. When sorting heaps, nodes can be arranged so each parent contains a lesser value than its children. In computer science, this is called a *min-heap*.



A heap structure that maintains the min-heap property

#### **EXPLORING THE FRONTIER**

With Dijkstra, we used a concept called the frontier. Coded as a simple array, we compared the total weight of each path to find the shortest path.

```
var bestPath: Path = Path()
while frontier.count != 0 {
    //support path changes using the greedy approach
    bestPath = Path()
    var pathIndex: Int = 0

for x in 0..<frontier.count {
    var itemPath: Path = frontier[x]

    if (bestPath.total == nil) || (itemPath.total < bestPath.total) {
        bestPath = itemPath
        pathIndex = x
    }
}</pre>
```

While it accomplished our goal, we applied a brute force technique. In other words, we examined every potential Path to find the shortest path. This code segment executes in *linear time* or O(n). If the frontier contained a million rows, how would this impact the algorithm's overall performance?

#### THE HEAP STRUCTURE

Let's create a more efficient frontier. Named PathHeap, the data structure will extend the functionality of an array.

```
public class PathHeap {
    private var heap: Array<Path>
    init() {
        heap = Array<Path>()
    }

    //the number of frontier items
    var count: Int {
        return self.heap.count
    }
}
```

The PathHeap class includes two properties. To support good design, heap has been declared a private property. To track the number of items, count is declared as a computed property.

### **BUILDING THE QUEUE**

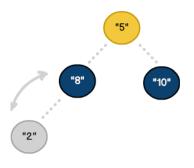
Searching the frontier more efficiently than O(n) will require a new way of thinking. We can improve our performance to O(1) with a heap. Using heapsort formulas, our new approach will involve arranging index values so the smallest item is positioned at the root.

```
//sort paths into a min-heap
func enQueue(key: Path) {
   heap.append(key)
   var childIndex: Float = Float(heap.count) - 1
   var parentIndex: Int! = 0

   //calculate parent index
   if childIndex != 0 {
      parentIndex = Int(floorf((childIndex - 1) / 2))
   }
}
```

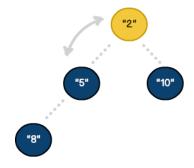
```
var childToUse: Path
    var parentToUse: Path
    //use the bottom-up approach
    while childIndex != 0 {
        childToUse = heap[Int(childIndex)]
        parentToUse = heap[parentIndex]
        //swap child and parent positions
        if childToUse.total < parentToUse.total {</pre>
             swap(&heap[parentIndex], &heap[Int(childIndex)])
        }
        //reset indices
        childIndex = Float(parentIndex)
        if (childIndex != 0) {
             parentIndex = Int(floorf((childIndex - 1) / 2))
        }
    } //end while
} //end function
```

The enQueue method accepts a single Path as a parameter. Unlike other sorting algorithms, our primary goal isn't to sort each item, but to find the smallest value. This means we can increase our efficiency by comparing a subset of values.



The enQueue process compares a newly added value

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The process continues until the smallest value is positioned at the root

Since the enQueue method maintains the min-heap property, we eliminate the task of finding the shortest path. In other words, we increase the algorithm's efficiency to O(1). Here, we implement a basic peek method to retrieve the root-level item.

```
//obtain the minimum path

func peek() -> Path! {

    if (heap.count > 0) {
        return heap[0] //the shortest path
    }
    else {
        return nil
    }
}
```

#### THE RESULTS

With the frontier refactored, let's see the applied changes. As new Paths are discovered, they are automatically sorted by the frontier. The count property forms the base case for our loop condition and the bestPath is retrieved using the peek method.

```
//construct the best path

var frontier: PathHeap = PathHeap()
var bestPath: Path = Path()

while frontier.count != 0 {

    //use the greedy approach to obtain the best path
    bestPath = Path()
    bestPath = frontier.peek()

.....
```

See the complete algorithm for Dijkstra's Shortest Path with Heaps on Github.

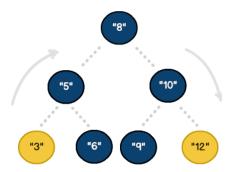
- » Greedy Approach http://en.wikipedia.org/wiki/Greedy\_algorithm
- » Binary Heaps http://en.wikipedia.org/wiki/Binary\_heap
- » Heapsort http://en.wikipedia.org/wiki/Heapsort
- » Base Case http://en.wikipedia.org/wiki/Mathematical\_induction

### **TRAVERSALS**

Throughout this series we've explored various data structures such as binary search trees and graphs. Once established, these objects work like a database - managing data in a structured format. Like most databases, their contents can also be explored through a process called *traversal*. In this chapter, we'll review traversing data structures and will examine the popular techniques of *Depth-First* and *Breadth-First* search.

#### **DEPTH-FIRST SEARCH**

Traversals are based on the idea of *visiting* each node in a data structure. In practical terms, traversals can be seen through everyday activities like network administration. To meet security requirements, administrators will often deploy software updates to an entire network as a single task. To see how traversal works, let's introduce the concept of *Depth-First* Search (DFS). As shown with this binary search tree, our goal will be to explore the left side of the model, visit the root node, then visit the right side.



The yellow nodes represent the first and last nodes in the traversal. The algorithm requires little code, but introduces some interesting concepts.

```
//dfs in-order traversal

func processAVLDepthTraversal() {

    //check for nil condition
    if self.key == nil {
        println("no key provided..")
        return
    }
}
```

```
//process the left side
if self.left != nil {
    left?.processAVLDepthTraversal()
}

//process the right side
if self.right != nil {
    right?.processAVLDepthTraversal()
}
```

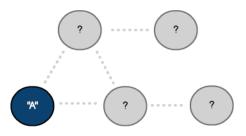
At first glance, we note the algorithm makes use of recursion. The AVLTree node (e.g. self), contains a key, as well as pointer references to its left and right nodes. For each side, (e.g., left and right) the base case consists of a straightforward check for nil. This process allows us to traverse the entire structure starting at the lowest value. When applied, the algorithm produces the following output:

```
3, 5, 6, 8, 9, 10, 12
```

#### **BREADTH-FIRST SEARCH**

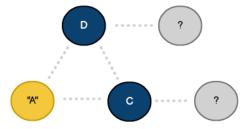
Breadth-First Search (BFS) is another technique used for traversing data structures. This algorithm is designed for open-ended data models and is typically used with graphs.

Our BFS algorithm combines techniques previously discussed including stacks, queues and shortest paths. With BFS, our goal is to visit all neighbors before visiting our neighbor's, neighbor. Unlike Depth-First Search, the algorithm is based on logical discovery.



We've chosen vertex A as the starting point. Unlike Dijkstra, BFS has no concept of a destination or frontier. The algorithm is complete when all connected nodes have been visited. As a result, the starting point could have been any node in our graph.

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Vertex A is marked as visited once its neighbors have been added to the queue.

As discussed, BFS works by exploring neighboring vertices. Since our data structure is an undirected graph, we need to ensure each node is visited only once. To account for this requirement we can use a generic queue:

```
//breadth first search
func traverseGraphBFS(startingv: Vertex) {
     var graphQueue: Queue<Vertex> = Queue<Vertex>()
     //queue a starting vertex
     graphQueue.enQueue(startingv)
     while !graphQueue.isEmpty() {
         //traverse the next queued vertex
         var vitem = graphQueue.deQueue() as Vertex!
         //add unvisited vertices to the queue
         for e in vitem.neighbors {
             if e.neighbor.visited == false {
                 println("adding vertex: \((e.neighbor.key!)) to queue..")
                 graphQueue.enQueue(e.neighbor)
             }
         }
         vitem.visited = true
         println("traversed vertex: \(vitem.key!)..")
     } //end while
     println("graph traversal complete..")
 } //end function
```

The process starts by adding a single vertex to the queue. As nodes are dequeued, their neighbors are also added to the queue. The process is complete when all vertices are visited. To ensure nodes are not visited more than once, each vertex is marked with a boolean flag.

- » Traversal http://en.wikipedia.org/wiki/Tree\_traversal
- » Depth-First Search http://en.wikipedia.org/wiki/Depth-first\_search
- » Breadth-First Search http://en.wikipedia.org/wiki/Breadth-first\_search

## **HASH TABLES**

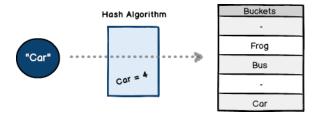
A hash table is a data structure that groups values to a key. As we've seen, structures like graphs, tries and linked lists follow this widely adopted model. In some cases, built-in Swift data types (like dictionaries) also accomplish the same goal. In this chapter, we'll examine the advantages of hash tables and will build our own custom hash table model in Swift.

#### **KEYS & VALUES**

As noted, there are numerous data structures that group values to a key. By definition, linked lists provide a straightforward way to associate related items. While the advantage of linked lists is flexibility, their downside is lack of speed. Since the only way to search a list is to traverse the entire set, their efficiency is typically limited to O(n). To contrast, a dictionary associates a value to a user-defined key. This helps pinpoint operations to specific entries. As a result, dictionary operations are typically O(1).

#### THE BASICS

As the name implies, a hash table consists of two parts - a key and value. However, unlike a dictionary, the key is a *calculated* sequence of numbers and / or characters. The output is known as a *hash*. The mechanism that creates a hash is known as a hash algorithm.



The above illustrates the components of a hash table. Using an array, values are stored in non-contiguous slots called buckets. The position of each value is computed by the hash function. As we'll see, most algorithms use their input to create a unique hash. In this example, the input of "Car" always produces the key result of 4.

#### THE DATA STRUCTURE

Here's a hash table data structure written in Swift. At first glance, we see the structure resembles a linked list. In a production environment, our HashNode could represent any combination of items, including custom objects. Additionally, there is no class property for storing a key.

```
//simple hash table structure

class HashNode {
    var firstname: String!
    var lastname: String!
    var next: HashNode!
}
```

#### THE BUCKETS

Before using our table, we must first define a bucket structure. If you recall, buckets are used to group node items. Since items will be stored in a non-contiguous fashion, we must first define our collection size. In Swift, this can be achieved with the following:

```
class HashTable {
    private var buckets: Array<HashNode!>

    //initialize the buckets with nil values
    init(capacity: Int) {
        self.buckets = Array<HashNode!>(count: capacity, repeatedValue:nil)
    }
}
```

#### **ADDING WORDS**

With the components in place, we can code a process for adding words. The addWord method starts by concatenating its parameters as a single String. The result is then passed to the createHash hash algorithm which, subsequently, returns an Int. Once complete, we conduct a simple check for an existing entry.

```
//add the key using the specified hash

func addWord(firstname: String, lastname: String) {
    var hashindex: Int!
    var fullname: String!

    //create a hashvalue using the complete name
    fullname = firstname + lastname
    hashindex = self.createHash(fullname)

var childToUse: HashNode = HashNode()
    var head: HashNode!
```

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```
childToUse.firstname = firstname
childToUse.lastname = lastname

//check for an existing list
if (buckets[hashindex] == nil) {
    buckets[hashindex] = childToUse
}
```

#### HASHING AND CHAINING

The key to effective hash tables is their hash functions. The createHash method is a straightforward algorithm that employs modular math. The goal? Compute an array index.

```
//compute hash index
func createHash(fullname: String) -> Int! {
    var remainder: Int = 0
    var divisor: Int = 0

    for key in fullname.unicodeScalars {
        divisor += Int(key.value)
    }

    //calculate the remainder
    remainder = divisor % buckets.count

    return remainder - 1
}
```

With any hash algorithm, the aim is to create enough complexity to eliminate *collisions*. Such a model will provide O(1) performance for insertion, modification and lookup. Collisions occur when different inputs compute to the same hash. In our example, the inputs of *Albert Einstein* and *Andrew Collins* produce the same hash result of 8.

The creation of hash algorithms is considered more art than science. As a result, there are many techniques to help reduce the potential of collisions. Beyond using modular math to compute a hash, we've applied a technique called *separate chaining*. By applying a process similar to building a linked list, this will allow multiple inputs to share the same hash.

```
//add the key using the specified hash
func addWord(firstname: String, lastname: String) {
   var hashindex: Int!
   var fullname: String!
```

Separate chaining can also be implemented with binary search trees. This can improve hash table performance to O( log n).

```
//create a hashvalue using the complete name
    fullname = firstname + lastname
    hashindex = self.createHash(fullname)
    var childToUse: HashNode = HashNode()
    var head: HashNode!
    childToUse.firstname = firstname
    childToUse.lastname = lastname
    //check for an existing list
    if buckets[hashindex] == nil {
        buckets[hashindex] = childToUse
    }
    else {
        println("a collision occured. implementing chaining..")
        head = buckets[hashindex]
        //append new item to the head of the list
        childToUse.next = head
        head = childToUse
        //update the chained list
        buckets[hashindex] = head
    }
}
```

- » Hash Table http://en.wikipedia.org/wiki/Hash\_table
- » Hash Algorithm http://en.wikipedia.org/wiki/Hash\_function
- » Modular Math https://www.khanacademy.org
- » MD5 Algorithm http://en.wikipedia.org/wiki/MD5

### **CLOSURES**

Throughout this series we've used Swift to build various models. As noted, one can build complex structures using common object-oriented (OO) techniques. As such, Swift is also known as a *functional* programming language. This idea extends the traditional OO paradigm with the notion that functions can act as *types*.

The idea that functions can act as types has numerous benefits. As with most functions, the idea of using a String, Int or Bool to pass data is common. Swift extends this idea - allowing functions to be used with variables, parameters and return types. In this chapter, we'll review how closures work and will discuss how to use them with algorithms.

#### THE CONCEPT

To introduce closures, let's review the native Array type. As we've seen, Swift arrays have the functionality one would expect. One can add, modify and remove objects. Furthermore, Arrays have three additional methods known as map, filter and reduce. Known as higher-order functions, these methods accept functions as a parameters.

```
//array of numbers
let allNumbers: Array<Int> = [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]

//determine if a number is even
func isEven(number: Int) -> Bool {
   return number % 2 == 0
}

//returns 2, 4, 6, 8 10
let evenNumbers: Array<Int> = allNumbers.filter(isEven)
```

#### **ANALYSIS**

In this example, filter accepts a function that returns values divisible by 2. When reviewing is-Even, there's nothing to distinguish it from any other function - thus making it reusable for other objects. Finally, when is Even is used as a parameter, its signature is removed.

#### THE SIGNIFICANCE

This sequence could be have been written as a single function. However, the significance is that is Even and its implementation are decoupled. This allows filter to use any function that accepts an Int and returns a Bool. Beyond Swift, the idea of anonymous functions can be seen in other languages like Python, Ruby and Java. As someone interested in Swift, you may have seen similar statements written as *closure expressions*. Now that we understand the significance of anonymous functions, let's see how they can be used with custom data structures.

#### **MAPPING LISTS**

Previously, we introduced linked lists and built a number of algorithms to manage LLNodes. Similar to an Array, a linked list can also be considered a collection type. As such, the idea of supporting higher-order functions is possible. To illustrate, let's extend our linked list class with a map function.

```
//map list content - higher order function
func map(formula: LLNode<T> -> T) -> LinkedList<T>! {
    ...
}
```

When working with closures, it can sometimes be challenging to understand their syntax. In our case, map takes a single parameter (formula) which is a function. With its syntax refined, formula accepts a generic LLNode<T> and returns a generic type T. Finally, the map function returns an optional.

```
//map list content - higher order function

func map(formula: LLNode<T> -> T) -> LinkedList<T>! {

    if head.key == nil {
        return nil
    }

    var current: LLNode! = head
    var results: LinkedList<T>! = LinkedList<T>()
    var newKey: T!

    while current != nil {

        //map based on formula
        newKey = formula(current)

        //add non-nil entries
        if newKey != nil {
              results.addLink(newKey)
        }
}
```

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```
current = current.next
}
return results
} //end function
```

In this example, LinkedList.map mimics the functionality seen with Array.map. As the function iterates through generic LLNodes, each one is passed to formula to be processed. Note the absence of the formula function body. This portion is determined at runtime with a closure expression:

```
//map nodes based on closure expression

func testLinkMapExpression() {

    //helper function - builds a linked list
    var linkedList: LinkedList<Int> = self.buildLinkedList()

    let results = linkedList.map { (node: LLNode<Int>) -> Int in
        return node.key * 2
    }
}
```

As previously shown, it is not required that functions be executed as closure expressions. However, their concise format makes it the preferred choice.

#### TRAVERSALS REVISITED

In addition to linked lists, we also introduced the concept of traversing data structures. Using depth-first (DFS) and breadth-first search (BFS), our goal was to discover new nodes while printing their key. However, we can enhance these algorithms with closures. To illustrate, let's refactor our BFS algorithm.

```
//bfs traversal with inout trailing closure
func traverse(startingv: Vertex, formula: (inout node: Vertex) -> ()) {
   ...
}
```

Since our function is designed to work with graphs, traverse accepts a starting vertex and formula. Upon analyzing the formula, we see it accepts a vertex as an inout parameter and returns nil.

When declaring function signatures, nil values can be expressed as a keyword or with "()".

```
//bfs traversal with closure function
func traverse(startingv: Vertex, formula: (inout node: Vertex) -> ()) {
    //establish a new queue
    var graphQueue: Queue<Vertex> = Queue<Vertex>()
    //queue a starting vertex
    graphQueue.enQueue(startingv)
    while !graphQueue.isEmpty() {
        //traverse the next queued vertex
        var vitem: Vertex = graphQueue.deQueue() as Vertex!
        //add unvisited vertices to the queue
        for e in vitem.neighbors {
            if e.neighbor.visited == false {
                println("adding vertex: \((e.neighbor.key!)) to queue..")
                graphQueue.enQueue(e.neighbor)
            }
        }
        //pass by reference - no return value required
        formula(node: &vitem)
    } //end while
    println("graph traversal complete..")
}
```

Similar to the map function, traverse invokes its own formula as it iterates through discovered vertices. However, since the formula parameter is passed by reference, there's no need to declare a return value. This allows the closure to fully encapsulate any changes.

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```
//bfs traversal with closure expression
func testBFSTraverseExpression() {
    var testGraph: SwiftGraph = SwiftGraph()
    ....
    testGraph.traverse(vertexA) { (inout node: Vertex) -> () in
        node.visited = true
        println("traversed vertex: \((node.key!).."))
    }
}
```

See the complete suite of algorithm unit tests on Github.

While our trailing closure updates a single boolean property, a more complex implementation could perform any number of operations, including manipulating objects outside its local scope.

- » Anonymous Functions https://en.wikipedia.org/wiki/Anonymous\_function
- » Closures https://developer.apple.com/library

## THE PROJECT

Started in 2014, this project was originally based on a series of code snippets written in Objective-C. The goal was to practice common programming techniques for technical interviews. At the time, I had considered expanding the project to other languages such as Java and Python. However, when Swift was introduced, it provided the perfect blend of concise syntax and modern language features.

The code and selected essays are open-source. As a result, they are available online for others to review, critique and build upon. The openness of the Internet has allowed me to solicit feedback, reconsider ideas and, ultimately, create a product I hope will help and inspire others. As the Swift language evolves, it will be exciting to see what new platforms and projects it will impact.

Have an idea for this project? Submit feedback at waynewbishop.com/feedback.

# **ACKNOWLEDGMENTS**

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