TALLINNA TEHNIKAÜLIKOOL

INFOTEHNOLOOGIA TEADUSKOND IT SÜSTEEMIDE ARENDUS

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LOOGIKAFUNKTSIOONIDE SÜSTEEM

Kodutöö 1

Autorideklaratsioon

Kinnitan, et olen koostanud antud kodutöö iseseisvalt ning seda ei ole kellegi teise poolt varem kaitsmisele esitatud. Kõik töö koostamisel kasutatud teiste autorite tööd, olulised seisukohad, kirjandusallikatest ja mujalt pärinevad andmed on töös viidatud.

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1. Lähteülesande genereerimine

Loogikaülesanne luuakse matrikli 176119IDDR järgi.

fn	ühed	määramatused
1:	20CE0223	AEF560B
2:	19345B97	866C932
3:	99B1AD47	333B39C2
4:	171022C3	7B00B96

Table 1. Ühtede ja määramatuste piirkonnad funktsioonides

Tabeli 1 abil saadakse järgmine funktsioonide süsteem:

$$f1(x_1, x_2, x_3, x_4) = \sum (0, 2, 3, 12, 14)_1(5, 6, 10, 11, 15)_{_}$$

$$f2(x_1, x_2, x_3, x_4) = \sum (1, 3, 4, 5, 7, 9, 11)_1(2, 6, 8, 12)_{_}$$

$$f3(x_1, x_2, x_3, x_4) = \sum (1, 4, 7, 9, 10, 11, 13)_1(2, 3, 12)_{_}$$

$$f4(x_1, x_2, x_3, x_4) = \sum (0, 1, 2, 3, 7, 12)_1(6, 9, 11)_{_}$$

Samaväärne tõeväärtustabel on kuvatud tabelis 2

	x_1	x_2	x_3	x_4	f1	f2	f3	f4
0	0	0	0	0	1	0	0	0
1	0	0	0	1	0	1	1	1
2	0	0	1	0	1	-	-	1
3	0	0	1	1	1	1	-	1
4	0	1	0	0	0	1	1	0
5	0	1	0	1	-	1	0	0
6	0	1	1	0	-	-	0	-
7	0	1	1	1	0	1	1	1
8	1	0	0	0	0	-	0	0
9	1	0	0	1	0	1	1	-
Α	1	0	1	0	-	0	1	0
В	1	0	1	1	-	1	1	-
С	1	1	0	0	1	-	-	1
D	1	1	0	1	0	0	1	0
Е	1	1	1	0	1	0	0	0
F	1	1	1	1	-	0	0	0

Table 2. Funktsioonide süsteem tõeväärtustabeli kujul

2. Minimeerimine

Minimeerimine on tehtud programmi espresso¹ abil. Sisendiks on tabelis 2 toodud tõeväärtus tabel. Argumendi –Dopoall kasutamisel olen välja valinud kaks huvitavamat lahendust erinevate faasidega.

Kodutöö ülesande kirjelduses on öeldud, et tuleks optimeerida pindala ning kiirust. Lisaks on piiratud, et loogika elementidel saab olla kuni 3 sisendit. Ehk siis espresso –Dopoall väljundis on tähtis jälgida implikantide arvu (c) ning sisendite ja väljundite koguarvu (tot).

Listing 2.1. -Dopoall faas 0000

Faasi 0000 implikantide arv on c=9, teiste faaside korral on see arv suurem.

Kogu espresso -Dopoall leiab lisade all olevast listingust nr1.

Listing 2.2. -o equtott faas 0000

```
y1 = (!x3&x4) | (!x1&x2) | (x1&!x2&!x4);

y2 = (!x2&!x3&!x4) | (x1&x2&x4) | (x1&!x2&!x4) | (x1&x2&x3);

y3 = (x2&x3&!x4) | (!x1&x2&!x3&x4) | (!x2&!x3&!x4) | (x1&x2&x3);

y4 = (!x1&x2&!x3&x4) | (!x1&!x3&!x4) | (x1&x2&x4) | (x1&!x2&!x4) |

(x1&x2&x3);
```

Kui vaadata –eqntott argumendi väljundit faaasi 0000 korral siis on näha, et meil tekib väga palju üle 3 sisendiga loogika elemente. Faasi 0000 valimine edasiseks optimeerimiseks ei oleks mõtekas.

https://github.com/classabbyamp/espresso-logic

Listing 2.3. -Dopoall faas 0101

Faasi 0101 korral on näha, et implikante on ühe võrra rohkem kuid kogu sisendite ja väljundite arv tot=39 mis on võrreldes teiste faasidega kõige väiksem.

Listing 2.4. -o eqntott faas 0101

Vaadates -eqntott argumendiga saadud tulemust näeme, et üle 3 sisendiga loogika elemente on siin ka üsna vähe.

Edasiseks optimeerimiseks võtame aluseks faasi 0101.

3. Minimeerimine

3.1 Esialgne funktsioonide süsteemi skeem

Kirjutatakse välja esialgne skeem ilma elementide sisendite piiranguta ning see järel natuke lahti kirjutades vastavalt ülesande 3 sisendiga loogikaelementide piirangule.

$t_1 = x_1 \overline{x_2}$	
$t_2 = \overline{x_3} x_4$	
$t_3 = \overline{x_1} x_2$	$[=t_5]$
$t_4 = \overline{x_2} x_4$	
$t_5 = \overline{x_1} x_2$	$[=t_{3}]$
$t_{61} = \overline{x_1} \overline{x_3}$	
$t_6 = t_{61} x_2 x_4$	
$t_7 = \overline{x_1} x_3 \overline{x_4}$	
$t_8 = x_1 x_2 x_3$	$[=t_{101}x_3]$
$t_9 = \overline{x_2} \overline{x_3} \overline{x_4}$	
$t_{101} = x_1 x_2$	
$t_{10} = \underline{t_{101}} \overline{x_3} \overline{x_4}$	
$t_{11} = \overline{x_1} x_3$	
$t_{12} = \overline{x_2} x_4$	
$y_1 = \overline{t_1 t_2 t_3}$	
$y_2 = t_4 t_5$	
$y_{31} = t_6 t_7$	
$y_3 = \overline{y_{31} t_8 t_9}$	
$y_4 = t_{10} t_{11} t_{12}$	
	$t_{2} = \overline{x_{3}} x_{4}$ $t_{3} = \overline{x_{1}} x_{2}$ $t_{4} = \overline{x_{2}} x_{4}$ $t_{5} = \overline{x_{1}} x_{2}$ $t_{61} = \overline{x_{1}} \overline{x_{3}}$ $t_{6} = t_{61} x_{2} x_{4}$ $t_{7} = \overline{x_{1}} x_{3} \overline{x_{4}}$ $t_{8} = x_{1} x_{2} x_{3}$ $t_{9} = \overline{x_{2}} \overline{x_{3}} \overline{x_{4}}$ $t_{101} = x_{1} x_{2}$ $t_{10} = t_{101} \overline{x_{3}} \overline{x_{4}}$ $t_{11} = \overline{x_{1}} x_{3}$ $t_{12} = \overline{x_{2}} x_{4}$ $y_{1} = \overline{t_{1}} t_{2} t_{3}$ $y_{2} = t_{4} t_{5}$ $y_{31} = t_{6} t_{7}$ $y_{3} = \overline{y_{31}} t_{8} t_{9}$

3.2 Pindala ja viite analüüs

Järgmisena analüüsitakse loogikafunktsioonide süsteemi pindala ja viidet. Viite parameetrid on võetud koduse ülesande lehelt ning on toodud tabelis 3.

Element	Suurus	Viide
2-NAND	1.0	1.0
bnot	1.5	1.5
2-NOR	1.5	1.5
3-NAND	1.5	1.5
2-OR	2.0	2.0
2-AND	2.0	2.0
2-XOR	2.0	2.0
3-NOR	2.0	2.0
3-OR	2.5	2.5
3-AND	2.5	2.5
3-XOR	2.5	2.5

Table 3. Loogika elementide suurused ja viited

Implikantide järel on välja toodud realiseeritava loogika elemendi pindala/viide ning kogu viide.

$x_{1i} = \overline{x_1}$	[1.5/1.5]	1.5
$x_{2i} = \overline{x_2}$	[1.5/1.5]	1.5
$x_{3i} = \overline{x_3}$	[1.5/1.5]	1.5
$x_{4i} = \overline{x_4}$	[1.5/1.5]	1.5
$c_1 = x_{1i}x_2$	[2.0/2.0]	1.5 + 2.0 = 3.5
$c_2 = x_1 x_2$	[2.0/2.0]	2.0
$t_1 = x_1 x_{2i}$	[2.0/2.0]	1.5 + 2.0 = 3.5
$t_2 = x_{3i}x_4$	[2.0/2.0]	1.5 + 2.0 = 3.5
$t_4 = x_{2i}x_4$	[2.0/2.0]	1.5 + 2.0 = 3.5
$t_{61} = x_{1i}x_{3i}$	[2.0/2.0]	1.5 + 2.0 = 3.5
$t_6 = t_{61} x_2 x_4$	[2.5/2.5]	3.5 + 2.5 = 6.0
$t_7 = x_{1i}x_3x_{4i}$	[2.5/2.5]	1.5 + 2.5 = 3.5
$t_8 = c_2 x_3$	[2.0/2.0]	2.0 + 2.0 = 4.0
$t_9 = x_{2i} x_{3i} x_{4i}$	[2.5/2.5]	1.5 + 2.5 = 3.5
$t_{10} = c_2 x_{3i} x_{4i}$	[2.5/2.5]	2.0 + 2.5 = 4.5
$t_{11} = x_{1i}x_3$	[2.0/2.0]	1.5 + 2.0 = 3.5
$t_{12} = x_{2i}x_4$	[2.0/2.0]	1.5 + 2.0 = 3.5
$y_{1i} = t_1 t_2 c_1$	[2.5/2.5]	3.5 + 2.5 = 6.0
$y_1 = \overline{y_{1i}}$	[1.5/1.5]	6.0 + 1.5 = 7.5
$y_2 = t_4 c_1$	[2.0/2.0]	3.5 + 2.0 = 5.5
$y_{31} = t_6 t_7$	[2.0/2.0]	6.0 + 2.0 = 8.0
$y_{3i} = y_{31} t_8 t_9$	[2.5/2.5]	8.0 + 2.5 = 10.5
$y_3 = \overline{y_{3i}}$	[1.5/1.5]	10.5 + 1.5 = 12.0
$y_4 = t_{10} t_{11} t_{12}$	[2.5/2.5]	4.5 + 2.5 = 7.0

Elemendid: 6 x NOT, 9 x 2-AND, 4 x 3-AND, 2 x 2-OR, 3 x 3-OR.

Kokku: 24 elementi, suurus 46, kriitiline tee 12.

3.3 Ühiste alamavaldiste otsimine

$$y_{1} = (x_{1} \overline{x_{2}})|(\overline{x_{3}} x_{4})|(\overline{x_{1}} x_{2})$$

$$/(\overline{x_{3}} x_{4}) \rightarrow (x_{1} \overline{x_{2}})|(\overline{x_{1}} x_{2}) = x_{1} \oplus x_{2}$$

$$y_{2} = (\overline{x_{2}} x_{4})|(\overline{x_{1}} x_{2})$$

$$y_{3} = (\overline{x_{1}} x_{2} \overline{x_{3}} x_{4})|(\overline{x_{1}} x_{3} \overline{x_{4}})|(x_{1} x_{2} x_{3})|(\overline{x_{2}} \overline{x_{3}} \overline{x_{4}})$$

$$/\overline{x_{1}} \rightarrow (x_{2} \overline{x_{3}} x_{4})|(x_{3} \overline{x_{4}})$$

$$/x_{2} \rightarrow (\overline{x_{1}} \overline{x_{3}} x_{4})|(x_{1} x_{3})$$

$$/\overline{x_{2}} \rightarrow (\overline{x_{3}} \overline{x_{4}}) \qquad (\overline{x_{3}} \overline{x_{4}}) = c_{1}$$

$$/x_{3} \rightarrow (\overline{x_{1}} x_{2} x_{4})|(\overline{x_{2}} \overline{x_{4}})$$

$$/\overline{x_{4}} \rightarrow (\overline{x_{1}} x_{3})|(\overline{x_{2}} \overline{x_{3}})$$

$$y_{4} = (x_{1} x_{2} \overline{x_{3}} \overline{x_{4}})|(\overline{x_{1}} x_{3})|(\overline{x_{2}} x_{4})$$

$$/(x_{1} x_{2}) \rightarrow (\overline{x_{3}} \overline{x_{4}}) = c_{1}$$

$$/(x_{3} \overline{x_{4}}) \rightarrow (x_{1} x_{2}) = c_{2}$$

Suur enamus optimeeringuid on leitud intuitiivselt ning pole siin eraldi välja toodud.

3.4 Optimeeritud pindala ja viite analüüs

Elemendid: 5 x NOT, 4 x 2-AND, 2 x 3-AND, 1 x 3-OR, 10 x 2-NAND,

Kokku: 22 (-2) elementi, suurus 33 (-13), kriitiline tee 8 (-4).

Optimeeritud loogikasüsteemil on väiksem pindala, väiksem voolu tarve ning on kiirem.

4. Modeleerimine

Modeleerimiseks on kasutatud ghdl ning gtkwave rakendusi. VHDL koodi aluseks on kodutöö näidis projekti kood.

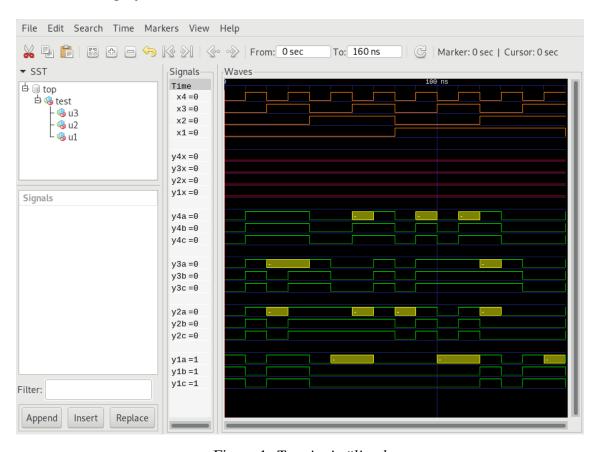


Figure 1. Testpingi väljund

Joonisel 1, x_1, x_2, x_3, x_4 on testpingi sisendid, y_1x, y_2x, y_3x, y_4x on testpingi väljundid ja signaalid $y_{1,2,3,4} \{a,b,c\}$ on tabeli, espresso ja optimeeritud loogikaskeemi väljundid.

Joonis 2 kuvatud signaalid vastavad lisas toodud opt10.vhdl koodile mille listing nr5 leiab lisadest. Joonis 2 kuvatud signaalid vastavad lisas toodud opt10.vhdl koodile mille listing nr5 leiab lisadest.

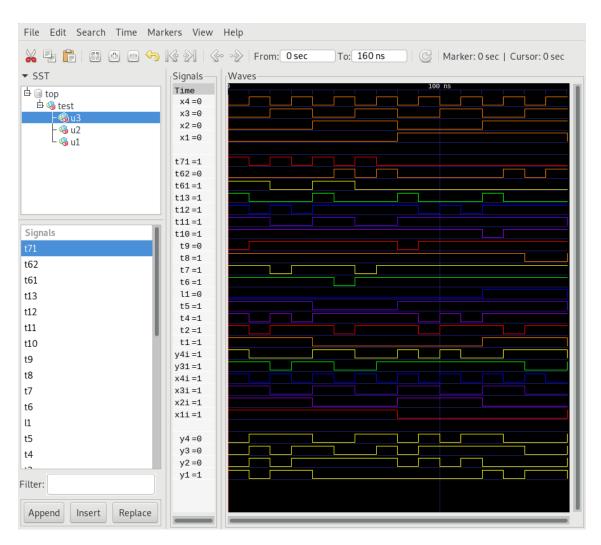


Figure 2. Optimeeritud loogikaskeemi sisemised väärtused

Lisad

Lisa 1 - espresso -Dopoall

Listing 1. Programmi espresso -Dopoall väljund

```
.i 4
.0 4
0000 1000
0001 0111
0010 1--1
0011 11-1
0100 0110
0101 -100
0110 --0-
0111 0111
1000 0-00
1001 011-
1010 -010
1011 -11-
1100 1--1
1101 0010
1110 1000
1111 -000
# phase is ---- 0000
               Time was 0.00 sec, cost is c=9(0) in=26 out=16 tot=42
# ESPRESSO
# phase is ---- 0001
# ESPRESSO
                 Time was 0.00 sec, cost is c=10(0) in=30 out=15 tot=45
# phase is ---- 0010
# ESPRESSO
                 Time was 0.00 \text{ sec}, cost is c=10(0) \text{ in}=30 \text{ out}=18 \text{ tot}=48
# phase is ---- 0011
# ESPRESSO
                Time was 0.00 sec, cost is c=10(0) in=28 out=15 tot=43
# phase is ---- 0100
# ESPRESSO
                 Time was 0.00 \text{ sec}, cost is c=10(0) \text{ in}=26 \text{ out}=15 \text{ tot}=41
# phase is ---- 0101
                 Time was 0.00 sec, cost is c=10(0) in=27 out=12 tot=39
# ESPRESSO
# phase is ---- 0110
```

```
# ESPRESSO
               Time was 0.00 sec, cost is c=10(0) in=27 out=17 tot=44
# phase is ---- 0111
# ESPRESSO
                 Time was 0.00 sec, cost is c=10(0) in=26 out=14 tot=40
# phase is ---- 1000
                 Time was 0.00 \text{ sec}, cost is c=10(0) \text{ in}=30 \text{ out}=15 \text{ tot}=45
# ESPRESSO
# phase is ---- 1001
                  Time was 0.00 sec, cost is c=11(0) in=30 out=14 tot=44
# ESPRESSO
# phase is ---- 1010
# ESPRESSO
                  Time was 0.00 \text{ sec}, cost is c=11(0) \text{ in}=31 \text{ out}=16 \text{ tot}=47
# phase is ---- 1011
# ESPRESSO
                 Time was 0.00 \text{ sec}, cost is c=10(0) \text{ in}=26 \text{ out}=15 \text{ tot}=41
# phase is ---- 1100
                  Time was 0.00 \text{ sec}, cost is c=12(0) \text{ in}=32 \text{ out}=14 \text{ tot}=46
# ESPRESSO
# phase is ---- 1101
# ESPRESSO
                  Time was 0.00 sec, cost is c=10(0) in=28 out=13 tot=41
# phase is ---- 1110
# ESPRESSO
                 Time was 0.00 sec, cost is c=10(0) in=27 out=15 tot=42
# phase is ---- 1111
# ESPRESSO
                 Time was 0.00 \text{ sec}, cost is c=10(0) \text{ in}=26 \text{ out}=15 \text{ tot}=41
```

Lisa 1 - VHDL kood

Listing 2. f_system.vhd

Listing 3. fs1_table.vhd

```
--- IAY0150 - Homework #1. Truth table
--- (C) Arti Zirk - 2019 - Tallinn
--- library IEEE; use IEEE.std_logic_1164.all; architecture tabel of f_system is
```

```
begin
  process (x1, x2, x3, x4)
    variable in_word, out_word: std_logic_vector (3 downto 0);
  begin
    in_word := x1 & x2 & x3 & x4;
    case in_word is
      when "0000" => out_word := "1000";
      when "0001" => out_word := "0111";
      when "0010" \Rightarrow out_word := "1--1";
      when "0011" => out_word := "11-1";
      when "0100" \Rightarrow out_word \Rightarrow "0110";
      when "0101" \Rightarrow out_word := "-100";
      when "0110" => out_word := "--0-";
      when "0111" => out_word := "0111";
      when "1000" => out_word := "0-00";
      when "1001" \Rightarrow out_word \Rightarrow "011-";
      when "1010" => out word := "-010";
      when "1011" => out_word := "-11-";
      when "1100" \Rightarrow out_word \Rightarrow "1--1";
      when "1101" => out_word := "0010";
      when "1110" => out_word := "1000";
      when "1111" => out_word := "-000";
      when others => out_word := "----";
    end case;
    y1 <= out_word(3);</pre>
                          y2 \le out_word(2);
                           y4 \le out\_word(0);
    y3 <= out_word(1);
  end process;
end architecture tabel;
```

Listing 4. fs1_espr.vhd

Listing 5. fs1_opt1o.vhd

```
-- IAY0150 - Homework #1.
_____
-- (C) Arti Zirk - 2019 - Tallinn
_____
library IEEE; use IEEE.std_logic_1164.all;
architecture optil of f_system is
  signal x1i, x2i, x3i, x4i, y31, y4i, t1: std_logic;
  signal t6, t7, t8, t9, t10, t11, t12: std_logic;
  signal t2, t3, t4, t5, l1, t13, t61, t62, t71: std_logic;
begin
  x1i <= not x1;
  x2i \le not x2;
  x3i \le not x3;
  x4i \le not x4;
  11 \le x1 \text{ and } x2;
  t1 \le not (x1 xor x2);
  t2 <= x3i nand x4;
  y1 \le t1 and t2;
  t4 \le x2i \text{ nand } x4;
  t5 \le x1i \text{ nand } x2;
  y2 <= t4 nand t5;
  t61 <= x1 nor x3;
  t62 \le x2 \text{ and } x4;
  t6 <= t61 nand t62;
  t71 \le x1 \text{ nor } x4;
  t7 \le t71 \text{ nand } x3;
  t8 <= 11 nand x3;
  t9 <= x2 or x3 or x4;
```

```
y31 <= t6 and t7 and t8;
y3 <= y31 and t9;

t13 <= x3 nor x4;
t10 <= 11 nand t13;
t11 <= x1i nand x3;
t12 <= x2i nand x4;
y4i <= t10 and t11 and t12;
y4 <= not y4i;
end architecture opti1;</pre>
```

Listing 6. fs1_test.vhd

```
_____
-- IAY0150 - Homework #1. Test bench for the example task.
______
-- (C) Peeter Ellervee - 2016 - Tallinn
library IEEE; use IEEE.std_logic_1164.all;
entity test is
end entity test;
library IEEE; use IEEE.std_logic_1164.all;
architecture bench of test is
 signal x1, x2, x3, x4: std_logic;
 signal yla, ylb, ylc, y2a, y2b, y2c: std_logic;
 signal y3a, y3b, y3c, y4a, y4b, y4c: std_logic;
 signal y1x, y2x, y3x, y4x: std_logic;
 component f_system
   port ( x1, x2, x3, x4: in std_logic;
         y1, y2, y3, y4: out std_logic );
 end component;
 for U1: f_system use entity work.f_system(tabel);
 for U2: f_system use entity work.f_system(espresso);
 for U3: f_system use entity work.f_system(optil);
 function compare_signals (s1, s2, s3: std_logic) return std_logic is
 begin
   if s1='-' then
     if s2/=s3 then return 'X'; end if;
   else
     if s1/=s2 or s1/=s3 then return 'X'; end if;
   end if;
   return '0';
 end function compare_signals;
```

```
begin
  -- Input signals (after every 10 ns)
  x1 <= '0' after 0 ns, '1' after 80 ns, '0' after 160 ns;
  x2 \le '0' after 0 ns, '1' after 40 ns, '0' after 80 ns, '1' after 120 ns;
  x3 <= '0' after 0 ns, '1' after 20 ns, '0' after 40 ns, '1' after 60 ns,
        '0' after 80 ns, '1' after 100 ns, '0' after 120 ns, '1' after 140 ns;
  x4 \leftarrow 0 after 0 ns, '1' after 10 ns, '0' after 20 ns, '1' after 30 ns,
        '0' after 40 ns, '1' after 50 ns, '0' after 60 ns, '1' after 70 ns,
        '0' after 80 ns, '1' after 90 ns, '0' after 100 ns, '1' after 110 ns,
        '0' after 120 ns, '1' after 130 ns, '0' after 140 ns, '1' after 150 ns;
  -- System of Boolean functions
  U1: f_system port map (x1, x2, x3, x4, y1a, y2a, y3a, y4a);
  U2: f_system port map (x1, x2, x3, x4, y1b, y2b, y3b, y4b);
  U3: f_system port map (x1, x2, x3, x4, y1c, y2c, y3c, y4c);
  --y1c<=y1b; y2c<=y2b; y3c<=y3b; y4c<=y4b;
  y1x <= compare_signals (y1a, y1b, y1c);</pre>
  y2x <= compare_signals (y2a, y2b, y2c);
  y3x <= compare_signals (y3a, y3b, y3c);
  y4x <= compare_signals (y4a, y4b, y4c);
end architecture bench;
```

Listing 7. make.sh

```
#!/bin/bash
set -x -e

# uses ghdl-mcode variant
# import vhd files
ghdl -i -g *.vhd
# make unit
ghdl -m test
# run unit and export logic graph
ghdl -r test --wave=test.ghw --stop-time=200ns
# send signal to gtkwave to reload open file
gsettings set com.geda.gtkwave reload 0
```