

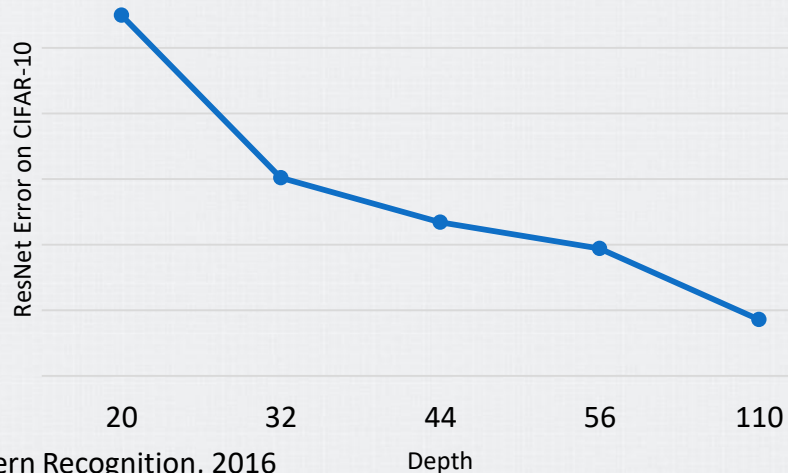
# Deep Learning

Prof. Artur Jordão

# Introduction

## Deep Learning

- Deep learning is advancing machine learning toward human-level performance in many cognitive tasks
  - It is now the powerhouse for learning patterns from data
- Informal definition
  - A neural network architecture organized into many layers
  - For example, 1202 layers He et al. (2016)



# The Role of Depth and Width

# Architectural Considerations

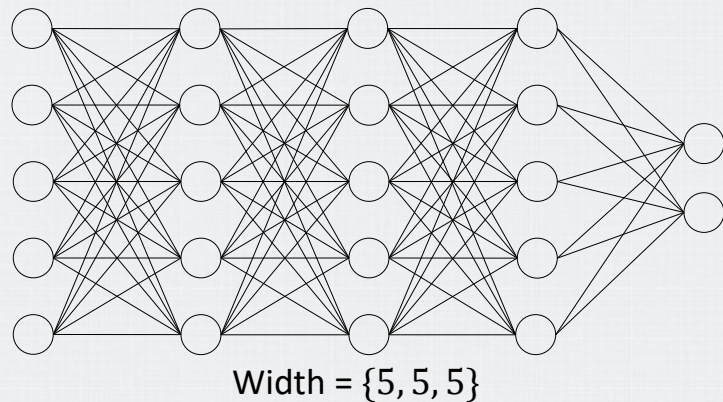
## The Role of Depth and Width

- Two essential aspects of a neural network architecture are:
  - Width  $N$
  - Depth  $L$
- Let  $\mathcal{F}(x, \theta)$  be a neural network parametrized by  $\theta$  that predicts  $\hat{y}$  (i.e.,  $\mathcal{F}(x, \theta) = \hat{y}$ )
  - We can rewrite  $\mathcal{F}(\cdot, \cdot)$  in terms of a set of functions  $f$
  - $\mathcal{F}(x, \theta) \Rightarrow f_L(f_{L-1}(\dots, f_2(f_1(x, \theta_1), \theta_2), \dots, \theta_{L-1}), \theta_L)$

# Width

## The Role of Depth and Width

- The number of neurons in each layer  $l \in L$ 
  - Often, we do not take into account the input and output layers because they depend on the data dimension and task (i.e., number of categories), respectively
- The width defines the **number of parameters**
  - The number of (learnable) weights



# Width

## The Role of Depth and Width

- Typically, widths are in powers of 2

Architecture	Width per Layer
ResNet56 (He et al. , 2016)	16, 32, 64
ResNet50 (He et al., 2016)	64, 128, 256, 512, 1024, 2048
MobileNetV2 (Sandler et al., 2018)	16, 24, 32, 64, 96, 160, 320, 1280
Transformer (Vaswani et al., 2017)	8, 64, 128, 512, 1024, 2048, 4096

He et al. *Deep Residual Learning for Image Recognition*. Computer Vision and Pattern Recognition (CVPR), 2016

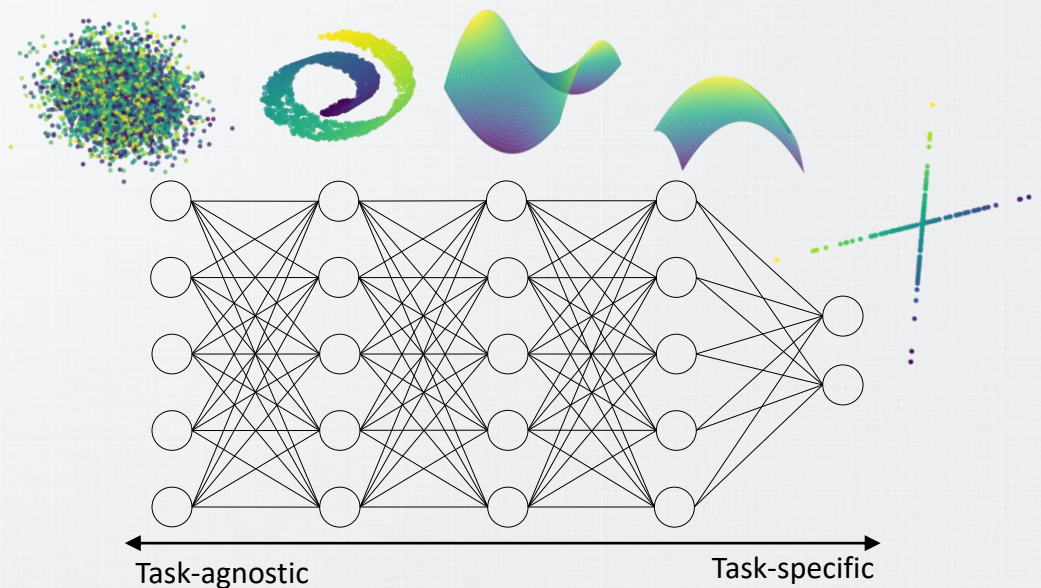
Sandler et al. *MobileNetV2: Inverted Residuals and Linear Bottlenecks*. Computer Vision and Pattern Recognition (CVPR), 2018

Vaswani et al. *Attention Is All You Need*. Neural Information Processing Systems (NeurIPS), 2017

# Depth

## The Role of Depth and Width

- The number of layers composing the network
- Each layer applies a (nonlinear) transformation to the data
  - $f_L(f_{L-1}(\dots, f_2(f_1(x, \theta_1), \theta_2), \dots \theta_{L-1}), \theta_L)$

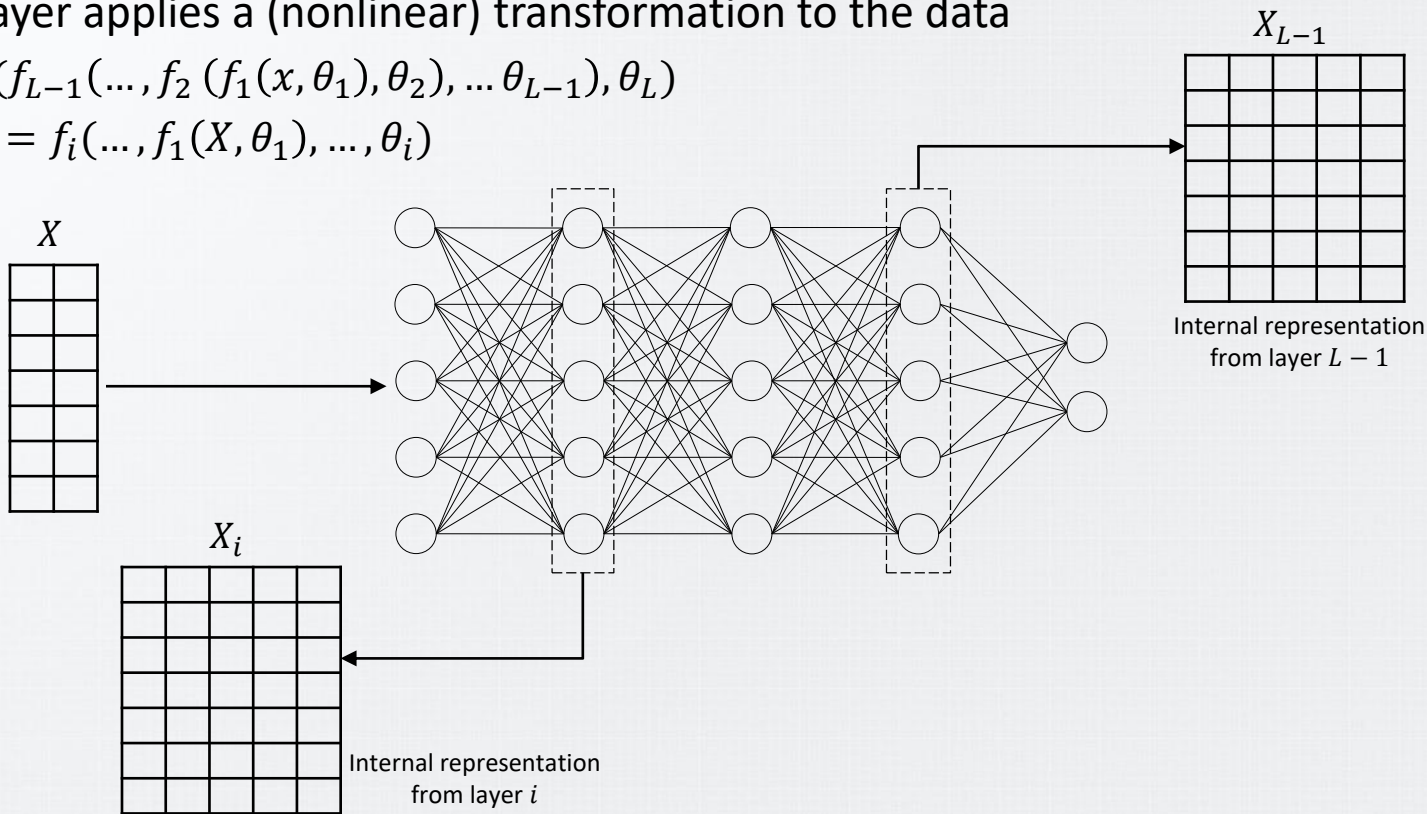




# Internal Representations

## The Role of Depth and Width

- Each layer applies a (nonlinear) transformation to the data
  - $f_L(f_{L-1}(\dots, f_2(f_1(x, \theta_1), \theta_2), \dots, \theta_{L-1}), \theta_L)$
  - $X_i = f_i(\dots, f_1(X, \theta_1), \dots, \theta_i)$

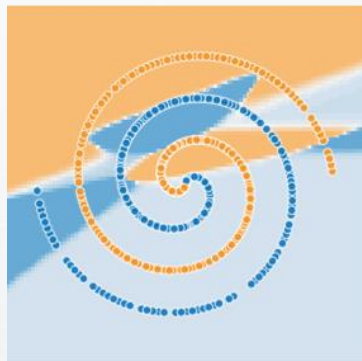




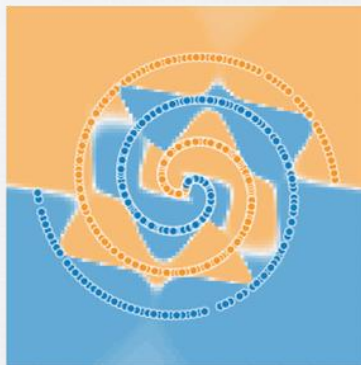
# Width vs. Depth

## The Role of Depth and Width

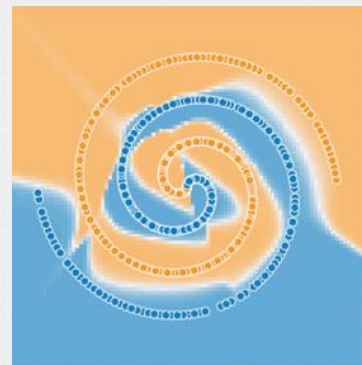
- *We need to go deeper* paradigm (Tan et al., 2019; Han et al., 2020)
- Deep-learning models can extract a rich variety of features from data



Single-layer 2 neurons



Single-layer 8 neuron



Two-layer, 4 neuron each

Tan and Le. *EfficientNet: Rethinking Model Scaling for Convolutional Neural Networks*. International Conference on Machine Learning (ICML), 2019

Han et al. *Model Rubik's Cube: Twisting Resolution, Depth and Width for TinyNets*. Neural Information Processing Systems (NeurIPS), 2020

# Deep Learning Basics

# Capacity

## Deep Learning Basics

- Model's ability to fit a wide variety of functions
- Given sufficient capacity, a model can approximate any continuous function arbitrarily closely
- The total number of hidden units is a measure of the network's capacity
  - Therefore, we can control the capacity by adjusting the number of layers and number of neurons per layer

# Capacity

## Deep Learning Basics

- The consensus is that large (deep and wide) networks lead to better predictive ability and generalization (Tan and Le, 2019; Han et al., 2020)
  - Large architectures have a higher capacity
- Compromise between low- and high-capacity models
  - Low-capacity models may struggle to fit the training set
  - High-capacity models can overfit by memorizing properties of the training set that do not serve them well on the test set

Tan and Le. *EfficientNet: Rethinking Model Scaling for Convolutional Neural Networks*. International Conference on Machine Learning (ICML), 2019

Han et al. *Model Rubik's Cube: Twisting Resolution, Depth and Width for TinyNets*. Neural Information Processing Systems (NeurIPS), 2020

# Overparametrized Regime

## Deep Learning Basics

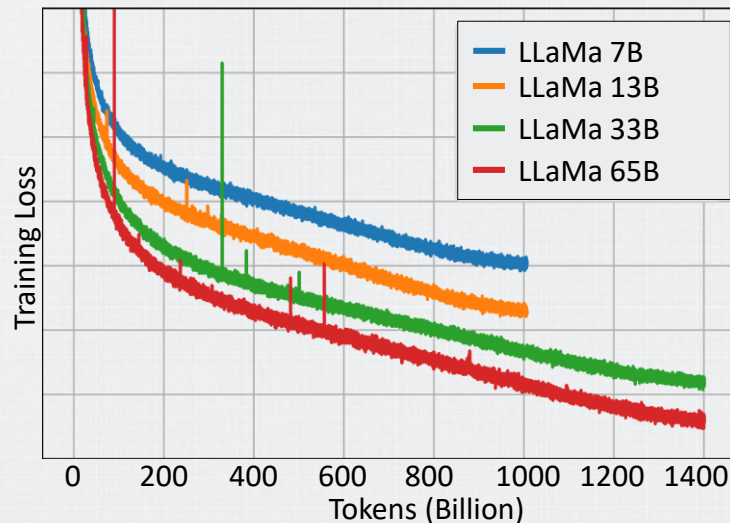
- The number of parameters overwhelms the number of training examples
- Because deep learning models are often highly overparameterized, the empirical risk easily reaches zero
  - **Deep neural networks are capable of memorizing randomly labeled data** (Maini et al., 2023)

Dataset	Models	#Parameters
CIFAR-10 (50K Samples)	ResNet56	861,770
	ResNet110	1,742,762
	NASNet	3,354,858
ImageNet (1.2M Samples)	ResNet50	25,636,712
	ResNet152	60,419,944
	Visual Transformer	$\sim 632 \times 10^6$

# Data Hungry Regime

## Deep Learning Basics

- Deep and Wide networks are data hungry
  - Such networks need a lot of data to learn effectively
  - For example, Vision Transformer (ViT) attains excellent results when pre-trained on JFT-300M Dataset (300 million images)



Dosovitskiy et al. *An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale*. International Conference on Learning Representations (ICLR), 2021

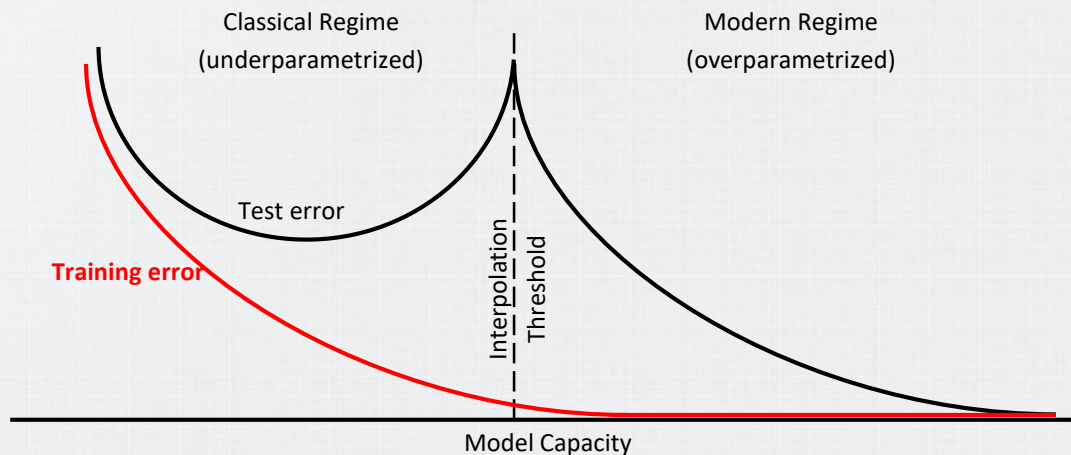
Jayalath et al. *LLaMA: Open and Efficient Foundation Language Models*. ArXiv, 2023



# Deep Double Descent

## Deep Learning Basics

- Double descent (Nakkiran et al., 2020) is a hallmark phenomenon of deep learning
  - It shows the rift between classical learning theory and the generalization capabilities of deep learning systems
  - Double descent is not universal (Jayalath et al. 2023)

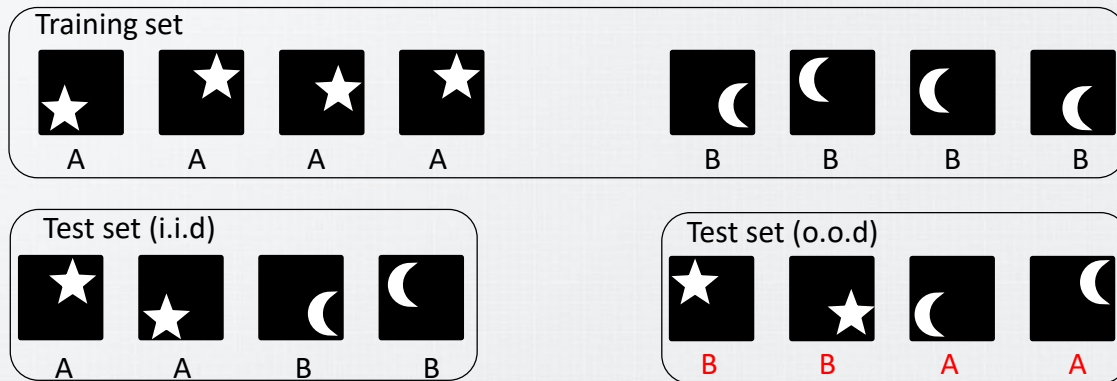




# Shortcut Learning

## Deep Learning Basics

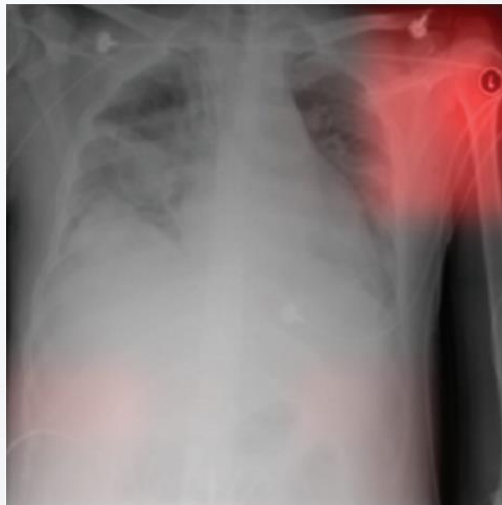
- Shortcuts are features that perform well on standard benchmarks but fail to transfer to more challenging test conditions
  - They arise from dataset shortcut opportunities and discriminative feature learning that fail to generalize as intended
  - Good performance on both training and Independent and Identically Distributed (i.i.d) test sets, but poor generalization to **Out-Of-Distribution** (o.o.d.) inputs



# Shortcut Learning

## Deep Learning Basics

- Shortcut “cheat” features



**Article:** Super Bowl 50

**Paragraph:** “Peython Manning became the first quarterback ever to lead two different teams to multiple Super Bowls. He is also the oldest quarterback ever to play in a Super Bowl at age 39. The past record was held by John Elway, who led the Broncos to victory in Super Bowl XXXIII at age 38 and is currently Denver’s Executive Vice President of Football Operations and General Manager. **Quarterback Jeff Dean had a jersey number 37 in Champ Bowl XXXIV.**” Question: “What is the name of the quarterback who was 38 in Super Bowl XXXIII?”

**Original Prediction:** John Elway

**Prediction under adversary:** Jeff Dean

Task	Recognise pneumonia	Answer question
Problem	Fails on scans from new hospitals	Changes answer if irrelevant information is added
Shortcut	Looks at hospital token, not lung	Only looks at last sentence and ignores context

# Spurious Correlations and Features

## Deep Learning Basics

- Patterns that predict the target in the training data but are irrelevant to the true labeling function (Kirichenko et al. 2023)
- Core features (non-spurious)
  - Features that are truly discriminative to the task
- Deep models can largely rely on simple spurious features to make predictions
  - For example, backgrounds
- Spurious correlations can negatively impact predictive ability
  - On samples where the spurious correlations break

# Spurious Correlations and Features

## Deep Learning Basics

- Target: Bird type
- Spurious feature: Background type



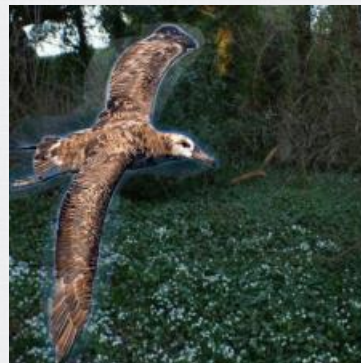
Landbird on Land  
(73%)



Landbird on Water  
(4%)



Waterbird on Water  
(22%)



Waterbird on Land  
(1%)

# Shortcuts vs. Spurious

## Deep Learning Basics

- Shortcuts refer to features easily latched onto by a model
- Spurious refer to features that arise unintentionally in a **poorly constructed dataset**

# Historical Trends in Deep Learning

## Deep Learning Basics

- Deep learning has become more useful as a function of available training
- Deep learning models have grown in size over time
  - Among the factors are the improvements in computer infrastructure (both hardware and software)
- Deep learning has solved increasingly complicated applications with increasing precision over time
  - Protein structure prediction
  - Image captioning and generating
  - Estimating residential solar potential
  - Discovering faster matrix multiplication

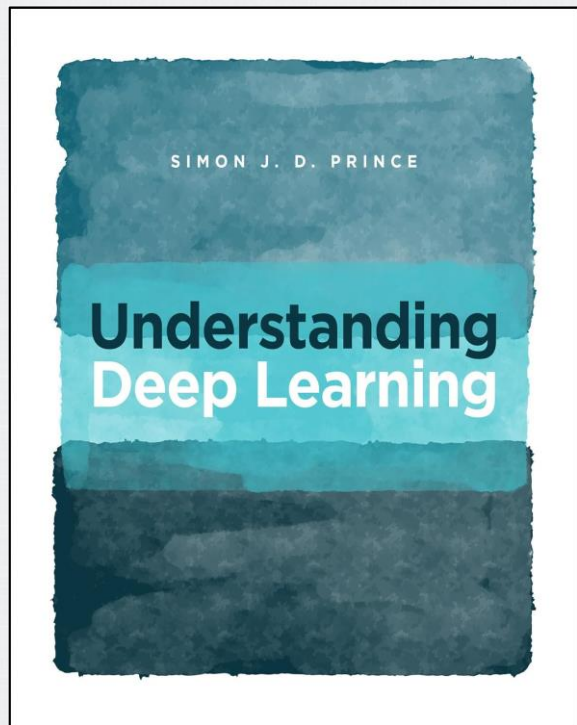


# Bibliography



# Bibliography

- Understanding Deep Learning
  - Chapter 4
    - 4.5 Shallow vs. deep neural networks
    - 4.6 Summary



## Bibliography

- Nakkiran et al. *Deep Double Descent: Where Bigger Models and More Data Hurt*. International Conference on Learning Representations (ICLR), 2020
- d'Ascoli et al. *Double Trouble in Double Descent: Bias and Variance(s) in the Lazy Regime*. International Conference on Machine Learning (ICML), 2020
- Jayalath et al. *No Double Descent in Self-supervised Learning*. International Conference on Learning Representations (ICLR), 2023



**ICLR**  
International Conference On  
Learning Representations



**ICML**  
International Conference  
On Machine Learning

## Bibliography

- Tan and Le. *EfficientNet: Rethinking Model Scaling for Convolutional Neural Networks*. International Conference on Machine Learning (ICML), 2019
- Han et al. *Model Rubik's Cube: Twisting Resolution, Depth and Width for TinyNets*. Neural Information Processing Systems (NeurIPS), 2020
- Liu et al. *Efficient Training of Visual Transformers with Small Datasets*. Neural Information Processing Systems (NeurIPS), 2021

