Flow on Gram-Schmidt Coordinates