SGN-41007 Pattern Recognition and Machine Learning

Exercise Set 2: January 15 – 19, 2017

Exercises consist of both pen&paper and computer assignments. Pen&paper questions are solved at home before exercises, while computer assignments are solved during exercise hours. The computer assignments are marked by $\boxed{\textbf{python}}$ and Pen&paper questions by $\boxed{\textbf{pen\&paper}}$

Before you start, load all the data for all questions from:

`http://www.cs.tut.fi/courses/SGN-41007/exercises/Ex2_data.zip`

1. $\boxed{\textbf{pen\&paper}}$ *Least squares fit.* Two measurements $x(n)$ and $y(n)$ depend on each other in a linear manner, and there are the following measurements available:

n	0	1	2
$x(n)$	7	9	2
$y(n)$	11.6	14.8	3.5

    We want to model the relationship between the two variables using the model:

    $$y(n) = ax(n) + b.$$

    Find the least squares estimates $\hat{a}$ and $\hat{b}$ that minimize the squared error.

2. $\boxed{\textbf{python}}$ *Least squares fit (like question 1 but with numpy).*

    Extract the contents (two numpy arrays) of `least_squares_data.zip` and open in numpy (see `numpy.load`). We want to model the relationship between the two variables using the model:

    $$y(n) = ax(n) + b.$$

    Find the least squares estimates $\hat{a}$ and $\hat{b}$ that minimize the squared error.

3. $\boxed{\textbf{python}}$ *Same as last week (Moodle) Question 1, but without numpy.*

    a) Read the file `locationData.csv"` into memory one line at a time (in a for loop). See similar example at the end of lecture slide set 1.

    b) Load the same data into another variable using `numpy.loadtxt`. Check that the contents of the two arrays are equal using `numpy.all` or `numpy.any`.

4. **python** *Load Matlab data into Python.*

a) Load the file `twoClassData.mat` into Python. This can be done as follows.

```
>>> from scipy.io import loadmat
>>> mat = loadmat("twoClassData.mat")
```

This generates a **dict** structure, whose elements can be accessed through their names.

```
>>> print(mat.keys()) # Which variables mat contains?
['y', 'X', '__version__', '__header__', '__globals__']
>>> X = mat["X"] # Collect the two variables.
>>> y = mat["y"].ravel()
```

The function `ravel()` transforms y from 400×1 matrix into a 400-length array. In Python these are different things unlike Matlab.

b) The matrix X contains two-dimensional samples from two classes, as defined by y. Plot the data as a scatter plot like the picture below. Hints:

- You can access all class 0 samples from X as: `X[y == 0, :]`.
- The samples can be plotted like: `plt.plot(X[:, 0], X[:, 1], 'ro')`
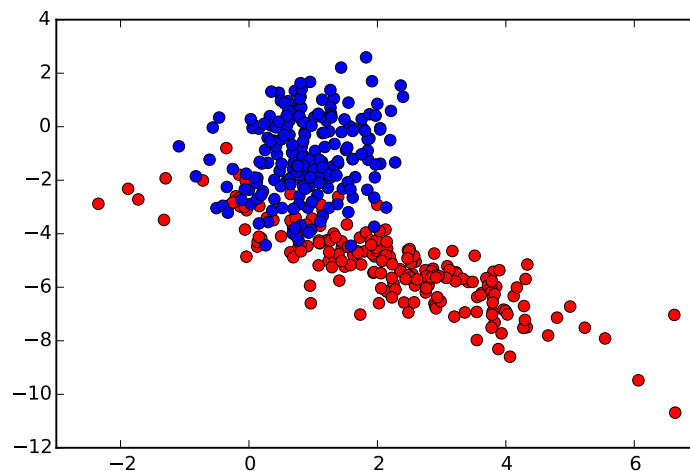
5. **python** *Remove the uneven illumination from a microscope image using least squares fitting like we did at the lecture.*

You may use the Python template as a basis:

`http://www.cs.tut.fi/courses/SGN-41007/exercises/task5_template.py`

Load the image into numpy array `Z` using the `imread` function of `matplotlib.image`[1]. Finally, show the image on screen (using

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[1]Note: There are several other ways of doing this, such as: `matplotlib.image.imread`, `scipy.ndimage.imread`, `PIL.Image.open` or `cv2.imread`

`matplotlib.pyplot.imshow`) and check that the image shape is 1300×1030. Let's next fit a 2nd order surface to the grayscales.

a) Create the explanatory variables (all x,y-coordinates in a matrix): `X, Y = np.meshgrid(range(1300), range(1030))`

b) Vectorize the matrices $\mathbf{X}, \mathbf{Y}, \mathbf{Z}$ using `ravel`, *e.g.*, `z = Z.ravel()`.

c) Prepare the design matrix $\mathbf{H}$ like in the lectures and solve the LS coefficients $\mathbf{c}$.

d) Compute the model prediction as `z_pred = np.dot(H, c)` and resize the vector to the original size.

e) Subtract the model prediction from the original image and show the result on screen.