Universidade de São Paulo Escola Politécnica - Engenharia de Computação e Sistemas Digitais

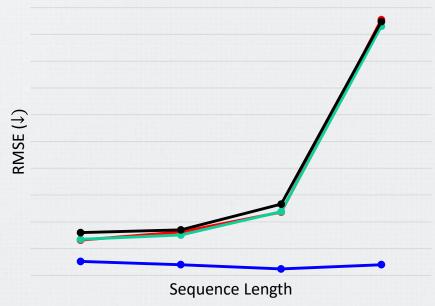
# Transformers, Modern MLP Architectures and Foundation Models

Prof. Artur Jordão

#### Introduction

**Transformers** 

- The transformer (Vaswani et al., 2017) architecture has revolutionized various fields of artificial intelligence, such as natural language understanding and computer vision
  - These models express long sequences of data better than recurrent models



#### Introduction

**Transformers** 

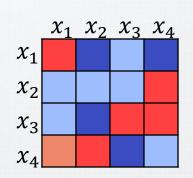
- Transformers-like models stands as the modern paradigm for solving cognitive tasks (Bengio et al., 2025)
- Surprisingly, these models perform on par or better than convolutional networks (Dosovitskiy et al., 2021)
  - Convolutional models have dominated deep learning for computer vision tasks

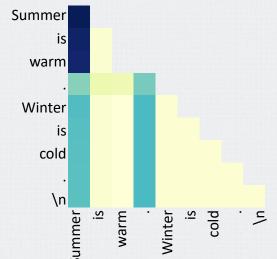
Model	CIFAR-10	ImageNet
ResNet	93.57	80.62
NASNet	97.60	74.00
Transformer	99.50	88.55

Bengio et al. International AI Safety Report. 2025

# **Self-Attention (SA)**

- At the heart of Transform lies the self-attention mechanism
  - Ability to learn pairwise relationships between all tokens/features in a given sequence
  - Attention to itself
- A self-attention,  $SA(\cdot)$ , block takes n inputs  $x_1, x_2, ... x_n$  and returns n output vectors of the same size
  - Each  $x_i$  has dimensions  $d \times 1$





#### **Values**

- A set of values is computed for each input in terms of  $v_i = W^v x_i + b^v$ 
  - $W^{v}$  indicates (learnable) weights
  - $b^{v}$  indicates the bias
- Note that the weights  $W^v \in \mathbb{R}^{d \times d}$  and biases  $b^v \in \mathbb{R}^d$  are shared across all inputs  $x_i \in \mathbb{R}^d$

# **Queries and Keys**

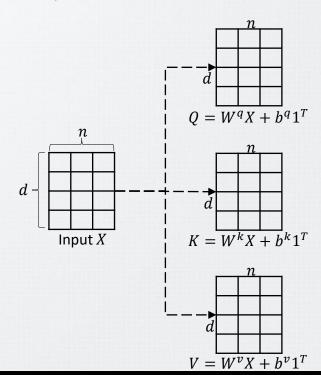
- Queries (q) and keys (k) are linear transformations
  - $q_i = W^q x_i + b^q$
  - $k_i = W^k x_i + b^k$
- The queries and keys must have the same dimensions

#### **Attention**

- The scalar weight  $a[x_i, x_n]$  is the attention that the nth output pays to input  $x_i$
- The n weights  $a[,x_n]$  are non-negative and sum to one
- The attention weights  $a[x_i, x_n]$  combine the values from different inputs
- $a[x_i, x_n] = Softmax(k_n^T q_n)$

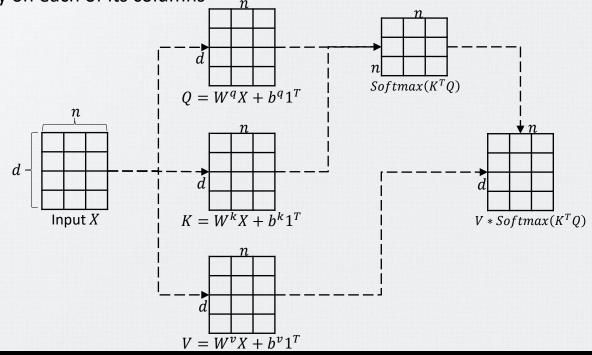
#### **Matrix Form**

- We can put Values, Keys and Queries into a compact form
  - Assuming that the n inputs  $x_n$  form the columns of the  $d \times n$  matrix X
- $V = W^{v}X + b^{v}1^{T}$ 
  - Values
- $Q = W^q X + b^q 1^T$ 
  - Queries
- $K = W^k X + b^k 1^T$ 
  - Keys



# **Self-Attention (SA)**

- $SA = V * Softmax(K^TQ)$ 
  - In this matrix form, the  $Softmax(\cdot)$  function takes a matrix and performs the softmax operation independently on each of its columns



### **Scaled Dot Product Self-Attention**

**Transformer Architecture** 

- The dot products in the attention computation can have large magnitudes
  - It moves the arguments to the softmax function into a region where the largest value completely dominates
  - Small changes to the inputs to the softmax function now have little effect on the output (i.e., the gradients are very small)
- We can scale the dot products by the square root of the dimension d of the queries and keys

• 
$$SA = V * Softmax\left(\frac{K^TQ}{\sqrt{d}}\right)$$

This is known as scaled dot product self-attention

#### **Multi-Head Attention**

- To enable the model to learn different representations, the architecture applies the self-attention mechanism multiple (h) times for the same input X
  - We name the hth self-attention as head
- Each head has its own set of weights (and biases)
  - $W^{vh}$ ,  $W^{qv}$ ,  $W^{kv}$
- The self-attention to the head h is:  $V_h * Softmax\left(\frac{K_h^T Q_h}{\sqrt{d}}\right)$
- Finally, we concatenate and project onto a learnable matrix  $W^o$ 
  - $Multihead(Q, K, V) = Concat(head_1, head_2, ..., head_h)W^o$

# **Complexity**

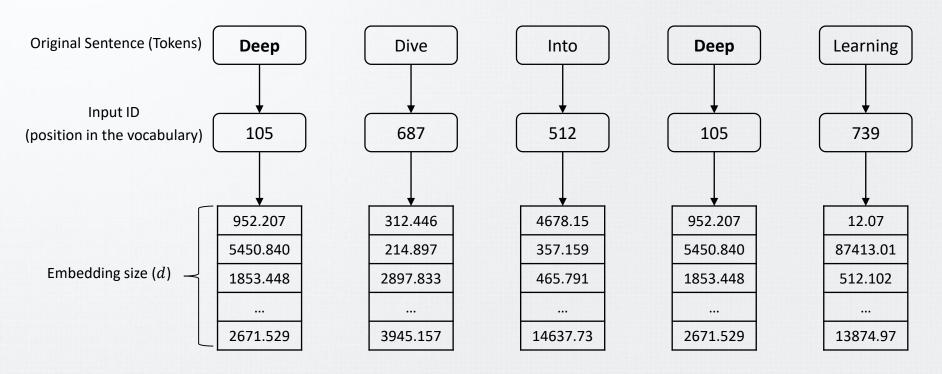
- Advantages of attention layers over recurrent and convolutional networks
  - Lower computational complexity
  - Higher connectivity: especially useful for learning long-term dependencies in sequences
- Definitions
  - *n*, sequence length
  - k, kernel size (convolutional layers)
  - *d*, representation dimension

Layer Type	Complexity per Layer		
Recurrent	$O(n \times d^2)$		
Convolutional	$O(k \times n \times d^2)$		
Self-Attention	$O(n^2 \times d)$		

# **Embedding**

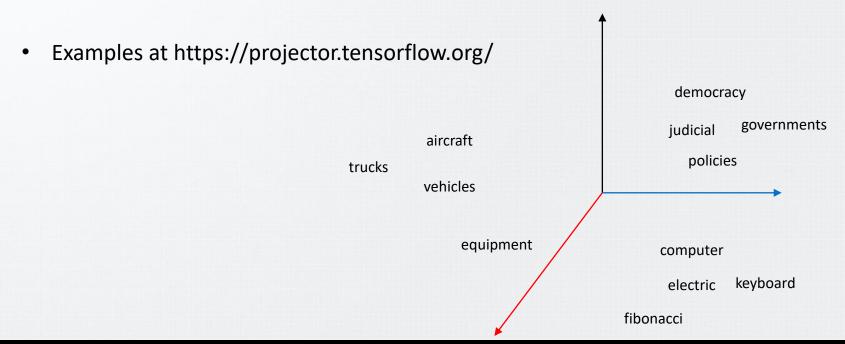
**Transformer Architecture** 

Examples at https://platform.openai.com/tokenizer



# The Role of Embedding

- The embedding maps words into a continuous vector space
  - Semantically similar words are positioned closer together
  - It helps models capture meaning and relationships between words effectively

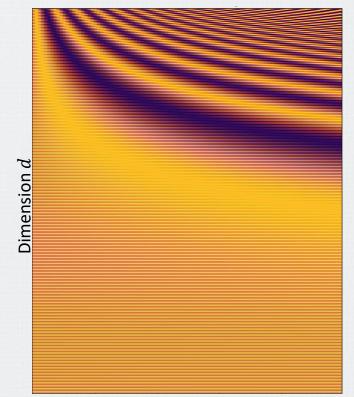


# **Positional Encoding**

- The previous components we have seen so far are unable to capture relative positions: they contain no recurrence or convolution
  - The computation is the same regardless of the order of the inputs  $x_n$
  - It is equivariant with respect to input permutations
- The positional encoding injects some information about the **relative or absolute position** of the input in the sequence
  - This component plays a role in Transformers-like models

# **Positional Encoding**

- Sinusoidal pattern (sine and cosine functions)
  - $PE_{(pos,2i)} = sin\left(\frac{pos}{10000\frac{2i}{d}}\right)$
  - $PE_{(pos,2i+1)} = cos\left(\frac{pos}{10000^{\frac{2i}{d}}}\right)$
  - pos is the index in the sequence and i is the ith position in d ( $i \in \{0, 1, 2 \dots (|d| 1)\}$ )

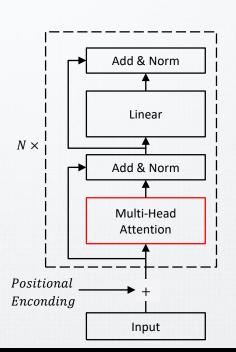


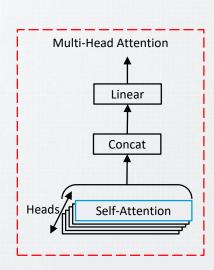
# **Positional Encoding**

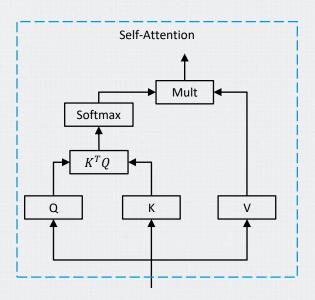
- Sinusoidal pattern (sine and cosine functions)
  - $PE_{(pos,2i)} = sin\left(\frac{pos}{10000\overline{d}}\right)$
  - $PE_{(pos,2i+1)} = cos\left(\frac{pos}{10000^{\frac{2i}{d}}}\right)$
  - pos is the index in the sequence and i is the ith position in d ( $i \in \{0, 1, 2 ... (|d| 1)\}$ )

Sequence	pos	i = 0	i = 1	i = 2	i = 3
1	0	$PE_{(00)} = \sin(0) = 0$	$PE_{01} = \cos(0) = 1$	$PE_{(02)} = \sin(0) = 0$	$PE_{(03)} = \cos(0) = 1$
Am	1	$PE_{10} = \sin(1) = 0.84$	$PE_{11} = \cos(1) = 0.54$	$PE_{(12)} = \sin(0.01) = 0.009$	$PE_{(13)} = cos(0.01) = 0.9999$
А	2	$PE_{20} = \sin(2) = 0.909$	$PE_{21} = \cos(2) = -0.416$	$PE_{(22)} = \sin(0.02) = 0.019$	$PE_{(23)} = cos(0.02) = 0.9998$
Robot	3	$PE_{30} = \sin(3) = 0.14$	$PE_{31} = \cos(3) = -0.989$	$PE_{32} = \sin(0.03) = 0.0299$	$PE_{33} = \cos(0.03) = 0.9995$

# **Overall Architecture**





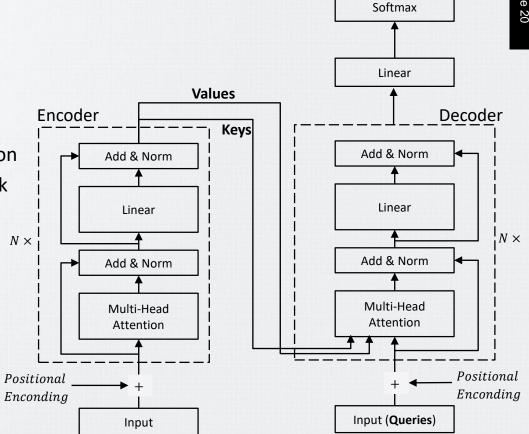


## **Overall Architecture**

**Transformer Architecture** 

Encoder

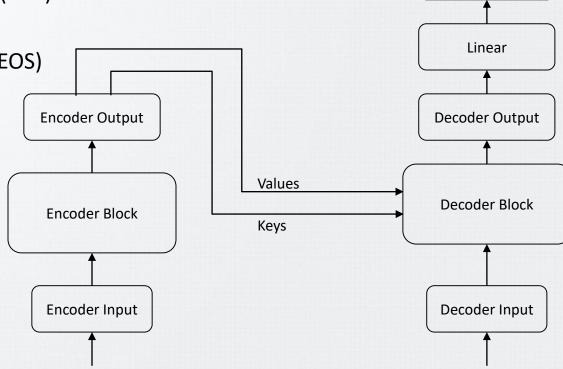
- Decoder
  - It performs multi-head attention on the output of the encoder stack



# **Training Stage**

**Transformer Architecture** 

- Start of Sequence (SOS)
- End of Sequence (EOS)



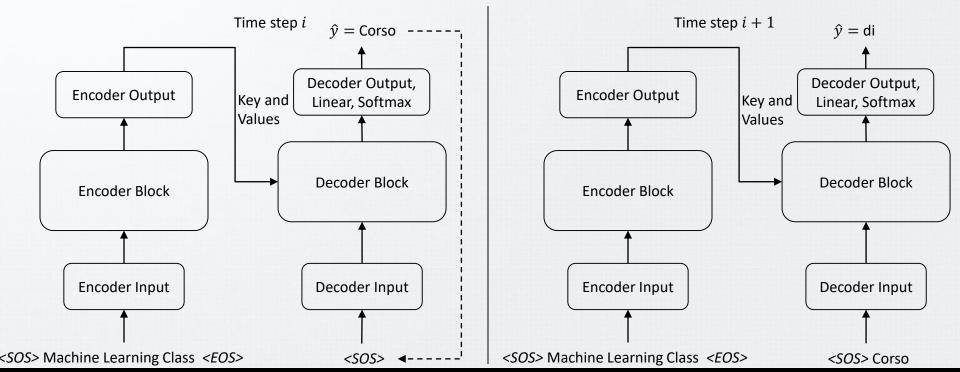
<SOS> Deep Learning and Neural Networks Class <EOS>

<SOS> Corso di Deep Learning e Reti Neurali <EOS>

Softmax

# **Inference Stage**

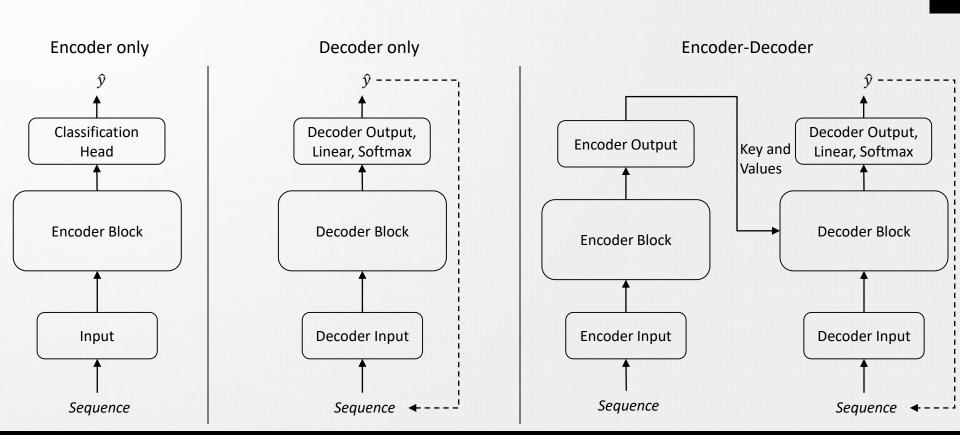
- Time steps
  - Append the previously output word (time step  $i \hat{y}$ ) to the decoder input (time step i + 1)



# **Architectures Encoder, Decoder and Encoder-Decoder**

- Encoder (only)
  - Effective to capture the full representation of a text
  - Non-autoregressive mechanism
  - Example: BERT
- Decoder (only)
  - Generative Al
  - Autoregressive
  - Examples: Llama and GPT
- Encoder-Decoder
  - Generative AI
    - Autoregressive
  - Sequence-to-Sequence

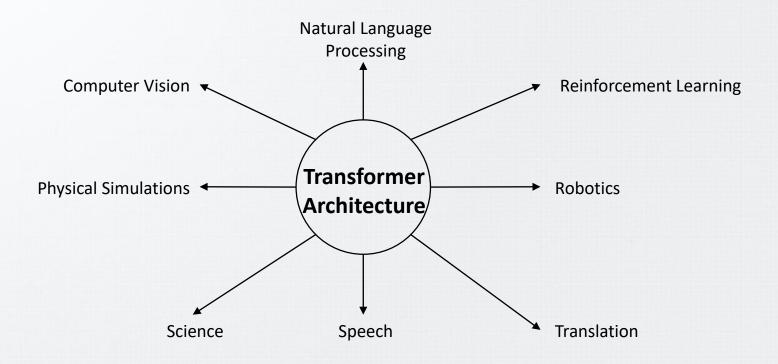
# **Architectures Encoder, Decoder and Encoder-Decoder**



# **Multiple Tasks**

**Transformer Architecture** 

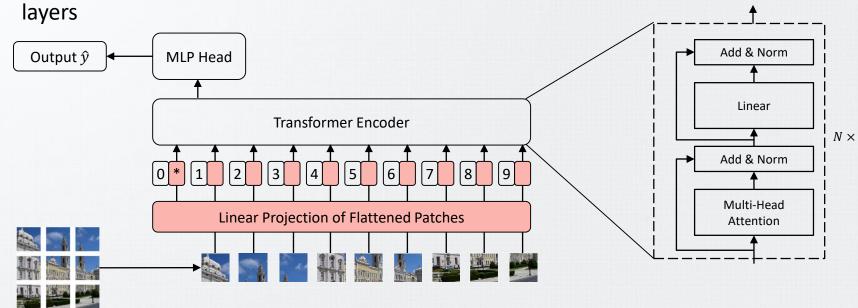
Copy & Paste (or plug & pRay) the transformer architecture and use it everywhere



## **Visual Transformer (ViT)**

**Transformer Architecture** 

- Transformer architecture for image recognition
- Transformer-based image recognition model that is fully built on the Transformer



Dosovitskiy et al. *An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale*. International Conference on Learning Representations (ICLR), 2021

# **Data Sensibility**

**Transformer Architecture** 

- To achieve state-of-the-art results, ViT requires pre-training on large datasets
  - For example, ImageNet-21k or JFT-300M dataset
- The lack of the typical convolutional inductive bias makes these models more data-hungry than common CNNs (Liu et al., 2021)

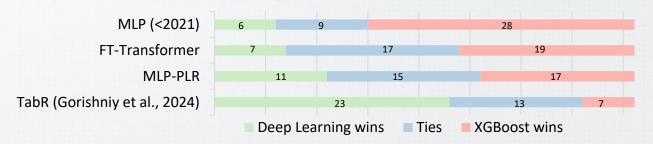
Model	CIFAR-10	CIFAR-100	Flowers102
ViT (variation)	84.19	65.16	31.73
ResNet-50	91.78	72.80	46.92

Source: Liu et al., 2021

#### **Transformer for Tabular Data**

**Transformer Architecture** 

- TabPFN (Hollmann et al., 2023)
  - A transformer model for classification that is pre-trained on synthetic data to be applied to unseen datasets, quickly and without hyperparameter tuning
- In the context of tabular data, transformers (and other neural networks) do not achieve state-of-the-art performance (Grinsztajn et al., 2022; Gorishniy et al. 2024)



Hollmann et al. *TabPFN: A Transformer That Solves Small Tabular Classification Problems in a Second*. International Conference on Learning Representations (ICLR), 2023

Grinsztajn et al. Why do tree-based models still outperform deep learning on typical tabular data? Neural Information Processing Systems (NeurIPS), 2022

Gorishniy et al. TabR: Tabular Deep Learning Meets Nearest Neighbors. International Conference on Learning Representations (ICLR), 2024

# **Modern MLP Architectures**

#### Introduction

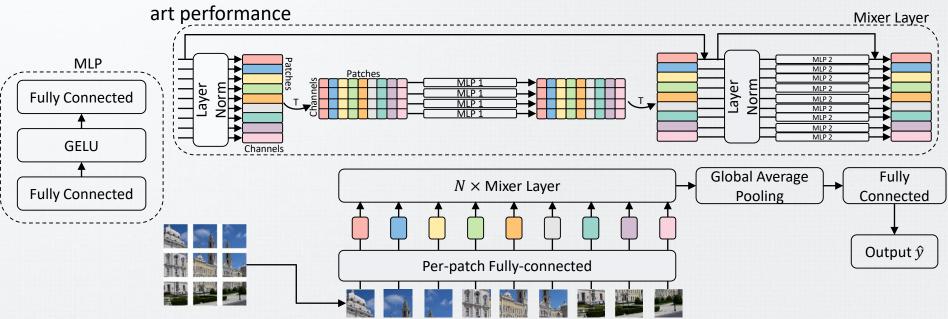
**Modern MLP Architectures** 

- MLP architectures demonstrate better generalization because they capture global representations (e.g., structure) more effectively than CNN methods (Guo et al., 2023)
- Compared to CNNs and Transformers, these vision MLP architectures involve less inductive bias and have potential to be applied to more diverse tasks (Tang et al., 2022)

#### **Architecture Overview**

**Modern MLP Architectures** 

- The architecture is based entirely on multi-layer perceptrons (MLPs)
  - It does not employ any convolution or self-attention layer
  - Require pre-training on large datasets (i.e., ~100M images) to reach achieve state-of-theart performance



Tolstikhin et al. MLP-Mixer: An all-MLP Architecture for Vision. Neural Information Processing Systems (NeurIPS), 2021

#### **Definition**

- Large deep learning models trained on a broad range of data (web-scale training)
   with the capacity to transfer their knowledge to unseen (downstream) tasks
  - Impressive generalization abilities
- Any model is trained on broad data (generally using self-supervision at scale), for which we can adapt it to a wide range of downstream tasks (Bommasani et al., 2021)
- Transformer architectures have ushered in the era of foundation models
  - Most foundation models are based on Transformers

# **Keys to Foundation Models**

- We could transfer the large-scale knowledge captured in these models to target (downstream) tasks by training on a small amount of labeled data
- Keys to Foundation Models
  - Fine-tuning
  - Self-supervised learning

#### **Inductive Bias**

**Foundation Models** 

- The tendency of a model to prioritize one solution over another as it extrapolates between data points
- Inductive biases (prior knowledge) show preferences for solutions with certain properties
  - The preference for one choice over others
- Types of inductive bias
  - Locality and translation invariance (CNNs): Bias towards identifying patterns independent of their location within the image
  - Relational (GNNs): Bias towards prioritizing information from neighbors nodes
  - Simplicity Bias (Kirichenko et al., 2023): Bias towards rely on the simple features while ignoring predictive and complex features

Bommasani et al. Last Layer Re-training is Sufficient for Robustness to Spurious Correlations. International Conference on Learning Representations (ICLR), 2023

#### **Inductive Bias**

- Transformers and MLPs architectures don't have inductive bias of convolutional networks
  - By using huge amounts of data, it can surmount this disadvantage
- Scaling compute compensates for the lack of inductive bias (Tolstikhin et al, 2021; Bachmann et al., 2023)

15*T* Tokens

# **Popular Foundation Models**

**Foundation Models** 

Model	Task	Number of Parameters	Al Research Organization	Dataset size (Corpous size)
AlphaFold	Protein folding	18M - 60M	DeepMind	3.3 <i>B</i>
CLIP	Image classification	63 <i>M</i>	OpenAl	400M (image-text pairs)
BERT	Language Understanding Question Answering	110 <i>M</i> – 340 <i>M</i>	Google	3.3 <i>B</i>
BART	Text generation/Understanding	140M - 400M	Facebook	33 <i>B</i>
StableDiffusion	Text-to-image generation	890 <i>M</i>	LMU Munich + Stability.ai + Eleuther.ai	5B (image-text pairs)
DALL-E	Text-to-image generation	12 <i>B</i>	OpenAl	250M (image-text pairs)
GPT-3	Language Understanding	175 <i>B</i>	OpenAl	500 <i>B</i>

Meta

Llama 3 Multitask 8B/70B/405BAmatriain et al. *Transformer models: an introduction and catalog.* ArXiv 2023

#### Llama 3

- Llama 3 uses a standard, dense Transformer architecture (Vaswani et al., 2017)
  - Regarding architecture, the model does not deviate significantly from Llama and Llama 2
  - Its performance gains are primarily driven by improvements in data quality and diversity
- The model supports context window to 128K tokens

## Llama 3 – Training Recipe

**Foundation Models** 

- AdamW optimizer and lower batch size (4M tokens) early in training and increase (8M) it subsequently
- The training dynamic is very stable with few loss spikes but without requiring interventions to correct for model training divergence

Component	8 <i>B</i>	70 <i>B</i>	405 <i>B</i>
Number of Layers	32	80	126
Model Dimension	4096	8192	16384
Attention Heads	32	64	128
Activation	SwiGLU (Shazeer et al. 2020)		
Positional Embedding	RoPe (Su et al., 2024)		

Su et al. Roformer: Enhanced Transformer with Rotary Position Embedding. Neurocomputing, 2024

Shazeer et al. GLU Variants Improve Transformer. ArXiv, 2020

# Llama 3 – Computational Issues

**Foundation Models** 

- The largest model training involved up to 16K H100 GPUs distributed globally
- The complexity of 16K GPU training raises potential failure

• During a **54-day** snapshot period of pre-training, the process experienced a total of 466 job

interruptions

Component	Caterogy	% of Interruptions
Faulty GPU	GPU	30.1
Software Bug	GPU	12.9
Network Switch/Cable	Network	8.4
Host Maintenance	Unplanned Maintenance	7.6
Server Chassis	Host	0.5

Llama Team. The Llama 3 Herd of Models. ArXiv 2024

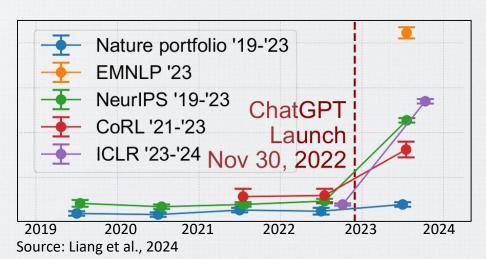
#### **ChatGPT**

#### **Foundation Models**

The impact of ChatGPT on the popularization of Transformers

 OpenAI released ChatGPT in November 2022, making it the fastest-growing app in history, reaching 1 million users in less than a month and 100 million in less than two months

(Amatriain et al., 2023)



Amatriain et al. Transformer models: an introduction and catalog. ArXiv 2023

Liang et al. Monitoring AI-Modified Content at Scale: A Case Study on the Impact of ChatGPT on AI Conference Peer Reviews. International Conference on Machine Learning (ICML), 2024

#### **ChatGPT**

#### **Foundation Models**

The impact of ChatGPT on the popularization of Transformers

#### **CVPR Review Policy**

LLM policy: Remember that you can use an LLM to refine your review text if you think it is helpful. But you CAN'T show the paper to an LLM in any way, because doing so is a major violation of policy. We think we can detect people showing papers to LLMs, and we will prosecute people we catch. Don't do this.

What is the LLM Policy for referees in CVPR 2024?

Details: https://cvpr.thecvf.com/Conferences/2024/ReviewerGuidelines

Referees may use any device, including an **LLM**, **to polish their review wording**, but must vouch for, and be responsible for, the accuracy of the review. It is a significant act of referee misconduct to allow an LLM to see a submission. **PCs interpret showing a submission to an LLM as a deliberate referee violation of confidentiality.** 

Clarification on Large Language Model Policy LLM (Details: https://icml.cc/Conferences/2023/Ilm-policy)

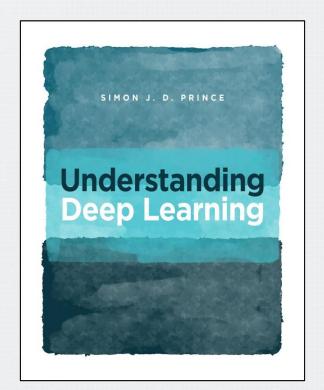
Papers that include text generated from a large-scale language model (LLM) such as ChatGPT are prohibited unless the produced text is presented as a part of the paper's experimental analysis.

• The Large Language Model (LLM) policy for ICML 2023 prohibits text produced entirely by LLMs (i.e., "generated"). This does not prohibit authors from using LLMs for **editing or polishing author-written text**.

# A Change of Paradigm

Classic Machine Learning	<b>Foundation Model Learning</b>	
Single model	Model Zoos	
Model is trained from scratch	Model is rigid and cannot always be modified (often accessible via API)	
Model is the "secret sauce"	Data is the "secret sauce"	
Trivial to fine-tune	Non trivial to fine-tune and maintain over time	
With sufficient funding, it is possible to establish a local infrastructure	Shortage of accelerators	

- Understanding Deep Learning
  - Chapter 12
    - 12.2 Dot-product self-attention
    - 12.3 Extensions to dot-product self-attention
    - 12.4 Transformers



- Vaswani et al. Attention Is All You Need. Neural Information Processing Systems (NeurIPS), 2017
- Dosovitskiy et al. An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale. International Conference on Learning Representations (ICLR), 2021
- Liu et al. Efficient Training of Visual Transformers with Small Datasets. Neural Information Processing Systems (NeurIPS), 2021







- Bachmann et al. Scaling MLPs: A Tale of Inductive Bias. Neural Information Processing Systems (NeurIPS), 2023
- Touvron et al. ResMLP: Feedforward Networks for Image Classification With Data-Efficient Training. Pattern Analysis and Machine Intelligence (PAMI), 2023
- Liu et al. *Understanding the Difficulty of Training Transformers*. Conference on Empirical Methods in Natural Language Processing (EMNLP), 2020





PATTERN ANALYSIS AND