**Solutions** 

What is an access network?
A network that allows a host to connect to the internet

- 2) **Throughput** is the rate at which bits are actually transferred between sender/receiver.
- 3) Describe the sources of nodal delay in packet-switched networks.

Processing delay: Time spent processing header information, checking bit errors, and deciding outport link

Queueing delay: Time waiting for the transmission medium

Transmission delay: Time spent being placed on the transmission medium, limited by the transmission protocol.

Propagation delay: Time spent traveling on the physical medium

- 4) What is the equation for end-to-end delay?  $d_{\text{nodal}} = d_{\text{proc}} + d_{\text{queue}} + d_{\text{trans}} + d_{\text{prop}}$
- 5) Consider two hosts (A and B) connected by a single link with transmission rate **R** bps. The hosts are separated physically by **d** meters along a cable for which the speed of propagation is **s** meters per second. Host A sends a packet of length **L** bits to host B
  - a. Show the propagation delay  $d_{prop}$  in terms of d and s:  $d_{prop} = d/s$
  - b. Show the transmission delay  $d_{trans}$  in terms of L and R:  $d_{trans} = L/R$
  - c. Suppose Host A begins to transmit at time t=0. At time  $t=d_{trans}$  where is the last bit of the packet?

Just leaving the sending host (Host A)

- d. Suppose that  $d_{prop}>d_{trans}$ . At time  $t=d_{trans}$ , where is the first bit of the packet? Somewhere in the link between Host A and Host B
- e. Suppose that  $d_{prop} < d_{trans}$ . At time  $t = d_{trans}$ , where is the first bit of the packet? At the receiving host (Host B)
- f. Let  $s = 2.5 \times 10^8$  m/s, L = 120 bits, R = 56 Kbps. Find d such that  $d_{prop} = d_{trans}$ . Set d/s = L/R 120 / 56,000 = d / 250,000,000  $\textbf{d} = 250,000,000 * 120 / 56,000 = 535,714.28 m <math>\approx 535.7$  km
- 6) Suppose that there are N packets in a router's queue. Given a constant packet length of L, and a constant transmission rate R, what is the average queuing delay for the N packets?

 $1^{st}$  packet delay =0;  $2^{nd}$  packet delay=L/R;  $3^{rd}$  packet delay = 2L/R; etc So, average delay for N packets is

$$\frac{\left[\frac{L}{R} + \frac{2L}{R} + \dots + \frac{(N-1)L}{R}\right]}{N} = \frac{N(N-1)L}{2NR} = \frac{L(N-1)}{2R} \text{ seconds}$$

## **Explanation:**

To simplify  $\left[\frac{L}{R} + \frac{2L}{R} + \dots + \frac{(N-1)L}{R}\right]/N$ , use the summation formula  $\sum_{i=1}^{p} i = \frac{p(p+1)}{2}$ , or solve algebraically as follows:

Combine the first term and last term of the numerator.

$$L/R + (N-1)L/R = NL/R$$

Then combine the second term and the next-last term.

$$2L/R + (N-2)L/R = NL/R$$
 etc. 
$$3L/R + (N-3)L/R = NL/R, \quad 4L/R + (N-4)L/R = NL/R$$

So we end up with (N-1)/2 pairs that add up to NL/R, i.e.,  $\frac{N-1}{2} * \frac{NL}{R}$ 

and 
$$\frac{\binom{N-1}{2}\binom{NL}{R}}{N} = \frac{N(N-1)L}{2NR} = \frac{L(N-1)}{2R}$$

Note: depending on whether N is even or odd, we might have one term that doesn't have another term with which to be combined, but this is handled correctly because (N-1)/2 will have a remainder of 1 when N is even.