

Fabric-Elasticity Relationships in Cortical Bone

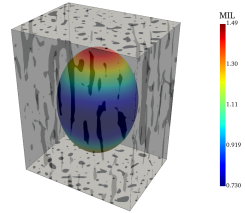
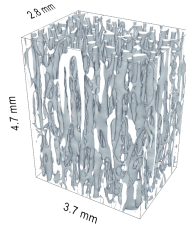
Mathieu Simon

January, 2025

Material

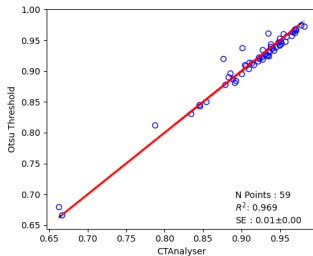
Data

- 59 scans
- 6.5 μm voxel size
- RUS measurements
- CTAnalyser

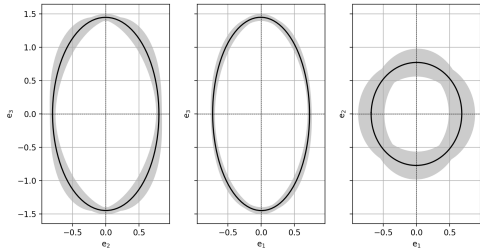


Segmentation

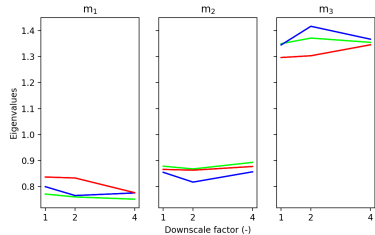
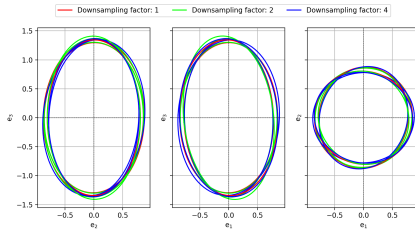
Mean Otsu threshold



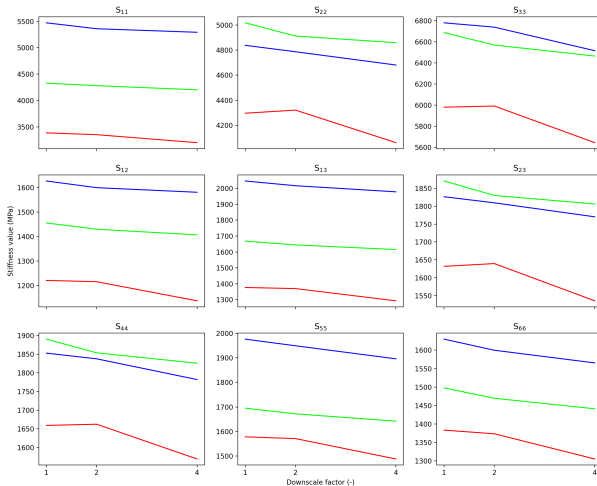
Fabric distribution



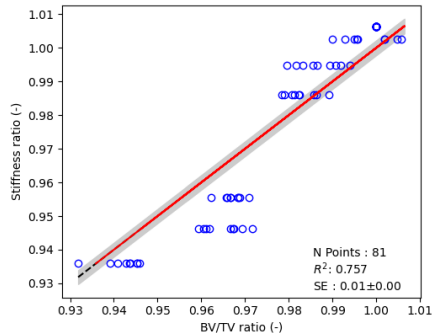
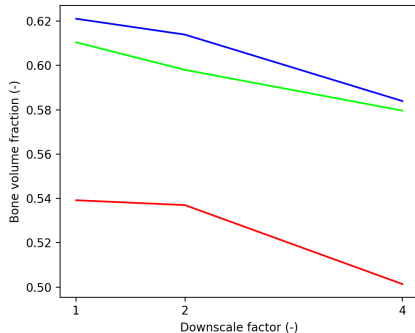
Resolution Effect - Fabric



Resolution Effect - Elasticity



Resolution Effect - Elasticity II

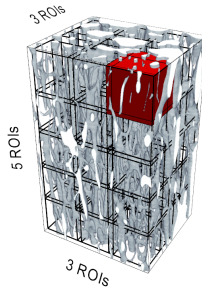


Convergence Study

Setup

- 1mm ROI side length
- 3x3x5 ROIs
- 65 μm margin
- Groups of 1, 2, ..., 45 ROIs

→ $\sim 2^{45}$ possibilities

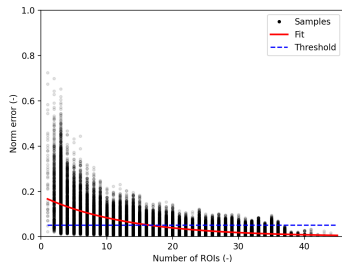


Convergence Study

Sampling

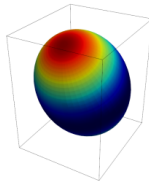
- Balanced clustering
 - Linear sum assignment
 - $216 \cdot 10^6$ possibilities
- N samples = 1000
- Norm Error
- Threshold = 0.05

→ 15-16 ROIs

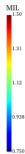


Material Effect

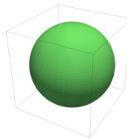
Structure



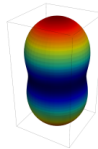
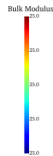
Fabric



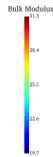
Material



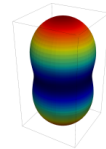
Isotropic



Transverse Isotropic



Mechanics



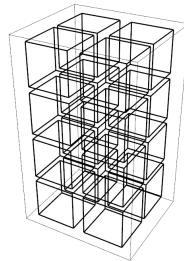
Transverse Isotropic



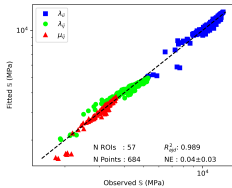
Homogenization

Setup

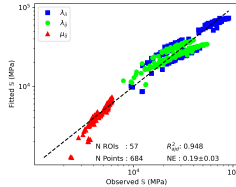
- Downsampling factor: 2
- $16 \times 1 \text{ mm}^3$ ROIs
- Isotropic vs transverse
- Mean \bar{S} / Sample



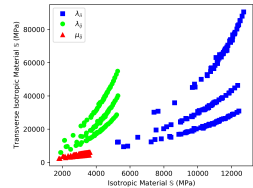
Homogenization Results



Isotropic



Transverse



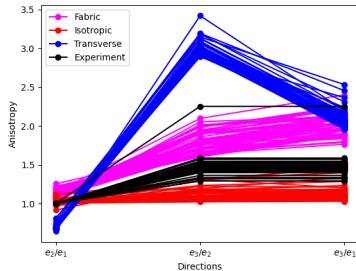
Comparison

Comparison with Trabecular Bone

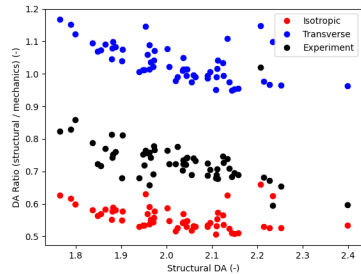
$$\mathbb{S}_{Ts} = \mathbb{S}_T / |\mathbb{S}_T| * |\mathbb{S}_I|$$

Study	Bone type	Resolution	λ_0	λ_0'	μ_0	k	l	DA
Gross et al.	Trab.	18	4609	3692	3738	1.60	0.99	1.67
Panyasantisuk et al.	Trab.	36	3841	3076	3115	1.60	0.99	1.54
Simon et al	Trab.	61	2738	1662	2187	1.60	0.99	1.99
Present study	Cort. (\mathbb{S}_I)	13	4882	4809	3645	1.60	0.99	2.02
Present study	Cort. (\mathbb{S}_{Ts})	13	6309	6278	1194	1.60	0.99	2.02

Anisotropy

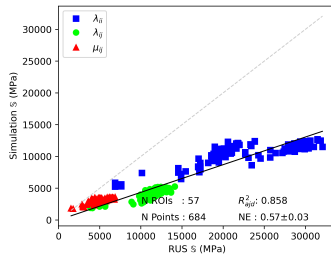


Main directions DA

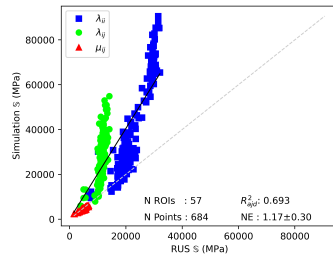


DA ratios (e_3/e_1)

Homogenization - Comparison with RUS



Isotropic Material



Transverse Isotropic Material

Comparison l Exponent

$$S_{Is} = S_I / |S_I| * |S_T|$$

Parameters	λ_0	λ_0'	μ_0	k	l
Isotropic	21480	21156	16035	1	0.075
Transverse	27757	26935	5070	1	0.66