1. 
$$softmax(x_i) = \frac{e^{x_i}}{\sum e^{x_j}}$$
  
2.  $softmax(x_i + c) = \frac{e^{x_i + c}}{\sum_j e^{x_j + c}} = \frac{e^{x_i}e^c}{\sum_j e^{x_i}e^c}$   
3.  $softmax(x_i + c) = \frac{e^{x_i}}{\sum_j e^{x_j}} = softmax(x_i)$ 

In (1) we have the general form of the softmax equation. Translating by a scalar c, allows us to expand terms (2). In (2) we also find that by using basic exponent rules the scalar term actually falls out. This allows us to assert in (3) that the softmax is invariant to translation as  $softmax(x_i + c) = softmax(x_i)$ .

Often it is a good idea to use  $c = -max(x_i)$  because this scales the terms by shifting them all by the maximum value, such that the largest value will turn to  $1 (e^{xi\_max-xi\_max} = 1)$ , and the rest will be scaled between 0-1. With this in mind, it is not hard to see that this method of shifting can prevent some numerical overflow and promote stability.

- 1. Values from softmax range from 0-1, with the resultant sum being 1.
- 2. One could say that "softmax takes an arbitrary real valued vector x and turns it into a [*probability distribution*]
- 3. Steps of Softmax
  - a. Take the exponential of each outcome to find the outcome frequency
  - b. Find the sum of all the outcome frequencies
  - c. Normalize by the sum of the outcome frequencies to find the total outcome frequency (the probability of each occurance)

Generally, in a forward pass of a fully-connected layer we would use the equation: y = wx + b

Applying this to between two fully-connected layers without an activation looks like the process derived below:

1. 
$$y_l = w_l x_l + b_l$$
  
2.  $y_l = w_l (w_{l-1} x_{l-1} + b_{l-1}) + b_l$   
3.  $y_l = w_l w_{l-1} x_{l-1} + w_l b_{l-1} + b_l$   
4.  $y_l = w' x_{l-1} + b'$   
5.  $y_l = wx + b$ 

At step (5) we can observe that we ended up with the same general form as we did when we started, showing that a multi-layer network without activiations is equivalent to doing a linear regression problem.

The derivative of the sigmoid function is given by the following formula:

$$\frac{d}{dx}\sigma(x) = \sigma(x)\cdot(1-\sigma(x))$$

where  $\sigma(x)$  is the sigmoid function. This formula can be derived by applying the chain rule to the sigmoid function, which is defined as:

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

First, we can rewrite the derivative using the definition of the sigmoid function:

$$\frac{d}{dx}\sigma(x) = \frac{d}{dx}\frac{1}{1+e^{-x}}$$

Next, we can apply the chain rule to take the derivative of the fraction. The derivative of the numerator is simply 1, and the derivative of the denominator is given by the following:

$$\frac{d}{dx}(1+e^{-x}) = \frac{d}{dx}1 + \frac{d}{dx}e^{-x} = 0 - e^{-x} = -e^{-x}$$

Therefore, the derivative of the sigmoid function is given by:

$$\frac{d}{dx}\sigma(x) = \frac{1}{1+e^{-x}} \cdot \left(0 - \frac{1}{1+e^{-x}}\right)$$

$$= \frac{1}{1+e^{-x}} \cdot \frac{-1}{1+e^{-x}} = \frac{1}{(1+e^{-x})^2}$$

$$= \sigma(x) \cdot (1 - \sigma(x))$$

The gradient of the loss function J with respect to y can be written as:

$$\frac{\partial J}{\partial y}$$

Since y is a function of W, x, and b, we can use the chain rule to compute the partial derivatives of J with respect to W, x, and b.

First, let's find the partial derivative of J with respect to W. We can write:

$$\frac{\partial J}{\partial W} = \frac{\partial J}{\partial u} \frac{\partial y}{\partial W}$$

Take the derivative of y wrt W:

$$\frac{\partial y}{\partial W} = x$$

Therefore, the partial derivative of J with respect to W is given by:

$$\frac{\partial J}{\partial W} = \frac{\partial J}{\partial y} \cdot x$$

Next, let's find the partial derivative of J with respect to x. We can write:

$$\frac{\partial J}{\partial x} = \frac{\partial J}{\partial y} \frac{\partial y}{\partial x}$$

Find the derivative of y wrt x:

$$\frac{\partial y}{\partial x} = W$$

Therefore, the partial derivative of J with respect to x is given by:

$$\frac{\partial J}{\partial x} = \frac{\partial J}{\partial y} \cdot W$$

Finally, let's find the partial derivative of J with respect to b. We can write:

$$\frac{\partial J}{\partial b} = \frac{\partial J}{\partial y} \frac{\partial y}{\partial b}$$

Take the derivative of y wrt b:

$$\frac{\partial y}{\partial b} = 1$$

Therefore, the partial derivative of J with respect to b is given by:

$$\frac{\partial J}{\partial b} = \frac{\partial J}{\partial y} \cdot 1$$

To summarize, we have found that the partial derivatives of the loss function J with respect to W, x, and b are given by:

$$\frac{\partial J}{\partial W} = \frac{\partial J}{\partial y} \cdot x$$

$$\frac{\partial J}{\partial x} = \frac{\partial J}{\partial y} \cdot W$$
$$\frac{\partial J}{\partial b} = \frac{\partial J}{\partial y}$$

In matrix form, these equations can be written as:

$$\frac{\partial J}{\partial W} = \frac{\partial J}{\partial y} \cdot X$$
$$\frac{\partial J}{\partial x} = W \cdot \frac{\partial J}{\partial y}$$
$$\frac{\partial J}{\partial b} = 1 \cdot \frac{\partial J}{\partial y}$$

Where X, W, 1 are all matrices.

1. The sigmoid can only output values between 0,1 and its derivate can only output values between 0, 0.25. If we are propagating these small values sequentially over many layers we can expect the gradients to continually decrease until they "vanish".

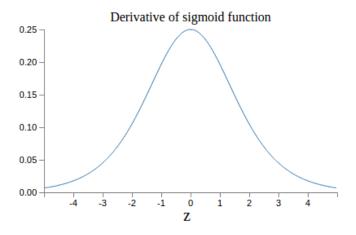


Figure 1. Plot of sigmoid derivative

- 2. The sigmoid is capable of outputting between (0,1) while tanh can output between (-1, 1). During training if you obtain a network with a lot of 0 outputs the sigmoid would also output a lot of signals that map to 0, which may cause the subsequent gradient to go to 0 and the learning for the network to stall.
- 3. As is apparent given figure 2, the derivate of tanh produces a higher maximum peak than the sigmoid derviative: leading to a greater descent and update of the weights & biases during learning.

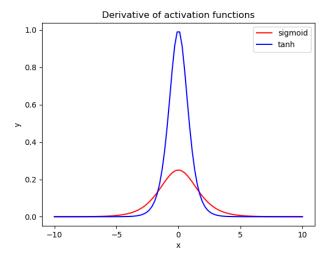


Figure 2. Plot of tanh derivative

4. The tanh and sigmoid are defined as:

$$\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$
 $\sigma(x) = \frac{1}{1 + e^{-x}}$ 

Here is the numerator of the tanh:

$$e^x - e^{-x} = \frac{1}{\sigma(-x)} - \frac{1}{\sigma(x)} = \frac{\sigma(x) - \sigma(-x)}{\sigma(x) \cdot \sigma(-x)}$$

Here is the denominator of the tanh:

$$e^x + e^{-x} = \frac{1}{\sigma(-x)} + \frac{1}{\sigma(x)} = \frac{\sigma(x) + \sigma(-x)}{\sigma(x) \cdot \sigma(-x)}$$

Therefore, the tanh function can be written in terms of the sigmoid function as:

$$\tanh(x) = \frac{\frac{\sigma(x) - \sigma(-x)}{\sigma(x) \cdot \sigma(-x)}}{\frac{\sigma(x) + \sigma(-x)}{\sigma(x) \cdot \sigma(-x)}}$$
$$= \frac{\sigma(x) - \sigma(-x)}{\sigma(x) + \sigma(-x)}$$

This shows that the tanh function can be expressed in terms of the sigmoid function.

It is not a good idea to initialize a network with all zeros for one because if all the weights are the same the neurons will end up learning the same thing, it will lead to symmetry across the network. It also may prevent the network from being able to generalize new data because if it ends up outputting the same constant value it won't have learned any new patters from the data

By imposing randomness without the system we can help to maximize the potential for a local minima to be reached, and often more quickly. The weights are instantiated based on the size of the layer due to the fact that the variance of the distribution should be unque to that layer so that any issues regarding exploding/vanishing gradients can be mitigated. This is best visualized with the graph from the 6<sup>th</sup> page of the pdf given on "Understanding the difficulty of training deep feedforward neural networks" (below)

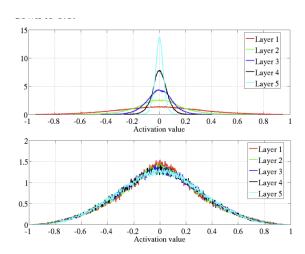


Figure 3. Standard activation values for tanh (top) and normalized initialization (bottom)

```
def sigmoid(x):
   # Simply the equation for a sigmoid activation function
   res = 1 / (1 + np.exp(-x))
   return res
def forward(X, params, name='', activation=sigmoid):
   Do a forward pass
   Keyword arguments:
   X -- input vector [Examples x D]
   params -- a dictionary containing parameters
   name -- name of the layer
   activation -- the activation function (default is sigmoid)
   pre_act, post_act = None, None
   # get the layer parameters
   W = params['W' + name]
   b = params['b' + name]
   #####################################

    Forward prop without activation: W.T * X + b

   2. Pass through the activation function
   pre_act = np.dot(X, W) + b
   post_act = activation(pre_act)
   # these will be important in backprop
   params['cache_' + name] = (X, pre_act, post_act)
   return post_act
```

```
def softmax(x):
   res = None
   ##### your code here #####
   1. For numerical stability, shift all values over so the maximum is now 0
      - expand the dims so you can broadcast, need a singleton dimension
   2. Exponentiate all the xvals
   3. Take a cumulative sum acros the rows, so you can softmax each example
   4. Get the softmax result to make a probability vector
   - Gives prob. that a particular input is of a particular class
   x_shift = x - np.expand_dims(np.amax(x, axis=1), axis=1)
   x_{exp} = np.exp(x_{shift})
   x_sum = np.sum(x_exp, axis=1, keepdims=True)
   res = x_exp / x_sum
   return res
```

```
def backwards(delta, params, name='', activation_deriv=sigmoid_deriv):
   Do a backwards pass
   Keyword arguments:
   delta -- errors to backprop
   params -- a dictionary containing parameters
   name -- name of the layer
   activation_deriv -- the derivative of the activation_func
   grad_X, grad_W, grad_b = None, None, None
   # everything you may need for this layer
   W = params['W' + name]
   b = params['b' + name]
   X, pre_act, post_act = params['cache_' + name]
   # do the derivative through activation first
   # (don't forget activation_deriv is a function of post_act)
   # then compute the derivative W, b, and X
   #############################
   ##### your code here #####
   ##############################
   grad A = delta * activation deriv(post act)
   grad_X = np.dot(grad_A, W.T)
   grad_W = np.dot(X.T, grad_A)
   grad_b = np.sum(grad_A, axis=0)
   # store the gradients
   params['grad_W' + name] = grad_W
   params['grad_b' + name] = grad_b
    return grad_X
```

```
def get_random_batches(x, y, batch_size):
   batches = []
   #####################################
   ##### vour code here #####
   # shuffled the data
   shuffled_x, shuffled_y = shuffled_data(x, y)
   # get the number of batches
   num_batches = x.shape[0] / batch_size
   # split the batches into number of batches
   xbatches = np.split(shuffled_x, num_batches)
   ybatches = np.split(shuffled y, num_batches)
   # for the splot arrays, zip them together, then append them to batches
   for xbatch, ybatch in zip(xbatches, ybatches):
       batches.append((xbatch, ybatch))
   return batches
def shuffled_data(x, y):
   shuffled_ind = np.random.permutation(x.shape[0])
   shuffled_x = x[shuffled_ind, :]
   shuffled_y = y[shuffled_ind, :]
   return shuffled_x, shuffled_y
```

```
for k, v in params.items():
    if '_' in k:
            params_copy = copy.deepcopy(params)
            for i in range(v.shape[0]):
                for j in range(v.shape[1]):
                    v[i, j] += eps
                    h1 = forward(x, params_copy, 'layer1')
                    probs = forward(h1, params_copy, 'output', softmax)
                    loss_pluseps, acc_minuseps = compute_loss_and_acc(y, probs)
                    v[i, j] -= 2*eps
                    # Subtract Epsilon
                    h1 = forward(x, params_copy, 'layer1')
                    probs = forward(h1, params_copy, 'output', softmax)
                    loss_minuseps, acc_minuseps = compute_loss_and_acc(
                        y, probs)
                    params[k][i, j] = (loss_pluseps-loss_minuseps)/(2*eps)
                    v[i, j] += eps
       elif "b" in k:
            params_copy = copy.deepcopy(params)
            for i in range(v.shape[0]):
                v[i] += eps
                h1 = forward(x, params_copy, 'layer1')
                probs = forward(h1, params_copy, 'output', softmax)
                loss_pluseps, acc_minuseps = compute_loss_and_acc(y, probs)
                v[i] -= 2*eps
                # Subtract Epsilon & do forward prop
                h1 = forward(x, params_copy, 'layer1')
                probs = forward(h1, params_copy, 'output', softmax)
                loss_minuseps, acc_minuseps = compute_loss_and_acc(y, probs)
                params[k][i] = (loss_pluseps-loss_minuseps)/(2*eps)
                v[i] += eps
```

## Q3.1: Code

```
1 ∨ import string
     import pickle
     import numpy as np
     import scipy.io
     import matplotlib.pyplot as plt
     from mpl toolkits.axes grid1 import ImageGrid
     from nn import *
     train_data = scipy.io.loadmat('../data/nist36_train.mat')
     valid data = scipy.io.loadmat('.../data/nist36 valid.mat')
11
     test_data = scipy.io.loadmat('../data/nist36_test.mat')
13
     train_x, train_y = train_data['train_data'], train_data['train_labels']
     valid_x, valid_y = valid_data['valid_data'], valid_data['valid_labels']
     test_x, test_y = test_data['test_data'], test_data['test_labels']
16
18 ∨ if False: # view the data
19
         np.random.shuffle(train_x)
20 🗸
         for crop in train x:
21
             plt.imshow(crop.reshape(32, 32).T, cmap="Greys")
             plt.show()
23
24
     max iters = 50
25
26
     batch_size = 64
27
     learning rate = 1e-3
28
     hidden size = 64
29
31
32
34
     batches = get_random_batches(train_x, train_y, batch_size)
35
     batch num = len(batches)
37
     params = {}
39
     # initialize layers
40
     initialize weights(train x.shape[1], hidden size, params, "layer1")
41
     initialize weights(hidden size, train y.shape[1], params, "output")
42
     layer1_W_initial = np.copy(params["Wlayer1"]) # copy for Q3.3
```

```
train loss = []
valid_loss = []
train_acc = []
valid_acc = []
for itr in range(max_iters):
    h1 = forward(train_x, params, 'layer1')
    probs = forward(h1, params, 'output', softmax)
    loss, first_acc = compute_loss_and_acc(train_y, probs)
    train_loss.append(loss/train_x.shape[0])
    train_acc.append(first_acc)
    h1 = forward(valid_x, params, 'layer1')
    probs = forward(h1, params, 'output', softmax)
    loss, acc = compute_loss_and_acc(valid_y, probs)
    valid_loss.append(loss/valid_x.shape[0])
    valid_acc.append(acc)
    total_loss = 0
    avg_acc = 0
    for xb, yb in batches:
        h1 = forward(xb, params, 'layer1')
        probs = forward(h1, params, 'output', softmax)
        # be sure to add loss and accuracy to epoch totals
        loss, acc = compute_loss_and_acc(yb, probs)
        total loss += loss
        avg_acc += acc
        delta1 = probs - yb
        delta2 = backwards(delta1, params, 'output', linear_deriv)
        backwards(delta2, params, 'layer1', sigmoid_deriv)
        for k, v in sorted(list(params.items())):
                name = k.split('_')[1]
                params[name] -= learning_rate * params[k]
    avg_acc /= len(batches)
    if itr % 2 == 0:
        print("itr: {:02d} \t loss: {:.2f} \t acc : {:.2f}".format(
            itr, total_loss, first_acc))
h1 = forward(valid_x, params, 'layer1')
probs = forward(h1, params, 'output', softmax)
loss, acc = compute_loss_and_acc(valid_y, probs)
valid_loss.append(loss/valid_x.shape[0])
valid_acc.append(acc)
h1 = forward(train_x, params, 'layer1')
probs = forward(h1, params, 'output', softmax)
loss, acc = compute_loss_and_acc(train_y, probs)
train loss.append(loss/train x.shape[0])
train_acc.append(acc)
```

# Q3.1: Results

• Hyperparameters:

Learning Rate: 2e-3Batch Size: 64

o Epochs: 50

• Results:

Training Accuracy: 83%
Validation Accuracy: 75.1%
Testing Accuracy: 75.6%

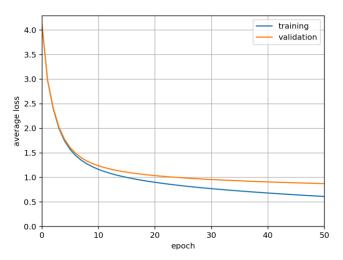


Figure 4. Loss for training and validation sets

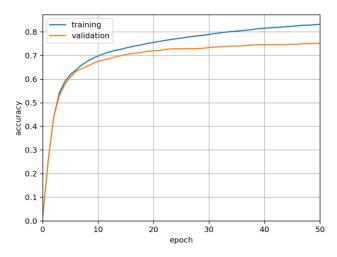


Figure 5. Accuracy for training and validation sets

## Learning Rate 10x Smaller:

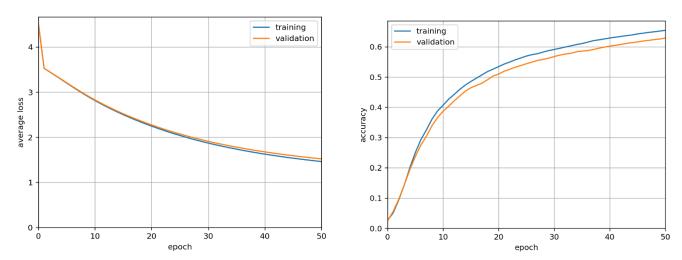


Figure 6. Loss & Accuracy for learning rate = 2e-4

• Hyperparameters:

o Learning Rate: 2e-4

Batch Size: 64Epochs: 50

• Results:

o Training Accuracy: 65%

o Validation Accuracy: 62.9%

o Testing Accuracy: 63.9%

### Learning Rate 10x Larger:

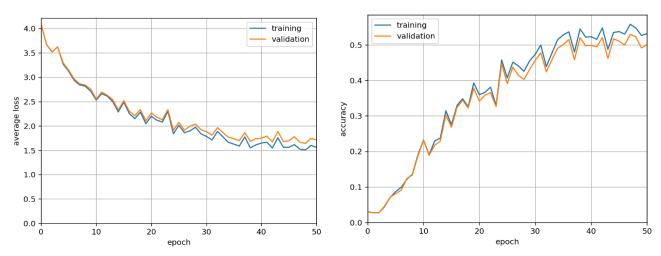


Figure 7. Loss & Accuracy for learning rate = 2e-2

• Hyperparameters:

o Learning Rate: 2e-2

Batch Size: 64Epochs: 50

Results:

Training Accuracy: 55%
Validation Accuracy: 50%
Testing Accuracy: 51.3%

#### **Comments:**

- In the learning rate of 2e-4, we observe a smooth curve with a gradual increase in accuracy, however the learning isn't fast enough to plateau before the imposed number of epochs.
- In the learning rate of 2e-2 there is a much higher oscillation in learning and loss curves, seemingly producing a highly erractic learning profile. This also resulted in a much loser accuracy for all three data sets than the smaller learning rates.
- Between these two datasets and the original learning rate, the original still produced the best results on the test set at an accuracy of 75.6%. However, just looking at the altered learning rates in Q3.2, the slower learning rate performed better (63.9% vs 51.3% accuracies.

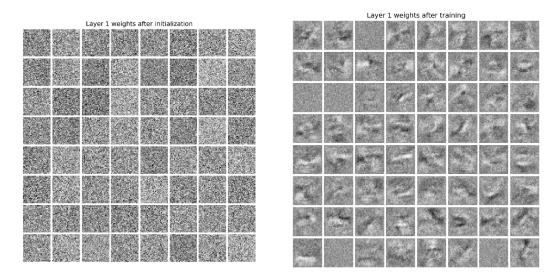


Figure 8. Weights after initialization (left) and after training (right)

#### Comments:

The network used to generate figure 8 used the hyperparameters given in Q3.1.1. Visually, the weights given after initialization have no visably recognized patterns – just looks like pure white noise. After training the weights are beginning to show resemblance of learning shape or form, hinting at the fact that they are gaining information about how to accurately predict the MNIST dataset.

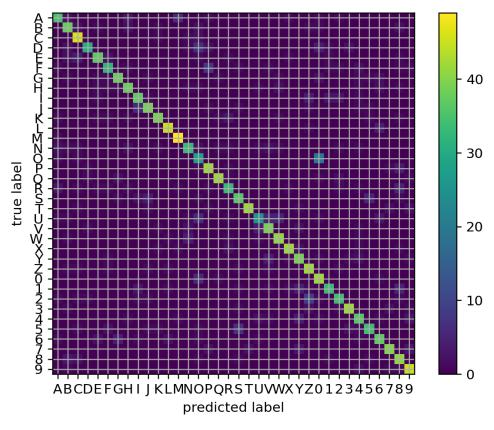


Figure 9. Confusion Matrix for testing data on the MNIST dataset

#### Comments

Here, the hyperparameters used were the same as in Q3.1 (lr = 2e-3, batch size = 64, epochs = 50). The most confused character seemed to be "0" versus "0", which is more than intuitive. Some other lesser confused characters were "2" and "Z", "S" and "5", and "F" and "P". These are reasonable results to obtain, as they are virtually the same penstroke, and depending on two wrote the F/P they are generally similar besides being closed in the off-vertical position.

### Assumptions:

- 1. The letters written are fully connected
  - a. As seen through the O, E, T if the letters are not fully connected there would be multiple bounding boxed surrounding a singular letter
- 2. The letters should not be fully connected
  - a. Our classification would not work for letters that are connected, say if they were written in cursive as the letters are by nature not standalone

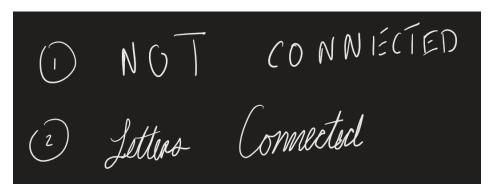
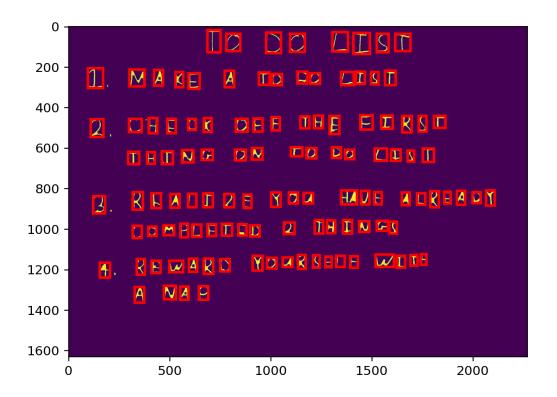
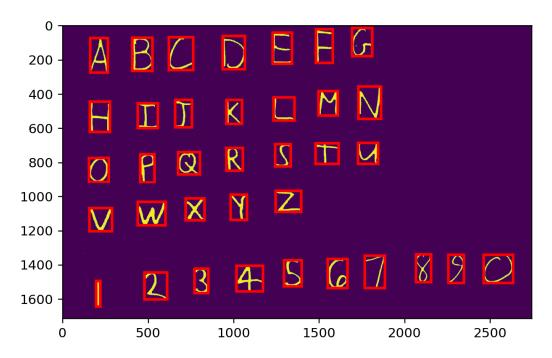
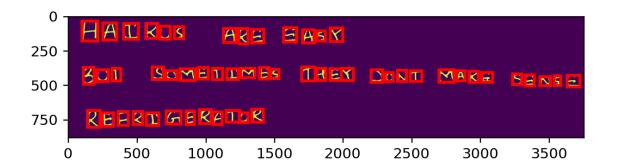


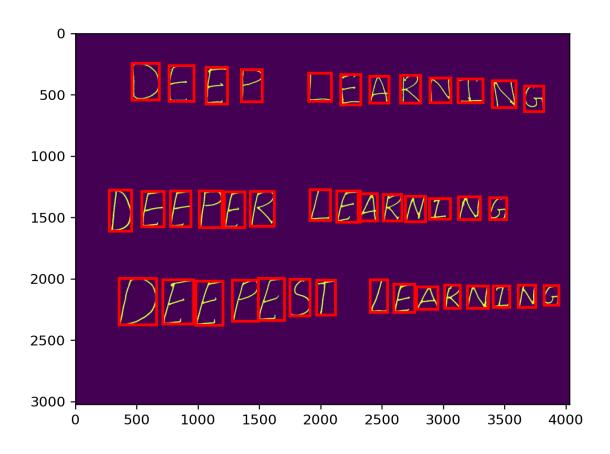
Figure 10. Example of assumptions made by our model

```
def findLetters(image):
   bboxes = []
   bw = None
   # insert processing in here
   # one idea estimate noise -> denoise -> greyscale -> threshold -> morphology -> label -> skip small boxes
   ##### your code here #####
   # denoise the image
         image, weight=0.1, channel_axis=-1)
   # change the image to gray
   image = skimage.color.rgb2gray(image)
   thresh = skimage.filters.threshold_otsu(image)
   bw = skimage.morphology.closing(
       image <= thresh, skimage.morphology.square(10)).astype(np.float32)</pre>
   cleared = skimage.segmentation.clear_border(bw)
   label_image = skimage.measure.label(cleared)
   # to make the background transparent, pass the value of `bg_label`,
   # and leave `bg_color` as `None` and `kind` as `overlay`
   image_label_overlay = skimage.color.label2rgb(
       label_image, image=image, bg_label=0)
   # ax.imshow(image_label_overlay)
   for region in skimage.measure.regionprops(label_image):
        # take regions with large enough areas
       if region.area >= 300:
           bboxes.append(region.bbox)
   return bboxes, bw
```









```
for img in os.listdir('../images'):
   im1 = skimage.img_as_float(
       skimage.io.imread(os.path.join('../images', img)))
   bboxes, bw = findLetters(im1)
   plt.imshow(bw)
   for bbox in bboxes:
       minr, minc, maxr, maxc = bbox
       rect = matplotlib.patches.Rectangle((minc, minr), maxc - minc, maxr - minr,
                                            fill=False, edgecolor='red', linewidth=2)
       plt.gca().add patch(rect)
   plt.show()
   def sorted_arr(arr):
       xvals = []
           xvals.append(i[1])
       xvals.sort()
       result = []
       for i in xvals:
            for j in arr:
               if i == j[1]:
                   result.append(j)
       return result
   rows = []
   realtime_arr = [bboxes[0]]
   for i in range(1, len(bboxes)):
       curr_bbox = bboxes[i]
       box_center_y = (curr_bbox[2] + curr_bbox[0])/2
       ref_bbox = realtime_arr[-1]
       if box_center_y < ref_bbox[0] or box_center_y > ref_bbox[2]:
           rows.append(realtime_arr)
           realtime_arr = []
           realtime_arr.append(curr_bbox)
            realtime_arr.append(curr_bbox)
   rows.append(realtime_arr)
```

```
def get_image(bbox):
    y1, x1, y2, x2 = bbox
    ex = bw[y1:y2, x1:x2]
    height = y2 - y1
    if height > width:
       pad_amt = int(height/2)
       ex = np.pad(ex, (pad_amt, pad_amt), "constant")
    elif width > height:
       pad_amt = int(width/2)
       ex = np.pad(ex, (pad_amt, pad_amt), "constant")
    where_0 = np.where(ex == 0)
    where_1 = np.where(ex == 1)
    ex[where_0] = 1
    ex[where_1] = 0
    if img == "04 deep.jpg":
       ex = cv2.erode(ex, np.ones((14, 14)), iterations=1)
    elif img == "02_letters.jpg":
       ex = cv2.erode(ex, np.ones((4, 4)), iterations=1)
       ex = cv2.erode(ex, np.ones((7, 7)), iterations=1)
    ex = cv2.resize(ex.T, (32, 32))
    ex = ex.flatten()
   return ex
for row in range(len(rows)):
    rows[row] = sorted_arr(rows[row])
    for letter in range(len(rows[row])):
        rows[row][letter] = get_image(rows[row][letter])
import string
letters = np.array(
   [_ for _ in string.ascii_uppercase[:26]] + [str(_) for _ in range(10)])
params = pickle.load(open('q3_weights.pickle', 'rb'))
##### your code here #####
```

## Q4.4: Results

Ground Truth:	Predicted:	Added Spaces
TO DO LIST	TØCCLIST	TO CC LIST
1 MAKE A TO DO LIST	IHAKEATODØLIST 2CHECKOFETHFFIRST THINGONTODOLXST 2R2ALI2EYOUHVEALR2ADY COAPLET2D2YHINØS 4REWAXDYOURSELF4ITH ANAP	I HAKE A TO DO LIST
2 CHECK OFF THE FIRST		2 CHECK OFE THF FIRST
THING ON TO DO LIST		THING ON TO DO LXST
3 REALIZE YOU HAVE ALREADY		2 R2ALI2E YOU HVE ALR2ADY
COMPLETED 2 THINGS		COAPLET2D 2 YHINOS
4 REWARD YOURSELF WITH		4 REWAXD YOURSELF 4ITH
A NAP		ANAP
ABCDEFG	XSCCCFC	XSCCCFC
HIJKLMN	HIJKCKU CYUXST4 V4XYI XXS4SUJXYC	HIJKCKU
OPQRSTU		CYUXST4
VWXYZ		V4XYI
1234567890		XXS4SUJXYC
HAIKUS ARE EASY	HAIRUSAREEASY	HAIRUS ARE EASY
BUT SOMETIMES THEY DON'T MAKE	BLTSOMETIHESTHEYUONTMAK2SENSR	BLT SOMETIHES THEY UONT MAK2 SENSR
SENSE	REFRI6ERATOR	REFRIGERATOR
REFRIDGERATOR		
DEEP LEARNING	CFCYCEARNI44	CFCY CEARNI44
DEEPER LEARNING	UEEYFYLEARKING	UEEYFY LEARKIN6
DEEPEST LEARNING	UFFYESTLEARNING	UFFYEST LEARNING

#### Comments:

The network seemed to perform fairly well for all samples, the worst performing by inspection was that of the letters image file. However, it did have accuracy in guessing some letters like in the second row (H, I, J, K...). I tdid not perform well on the numbers outside of four, but some of the mistakes were reasonble, like the guess of an S for 5 and a C for 0. The rest the images had reasonable estimations of the sentences. An interesting note is that I had to dialate the images differently, as different sample images had different pen strokes, some of the images required more dialation to more closely match the testing data set that the network was trained on.

```
train_data = scipy.io.loadmat('../data/nist36_train.mat')
valid_data = scipy.io.loadmat('../data/nist36_valid.mat')
test_data = scipy.io.loadmat('../data/nist36_test.mat')
train_x, train_y = train_data['train_data'], train_data['train_labels']
valid_x, valid_y = valid_data['valid_data'], valid_data['valid_labels']
test_x, test_y = test_data['test_data'], test_data['test_labels']
examples = train x.shape[0]
input_size = train_x.shape[1]
classes = train_y.shape[1]
train_y = np.argmax(train_y, 1)
valid_y = np.argmax(valid_y, 1)
test_y = np.argmax(test_y, 1)
train_x = torch.from_numpy(train_x).to(torch.float32)
train_y = torch.from_numpy(train_y)
valid x = torch.from numpy(valid x).to(torch.float32)
valid_y = torch.from_numpy(valid_y)
test_x = torch.from_numpy(test_x).to(torch.float32)
test_y = torch.from_numpy(test_y)
train_ds = TensorDataset(train_x, train_y)
valid_ds = TensorDataset(valid_x, valid_y)
test_ds = TensorDataset(test_x, test_y)
train_data = DataLoader(train_ds, batch_size=32,
                        shuffle=True)
valid_data = DataLoader(valid_ds, batch_size=32,
                        shuffle=True)
test data = DataLoader(test ds, batch size=32,
                      shuffle=True)
```

```
max_iters = 50
 batch_size = 64
 learning_rate = 2e-3
 hidden_size = 64
v model = torch.nn.Sequential(
     torch.nn.Linear(input_size, hidden_size),
     torch.nn.Sigmoid(),
     torch.nn.Linear(hidden_size, classes),
     torch.nn.LogSoftmax(dim=1))
 print(model)
 loss_funct = nn.NLLLoss()
 optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate)
v nn_params = {"training acc": 0,
               "training loss": 0,
              "validation loss": 0,
              "testing acc": 0,
 nn_output = np.zeros(shape=(6, max_iters))

v for i in range(max_iters):
     iter_acc = 0
     iter_loss = 0
     for batch_train in train_data:
         batch_x, batch_y = batch_train
         optimizer.zero_grad()
         y_pred = model(batch_x)
         loss = loss_funct(y_pred, batch_y)
         iter_loss = loss.item()
         loss.backward()
         optimizer.step()
          _, predicted = torch.max(y_pred.data, 1)
         iter_acc += torch.sum(predicted == batch_y).item()
     iter_acc /= examples
     nn_params["training acc"] = (nn_params['training acc'] + iter_acc) / 2
     nn_params['training loss'] = iter_loss
```

```
validation data ====
   iter acc = 0
   iter loss = 0
   y_pred = model(valid_x)
   loss = loss_funct(y_pred, valid_y)
   iter_loss = loss.item()
   _, predicted = torch.max(y_pred.data, 1)
   iter_acc += torch.sum(predicted == valid_y).item()
   iter_acc /= valid_x.size(0)
   nn_params["validation acc"] = (nn_params['validation acc'] + iter_acc) / 2
   nn_params['validation loss'] = iter_loss
   iter acc = 0
   iter_loss = 0
   y_pred = model(test_x)
   loss = loss_funct(y_pred, test_y)
   iter_loss = loss.item()
   , predicted = torch.max(y pred.data, 1)
   iter_acc += torch.sum(predicted == test_y).item()
   iter_acc /= test_x.size(0)
   nn_params["testing acc"] = (nn_params['testing acc'] + iter_acc) / 2
   nn_params['testing loss'] = iter_loss
       f"Iter: {i} | Training Acc: {round(nn_params['training acc']*100, 2)}
   nn_output[0, i] = nn_params['training acc']
   nn_output[1, i] = nn_params['validation acc']
   nn_output[2, i] = nn_params['testing acc']
   nn_output[3, i] = nn_params['training loss']
   nn_output[4, i] = nn_params['validation loss']
   nn_output[5, i] = nn_params['testing loss']
 = np.arange(1, max_iters + 1)
olt.figure(1)
olt.title("Q6.1.1 Accuracy Curve")
olt.plot(x, nn_output[0, :] * 100, label="Training Accuracy")
olt.plot(x, nn_output[1, :] * 100, label="Validation Accuracy")
olt.plot(x, nn_output[2, :] * 100, label="Testing Accuracy")
olt.legend()
```

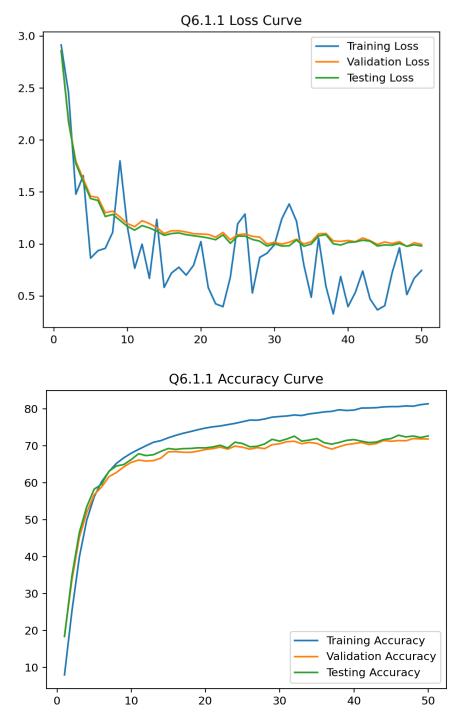
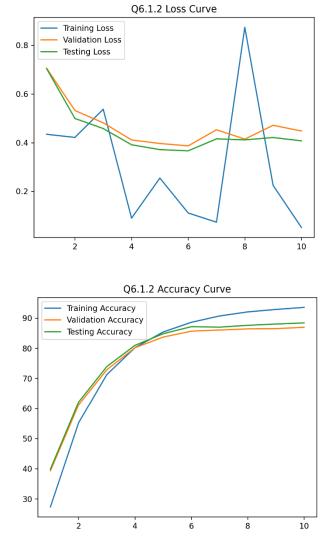


Figure 11. Loss & Accuracy curves for fully connected network recreated in Pytorch



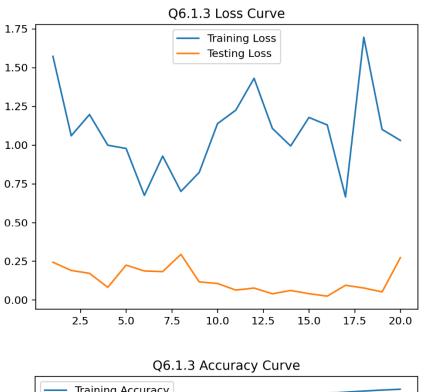
**Figure 12.** Loss & Accuracy curves for ConvNet on MNIST data

## Comments:

Integrating convolutional layers, with the same hyperparamters (lr = 2e-3, batch size = 64, epochs = 50), allowed this neural net to converge to a higher lever of accuracy than the fully connected network five times quicker (10 epochs versus 50 epochs).

```
batch_size = 64
 learning_rate = 2e-3
 hidden_size = 150
v model = torch.nn.Sequential(
    torch.nn.Conv2d(in_channels=1, out_channels=7, kernel_size=3),
     torch.nn.MaxPool2d(kernel_size=2, stride=2),
     torch.nn.Conv2d(in_channels=7, out_channels=13, kernel_size=5),
     torch.nn.MaxPool2d(kernel_size=2, stride=2),
     torch.nn.Linear(325, hidden_size),
     torch.nn.Linear(hidden_size, classes),
     torch.nn.LogSoftmax(dim=1))
 loss_funct = nn.NLLLoss()
 optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate)
v nn_params = {"training acc": 0,
              "training loss": 0,
              "validation acc": 0,
              "testing loss": 0
 nn_output = np.zeros(shape=(6, max_iters))
v for i in range(max_iters):
     iter_acc = 0
     iter_loss = 0
     for batch_train in train_data:
         batch x, batch y = batch train
         batch_x = batch_x.view(-1, 1, 32, 32)
         optimizer.zero_grad()
         y_pred = model(batch_x)
         loss = loss_funct(y_pred, batch_y)
         iter_loss = loss.item()
         loss.backward()
         optimizer.step()
         _, predicted = torch.max(y_pred.data, 1)
         iter_acc += torch.sum(predicted == batch_y).item()
     iter_acc /= examples
     nn_params["training acc"] = (nn_params['training acc'] + iter_acc) / 2
     nn_params['training loss'] = iter_loss
```

```
iter acc = 0
iter_loss = 0
valid_x = valid_x.view(-1, 1, 32, 32)
y_pred = model(valid_x)
loss = loss_funct(y_pred, valid_y)
iter_loss = loss.item()
_, predicted = torch.max(y_pred.data, 1)
iter_acc += torch.sum(predicted == valid_y).item()
iter_acc /= valid_x.size(0)
nn_params["validation acc"] = (nn_params['validation acc'] + iter_acc) / 2
nn_params['validation loss'] = iter_loss
# ----- testing data -----
iter acc = 0
iter_loss = 0
test_x = test_x.view(-1, 1, 32, 32)
y_pred = model(test_x)
loss = loss_funct(y_pred, test_y)
iter_loss = loss.item()
_, predicted = torch.max(y_pred.data, 1)
iter_acc += torch.sum(predicted == test_y).item()
iter_acc /= test_x.size(0)
nn_params["testing acc"] = (nn_params['testing acc'] + iter_acc) / 2
nn_params['testing loss'] = iter_loss
print(
   f"Iter: {i} | Training Acc: {round(nn_params['training acc']*100, 2)}
nn_output[0, i] = nn_params['training acc']
nn_output[1, i] = nn_params['validation acc']
nn_output[2, i] = nn_params['testing acc']
nn_output[3, i] = nn_params['training loss']
nn_output[4, i] = nn_params['validation loss']
nn_output[5, i] = nn_params['testing loss']
```



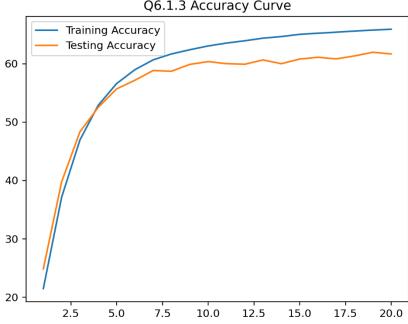


Figure 13. Loss & Accuracy curve for CIFAR-10 ConvNet

```
transform = transforms.Compose(
   [transforms.ToTensor(),
    transforms.Normalize((0.5, 0.5, 0.5), (0.5, 0.5, 0.5))])
batch_size = 10
trainset = torchvision.datasets.CIFAR10(root='./data', train=True,
                                      download=True, transform=transform)
trainloader = DataLoader(trainset, batch_size=batch_size,
                      shuffle=True)
batch_size = 10
testset = torchvision.datasets.CIFAR10(root='./data', train=False,
                                     download=True, transform=transform)
testloader = DataLoader(testset, shuffle=False)
# establish params
max_iters = 20
# pick a batch size, learning rate
learning_rate = 1e-3
hidden_size = 64
device = torch.device("cuda:0" if torch.cuda.is_available() else "cpu")
model = torch.nn.Sequential(
   torch.nn.Conv2d(in_channels=3, out_channels=6, kernel_size=5),
   torch.nn.ReLU(),
   torch.nn.MaxPool2d(kernel_size=2, stride=2),
   torch.nn.Conv2d(in_channels=6, out_channels=16, kernel_size=5),
   torch.nn.ReLU(),
   torch.nn.MaxPool2d(kernel_size=2, stride=2),
   torch.nn.Flatten(),
   torch.nn.Linear(16*25, 20),
   torch.nn.ReLU(),
   torch.nn.Linear(20, 10),
   torch.nn.LogSoftmax(dim=1)).to(device)
loss_funct = nn.NLLLoss()
optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate)
```

```
nn_params = {"training acc": 0, "training loss": 0,
            "testing loss": 0
nn_output = np.zeros(shape=(6, max_iters))
for i in range(max_iters):
   print("Begin Iteration:", i)
   iter_acc = 0
   iter_loss = 0
   for batch_train in trainloader:
       batch_x, batch_y = batch_train
       optimizer.zero_grad()
       y_pred = model(batch_x)
       loss = loss_funct(y_pred, batch_y)
       iter_loss = loss.item()
       loss.backward()
       optimizer.step()
        _, predicted = torch.max(y_pred.data, 1)
       iter_acc += torch.sum(predicted == batch_y).item()
   iter_acc /= trainset.data.shape[0]
   nn_params["training acc"] = (nn_params['training acc'] + iter_acc) / 2
   nn_params['training loss'] = iter_loss
   # ----- testing data -----
   iter_acc = 0
   iter_loss = 0
   for batch_test in testloader:
       test_x, test_y = batch_test
       y_pred = model(test_x)
       loss = loss_funct(y_pred, test_y)
       iter_loss = loss.item()
       _, predicted = torch.max(y_pred.data, 1)
       iter_acc += torch.sum(predicted == test_y).item()
   iter_acc /= testset.data.shape[0]
   print("Testing Iteration", i, "Complete.")
   nn_params["testing acc"] = (nn_params['testing acc'] + iter_acc) / 2
   nn_params['testing loss'] = iter_loss
```

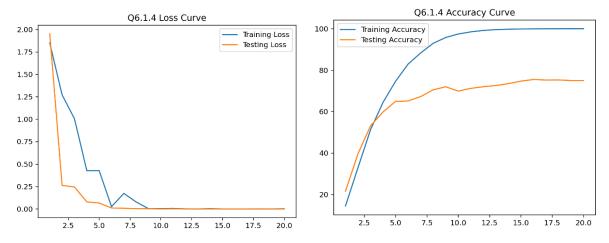


Figure 14. Loss & Accuracy curves for ConvNet on SUN Dataset

## **Comments:**

- Neural Network Approach to Learning:
  - Hyperparameters:
    - Learning Rate: 1e-3
    - Batch Size: 128
    - Epochs: 20
  - o Results:
    - Training Accuracy: 99.9%
    - Validation Accuracy: 74.9%
- Classical BOW Results:
  - 0 67.2%
- Here we saw that the neural network approach performed roughly 8% better than the classical approach the same when you just consider the testing data, but blew the classical approach out of the water in terms of the training data. Since I just used the data set from HW, I only had 160 samples to learn on for the training set. This may have led to the lack of performance on the testing data, if I had had more time, I would've liked to find a way to obtain more training data and added more generalizations to the data so that it would have been able to transfer its performance from training to testing and not overfit to the training set.

```
batch_size = 128
testval_transform = transforms.Compose([
   transforms.RandomHorizontalFlip(),
   transforms.ToTensor(),
   transforms.Normalize(mean=[0.485, 0.456, 0.406],
                         std=[0.229, 0.224, 0.225]),
   transforms.Resize((256, 256))
train_transform = transforms.Compose([
   transforms.RandomHorizontalFlip(),
   transforms.ToTensor(),
   transforms.Normalize(mean=[0.485, 0.456, 0.406],
                         std=[0.229, 0.224, 0.225]),
   transforms.Resize((256, 256))
device = torch.device("cuda:0" if torch.cuda.is_available() else "cpu")
# ? Training Data
trainset = torchvision.datasets.ImageFolder(
   root='../data/oxford-flowers17/train', transform=train_transform)
trainloader = DataLoader(trainset, batch_size=batch_size,
                        shuffle=True, pin_memory=True)
# ? Testing Data
testset = torchvision.datasets.ImageFolder(
   root='.../data/oxford-flowers17/test', transform=testval_transform)
testloader = DataLoader(testset, pin_memory=True)
# ? Validation Data
valset = torchvision.datasets.ImageFolder(
   root='.../data/oxford-flowers17/val', transform=testval_transform)
valloader = DataLoader(valset, pin_memory=True)
# establish params
max_iters = 50
# pick a batch size, learning rate
hidden_size = 64
learning_rate = 1e-3
classes = 17
device = torch.device("cuda:0" if torch.cuda.is_available() else "cpu")
```

```
model = torch.nn.Sequential(
   torch.nn.Conv2d(in_channels=3, out_channels=6, kernel_size=5),
   torch.nn.MaxPool2d(kernel_size=2, stride=2),
   torch.nn.Conv2d(in_channels=6, out_channels=16, kernel_size=5),
   torch.nn.ReLU(),
   torch.nn.MaxPool2d(kernel_size=2, stride=2),
   torch.nn.Flatten(),
   torch.nn.Linear(59536, 800),
   torch.nn.ReLU(),
   torch.nn.Linear(800, classes),
   torch.nn.ReLU(),
).to(device)
loss_funct = nn.CrossEntropyLoss()
optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate)
nn_params = {"training acc": 0,
             "training loss": 0,
             "validation acc": 0,
             "testing acc": 0,
             "testing loss": 0
nn_output = np.zeros(shape=(6, max_iters))
for i in range(max_iters):
   iter_acc = 0
   iter loss = 0
   for batch_train in trainloader:
       batch_x, batch_y = batch_train
       optimizer.zero_grad()
       y_pred = model(batch_x)
       loss = loss_funct(y_pred, batch_y)
       iter_loss = loss.item()
       loss.backward()
       optimizer.step()
        _, predicted = torch.max(y_pred.data, 1)
       iter_acc += torch.sum(predicted == batch_y).item()
   iter_acc /= len(trainset.imgs)
   nn_params["training acc"] = (nn_params['training acc'] + iter_acc) / 2
   nn_params['training loss'] = iter_loss
   print(f"Training Iteration {i} complete")
```

```
iter_acc = 0
iter_loss = 0
for batch_val in valloader:
   batch_x, batch_y = batch_val
   y_pred = model(batch_x)
   loss = loss_funct(y_pred, batch_y)
   iter_loss = loss.item()
   optimizer.step()
    _, predicted = torch.max(y_pred.data, 1)
   iter_acc += torch.sum(predicted == batch_y).item()
iter_acc /= len(valset.imgs)
nn_params["validation acc"] = (nn_params['validation acc'] + iter_acc) / 2
nn_params['validation loss'] = iter_loss
print(f"Validation Iteration {i} complete")
# =========== testing data =============
iter_acc = 0
iter_loss = 0
for batch_test in testloader:
   batch_x, batch_y = batch_test
   y_pred = model(batch_x)
   loss = loss_funct(y_pred, batch_y)
   iter_loss = loss.item()
    _, predicted = torch.max(y_pred.data, 1)
   iter_acc += torch.sum(predicted == batch_y).item()
iter_acc /= len(testset.imgs)
nn_params["testing acc"] = (nn_params['testing acc'] + iter_acc) / 2
nn_params['testing loss'] = iter_loss
   f"Iter: {i+1} | Training Acc: {round(nn_params['training acc']*100, 2)}
nn_output[0, i] = nn_params['training acc']
nn_output[1, i] = nn_params['validation acc']
nn_output[2, i] = nn_params['testing acc']
nn_output[3, i] = nn_params['training loss']
nn_output[4, i] = nn_params['validation loss']
nn_output[5, i] = nn_params['testing loss']
```

```
batch_size = 128 # 64
v testval transform = transforms.Compose([
     transforms.Resize((256, 256)),
v train_transform = transforms.Compose([
     transforms.RandomHorizontalFlip(),
     transforms.ToTensor(),
     transforms.Normalize(mean=[0.485, 0.456, 0.406],
                          std=[0.229, 0.224, 0.225]),
     transforms.Resize((256, 256))
 device = torch.device("cuda:0" if torch.cuda.is_available() else "cpu")
 # ? Training Data
 trainset = torchvision.datasets.ImageFolder(
     root='../data/oxford-flowers17/train', transform=train_transform)
v trainloader = DataLoader(trainset, batch_size=batch_size,
                    shuffle=True)
 # ? Testing Data
v testset = torchvision.datasets.ImageFolder(
     root='.../data/oxford-flowers17/test', transform=testval_transform)
 testloader = DataLoader(testset)
 # ? Validation Data
valset = torchvision.datasets.ImageFolder(
     root='.../data/oxford-flowers17/val', transform=testval_transform)
 valloader = DataLoader(valset)
 max_iters = 30
 learning_rate = 1e-5
 device = torch.device("cuda:0" if torch.cuda.is_available() else "cpu")
```

```
model = squeezenet1_1(pretrained=True).to(device=device)
for param in model.parameters():
    param.requires_grad = False
final_conv = nn.Conv2d(512, 17, kernel_size=1)
model.classifier = nn.Sequential(
   nn.Dropout(p=0.5), final_conv, nn.ReLU(
       inplace=True), nn.AdaptiveAvgPool2d((1, 1))
for param in model.classifier.parameters():
   param.requires_grad = True
loss_funct = nn.CrossEntropyLoss()
optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate)
nn_params = {"training acc": 0,
            "validation acc": 0,
nn_output = np.zeros(shape=(6, max_iters))
for i in range(max_iters):
    iter_acc = 0
    iter_loss = 0
    for batch_train in trainloader:
        batch_x, batch_y = batch_train
        optimizer.zero_grad()
        y_pred = model(batch_x)
        loss = loss_funct(y_pred, batch_y)
        iter_loss = loss.item()
        loss.backward()
       optimizer.step()
        _, predicted = torch.max(y_pred.data, 1)
        iter_acc += torch.sum(predicted == batch_y).item()
    iter acc /= len(trainset.imgs)
    nn_params["training acc"] = (nn_params['training acc'] + iter_acc) / 2
    nn_params['training loss'] = iter_loss
    print(f"Training Iteration {i+1} complete")
```

```
iter acc = 0
iter loss = 0
for batch val in valloader:
   batch_x, batch_y = batch_val
   y_pred = model(batch_x)
   loss = loss_funct(y_pred, batch_y)
   iter_loss = loss.item()
    _, predicted = torch.max(y_pred.data, 1)
   iter acc += torch.sum(predicted == batch y).item()
iter_acc /= len(valset.imgs)
nn_params["validation acc"] = (nn_params['validation acc'] + iter_acc) / 2
nn_params['validation loss'] = iter_loss
print(f"Validation Iteration {i+1} complete")
# =================== testing data ===============
iter acc = 0
iter_loss = 0
for batch test in testloader:
   batch_x, batch_y = batch_test
   y_pred - model(batch_x)
   loss = loss_funct(y_pred, batch_y)
   iter_loss = loss.item()
    _, predicted = torch.max(y_pred.data, 1)
   iter acc += torch.sum(predicted == batch y).item()
iter_acc /= len(testset.imgs)
nn_params["testing acc"] = (nn_params['testing acc'] + iter_acc) / 2
nn_params['testing loss'] = iter_loss
print(f"Test Iteration {i+1} complete")
print(
    f"Iter: {i+1} | Training Acc: {round(nn_params['training acc']*100, 2)}
```

```
batch size = 128 # 64
transform = transforms.Compose([
   transforms.ToTensor(),
   transforms.Normalize(mean=[0.485, 0.456, 0.406],
                        std=[0.229, 0.224, 0.225]),
    transforms.Resize((256, 256))
device = torch.device("cuda:0" if torch.cuda.is available() else "cpu")
# ? Training Data
trainset = torchvision.datasets.ImageFolder(
   root='../data/oxford-flowers17/train', transform=transform)
trainloader = DataLoader(trainset, batch_size=batch_size,
                       shuffle=True)
testset = torchvision.datasets.ImageFolder(
   root='../data/oxford-flowers17/test', transform=transform)
testloader = DataLoader(testset)
valset = torchvision.datasets.ImageFolder(
   root='.../data/oxford-flowers17/val', transform=transform)
valloader = DataLoader(valset)
max_iters = 30
learning_rate = 1e-3
device = torch.device("cuda:0" if torch.cuda.is_available() else "cpu")
model = torch.nn.Sequential(
   torch.nn.Conv2d(in_channels=3, out_channels=6, kernel_size=5),
   torch.nn.MaxPool2d(kernel_size=2, stride=2),
   torch.nn.Conv2d(in_channels=6, out_channels=16, kernel_size=5),
   torch.nn.ReLU(),
    torch.nn.MaxPool2d(kernel_size=2, stride=2),
    torch.nn.Linear(59536, 1745),
    torch.nn.ReLU(),
    torch.nn.Linear(1745, 17),
    torch.nn.LogSoftmax(dim=1)).to(device)
loss_funct = nn.CrossEntropyLoss()
optimizer = torch.optim.Adam(model.parameters(), lr=learning rate)
```

## Q6.2: Custom Network

```
nn_params = {"training acc": 0,
             "training loss": 0,
             "testing acc": 0,
nn_output = np.zeros(shape=(6, max_iters))
for i in range(max_iters):
    iter_acc = 0
    iter_loss = 0
    for batch_train in trainloader:
       batch_x, batch_y = batch_train
       optimizer.zero_grad()
       y_pred = model(batch_x)
        loss = loss_funct(y_pred, batch_y)
        iter_loss = loss.item()
       loss.backward()
       optimizer.step()
        _, predicted = torch.max(y_pred.data, 1)
        iter_acc += torch.sum(predicted == batch_y).item()
    iter_acc /= len(trainset.imgs)
    nn_params["training acc"] = (nn_params['training acc'] + iter_acc) / 2
    nn_params['training loss'] = iter_loss
    print(f"Training Iteration {i+1} complete")
```

```
iter acc = 0
iter_loss = 0
for batch val in valloader:
   batch_x, batch_y = batch_val
   y_pred = model(batch_x)
   loss = loss_funct(y_pred, batch_y)
   iter_loss = loss.item()
    _, predicted = torch.max(y_pred.data, 1)
   iter_acc += torch.sum(predicted == batch_y).item()
iter acc /= len(valset.imgs)
nn_params["validation acc"] = (nn_params['validation acc'] + iter_acc) / 2
nn params['validation loss'] = iter loss
print(f"Validation Iteration {i+1} complete")
# =========== testing data =============
iter acc = 0
iter_loss = 0
for batch_test in testloader:
   batch x, batch y = batch test
   y_pred = model(batch_x)
   loss = loss_funct(y_pred, batch_y)
   iter loss = loss.item()
    _, predicted = torch.max(y_pred.data, 1)
   iter_acc += torch.sum(predicted == batch_y).item()
iter_acc /= len(testset.imgs)
nn_params["testing acc"] = (nn_params['testing acc'] + iter_acc) / 2
nn_params['testing loss'] = iter_loss
print(f"Test Iteration {i+1} complete")
print(
    f"Iter: {i+1} | Training Acc: {round(nn_params['training acc']*100, 2)}
```

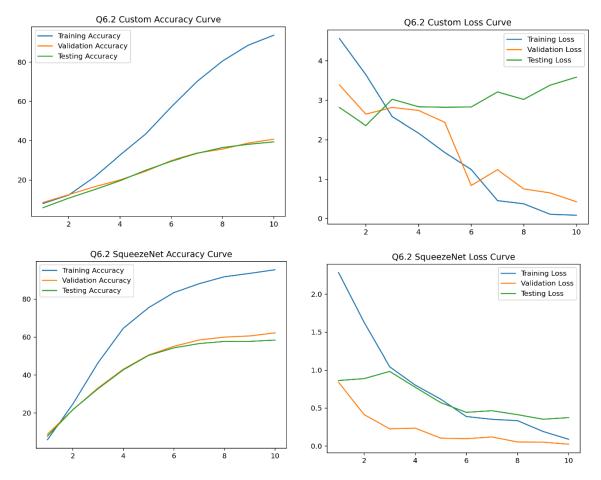


Figure 15. Loss & Accuracy Curves for SqueezeNet (Bottom) and custom ConvNet (Top)

## Comments

- Both networks were run for 10 epochs, in which the SqueezeNet performed on the test and validation accuracy. It seems that the SqueezeNet was able to generalize better to nontraining style data, displaying its robustness in learning.
- SqueezeNet Accuracies:

o Train: 95.4%

o Test: 58.4

o Validation: 62.2%

• Custom Network:

Train: 93.6%Test: 36.8%

o Validation: 37.6%