**Self-Check Exercises: Lecture 42** 

**Solutions** 

- 1) What is message encryption? (High-level is OK)
  Altering the contents of a message so that it is difficult (or impossible) to ascertain the original message, unless you are the intended recipient, by means of cryptography.
- 2) How would encryption work with public key encryption?

  Sender encrypts with recipient's registered public key. Recipient decrypts with their own private key.
- 3) Use the RSA algorithm discussed in lecture to develop a public key and a private key for public-key encryption. Let p = 5, q = 11, e = 7, m is the original message, c is the encrypted message.

a. 
$$n = pq = 5 \times 11 = 55$$

b. 
$$z = (p-1)(q-1) = 4 \times 10 = 40$$

c. d = 23

There are several possibilities. Choose d so that ed-1 is exactly divisible by z. If we choose d = 23,  $ed-1 = 7 \times 23 - 1 = 160$ , which is divisible by 40.

- d.  $c = \text{Kpublic}(m) = \frac{m^e \mod n}{n}$
- e. Kprivate(c) =  $c^d \mod n$
- f. Kprivate(Kpublic(m)) = m
- 4) How might authentication work with public key encryption? (Textbook will be helpful here)

Sender encrypts a signature with a registered private key, and distributes public key. If this known public key correctly decrypts the signature, we know the sender to be who we think they are.