A Parallel Algorithms Library | N3554

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1 Executive Summary

We introduce a library of algorithms with parallel execution semantics. Some of these algorithms have semantics similar to the existing standard library of sequential algorithms. Some of the algorithms we propose are novel.

We introduce three parallel execution policies for parallel algorithm execution: std::seq, std::par, and std::vec, as well as a facility for vendors to provide non-standard execution policies as extensions. These policy objects may be used to specify how a parallel algorithm should be executed:

```
std::vector<int> vec = ...
// legacy sequential sort
std::sort(vec.begin(), vec.end());
// explicit sequential sort
std::sort(std::seq, vec.begin(), vec.end());
// parallel sort
std::sort(std::par, vec.begin(), vec.end());
// vectorized sort in the current thread
std::sort(std::seq_vec, vec.begin(), vec.end());
// parallel, vectorized sort
std::sort(std::par_vec, vec.begin(), vec.end());
// sort with dynamically-selected execution
size_t threshold = ...
std::execution_policy exec = std::seq;
if(vec.size() > threshold)
  exec = std::par;
std::sort(exec, vec.begin(), vec.end());
```

```
// parallel sort with non-standard implementation-provided execution policies:
std::sort(vectorize_in_this_thread, vec.begin(), vec.end());
std::sort(submit_to_my_thread_pool, vec.begin(), vec.end());
std::sort(execute_on_that_gpu, vec.begin(), vec.end());
std::sort(offload_to_my_fpga, vec.begin(), vec.end());
std::sort(send_this_computation_to_the_cloud, vec.begin(), vec.end());
```

Algorithms invoked with std::seq execute internally in sequential order in the calling thread.

Algorithms invoked with std::par are permitted to execute internally in an unordered fashion in unspecified threads. It is the caller's responsibility to ensure that the invocation does not introduce data races or deadlocks.

Algorithms invoked with std::par_vec are permitted to execute internally in an unordered fashion in unspecified threads. In addition to the restrictions implied by std::par, it is the caller's responsibility to ensure that a std::vec invocation does not throw exceptions or attempt to perform synchronization operations.

Algorithms invoked with std::seq_vec are permitted to execute in an unordered fashion in the current thread. In addition to the restrictions implied by std::par, it is the caller's responsibility to ensure that a std::vec invocation does not throw exceptions or attempt to perform synchronization operations.

Algorithms invoked without an execution policy execute as if they were invoked with std::seq.

An implementation may provide additional execution policies besides std::seq, std::par, std::seq_vec, or std::par_vec.

This proposal is a pure addition to the existing C++ standard library; we do not believe it alters the semantics of any existing functionality.

2 Design Notes and Outstanding Questions

Before introducing the detailed specification of our proposal, we begin by outlining our rationale and by noting that we have identified a number of outstanding questions which require further work to resolve.

2.1 General Considerations

This proposal is motivated by a strong desire to provide a standard model of parallelism enabling performance portability across the broadest possible range of parallel architectures. For this reason, we have exposed parallelism in the most abstract manner possible in order to avoid presuming the existence of a particular parallel machine model. In particular, we have intentionally avoided a specification which would be required to introduce concurrency by creating threads. Additionally, our proposal's semantics ensure that a sequential implementation is always a valid realization of an algorithm invocation.

One limitation of STL-like algorithms is that they encourage the programmer to engage in a style of programming which may be an obstacle to achieving large absolute performance. For example, in situations where a sequential programmer might implement a program using a single for loop, a parallel programmer might express the same program as a sequence of separate gather, for_each, and scatter phases. This is troublesome because in many cases the performance of most STL algorithms is bounded by the speed of memory bandwidth, and the rate of memory bandwidth scaling on parallel architectures is slowing.

One way to ameliorate such problems is to combine the use of parallel algorithms with "fancy" iterators in the style of the Boost Iterator Library. Iterators such as transform_iterator can fuse the effect of

std::transform into another algorithm call, while a permutation_iterator can fuse a scatter or gather. By fusing together several "elemental" operations into a single function consumed by a parallel algorithm, memory bandwidth requirements can be reduced significantly. However, because this idea is orthogonal to the idea of parallel algorithms, this proposal does not include a novel iterator library.

While we are enthusiastic that our library solution to parallelism can offer a portable way to author programs for parallel architectures, we acknowledge that it is only a partial solution for parallelism. We expect our library to coexist in an ecosystem of standard language and library constructs which target parallelism at varying levels of abstraction.

2.2 Naming

Integrating and exposing a new library of parallel algorithms into the existing C++ standard library is an interesting challenge. Because this proposal introduces a large set of novel parallel algorithms with semantics subtly different from their existing sequential counterparts, it is crucial to provide the programmer with the means to safely and unambiguously express her parallelization intent. By the same token, it is important for the library interface to distinguish between the different concurrency guarantees provided by parallel and sequential algorithms. Yet, the interface must be flexible enough such that parallelization does not become burdensome.

The primary means by which the user will interact with the standard parallel algorithms library will be by invoking parallel algorithms by name. Because many parallel algorithm names are already taken by their sequential counterparts (e.g., sort), we require a way to disambiguate these invocations.

After considering a variety of alternative designs, we propose to integrate parallelism into the existing standard algorithm names and distinguish parallelism via parallel execution policies with distinct types. As the code sample in the executive summary demonstrates, we feel that this scheme provides deep integration with the existing standard library.

2.2.1 Rejected Alternative Naming Schemes

Here, we discuss the rationale for rejecting alternative schemes we considered.

A parallel_Name Prefix A simple way to disambiguate parallel algorithms from their sequential versions would be simply to give them new, unique names. Indeed, this is the approach suggested by Intel & Microsoft's earlier paper N3429 and is the one taken in their libraries (i.e. Threading Building Blocks & Parallel Patterns Library, respectively). It is impossible for a human reader or implementation to confuse a call to std::for_each for std::parallel_for_each and vice versa.

While such an approach could be standardized safely, it is unclear that this scheme is scalable from the six or so algorithms provided by TBB & PPL to the large set of algorithms we propose to parallelize. The following two code examples demonstrate issues we anticipate.

By requiring the programmer to choose between two static names, it seems impossible to allow the dynamic selection between the sequential or parallel version of an algorithm without imposing an unnecessary burden on the programmer:

```
std::vector sort_me = ...
size_t parallelization_threshold = ...

if(sort_me.size() > parallelization_threshold)
{
   std::parallel_sort(sort_me.begin(), sort_me.end());
}
```

```
else
{
   std::sort(sort_me.begin(), sort_me.end());
}
```

It is likely that this idiom would become a repetitive burden prone to mistakes.

A similar problem exists for static decisions. Consider a function template which wishes to make a static decision regarding parallelism:

```
template<bool parallelize>
void func(std::vector &vec)
{
   if(parallelize)
   {
      std::parallel_transform(vec.begin(), vec.end(), vec.begin(), f);
      std::parallel_sort(vec.begin(), vec.end());
      std::parallel_unique(vec.begin(), vec.end());
   }
   else
   {
      std::transform(vec.begin(), vec.end(), vec.begin(), f);
      std::sort(vec.begin(), vec.end());
      std::unique(vec.begin(), vec.end());
   }
}
```

This idiom requires the programmer to repeat the function body twice even though the semantics of both implementations are largely identical.

Finally, such a scheme also seems unnecessarily verbose: a sophisticated program composed of repeated calls to a large variety of parallel algorithms would become a noisy repetition of parallel_.

We require a scheme which preserves the safety of unique names but which can also be terse, flexible, and resilient to programmer error. Distinguishing parallel algorithms by execution policy parameters ensures safe disambiguation while also enabling the same terse style shared by the existing algorithms library. The execution policy parameter also provides flexibility and solves the problems of the previous two code examples.

With execution policies, the first dynamic parallelization example becomes:

```
std::vector sort_me = ...
size_t threshold = ...

std::execution_policy exec = std::seq;

if(sort_me.size() > threshold)
{
   exec = std::par;
}

std::sort(exec, sort_me.begin(), sort_me.end());
```

The second static parallelization example becomes:

```
template<ExecutionPolicy>
void func(ExecutionPolicy &exec, std::vector &vec)
{
   std::transform(exec, vec.begin(), vec.end(), vec.begin(), f);
   std::sort(exec, vec.begin(), vec.end());
   std::unique(exec, vec.begin(), vec.end());
}
```

A Nested std::parallel Namespace Another naming scheme would be to provide overloads of the existing standard algorithms in a nested std::parallel namespace. This scheme would avoid many of the problems we identified with distinguishing parallel algorithms by a name prefix. However, we observed that a namespace would introduce ambiguities when algorithms are invoked via argument dependent lookup:

```
void func(std::vector &vec)
{
   transform(vec.begin(), vec.end(), vec.begin(), f);
   sort(vec.begin(), vec.end());
   unique(vec.begin(), vec.end());
}
```

Are the algorithms invoked by func parallel or not? A reader must search for using to be sure.

Finally, we note that nested namespaces inside std:: are unconventional and generally frowned upon.

2.3 Vectorization

In addition to sequential and parallel execution policies, we consider vectorization as a third or fourth possibility. In many architectures, an increasing amount of parallelism is exposed via SIMD units. Naturally, affording parallel programmers a simple, standard means of accessing these resources is desirable. Like std::par_vec execution policy would permit an algorithm invocation to distribute execution across a collection of threads. However, stronger requirements on the behavior of iterator and functor arguments than those permitted by both std::seq and std::par would allow the implementation greater opportunity to exploit vectorization. These requirements would preclude the use of locks and exceptions in functors, for example. An analogous policy, std::seq_vec, would allow vectorization, but isolate it to the current thread.

Whether or not we decide to propose to include a policies for vectorization, we expect our library solution to parallelism to complement other library and language forms of vectorization and parallelism in an eventual standard. Just as the existing sequential std::for_each library function coexists with the sequential for loop language construct, we expect a future C++ standard to offer the programmer a variety of complementary choices along a spectrum of abstraction.

2.4 Execution Policies as Stateful Types

We propose that parallel execution policies have distinct, stateful types:

```
namespace std
{
  class sequential_execution_policy { ... };
  extern const sequential_execution_policy seq;
```

Owing to the variety of parallel architectures we propose that implementations be permitted to define non-standard implementation-defined execution policies as extensions. We expect that users with special knowledge about their standard library implementation and underlying parallel architecture will exploit these policies to achieve higher performance.

We believe this design represents existing practice and have tabulated a list of some examples found in parallel algorithm libraries in production:

Library	Execution Policy Type	Notes
Thrust	thrust::execution_policy	Controls algorithm dispatch to several
		different parallel backend targets
TBB	tbb::auto_partitioner	Selects an automatic partitioning strategy
PPL	concurrency::affinity_partitioner	Improves algorithm cache affinity
Boost.MPI	boost::mpi::communicator	Coordinates MPI ranks such that they can
		cooperate in collective algorithms
Parallel libstdc++	gnu_parallel::_Parallelism	Selects from among several parallel
		execution strategies
C++AMP	concurrency::accelerator_view	Controls algorithm execution locality
Bolt	bolt::cl::control	Controls algorithm command queue, debug
		information, load balancing, etc.

Table 1: Examples of execution policies found in existing libraries

We propose that parallel algorithms receive execution policy objects as their first, instead of last, parameter primarily for two reasons:

- 1. It mirrors the form of std::async's interface.
- 2. The first argument allows the reader to easily note the invocation's parallelization at a glance.
- 3. It preserves the desirable property that algorithms invoked with a lambda look similar to a for loop: $std::for_each(std::par, vec.begin(), vec.end(), [](int &x){ x += 13; });$

An alternative design would place the execution policy last and provide a default value:

```
template<typename Iterator,
         typename ExecutionPolicy>
void algo(Iterator first, Iterator last, ExecutionPolicy &&exec = std::par);
```

This design would collapse the "surface area" of the algorithms API considerably and provide deeper integration into the existing standard algorithms as execution policies become just a final, optional parameter.

Of the libraries we surveyed, Thrust, Boost.MPI, C++ AMP, and Bolt consistently placed execution policy parameters first. PPL tended to place execution policies last, but occasionally accepted execution policy-like hints such as allocators first. TBB and GNU parallel libstdc++ consistently placed execution policies last.

2.4.1 Rejected Execution Policy Designs

However, other designs are possible. An alternative design might require all parallel execution policies to be derived from a common root type, say, std::execution_policy:

```
namespace std
class execution_policy { ... };
class sequential_execution_policy : public execution_policy { ... };
extern const sequential execution policy seq;
class parallel_execution_policy : public execution_policy { ... };
extern const parallel execution policy par;
}
Instead of a template parameter, algorithm interfaces would receive references to std::execution_policy:
```

```
template<typename Iterator>
void algo(std::execution_policy &exec, Iterator first, Iterator last);
```

We rejected this design for a number of reasons:

- Erasing the concrete type of the execution policy may make dispatching the algorithm's implementation more expensive than necessary. We worry that for std::seq invocations across small sequences, the cost of type erasure and algorithm dispatch could dominate the cost of the algorithm.
- Requiring an execution policy's type to derive from a particular root type may make it impractical for implementations to define non-standard policies.

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- Requiring an execution policy's type to derive from a root would preclude treating policies as simple types with value semantics. Inheritance from a common root would require APIs to receive policies by reference or pointer.
- By making the execution policy parameter a concrete type, we would have to commit to either lvalue or rvalue reference semantics for the parameter. With a template parameter, we may support both.
- Erasing the concrete type of the execution policy would require the implementation to instantiate code for all possible policies for each algorithm invocation. Because parallel algorithm implementations are often significantly more complex than their sequential counterparts, this may result in substantial code generation at each call site.

In our survey of existing library designs, we observed that libraries tended not to adopt a common root type for execution policies.

The exception is Thrust, which exposes a common execution policy root type which allows users of the library to create novel execution policies. However, this proposal's design reserves that privilege for the library implementation.

Some libraries accept a variety of execution policy types to allow for algorithm customization, while others require a single concrete type.

For example, both TBB and PPL allow for customization and receive their partitioner arguments as template parameters. Similarly, GNU parallel libstdc++ exposes policies as a forest of inheritance trees. The roots of individual trees are unrelated.

Other libraries do not appear to allow for a variety of policies and instead provide a single concrete policy type. These types do not appear to allow customization through inheritance. Boost.MPI, C++ AMP, and Bolt are examples.

Another alternative design might require all parallel execution policies to have the same type:

```
namespace std
{
    class execution_policy { ... };
    extern const execution_policy seq;
    extern const execution_policy par;
}
in this alternative design, algorithms would receive such policies by value:
template<typename Iterator>
void algo(execution_policy exec, Iterator first, Iterator last);
```

This interface shares most of the same drawbacks as the previous, but allows trafficking execution polices by value.

On the other hand, our proposed algorithm parallel execution policy parameters are similiar in form and spirit to std::async's launch policy parameter, which is a dynamic bitfield. There could be some value in mirroring the convention of std::async's interface in the parallel algorithms library.

2.5 for_each Interface Consistency

Because a parallel version of for_each cannot accumulate state in its function object argument, the interface we propose for for_each returns a copy of its last iterator parameter instead of a copy of its function object:

The rationale for this choice is to avoid discarding iterator information originating in higher-level algorithms implemented through lowerings to for_each.

For example, because for_each returns an iterator, copy may be implemented through a lowering to for_each:

Without for_each's result, copy must be implemented through some other non-standard means, which may be burdensome. While implementations of the standard library could work around this limitation, it would be regrettable to impose this burden on programmers who wish to implement algorithms with a similar iterator interface.

This is also the motivation behind the addition of our proposed for_each_n algorithm, which may implement algorithms such as copy_n, fill_n, etc.

On the other hand, it may be safer to require our parallel for_each to simply return a copy of its function object for consistency's sake.

2.6 Iterator Traversal Requirements

Even though random access to data is a prerequisite for parallel execution, we propose that the interface to parallel algorithms should not impose additional requirements over the existing standard library on the traversal categories of their iterator parameters. In the absense of random access iterators, an implementation may elect to fall back to sequential execution. Alternatively, an implementation may elect to introduce temporary copies of input and output ranges.

2.7 Associativity/Commutativity of Binary Operators

Some parallel algorithms such as reduce place stricter requirements on the binary operations they receive than do analogous sequential algorithms such as accumulate.

In particular, reduce requires its binary operation parameter to be both mathematically associative and commutative in order to accommodate a parallel sum.

To our knowledge, what it means for a binary function object to be associative or commutative is not well-defined by the C++ standard. However, the standard does make such an effort for other mathematical operations, such as strict weak comparison.

For algorithms which require associative binary operators like reduce, should we define concepts such as AssociativeOperation similarly to Compare instead of using BinaryOperation?

Because floating point operations are non-associative, a useful definition of this concept would need to be flexible.

2.8 Machine Width and Space Complexity

Our proposal provides asymptotic upper bounds on work complexity for each parallel algorithm in terms of the input size. Asymptotic guarantees on space complexity would be useful as well, particularly because unlike the typical sequential algorithm, many parallel algorithms require non-trivial temporary storage. The size of such temporary storage requirements often depends on the size of the parallel machine.

Unfortunately, C++ does not currently support a notion of parallel machine size. The closest analogue seems to be the value returned by the function std::thread::hardware_concurrency.

At first glance, relating work complexity to the result of std::thread::hardware_concurrency might seem like a reasonable thing to do. However, we note that the value of this function is merely advisory; it is not guaranteed to correspond to an actual physical machine width. The second more significant problem with interpreting std::thread::hardware_concurrency as machine width is that it presumes a particular machine model of parallelism, i.e., one in which the basic primitive of parallelism is a single thread. While this is a good model for some parallel architectures, it is a poor fit for others. For example, the width of a parallel machine with a significant investment in SIMD vector units would be ill-described in terms of threads.

2.9 Container Support for Parallelism

A parallel algorithms library is a fine starting point for exposing parallelism to programmers in an accessible manner. However, algorithms are only a part of a complete solution for authoring parallel C++ programs. In addition to algorithms, the standard library also provides containers for manipulating data in a safe and convenient manner. While this proposal is focused exclusively on standard algorithms, many of the operations on standard containers such as std::vector also offer rich opportunities for parallelism. As in sequential programs, without support for parallelism in containers, authoring sophisticated parallel programs will become burdensome as programmers will be forced to manage data in an ad hoc fashion.

Should containers such as std::vector be enhanced analogously to the standard algorithms to support parallel execution? We plan to explore the design of such a library in a future paper.

3 Algorithm execution policies

```
Header <execution_policy> synopsis

namespace std
{

template < class T > struct is_execution_policy;

class parallel_execution_policy
{
   public:
      void swap(parallel_execution_policy &other);
```

```
// implementation-defined public members follow
  private:
    // implementation-defined state follows
};
void swap(parallel_execution_policy &a, parallel_execution_policy &b);
template<> struct is_execution_policy<parallel_execution_policy> : true_type {};
extern const parallel_execution_policy par;
class sequential_execution_policy
  public:
    void swap(sequential_execution_policy &other);
    // implementation-defined public members follow
    . . .
  private:
    // implementation-defined state follows
};
void swap(sequential_execution_policy &a, sequential_execution_policy &b);
template<> struct is_execution_policy<sequential_execution_policy> : true_type {};
extern const sequential_execution_policy seq;
class sequential_vector_execution_policy
  public:
    void swap(sequential_vector_execution_policy &other);
    // implementation-defined public members follow
  private:
    // implementation-defined state follows
};
void swap(sequential_vector_execution_policy &a, sequential_vector_execution_policy &b);
template<> struct is_execution_policy<sequential_vector_execution_policy> : true_type {};
extern const sequential vector execution policy seq vec;
class parallel_vector_execution_policy
```

```
{
  public:
    void swap(parallel_vector_execution_policy &other);
    // implementation-defined public members follow
  private:
    // implementation-defined state follows
};
void swap(parallel_vector_execution_policy &a, parallel_vector_execution_policy &b);
template<> struct is_execution_policy<parallel_vector_execution_policy> : true_type {};
extern const parallel_vector_execution_policy par_vec;
// implementation-defined execution policy extensions follow
class execution_policy
  public:
    template < class Execution Policy >
    execution_policy(const ExecutionPolicy &exec,
                      typename enable_if<</pre>
                        is_execution_policy<ExecutionPolicy>::value
                      >::type * = 0);
    template < class Execution Policy >
    typename enable_if<</pre>
      is_execution_policy<ExecutionPolicy>::value,
      execution_policy &
    >::type
    operator=(const ExecutionPolicy &exec);
    void swap(execution_policy &other);
    // obtains the typeid of the stored target
    const type_info& target_type() const;
    // obtains a pointer to the stored target
    template<class ExecutionPolicy>
    typename enable_if<</pre>
      is_execution_policy<ExecutionPolicy>::value,
      ExecutionPolicy *
    >::type
    target();
    template<class ExecutionPolicy>
    typename enable_if<</pre>
      is_execution_policy<ExecutionPolicy>::value,
      const ExecutionPolicy *
```

```
>::type
  target() const;

private:
    ...
};

void swap(execution_policy &a, execution_policy &b);
}
```

4 Class template is_execution_policy

```
namespace std {
  template<class T> struct is_execution_policy
    : integral_constant<bool, see below> { };
}
```

- 1. is_execution_policy can be used to detect parallel execution policies for the purpose of excluding parallel algorithm signatures from otherwise ambiguous overload resolution participation.
- 2. If T is the type of a standard or implementation-defined non-standard execution policy, is_execution_policy<T> shall be publicly derived from integral_constant<bool,true>, otherwise from integral_constant<bool,false>.
- 3. The effect of specializing is_execution_policy for a type which is not defined by library is unspecified. [Note: This provision reserves the privilege of creating non-standard execution policies to the library implementation. end note.]

5 Class execution_policy

1. Objects of type execution_policy may be used to dynamically control the invocation of parallel algorithms.

6 Execution Policies and Their Effect on Algorithm Execution

Execution policies describe the manner in which the algorithms apply the user-provided function objects.

- 1. The applications of the function objects in the algorithms invoked with the sequential_execution_policy execute in sequential order in the calling thread.
- 2. The applications of the function objects in the algorithms invoked with the parallel_execution_policy are permitted to execute in an unordered fashion in unspecified threads, or indeterminately sequenced if executed on one thread. [Note: It is the caller's responsibility to ensure correctness, for example that the invocation does not introduce data races or deadlocks. end note] [Example:

```
int a[] = {0,1};
std::vector<int> v(2);
std::for_each(std::par, std::begin(a), std::end(a), [&](int i) {
    v[i] = i*2+1;
});
```

The program above has a data race because of the unsynchronized access to the container v — end example] [Example:

```
std::atomic<int> x = 0;
int a[] = {1,2};
std::for_each(std::par , std::begin(a), std::end(a), [](int n) {
    x.fetch_add( 1 , std::memory_order_relaxed );
    // spin wait for another iteration to change the value of x
    while( x.load( std::memory_order_relaxed ) == 1 )
    ;
});
```

The above example depends on the order of execution of the iterations, and is therefore undefined (may deadlock). — end example] [Example:

```
int x;
std::mutex m;
int a[] = {1,2};
std::for_each( std::par , std::begin(a), std::end(a), [&](int) {
    m.lock();
    ++x;
    m.unlock();
});
```

The above example synchronizes access to object \mathbf{x} ensuring that it is incremented correctly. — end example]

3. The applications of the function objects in the algorithms invoked with vector_execution_policy are permitted to execute in an unordered fashion in unspecified threads, or unsequenced if executed on one thread. [Note: as a consequence, function objects governed by the vector_execution_policy policy must not synchronize with each other. Specifically, they must not acquire locks. — end note] [Example:

```
int x;
std::mutex m;
int a[] = {1,2};
std::for_each( std::par_vec , std::begin(a), std::end(a), [&](int) {
    m.lock();
    ++x;
    m.unlock();
});
```

The above program is invalid because the applications of the function object are not guaranteed to run on different threads. [Note: the application of the function object may result in two consecutive calls to ${\tt m.lock}$ on the same thread, which may deadlock — end note] — end example]

[Note: The semantics of a parallel_execution_policy or vector_execution_policy invocation allow the implementation to fall back to sequential execution if the system cannot parallelize an algorithm invocation due to lack of resources. - end note.]

4. An implementation may provide additional execution policy types besides parallel_execution_policy, sequential_execution_policy, vector_execution_policy, or execution_policy. Objects of type execution_policy must be constructible and assignable from any additional non-standard execution policy provided by the implementation.

- 5. Algorithms invoked with an execution policy argument of type execution_policy execute internally as if invoked with a sequential_execution_policy, a parallel_execution_policy, or a non-standard implementation-defined execution policy depending on the dynamic value of the execution_policy object.
- 6. Algorithms invoked without an execution policy argument execute as if they were invoked with an execution policy argument of type sequential_execution_policy.
- 7. Implementations of sequential_execution_policy, parallel_execution_policy, and vector_execution_policy are permitted to provide additional non-standard data and function members.

[Note: This provision permits objects of these types to be stateful. – end note.]

7 Example Usage of execution_policy:

```
std::execution_policy allows us to dynamically control algorithm execution:
std::vector<float> sort_me = ...
std::execution_policy exec = std::seq;
if(sort_me.size() > threshold)
  exec = std::par;
std::sort(exec, sort_me.begin(), sort_me.end());
std::execution_policy allows us to pass execution policies through a binary interface:
void some_api(std::execution_policy exec, int arg1, double arg2);
void foo()
  // call some_api with std::par
  some_api(std::par, 7, 3.14);
Retrieving the dynamic value from an std::execution policy an API similar to std::function:
void some_api(std::execution_policy exec, int arg1, double arg2)
{
  if(exec.target_type() == typeid(std::seq))
    std::cout << "Received a sequential policy" << std::endl;</pre>
    std::sequential_execution_policy *exec_ptr = exec.target<std::sequential_execution_policy>();
  }
  else if(exec.target_type() == typeid(std::par))
    std::cout << "Received a parallel policy" << std::endl;</pre>
    std::parallel execution policy *exec ptr = exec.target<std::parallel execution policy>();
```

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}

```
else if(exec.target_type() == typeid(std::vec))
{
   std::cout << "Received a vector policy" << std::endl;
   std::vector_execution_policy *exec_ptr = exec.target<std::vector_execution_policy>();
}
else
{
   std::cout << "Received some other kind of policy" << std::eedl;
}</pre>
```

In the current design, std::execution_policy::target returns a pointer similar to std::function::target. However, std::execution_policy's current design precludes an "empty" or invalid state. An alternative design might require std::execution_policy::target to return a reference and throw an exception in the case of type mismatch.

8 Reporting Exceptions

8.1 Exception behavior of functions launched through a std::sequential_execution_policy argument

An algorithm invoked with a sequential execution policy reports exceptional behavior in the same manner as the legacy algorithms.

8.2 Exception behavior of functions launched through a std::parallel_execution_policy argument

An algorithm invoked with a parallel execution policy may report exceptional behavior by throwing an exception.

A parallel algorithm may report exceptional behavior to the caller by throwing one of three exception types:

- If temporary memory resources are required by the algorithm and none are available, the algorithm may throw std::bad_alloc.
- If parallel resources are required by the algorithm and none are available, the algorithm may throw std::system_error.
- If one or more uncaught exceptions are thrown for any other reason during the execution of the algorithm:
 - The exception is collected in an exception_list associated with the algorithm's invocation.
 - If the exception_list associated with the algorithm's invocation is non-empty, it is thrown once all tasks have terminated.

Note that these guarantees imply that all exceptions thrown during the execution of the algorithm are communicated to the caller. It is unspecified whether an algorithm implementation will "forge ahead" after encountering and capturing a user exception.

8.3 Exception behavior of functions launched through a std::vector_execution_policy argument

If program-defined code invoked by an algorithm invoked with a vector execution policy throws an exception, the behavior is undefined.

Header <exception> synopsis

```
namespace std {
  class exception_list
  {
    public:
      typedef exception_ptr
                                 value_type;
      typedef const value type& reference;
      typedef const value_type& const_reference;
      typedef size_t
                                 size_type;
      typedef unspecified
                                 iterator;
      typedef unspecified
                                 const_iterator;
      size_t size() const;
      iterator begin() const;
      iterator end() const;
      const char *what() const;
    private:
      std::list<exception_ptr> exceptions_; // exposition only
  };
}
```

9 Interaction with Threads

For algorithms invoked with a sequential execution policy argument:

- 1. Program-defined functions arising from the manipulation of algorithm parameters (e.g., functors, iterators, etc.) are invoked in the calling thread of execution.
- 2. Program-defined functions arising from the manipulation of algorithm parameters are invoked in sequential order.
- 3. Algorithms synchronize with the caller.

For algorithms invoked with a parallel_execution_policy argument:

- 1. It is the responsibility of the algorithm implementation to allocate temporary storage in a thread-safe manner.
 - [Note: One way to guarantee this is to allocate all dynamic storage in the calling thread before concurrent computation begins. end note.]
- 2. It is unspecified in which thread(s) program-defined functions arising from the manipulation of algorithm parameters are invoked.

- 3. It is unspecified in which order program-defined functions arising from the manipulation of algorithm parameters are invoked.
- 4. Algorithm invocations synchronize with the caller.
- 5. Algorithms make no guarantee of forward progress.
 - [Note: Program-defined code executed by an algorithm's invocation of a functor or iterator dereference cannot wait on the result of another invocation. end note.]
- 6. An algorithm's behavior is undefined if program-defined code executed through algorithm parameter manipulation may introduce a data race.

For algorithms invoked with a sequential_vector_execution_policy or parallel_vector_execution_policy argument:

- 1. A vectorizable algorithm invocation inherits all the previous restrictions of parallel_execution_policy.
- 2. An algorithm's behavior is undefined if program-defined code executed through algorithm parameter manipulation throws an exception.
- 3. An algorithm's behavior is undefined if program-defined code executed through algorithm parameter mainpulation attempts to synchronize.

10 Proposed Additions to Algorithms and Algorithm-like functions

Here we enumerate the additions we propose to the standard algorithms library.

We propose to overload an existing algorithm name when the existing C++11 specification allows sufficient discretion for a parallel implementation (e.g., transform) or when we feel no other name would be appropriate (e.g., for_each, inner_product).

We propose to introduce a new algorithm name when the existing analogous algorithm name implies a sequential implementation (e.g., accumulate versus reduce).

11 Overloads of Existing Algorithms Introduced by this Proposal

11.1 Existing specialized algorithms from <memory>

11.1.1 Header <memory> synopsis

```
const T& x);
  template < class Execution Policy,
            class ForwardIterator, class Size>
    ForwardIterator uninitialized_fill_n(ExecutionPolicy &&exec,
                                            ForwardIterator first, Size n,
                                            const T& x);
}
11.1.2 uninitialized_copy [uninitialized.copy]
template < class Execution Policy,
          class InputIterator, class ForwardIterator>
  ForwardIterator uninitialized_copy(ExecutionPolicy &&exec,
                                        InputIterator first, InputIterator last,
                                        ForwardIterator result);
template<class ExecutionPolicy,</pre>
          class InputIterator, class Size, class ForwardIterator>
  ForwardIterator uninitialized_copy_n(ExecutionPolicy &&exec,
                                          InputIterator first, Size n,
                                          ForwardIterator result);
  1. Effects: Copy constructs the element referenced by every iterator i in the range [result,result +
     (last - first)) as if by the expression
     ::new (static cast<void*>(&*i))
         typename iterator_traits<ForwardIterator>::value_type(*(first + (i - result)))
     The execution of the algorithm is parallelized as determined by exec.
  2. Returns: result + (last - first).
  3. Complexity: O(last - first).
  4. Remarks: Neither signature shall participate in overload resolution if
     is_execution_policy<ExecutionPolicy>::value is false.
template < class Execution Policy,
          class InputIterator, class Size, class ForwardIterator>
  ForwardIterator uninitialized_copy_n(ExecutionPolicy &&exec,
                                          InputIterator first, Size n,
                                          ForwardIterator result);
  1. Effects: Copy constructs the element referenced by every iterator i in the range [result, result + n)
     as if by the expression
     ::new (static_cast<void*>(&*i))
         typename iterator_traits<ForwardIterator>::value_type(*(first + (i - result)))
The execution of the algorithm is parallelized as determined by exec.
  2. Returns: result + n.
  3. Complexity: O(n).
  4. Remarks: The signature shall not participate in overload resolution if
     is_execution_policy<ExecutionPolicy>::value is false.
```

11.1.3 uninitialized_fill [uninitialized.fill]

1. Effects: Copy constructs the element referenced by every iterator i in the range [first,last) as if by the expression

```
::new (static_cast<void*>(&*i))
    typename iterator_traits<ForwardIterator>::value_type(x)
```

The execution of the algorithm is parallelized as determined by exec.

- 2. Complexity: O(last first).
- 3. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.1.4 uninitialized_fill_n [uninitialized.fill.n]

1. *Effects:* Copy constructs the element referenced by every iterator i in the range [first,first + n) as if by the expression

```
::new (static_cast<void*>(&*i))
    typename iterator_traits<ForwardIterator>::value_type(x)
```

The execution of the algorithm is parallelized as determined by exec.

- 2. Returns: first + n.
- 3. *Complexity:* O(n).
- 4. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2 Existing function Templates from <algorithm>

11.2.1 Header <algorithm> synopsis

```
bool all_of(ExecutionPolicy &&exec,
              InputIterator first, InputIterator last, Predicate pred);
template < class Execution Policy,
         class InputIterator, class Predicate>
 bool any_of(ExecutionPolicy &&exec,
              InputIterator first, InputIterator last, Predicate pred);
template < class Execution Policy,
         class InputIterator, class Predicate>
 bool none_of(ExecutionPolicy &&exec,
               InputIterator first, InputIterator last, Predicate pred);
template < class Execution Policy,
         class InputIterator, class T>
  InputIterator find(ExecutionPolicy &&exec,
                     InputIterator first, InputIterator last,
                     const T& value);
template < class Execution Policy,
         class InputIterator, class Predicate>
  InputIterator find_if(ExecutionPolicy &&exec,
                        InputIterator first, InputIterator last,
                        Predicate pred);
template<class ExecutionPolicy,</pre>
         class InputIterator, class Predicate>
  InputIterator find_if_not(ExecutionPolicy &&exec,
                            InputIterator first, InputIterator last,
                            Predicate pred);
template<class ExecutionPolicy,</pre>
         class ForwardIterator1, class ForwardIterator2>
  ForwardIterator1
    find_end(ExecutionPolicy &exec,
             ForwardIterator1 first1, ForwardIterator1 last1,
             ForwardIterator2 first2, ForwardIterator2 last2);
template < class Execution Policy,
         class ForwardIterator1, class ForwardIterator2,
         class BinaryPredicate>
 ForwardIterator1
    find_end(ExecutionPolicy &&exec,
             ForwardIterator1 first1, ForwardIterator1 last1,
             ForwardIterator2 first2, ForwardIterator2 last2,
             BinaryPredicate pred);
template < class Execution Policy,
         class InputIterator, class ForwardIterator>
  InputIterator
    find_first_of(ExecutionPolicy &&exec,
                  InputIterator first1, InputIterator last1,
                  ForwardIterator first2, ForwardIterator last2);
template < class Execution Policy,
         class InputIterator, class ForwardIterator,
         class BinaryPredicate>
  InputIterator
    find_first_of(ExecutionPolicy &&exec,
                  InputIterator first1, InputIterator last1,
```

```
ForwardIterator first2, ForwardIterator last2,
                  BinaryPredicate pred);
template < class Execution Policy,
         class ForwardIterator>
 ForwardIterator adjacent find(ExecutionPolicy &&exec, ForwardIterator first, ForwardIterator last);
template < class Execution Policy,
         class ForwardIterator, class BinaryPredicate>
 ForwardIterator adjacent_find(ExecutionPolicy &&exec, ForwardIterator first, ForwardIterator last,
                                 BinaryPredicate pred);
template < class Execution Policy,
         class InputIterator, class EqualityComparable>
  typename iterator_traits<InputIterator>::difference_type
    count(ExecutionPolicy &&exec,
          InputIterator first, InputIterator last, const EqualityComparable &value);
template < class Execution Policy,
         class InputIterator, class Predicate>
  typename iterator_traits<InputIterator>::difference_type
    count if (ExecutionPolicy &&exec,
             InputIterator first, InputIterator last, Predicate pred);
template<class ExecutionPolicy,</pre>
         class InputIterator1, class InputIterator2>
 pair<InputIterator1,InputIterator2>
    mismatch(ExecutionPolicy &&exec,
             InputIterator1 first1, InputIterator1 last1,
             InputIterator2 first2);
template < class Execution Policy,
         class InputIterator1, class InputIterator2, class BinaryPredicate>
 pair<InputIterator1,InputIterator2>
    mismatch(ExecutionPolicy &&exec,
             InputIterator1 first1, InputIterator1 last1,
             InputIterator2 first2, BinaryPredicate pred);
template<class ExecutionPolicy,</pre>
         class InputIterator1, class InputIterator2>
 bool equal(ExecutionPolicy &&exec,
             InputIterator1 first1, InputIterator1 last1,
             InputIterator2 first2);
template < class Execution Policy,
         class InputIterator1, class InputIterator2, class BinaryPredicate>
 bool equal(ExecutionPolicy &&exec,
             InputIterator1 first1, InputIterator1 last1,
             InputIterator2 first2, BinaryPredicate pred);
// modifying sequence operations:
// copy:
template<class ExecutionPolicy,</pre>
         class InputIterator, class OutputIterator>
  OutputIterator copy(ExecutionPolicy &&exec,
                      InputIterator first, InputIterator last,
                      OutputIterator result);
```

```
template < class Execution Policy,
         class InputIterator, class Size, class OutputIterator>
  OutputIterator copy_n(ExecutionPolicy &&exec,
                         InputIterator first, Size n,
                         OutputIterator result);
template < class Execution Policy,
         class InputIterator, class OutputIterator, class Predicate>
 OutputIterator
    copy_if(ExecutionPolicy &&exec,
            InputIterator first, InputIterator last,
            OutputIterator result, Predicate pred);
// move:
template<class ExecutionPolicy,</pre>
         class InputIterator, class OutputIterator>
 OutputIterator
    move(ExecutionPolicy &&exec,
         InputIterator first, InputIterator last,
         OutputIterator result);
// swap:
template < class Execution Policy,
         class ForwardIterator1, class ForwardIterator2>
 ForwardIterator2
    swap_ranges(ExecutionPolicy &&exec,
                ForwardIterator1 first1, ForwardIterator1 last1,
                ForwardIterator1 first2);
template < class Execution Policy,
         class InputIterator, class OutputIterator,
         class UnaryOperation>
  OutputIterator transform(ExecutionPolicy &&exec,
                            InputIterator first, InputIterator last,
                            OutputIterator result, UnaryOperation op);
template<class ExecutionPolicy,</pre>
         class InputIterator1, class InputIterator2, class OutputIterator,
         class BinaryOperation>
 OutputIterator
    transform(ExecutionPolicy &&exec,
              InputIterator1 first1, InputIterator1 last1,
              InputIterator2 first2, OutputIterator result,
              BinaryOperation binary_op);
template<class ExecutionPolicy,</pre>
         class ForwardIterator, class T>
  void replace(ExecutionPolicy &&exec,
               ForwardIterator first, ForwardIterator last,
               const T& old_value, const T& new_value);
template < class Execution Policy,
         class ForwardIterator, class Predicate, class T>
 void replace_if(ExecutionPolicy &&exec,
                  ForwardIterator first, ForwardIterator last,
                  Predicate pred, const T& new value);
```

```
template < class Execution Policy,
         class InputIterator, class OutputIterator, class T>
 OutputIterator
    replace_copy(ExecutionPolicy &&exec,
                 ForwardIterator first, ForwardIterator last,
                 OutputIterator result,
                 const T& old_value, const T& new_value);
template < class Execution Policy,
         class InputIterator, class OutputIterator, class Predicate, class T>
 OutputIterator
    replace_copy_if(ExecutionPolicy &&exec,
                    InputIterator first, InputIterator last,
                    OutputIterator result,
template < class Execution Policy,
         class ForwardIterator, class T>
 void fill(ExecutionPolicy &&exec,
            ForwardIterator first, ForwardIterator last, const T& value);
template < class Execution Policy,
         class OutputIterator, class Size, class T>
 void fill_n(ExecutionPolicy &&exec,
              OutputIterator first, Size n, const T& value);
template < class Execution Policy,
         class ForwardIterator, class Generator>
 void generate(ExecutionPolicy &&exec,
                ForwardIterator first, ForwardIterator last, Generator gen);
template<class ExecutionPolicy,</pre>
         class OutputIterator, class Size, class Generator>
 OutputIterator generate_n(ExecutionPolicy &&exec,
                            OutputIterator first, Size n, Generator gen);
template < class Execution Policy,
         class ForwardIterator, class T>
 ForwardIterator remove(ExecutionPolicy &&exec,
                         ForwardIterator first, ForwardIterator last, const T& value);
template < class Execution Policy,
         class ForwardIterator, class Predicate>
 ForwardIterator remove_if(ExecutionPolicy &&exec,
                            ForwardIterator first, ForwardIterator last, Predicate pred);
template < class Execution Policy,
         class InputIterator, class OutputIterator, class T>
 OutputIterator
    remove_copy(ExecutionPolicy &&exec,
                InputIterator first, InputIterator last,
                OutputIterator result, const T& value);
template < class Execution Policy,
         class InputIterator, class OutputIterator, class Predicate>
  OutputIterator
    remove_copy_if(ExecutionPolicy &&exec,
                   InputIterator first, InputIterator last,
                   OutputIterator result, Predicate pred);
template < class Execution Policy,
```

```
class ForwardIterator>
 ForwardIterator unique(ExecutionPolicy &&exec,
                         ForwardIterator first, ForwardIterator last);
template < class Execution Policy,
         class ForwardIterator, typename BinaryPredicate>
 ForwardIterator unique(ExecutionPolicy &&exec,
                         ForwardIterator first, ForwardIterator last
                         BinaryPredicate pred);
template < class Execution Policy,
         class InputIterator, class OutputIterator>
  OutputIterator
    unique_copy(ExecutionPolicy &&exec,
                InputIterator first, InputIterator last,
                OutputIterator result);
template < class Execution Policy,
         class InputIterator, class OutputIterator, class BinaryPredicate>
 OutputIterator
    unique_copy(ExecutionPolicy &&exec,
                InputIterator first, InputIterator last,
                OutputIterator result, BinaryPredicate pred);
template < class Execution Policy,
         class BidirectionalIterator>
 void reverse(ExecutionPolicy &&exec,
               BidirectionalIterator first, BidirectionalIterator last);
template < class Execution Policy,
         class BidirectionalIterator, class OutputIterator>
 OutputIterator
    reverse_copy(ExecutionPolicy &&exec,
                 BidirectionalIterator first,
                 BidirectionalIterator last, OutputIterator result);
template < class Execution Policy,
         class ForwardIterator>
 ForwardIterator rotate(ExecutionPolicy &&exec,
                         ForwardIterator first, ForwardIterator middle,
                         ForwardIterator last);
template<class ExecutionPolicy,</pre>
         class ForwardIterator, class OutputIterator>
 OutputIterator
    rotate_copy(ExecutionPolicy &&exec,
                ForwardIterator first, ForwardIterator middle,
                ForwardIterator last, OutputIterator result);
// partitions:
template < class Execution Policy,
         class InputIterator, class Predicate>
  bool is_partitioned(ExecutionPolicy &&exec,
                      InputIterator first, InputIterator last, Predicate pred);
template < class Execution Policy,
         class ForwardIterator, class Predicate>
 ForwardIterator
```

```
partition(ExecutionPolicy &&exec,
              ForwardIterator first,
              ForwardIterator last, Predicate pred);
template < class Execution Policy,
         class BidirectionalIterator, class Predicate>
 BidirectionalIterator
    stable_partition(ExecutionPolicy &&exec,
                     BidirectionalIterator first,
                     BidirectionalIterator last, Predicate pred);
template < class Execution Policy,
         class InputIterator, class OutputIterator1,
         class OutputIterator2, class Predicate>
pair<OutputIterator1, OutputIterator2>
partition_copy(ExecutionPolicy &&exec,
               InputIterator first, InputIterator last,
               OutputIterator1 out_true, OutputIterator2 out_false,
               Predicate pred);
template < class Execution Policy,
         class ForwardIterator, class Predicate>
 ForwardIterator partition_point(ExecutionPolicy &&exec,
                                   ForwardIterator first,
                                   ForwardIterator last,
                                   Predicate pred);
// sorting and related operations:
// sorting:
template < class Execution Policy,
         class RandomAccessIterator>
  void sort(ExecutionPolicy &&exec,
            RandomAccessIterator first, RandomAccessIterator last);
template < class Execution Policy,
         class RandomAccessIterator, class Compare>
  void sort(ExecutionPolicy &&exec,
            RandomAccessIterator first, RandomAccessIterator last, Compare comp);
template < class Execution Policy,
         class RandomAccessIterator>
 void stable_sort(ExecutionPolicy &&exec,
                   RandomAccessIterator first, RandomAccessIterator last);
template<class ExecutionPolicy,</pre>
         class RandomAccessIterator, class Compare>
  void stable_sort(ExecutionPolicy &&exec,
                   RandomAccessIterator first, RandomAccessIterator last,
                   Compare comp);
template < class Execution Policy,
         class RandomAccessIterator>
  void partial_sort(ExecutionPolicy &&exec,
                    RandomAccessIterator first,
                    RandomAccessIterator middle,
                    RandomAccessIterator last);
template < class Execution Policy,
         class RandomAccessIterator, class Compare>
  void partial sort(ExecutionPolicy &&exec,
```

```
RandomAccessIterator first,
                    RandomAccessIterator middle,
                    RandomAccessIterator last,
                    Compare comp);
template<class ExecutionPolicy,</pre>
         class InputIterator, class RandomAccessIterator>
 RandomAccessIterator
    partial_sort_copy(ExecutionPolicy &&exec,
                       InputIterator first, InputIterator last,
                      RandomAccessIterator result_first,
                      RandomAccessIterator result_last);
template < class Execution Policy,
         class InputIterator, class RandomAccessIterator,
         class Compare>
 RandomAccessIterator
    partial_sort_copy(ExecutionPolicy &&exec,
                       InputIterator first, InputIterator last,
                       RandomAccessIterator result first,
                      RandomAccessIterator result_last,
                       Compare comp);
template<class ExecutionPolicy,</pre>
         class ForwardIterator>
 bool is sorted(ExecutionPolicy &&exec,
                 ForwardIterator first, ForwardIterator last);
template<class ExecutionPolicy,</pre>
         class ForwardIterator, class Compare>
 bool is_sorted(ExecutionPolicy &&exec,
                 ForwardIterator first, ForwardIterator last,
                 Compare comp);
template < class Execution Policy,
         class ForwardIterator>
  ForwardIterator is_sorted_until(ExecutionPolicy &&exec,
                                   ForwardIterator first, ForwardIterator last);
template < class Execution Policy,
         class ForwardIterator, class Compare>
 ForwardIterator is_sorted_until(ExecutionPolicy &&exec,
                                   ForwardIterator first, ForwardIterator last,
                                   Compare comp);
template < class Execution Policy,
         class RandomAccessIterator>
 void nth element (ExecutionPolicy &&exec,
                   {\tt RandomAccessIterator\ first,\ RandomAccessIterator\ nth,}
                   RandomAccessIterator last);
template < class Execution Policy,
         class RandomAccessIterator, class Compare>
  void nth_element(ExecutionPolicy &&exec,
                   RandomAccessIterator first, RandomAccessIterator nth,
                   RandomAccessIterator last, Compare comp);
// binary search
template < class Execution Policy,
         class ForwardIterator, class T>
```

```
ForwardIterator
    lower_bound(ExecutionPolicy &&exec,
                ForwardIterator first, ForwardIterator last,
                const T& value);
template < class Execution Policy,
         class ForwardIterator, class T, class Compare>
 ForwardIterator
    lower_bound(ExecutionPolicy &&exec,
                ForwardIterator first, ForwardIterator last,
                const T& value, Compare comp);
template < class Execution Policy,
         class ForwardIterator, class T>
 ForwardIterator
    upper_bound(ExecutionPolicy &&exec,
                ForwardIterator first, ForwardIterator last,
                const T& value);
template < class Execution Policy,
         class ForwardIterator, class T, class Compare>
 ForwardIterator
    upper_bound(ExecutionPolicy &&exec,
                ForwardIterator first, ForwardIterator last,
                const T& value, Compare comp);
template < class Execution Policy,
         class ForwardIterator, class T>
 pair<ForwardIterator, ForwardIterator>
    equal_range(ExecutionPolicy &&exec,
                ForwardIterator first,
                ForwardIterator last, const T& value);
template < class Execution Policy,
         class ForwardIterator, class T, class Compare>
 pair<ForwardIterator, ForwardIterator>
    equal_range(ExecutionPolicy &&exec,
                ForwardIterator first,
                ForwardIterator last, const T& value,
                Compare comp);
template<class ExecutionPolicy,</pre>
         class ForwardIterator, class T>
 bool binary_search(ExecutionPolicy &&exec,
                     ForwardIterator first, ForwardIterator last,
                     const T& value);
template < class Execution Policy,
         class ForwardIterator, class T, class Compare>
 bool binary_search(ExecutionPolicy &&exec,
                     ForwardIterator first, ForwardIterator last,
                     const T& value, Compare comp);
// merge:
template<class ExecutionPolicy,</pre>
         class InputIterator1, class InputIterator2,
         class OutputIterator>
  OutputIterator
```

```
merge(ExecutionPolicy &&exec,
          InputIterator1 first1, InputIterator1 last1,
          InputIterator2 first2, InputIterator2 last2,
          OutputIterator result);
template<class ExecutionPolicy,</pre>
         class InputIterator1, class InputIterator2,
         class OutputIterator, class Compare>
  OutputIterator
    merge(ExecutionPolicy &&exec,
          InputIterator1 first1, InputIterator1 last1,
          InputIterator2 first2, InputIterator2 last2,
          OutputIterator result, Compare comp);
template < class Execution Policy,
         class BidirectionalIterator>
  void inplace_merge(ExecutionPolicy &&exec,
                     BidirectionalIterator first,
                     BidirectionalIterator middle,
                     BidirectionalIterator last);
template < class Execution Policy,
         class BidirectionalIterator,
         class Compare>
 void inplace_merge(ExecutionPolicy &&exec,
                     BidirectionalIterator first.
                     BidirectionalIterator middle,
                     BidirectionalIterator last, Compare comp);
// set operations:
template < class Execution Policy,
         class InputIterator1, class InputIterator2>
 bool includes (ExecutionPolicy &&exec,
                InputIterator1 first1, InputIterator1 last1,
                InputIterator2 first2, InputIterator2 last2);
template<class ExecutionPolicy,</pre>
         class InputIterator1, class InputIterator2, class Compare>
 bool includes (ExecutionPolicy &&exec,
                InputIterator1 first1, InputIterator1 last1,
                InputIterator2 first2, InputIterator2 last2,
                Compare comp);
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator>
 OutputIterator
    set_union(ExecutionPolicy &&exec,
              InputIterator1 first1, InputIterator1 last1,
              InputIterator2 first2, InputIterator2 last2,
              OutputIterator result);
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator, class Compare>
  OutputIterator
    set_union(ExecutionPolicy &&exec,
              InputIterator1 first1, InputIterator1 last1,
```

```
InputIterator2 first2, InputIterator2 last2,
              OutputIterator result, Compare comp);
template<class ExecutionPolicy,</pre>
         class InputIterator1, class InputIterator2,
         class OutputIterator>
  OutputIterator
    set_intersection(ExecutionPolicy &&exec,
                     InputIterator1 first1, InputIterator1 last1,
                     InputIterator2 first2, InputIterator2 last2,
                     OutputIterator result);
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator, class Compare>
 OutputIterator
    set_intersection(ExecutionPolicy &&exec,
                     InputIterator1 first1, InputIterator1 last1,
                     InputIterator2 first2, InputIterator2 last2,
                     OutputIterator result, Compare comp);
template<class ExecutionPolicy,</pre>
         class InputIterator1, class InputIterator2,
         class OutputIterator>
 OutputIterator
    set_difference(ExecutionPolicy &&exec,
                   InputIterator1 first1, InputIterator1 last1,
                   InputIterator2 first2, InputIterator2 last2,
                   OutputIterator result);
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator, class Compare>
 OutputIterator
    set_difference(ExecutionPolicy &&exec,
                   InputIterator1 first1, InputIterator1 last1,
                   InputIterator2 first2, InputIterator2 last2,
                   OutputIterator result, Compare comp);
template<class ExecutionPolicy,</pre>
         class InputIterator1, class InputIterator2,
         class OutputIterator>
 OutputIterator
    set_symmetric_difference(ExecutionPolicy &&exec,
                              InputIterator1 first1, InputIterator1 last1,
                              InputIterator2 first2, InputIterator2 last2,
                              OutputIterator result);
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator, class Compare>
  OutputIterator
    set_symmetric_difference(ExecutionPolicy &&exec,
                              InputIterator1 first1, InputIterator1 last1,
                              InputIterator2 first2, InputIterator2 last2,
                              OutputIterator result, Compare comp);
```

```
// minimum and maximum:
  template<class ExecutionPolicy,</pre>
           class ForwardIterator>
    ForwardIterator min_element(ExecutionPolicy &&exec,
                                 ForwardIterator first, ForwardIterator last);
                                 Compare comp);
  template < class Execution Policy,
           class ForwardIterator, class Compare>
    ForwardIterator min_element(ExecutionPolicy &&exec,
                                 ForwardIterator first, ForwardIterator last,
                                 Compare comp);
  template < class Execution Policy,
           class ForwardIterator>
    ForwardIterator max_element(ExecutionPolicy &&exec,
                                 ForwardIterator first, ForwardIterator last);
  template < class Execution Policy,
           class ForwardIterator, class Compare>
    ForwardIterator max_element(ExecutionPolicy &&exec,
                                 ForwardIterator first, ForwardIterator last,
  template < class Execution Policy,
           class ForwardIterator>
    pair<ForwardIterator, ForwardIterator>
      minmax_element(ExecutionPolicy &&exec,
                      ForwardIterator first, ForwardIterator last);
  template < class Execution Policy,
           class ForwardIterator, class Compare>
    pair<ForwardIterator, ForwardIterator>
      minmax_element(ExecutionPolicy &&exec,
                      ForwardIterator first, ForwardIterator last, Compare comp);
                                   Compare comp);
  template < class Execution Policy,
           class InputIterator1, class InputIterator2>
    bool
      lexicographical_compare(ExecutionPolicy &&exec,
                               InputIterator1 first1, InputIterator1 last1,
                               InputIterator2 first2, InputIterator2 last2);
  template < class Execution Policy,
           class InputIterator1, class InputIterator2, class Compare>
    bool
      lexicographical_compare(ExecutionPolicy &&exec,
                               InputIterator1 first1, InputIterator1 last1,
                               InputIterator2 first2, InputIterator2 last2,
                               Compare comp);
} // namespace parallel
11.2.2 All of [alg.all__of]
template < class Execution Policy,
         class InputIterator, class Predicate>
```

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: true if [first,last) is empty or pred(*i) is true for every iterator i in the range [first,last) and false otherwise.
- 3. Complexity: O(last first).
- 4. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.3 Any of [alg.any_of]

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: false if [first,last) is empty or if there is no iterator i in the range [first,last) such that pred(*i) is true, and true otherwise.
- 3. Complexity: O(last first).
- 4. *Remarks:* The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.4 None of [alg.none__of]

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: true if [first,last) is empty or if pred(*i) is false for every iterator i in the range [first,last), and false otherwise.
- 3. Complexity: O(last first).
- 4. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.5 Find [alg.find]

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: The first iterator i in the range [first,last) for which the following corresponding expression holds: *i == value, pred(*i) != false, pred(*i) == false. Returns last if no such iterator is found.
- 3. Complexity: O(last first).
- 4. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.6 Find end [alg.find.end]

- 1. *Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: The last iterator i in the range [first1,last1 (last2 first2)) such that for any non-negative integer n < (last2 first2), the following corresponding conditions hold: *(i + n) == *(first2 + n), pred(*(i + n), *(first2 + n)) != false. Returns last1 if [first2,last2) is empty or if no such iterator is found.

- 3. Requires: Neither operator== nor pred shall invalidate iterators or subranges, nor modify elements in the ranges [first1,last1)1 or[first2,last2).
- 4. Complexity: O(m * n), where m == last2 first1 and n = last1 first1 (last2 first2).
- 5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.7 Find first [alg.find.first.of]

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: The first iterator i in the range [first1,last1) such that for some iterator j in the range [first2,last2) the following conditions hold: *i == *j, pred(*i,*j) != false. Returns last1 if [first2,last2) is empty or if no such iterator is found.
- 3. Requires: Neither operator== nor pred shall invalidate iterators or subranges, nor modify elements in the ranges [first1,last1) or [first2,last2).
- 4. Complexity: O(m * n), where m == last1 first1 and n == last2 first2.
- 5. *Remarks:* The signatures shall not participate in overload resolution if is execution policy<ExecutionPolicy>::value is false.

11.2.8 Adjacent find [alg.adjacent.find]

1. Effects: The algorithm's execution is parallelized as determined by exec.

- 2. Returns: The first iterator i such that both i and i + 1 are in the range [first,last) for which the following corresponding conditions hold: *i == *(i + 1), pred(*i, *(i + 1)) != false. Returns last if no such iterator is found.
- 3. Requires: Neither operator== nor pred shall invalidate iterators or subranges, nor modify elements in the range [first,last).
- 4. Complexity: O(last first).
- 5. *Remarks:* The signatures shall not participate in overload resolution if is execution policy<ExecutionPolicy>::value is false.

11.2.9 Count [alg.count]

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: The number of iterators i in the range [first,last) for which the following corresponding conditions hold: *i == value, pred(*i) != false.
- 3. Complexity: O(last first).
- 4. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.10 Mismatch [alg.mismatch]

1. Effects: The algorithm's execution is parallelized as determined by exec.

2. Returns: A pair of iterators i and j such that j == first2 + (i - first) and i is the first iterator in the range [first1,last1) for which the following corresponding conditions hold:

```
!(i == *(first2 + (i - first1)))
pred(*i, *(first2 + (i - first1))) == false
```

Returns the pair last1 and first2 + (last1 - first1) if such an iterator i is not found.

- 3. Complexity: O(last1 first1).
- 4. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.11 Equal [alg.equal]

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: true if for every iterator i in the range [first1,last1) the following corresponding conditions hold: *i == *(first2 + (i first1)), pred(*i, *(first2 + (i first1))) != false. Otherwise, returns false.
- 3. Complexity: O(last1 first1).
- 4. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.12 Copy [alg.copy]

- 1. Effects: For each iterator i in the range [first,last), performs *(result + (i first) = *i. The algorithm's execution is parallelized as determined by exec.
- 2. Returns: result + (last first).
- 3. Requires: result shall not be in the range [first,last).

```
4. Complexity: O(last - first).
```

5. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

template < class Execution Policy,

- 1. Effects: For each non-negative integer i < n, performs *(result + i) = *(first + i). The algorithm's execution is parallelized as determined by exec.
- 2. Returns: result + n.
- 3. Complexity: O(n).
- 4. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

template < class Execution Policy,

class InputIterator, class OutputIterator, class Predicate>
OutputIterator

copy_if(ExecutionPolicy &&exec,

InputIterator first, InputIterator last,
OutputIterator result, Predicate pred);

- 1. Requires: The ranges [first,last) and [result,result + (last first)) shall not overlap.
- 2. Effects: Copies all of the elements referred to by the iterator i in the range [first,last) for which pred(*i) is true. The algorithm's execution is parallelized as determined by exec.
- 3. Complexity: O(last first).
- 4. Remarks: Stable.

The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.13 Move [alg.move]

```
template<class ExecutionPolicy,
        class InputIterator, class OutputIterator>
OutputIterator
   move(ExecutionPolicy &&exec,
        InputIterator first, InputIterator last,
        OutputIterator result);
```

- 1. Effects: For each iterator i in the range [first,last), performs *(result + (i first) = std::move(*i). The algorithm's execution is parallelized as determined by exec.
- 2. Returns: result (last first).
- 3. Requires: result shall not be in the range [first,last).
- 4. Complexity: O(last first).
- 5. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.14 Swap [alg.swap]

- 1. Effects: For each non-negative integer n < (last1 first1) performs: swap(*(first1 + n), *(first2 + n)). The algorithm's execution is parallelized as determined by exec.
- 2. Requires: The two ranges [first1,last1) and [first2,first2 + (last1 first1)) shall not overlap. *(first1 + n) shall be swappable with *(first2 + n).
- 3. Returns: first2 + (last1 first1).
- 4. Complexity: O(last1 first1).
- 5. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.15 Transform [alg.transform]

- 1. Effects: Assigns through every iterator i in the range [result,result + (last1 first1)) a new corresponding value equal to op(*(first1 + (i result)) or binary_op(*(first1 + (i result)), *(first2 + (i result)). The algorithm's execution is parallelized as determined by exec.
- 2. Requires: op and binary_op shall not invalidate iterators or subranges, or modify elements in the ranges [first1,last1], [first2,first2 + (last1 first1)], and [result,result + (last1 first1)].
- 3. Returns: result + (last1 first1).
- 4. Complexity: O(last first) or O(last1 first1).
- 5. Remarks: result may be equal to first in case of unary transform, or to first1 or first2 in case of binary transform.

The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.16 Replace [alg.replace]

3. Complexity: O(last - first).

4. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

- 1. Requires: The results of the expressions *first and new_value shall be writable to the result output iterator. The ranges [first,last) and [result,result + (last first)) shall not overlap.
- 2. Effects: Assigns to every iterator i in the range [result,result + (last first)) either new_value or *(first + (i result)) depending on whether the following corresponding conditions hold:

```
*(first + (i - result)) == old_value
pred(*(first + (i - result))) != false
```

The algorithm's execution is parallelized as determined by exec.

- 3. Complexity: O(last first).
- 4. *Remarks:* The signatures shall not participate in overload resolution if is execution policy<ExecutionPolicy>::value is false.

11.2.17 Fill [alg.fill]

- 1. Requires: The expression value shall be writable to the output iterator. The type Size shall be convertible to an integral type.
- 2. Effects: The first algorithm assigns value through all the iterators in the range [first,last). The second value assigns value through all the iterators in the range [first,first + n) if n is positive, otherwise it does nothing. The algorithm is parallelized as determined by exec.
- 3. Returns: fill_n returns first + n for non-negative values of n and first for negative values.
- 4. Complexity: O(last first) or O(n).
- 5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.18 Generate [alg.generate]

- 1. Effects: The first algorithm invokes the function object gen and assigns the value of gen through all the iterators in the range [first,last). The second algorithm invokes the function object gen and assigns the return value of gen through all the iterators in the range [first,first + n) if n is positive, otherwise it does nothing. The algorithms execution is parallelized as determined by exec.
- 2. Requires: gen takes no arguments, Size shall be convertible to an integral type.
- 3. Returns: generate_n returns first + n for non-negative values of nand first for negative values.
- 4. Complexity: O(last first) or O(n).
- 5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.19 Remove [alg.remove]

- 1. Requires: The type of *first shall satisfy the MoveAssignable requirements.
- 2. Effects: Eliminates all the elements referred to by iterator i in the range [first,last) for which the following corresponding conditions hold: *i == value, pred(*i) != false. The algorithm's execution is parallelized as determined by exec.
- 3. Returns: The end of the resulting range.
- 4. Complexity: O(last first).
- 5. Remarks: Stable.

The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

6. Note: Each element in the range [ret,last), where ret is the returned value, has a valid but unspecified state, because the algorithms can eliminate elements by swapping with or moving from elements that were originally in that range.

- 1. Requires: The ranges [first,last) and [result,result + (last first)) shall not overlap. The expression *result = *first shall be valid.
- 2. Effects: Copies all the elements referred to by the iterator i in the range [first,last) for which the following corresponding conditions do not hold: *i == value, pred(*i) != false. The algorithm's execution is parallelized as determined by exec.
- 3. Returns: The end of the resulting range.
- 4. Complexity: O(last first).
- 5. Remarks: Stable.

The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.20 Unique [alg.unique]

- 1. Effects: For a nonempty range, eliminates all but the first element from every consecutive group of equivalent elements referred to by the iterator i in the range [first + 1,last) for which the following conditions hold: *(i 1) == *i or pred(*(i 1), *i) != false. The algorithm's execution is parallelized as determined by exec.
- 2. Requires: The comparison function shall be an equivalence relation. The type of *first shall satisfy the MoveAssignable requirements.
- 3. Returns: The end of the resulting range.
- 4. Complexity: O(last first).
- 5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

- 1. Requires: The comparison function shall be an equivalence relation. The ranges [first,last) and [result,result + (last-first)) shall not overlap. The expression *result = *first shall be valid. If neither InputIterator nor OutputIterator meets the requirements of forward iterator then the value type of InputIterator shall be CopyConstructible and CopyAssignable. Otherwise CopyConstructible is not required.
- 2. Effects: Copies only the first element from every consecutive group of equal elements referred to by the iterator i in the range [first,last) for which the following corresponding conditions hold: *i == *(i 1) or pred(*i, *(i 1)) != false. The algorithm's execution is parallelized as determined by exec.
- 3. Returns: The end of the resulting range.
- 4. Complexity: O(last first).

5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.21 Reverse [alg.reverse]

- 1. Effects: For each non-negative integer i <= (last first)/2, applies iter_swap to all pairs of iterator first + i, (last i) 1. The algorithm's execution is parallelized as determined by exec.
- 2. Requires: *first shall be swappable.
- 3. Complexity: O(last first).
- 4. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

- 1. Effects: Copies the range [first,last) to the range [result,result + (last first)) such that
 for any non-negative integer i < (last first) the following assignment takes place: *(result +
 (last first) i) = *(first + i). The algorithm's execution is parallelized as determined by
 exec.</pre>
- 2. Requires: The ranges [first,last) and [result,result + (last first)) shall not overlap.
- 3. Returns: result + (last first).
- 4. Complexity: O(last first).
- 5. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.22 Rotate [alg.rotate]

Effects: For each non-negative integer i < (last - first), places the element from the position first + i into position first + (i + (last - middle)) % (last - first). The algorithm's execution is parallelized as determined by exec.

- 2. Returns: first + (last middle).
- 3. Remarks: This is a left rotate.

The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

- 4. Requires: [first,middle) and [middle,last) shall be valid ranges. ForwardIterator shall satisfy the requirements of ValueSwappable. The type of *first shall satisfy the requirements of MoveConstructible and the requirements of MoveAssignable.
- 5. Complexity: O(last first).

- 1. Effects: Copies the range [first,last) to the range [result,result + (last first)) such that
 for each non-negative integer i < (last first) the following assignment takes place: *(result +
 i) = *(first + (i + (middle first)) % (last first)). The algorithm's execution
 is parallelized as determined byexec'.</pre>
- 2. Returns: result + (last first).
- 3. Requires: The ranges [first,last) and [result,result + (last first)) shall not overlap.
- 4. Complexity: O(last first).
- 5. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.23 Partitions [alg.partitions]

- 1. Requires: InputIterator's value type shall be convertible to Predicate's argument type.
- 2. Effects: The algorithm's execution is parallelized as determined by exec.
- 3. Returns: true if [first,last) is empty or if [first,last) is partitioned by pred, i.e. if all elements that satisfy pred appear before those that do not.
- 4. Complexity: O(last first).
- 5. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

- 1. *Effects:* Places all the elements in the range [first,last) that satisfy pred before all the elements that do not satisfy it. The algorithm's execution is parallelized as determined by exec.
- 2. Returns: An iterator i such that for any iterator j in the range [first,i), pred(*j) != false, and for any iterator k in the range [i,last), pred(*k) == false.
- 3. Requires: ForwardIterator shall satisfy the requirements of ValueSwappable.
- 4. Complexity: O(last first).
- 5. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

- 1. *Effects:* Places all the elements in the range [first,last) that satisfy pred before all the elements that do not satisfy it. The algorithm's execution is parallelized as determined by exec.
- 2. Returns: An iterator i such that for any iterator j in the range [first,i), pred(*j) != false, and for any iterator k in the range [i,last), pred(*k) == false. The relative order of the elements in both groups is preserved.
- 3. Requires: BidirectionalIterator shall satisfy the requirements of ValueSwappable. The type of *first shall satisfy the requirements of MoveConstructible and of MoveAssignable.
- 4. Complexity: O(last first).
- 5. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

- 1. Requires: InputIterator's value type shall be Assignable, and shall be writable to the out_true and out_false OutputIterators, and shall be convertible to Predicate's argument type. The input range shall not overlap with either of the output ranges.
- 2. Effects: For each iterator i in [first,last), copies *i to the output range beginning with out_true if pred(*i) is true, or to the output range beginning with out_false otherwise. The algorithm's execution is parallelized as determined by exec.
- 3. Returns: A pair p such that p.first is the end of the output range beginning at out_true and p.second is the end of the output range beginning at out_false.
- 4. Complexity: O(last first).

5. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

- 1. Requires: ForwardIterator's value type shall be convertible to Predicate's argument type. [first,last) shall be partitioned by pred, i.e. all elements that satisfy pred shall appear before those that do not.
- 2. Effects: The algorithm's execution is parallelized as determined by exec.
- 3. Returns: An iterator mid such that all_of(first, mid, pred) and none_of(mid, last, pred) are both true.
- 4. Complexity: O(last first).
- 5. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.24 sort [alg.sort]

- 1. Effects: Sorts the elements in the range [first,last). The algorithm's execution is parallelized as determined by exec.
- 2. Requires: RandomAccessIterator shall satisfy the requirements of ValueSwappable. The type of *first shall satisfy the requirements of MoveConstructible and of MoveAssignable.
- 3. Complexity: O(n lg n), where n = last first.
- 4. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.25 stable_sort [stable.sort]

- 1. *Effects*: Sorts the elements in the range [first,last). The algorithm's execution is parallelized as determined by exec.
- 2. Requires: RandomAccessIterator shall satisfy the requirements of ValueSwappable. The type of *first shall satisfy the requirements of MoveConstructible and of MoveAssignable.
- 3. Complexity: O(n lg n), where n = last first.
- 4. Remarks: Stable.

The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.26 partial_sort [partial.sort]

1. Effects: Places the first middle - first sorted elements from the range [first,last) into the range [first,middle). The rest of the elements in the range [middle,last) are placed in an unspecified order.

The algorithm's execution is parallelized as determined by exec.

- Requires: RandomAccessIterator shall satisfy the requirements of ValueSwappable. The type of *first shall satisfy the requirements of MoveConstructible and of MoveAssignable.
 middle shall be in the range [first,last).
- 3. Complexity: O(m lg n), where m = last first and n = middle first.
- 4. *Remarks:* The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

```
11.2.27 partial_sort_copy [partial.sort.copy]
template < class Execution Policy,
         class InputIterator, class RandomAccessIterator>
  RandomAccessIterator
    partial_sort_copy(ExecutionPolicy &&exec,
                       InputIterator first, InputIterator last,
                       RandomAccessIterator result_first,
                       RandomAccessIterator result_last);
template < class Execution Policy,
         class InputIterator, class RandomAccessIterator,
         class Compare>
  RandomAccessIterator
    partial_sort_copy(ExecutionPolicy &&exec,
                       InputIterator first, InputIterator last,
                       RandomAccessIterator result_first,
                       RandomAccessIterator result last,
                       Compare comp);
  1. Effects: Places the first min(last - first, result_last - result_first) sorted elements into the
     range [result_first,result_first + min(last - first, result_last - result_first)).
     The algorithm's execution is parallelized as determined by exec.
  2. Returns: The smaller of: result_last or result_first + (last - first).
  3. Requires: RandomAccessIterator shall satisfy the requirements of ValueSwappable. The type of
     *result_first shall satisfy the requirements of MoveConstructible and of MoveAssignable.
  4. Complexity: O(m lg n), where m = last - first and n = min(last - first, result_last -
     result first).
  5. Remarks: The signatures shall not participate in overload resolution if
     is_execution_policy<ExecutionPolicy>::value is false.
11.2.28 is_sorted [is.sorted]
template < class Execution Policy,
         class ForwardIterator>
  bool is_sorted(ExecutionPolicy &&exec,
                  ForwardIterator first, ForwardIterator last);
  1. Effects: The algorithm's execution is parallelized as determined by exec.
  2. Returns: is_sorted_until(forward<ExecutionPolicy>(exec), first, last) == last
  3. Complexity: O(last - first).
  4. Remarks: The signature shall not participate in overload resolution if
     is_execution_policy<ExecutionPolicy>::value is false.
template < class Execution Policy,
         class ForwardIterator, class Compare>
  bool is_sorted(ExecutionPolicy &&exec,
                  ForwardIterator first, ForwardIterator last,
                  Compare comp);
```

```
1. Effects: The algorithm's execution is parallelized as determined by exec.
```

- 2. Returns: is_sorted_until(forward<ExecutionPolicy>(exec), first, last, comp) == last
- 3. Complexity: O(last first).
- 4. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

Compare comp);

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: If distance(first, last) < 2), returns last. Otherwise, returns the last iterator i in [first,last) for which the range [first,i) is sorted.

ForwardIterator first, ForwardIterator last,

- 3. Complexity: O(last first).
- 4. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.29 Nth element [alg.nth.element]

1. Effects: Reorders the range [first,last) such that the element referenced by nth is the element that would be in that position if the whole range were sorted. Also for any iterator i in the range [first,nth) and any iterator j in the range [nth,last) the following corresponding condition holds: !(*j < *i) or comp(*j, *i) == false.

The algorithm's execution is parallelized as determined by exec.

2. Requires: RandomAccessIterator shall satisfy the requirements of ValueSwappable. The type of *first shall satisfy the requirements of MoveConstructible and of MoveAssignable.

nth shall be in the range [first,last).

```
3. Complexity: O(last - first).
```

4. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.30 lower_bound [lower.bound]

- 1. Requires: The elements e of [first,last) shall be partitioned with respect to the expression e < value or comp(e, value).
- 2. Effects: The algorithm's execution is parallelized as determined by exec.
- 3. Returns: The furthermost iterator i in the range [first,last) such that for any iterator j in the range [first,i) the following corresponding conditions hold: *j < value or comp(*j, value) != false.
- 4. Complexity: O(lg (last first)).
- 5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.31 upper_bound [upper.bound]

1. Requires: The elements e of [first,last) shall be partitioned with respect to the expression !(value < e) or !comp(value, e).

- 2. Effects: The algorithm's execution is parallelized as determined by exec.
- 3. Returns: The furthermost iterator i in the range [first,last) such that for any iterator j in the range [first,i) the following conditions hold: !(value < *j) or comp(value, *j) == false.
- 4. Complexity: O(lg (last first)).
- 5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.32 equal_range [equal.range]

- Requires: The elements e of [first,last) shall be partitioned with respect to the expressions e < value and !(value < e) or comp(e, value) and !comp(value, e). Also, for all elements e of [first,last), e < value shall imply !(value < e) or comp(e, value) shall imply !comp(value, e).
- 2. Effects: The algorithm's execution is parallelized as determined by exec.
- 3. Returns:

ForwardIterator first, ForwardIterator last,

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const T& value);

- 1. Requires: The elements e of [first, last) are partitioned with respect to the expressions e < value and !(value < e) or comp(e, value) and !comp(value, e). Also, for all elements e of [first, last), e < value implies !(value < e) or comp(e, value) implies !comp(value, e).
- 2. Effects: The algorithm's execution is parallelized as determined by exec.
- 3. Returns: true if there is an iterator i in the range [first,last) that satisfies the corresponding conditions: !(*i < value) && !(value < *i) or comp(*i, value) == false && comp(value, *i) == false.
- 4. Complexity: O(lg (last first)).
- 5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.33 Merge [alg.merge]

```
template<class ExecutionPolicy,</pre>
         class InputIterator1, class InputIterator2,
         class OutputIterator>
  OutputIterator
    merge(ExecutionPolicy &&exec,
          InputIterator1 first1, InputIterator1 last1,
          InputIterator2 first2, InputIterator2 last2,
          OutputIterator result);
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator, class Compare>
  OutputIterator
    merge(ExecutionPolicy &&exec,
          InputIterator1 first1, InputIterator1 last1,
          InputIterator2 first2, InputIterator2 last2,
          OutputIterator result, Compare comp);
```

- 1. Effects: Copies all the elements of the two ranges [first1,last1) and [first2,last2) into the range [result,result_last), where result_last is result + (last1 first1) + (last2 first2), such that the resulting range satisfies is_sorted(result, result_last) or is_sorted(result, result_last, comp), respectively. The algorithm's execution is parallelized as determined by exec.
- 2. Requires: The ranges [first1,last1) and [first2,last2) shall be sorted with respect to operator or comp. The resulting range shall not overlap with either of the input ranges.
- 3. Returns: result + (last1 first1) + (last2 first2).
- 4. Complexity: O(m + n), where m = last1 first1 and n = last2 first2.
- 5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

- 1. Effects: Merges two sorted consecutive ranges [first,middle) and [middle,last), putting the result of the merge into the range [first,last). The resulting range will be in non-decreasing order; that is, for every iterator i in [first,last) other than first, the condition *i < *(i 1) or, respectively, comp(*i, *(i 1)) will be false. The algorithm's execution is parallelized as determined by exec.</p>
- 2. Requires: The ranges [first,middle) and [middle,last) shall be sorted with respect to operator or comp. BidirectionalIterator shall satisfy the requirements of ValueSwappable. The type of *first shall satisfy the requirementsof MoveConstructible and of MoveAssignable.
- 3. Remarks: Stable.
- 4. Complexity: O(m + n), wherem = middle firstandn = last middle'.
- 5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.34 Includes [includes]

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Requires: The ranges [first1,last1) and [first2,last2) shall be sorted with respect to operator or comp.
- 3. Returns: true if [first2,last2) is empty or if every element in the range [first2,last2) is contained in the range [first1,last1). Returns false otherwise.
- 4. Complexity: O(m + n), where m = last1 first1 and n = last2 first2.

5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

```
11.2.35 set_union [set.union]
```

```
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator>
  OutputIterator
    set_union(ExecutionPolicy &&exec,
              InputIterator1 first1, InputIterator1 last1,
              InputIterator2 first2, InputIterator2 last2,
              OutputIterator result);
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator, class Compare>
  OutputIterator
    set_union(ExecutionPolicy &&exec,
              InputIterator1 first1, InputIterator1 last1,
              InputIterator2 first2, InputIterator2 last2,
              OutputIterator result, Compare comp);
```

- 1. *Effects:* Constructs a sorted union of the elements from the two ranges; that is, the set of elements that are present in one or both of the ranges. The algorithm's execution is parallelized as determined by exec.
- 2. Requires: The resulting range shall not overlap with either of the original ranges.
- 3. Returns: The end of the constructed range.
- 4. Complexity: O(m + n), where m = last1 first1 and n = last2 first2.
- 5. Remarks: If [first1,last1) contains m elements that are equivalent to each other and [first2,last2) contains n elements that are equivalent to them, then all m elements from the first range shall be copied to the output range, in order, and then max(n-m,0) elements from the second range shall be copied to the output range, in order.

The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.36 set_intersection [set.intersection]

- 1. Effects: Constructs a sorted intersection of the elements from the two ranges; that is, the set of elements that are present in both of the ranges. The algorithm's execution is parallelized as determined by exec.
- 2. Requires: The resulting range shall not overlap with either of the original ranges.
- 3. Returns: The end of the constructed range.
- 4. Complexity: O(m + n), where m = last1 first1 and n = last2 first2.
- 5. Remarks: If [first1,last1) contains m elements that are equivalent to each other and [first2,last2) contains n elements that are equivalent to them, the first min(m,n) elements shall be copied from the first range to the output range, in order.

The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.37 set_difference [set.difference]

```
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator>
  OutputIterator
    set_difference(ExecutionPolicy &&exec,
                   InputIterator1 first1, InputIterator1 last1,
                   InputIterator2 first2, InputIterator2 last2,
                   OutputIterator result);
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator, class Compare>
  OutputIterator
    set_difference(ExecutionPolicy &&exec,
                   InputIterator1 first1, InputIterator1 last1,
                   InputIterator2 first2, InputIterator2 last2,
                   OutputIterator result, Compare comp);
```

- 1. Effects: Copies the elements of the range [first1,last1) which are not present in the range [first2,last2) to the range beginning at result. The elements in the constructed range are sorted. The algorithm's execution is parallelized as determined by exec.
- 2. Requires: The resulting range shall not overlap with either of the original ranges.
- 3. Returns: The end of the constructed range.
- 4. Complexity: O(m + n), where m = last1 first1 and n = last2 first2.
- 5. Remarks: If [first1,last1) contains m elements that are equivalent to each other and [first2,last2) contains n elements that are equivalent to them, the last max(m-n,0) elements from [first1,last1) shall be copied to the output range.

The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.38 set_symmetric_difference [set.symmetric.difference]

```
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator>
  OutputIterator
    set_symmetric_difference(ExecutionPolicy &&exec,
                              InputIterator1 first1, InputIterator1 last1,
                              InputIterator2 first2, InputIterator2 last2,
                              OutputIterator result);
template < class Execution Policy,
         class InputIterator1, class InputIterator2,
         class OutputIterator, class Compare>
  OutputIterator
    set_symmetric_difference(ExecutionPolicy &&exec,
                             InputIterator1 first1, InputIterator1 last1,
                              InputIterator2 first2, InputIterator2 last2,
                              OutputIterator result, Compare comp);
```

- 1. Effects: Copies the elements of the range [first1,last1) that are not present in the range [first2,last2), and the elements of the range [first2,last2) that are not present in the range [first1,last1) to the range beginning at result. The elements in the constructed range are sorted. The algorithm's execution is parallelized as determined by exec.
- 2. Requires: The resulting range shall not overlap with either of the original ranges.
- 3. Returns: The end of the constructed range.
- 4. Complexity: O(m + n), where m = last1 first1 and n = last2 first2.
- 5. Remarks: If [first1,last1) contains m elements that are equivalent to each other and [first2,last2) contains n elements that are equivalent to them, then |m-n| of those elements shall be copied to the output range: the last m-n of these elements from [first1,last1) if m>n, and the last n-m of these elements from [first2,last2) if m< n.

The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.2.39 Minimum and maximum [alg.min.max]

1. Effects: The algorithm's execution is parallelized as determined by exec.

```
[first,last) the following corresponding conditions hold: !(*j < *i) or comp(*j, *i) == false.
     Returns last if first == last.
  3. Complexity: O(last - first).
  4. Remarks: The signatures shall not participate in overload resolution if
     is_execution_policy<ExecutionPolicy>::value is false.
template < class Execution Policy,
         class ForwardIterator>
  ForwardIterator max_element(ExecutionPolicy &&exec,
                                 ForwardIterator first, ForwardIterator last);
template < class Execution Policy,
         class ForwardIterator, class Compare>
  ForwardIterator max_element(ExecutionPolicy &&exec,
                                 ForwardIterator first, ForwardIterator last,
                                 Compare comp);
  1. Effects: The algorithm's execution is parallelized as determined by exec.
  2. Returns: The first iterator i in the range [first,last) such that for any iterator j in the range
     [first,last) the following corresponding conditions hold: !(*i < *j) or comp(*i, *j) == false.
     Returns last if first == last.
  3. Complexity: O(last - first).
  4. Remarks: The signatures shall not participate in overload resolution if
     is_execution_policy<ExecutionPolicy>::value is false.
template < class Execution Policy,
         class ForwardIterator>
  pair<ForwardIterator, ForwardIterator>
    minmax_element(ExecutionPolicy &&exec,
                    ForwardIterator first, ForwardIterator last);
template < class Execution Policy,
         class ForwardIterator, class Compare>
  pair<ForwardIterator, ForwardIterator>
    minmax element(ExecutionPolicy &&exec,
                     ForwardIterator first, ForwardIterator last, Compare comp);
  1. Effects: The algorithm's execution is parallelized as determined by exec.
  2. Returns: make_pair(first, first) if [first,last) is empty, otherwise make_pair(m, M), where
     m is the first iterator in [first,last) such that no iterator in the range refers to a smaller element,
     and where M is the last iterator in [first,last) such that no iterator in the range refers to a larger
     element.
```

2. Returns: The first iterator i in the range [first,last) such that for any iterator j in the range

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4. Remarks: The signatures shall not participate in overload resolution if

is_execution_policy<ExecutionPolicy>::value is false.

3. Complexity: O(last - first).

11.2.40 Lexicographical comparison [alg.lex.comparison]

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: true if the sequence of elements defined by the range [first1,last1) is lexicographically less than the sequence of elements defined by the range [first2,last2) and false otherwise.
- 3. Complexity: O(min(m,n)), where m = last1 first1 and n = last2 first2.
- 4. Remarks: If two sequences have the same number of elements and their corresponding elements are equivalent, then neither sequence is lexicographically less than the other. If one sequence is a prefix of the other, then the shorter sequence is lexicographically less than the longer sequence. Otherwise, the lexicographical comparison of the sequences yields the same result as the comparison of the first corresponding pair of elements that are not equivalent.

An empty sequence is lexicographically less than any non-empty sequence, but not less than any empty sequence.

The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

11.3 Existing generalized numeric operations from <numeric>

11.3.1 Header <numeric> synopsis

```
template < class Execution Policy,
            class InputIterator, class OutputIterator>
    OutputIterator adjacent_difference(ExecutionPolicy &&exec,
                                          InputIterator first, InputIterator last,
                                          OutputIterator result);
  template < class Execution Policy,
            class InputIterator, class OutputIterator, class BinaryOperation>
    OutputIterator adjacent_difference(ExecutionPolicy &&exec,
                                          InputIterator first, InputIterator last,
                                          OutputIterator result,
                                          BinaryOperation binary_op);
}
template<class ExecutionPolicy,</pre>
          class InputIterator1, class InputIterator2, class T>
  T inner_product(ExecutionPolicy &&exec,
                    InputIterator1 first1, InputIterator1 last1,
                   InputIterator2 first2, T init);
  1. Effects: The algorithm's execution is parallelized as determined by exec.
  2. Returns: The result of the sum init + (*(first1 + i) * *(first2 + i) + ... for every integer
     i in the range [0, (last1 - first1)).
     The order of operands of the sum is unspecified.
  3. Requires: operator+ shall have associativity and commutativity.
     operator+ shall not invalidate iterators or subranges, nor modify elements in the ranges [first1,last1)
     or [first2, first2 + (last1 - first1)).
  4. Complexity: O(last1 - first1).
  5. Remarks: The signature shall not participate in overload resolution if
     is_execution_policy<ExecutionPolicy>::value is false.
template < class Execution Policy,
          class InputIterator1, class InputIterator2, class T,
          class BinaryOperation1, class BinaryOperation2>
  T inner_product(ExecutionPolicy &&exec,
                   InputIterator1 first1, InputIterator1 last1,
                   InputIterator2 first2, T init,
                   BinaryOperation1 binary_op1,
                   BinaryOperation2 binary_op2);
```

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: The result of the generalized sum whose operands are init and the result of the pairwise binary operation binary_op2(*i,*(first2 + (i first1))) for all iterators i in the range [first1,last1).

The generalized sum's operands are combined via application of the pairwise binary operation binary_op1.

The order of operands of the sum is unspecified.

- 3. Requires: binary_op1 shall have associativity and commutativity. binary_op1 and binary_op2 shall neither invalidate iterators or subranges, nor modify elements in the ranges [first1,last1) or [first2,first2 + (last1 - first1)). 4. Complexity: O(last1 - first1). 5. Remarks: The signature shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false. template < class Execution Policy, class InputIterator, class OutputIterator> OutputIterator adjacent_difference(ExecutionPolicy &&exec, InputIterator first, InputIterator last, OutputIterator result); template < class Execution Policy, class InputIterator, class OutputIterator, class BinaryOperation> OutputIterator adjacent_difference(ExecutionPolicy &&exec, InputIterator first, InputIterator last, OutputIterator result, BinaryOperation binary_op); 1. Effects: Performs *result = *first and for each iterator i in the range [first + 1, last), performs *result = *i - *(i - 1), or *result = binary_op(*i, *(i - 1)), respectively. The algorithm's execution is parallelized as determined by exec.
 - 2. Returns: result + (last first).
 - 3. Requires: The result of the expression *i *(i 1) or binary_op(*i, *(i 1)) shall be writable to the result output iterator.

Neither operator- nor binary_op shall invalidate iterators or subranges, nor modify elements in the range [first,last) or [result,result + (last - first)).

- 4. Complexity: O(last first).
- 5. Remarks: result may be equal to first.

The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

12 Novel Algorithms Introduced by this Proposal

- 12.1 Novel specialized algorithms from <memory>
- 12.1.1 None.
- 12.2 Novel algorithms from <algorithm>
- 12.2.1 Header <algorithm> synopsis

```
namespace std {
   // non-modifying sequence operations
   template<class ExecutionPolicy,</pre>
```

```
class ForwardIterator, class Function>
    ForwardIterator for_each(ExecutionPolicy &&exec,
                              ForwardIterator first, ForwardIterator last,
                              Function f);
  template < class Execution Policy,
           class InputIterator, class Size, class Function>
    InputIterator for_each_n(ExecutionPolicy &&exec,
                              InputIterator first, Size n,
                              Function f);
} // namespace parallel
Novel non-modifying sequence operations
12.2.2 For each [alg.foreach]
template < class Execution Policy,
         class ForwardIterator, class Function>
  ForwardIterator for_each(ExecutionPolicy &&exec,
                            ForwardIterator first, ForwardIterator last,
                            Function f);
template < class Execution Policy,
         class InputIterator, class Size, class Function>
  InputIterator for_each_n(ExecutionPolicy &&exec,
                            InputIterator first, Size n,
                            Function f);
```

- 1. Effects: The first algorithm applies f to the result of dereferencing every iterator in the range [first,last). The second algorithm applies f to the result of dereferencing every iterator in the range [first,first+n). The execution of the algorithm is parallelized as determined by exec. [Note: If the type of first satisfies the requirements of a mutable iterator, f may apply nonconstant functions through the dereferenced iterator. end note]
- 2. Returns: for_each returns last and for_each_n returns first + n for non-negative values of n and first for negative values.
- 3. Complexity: O(last first) or O(n).
- 4. Remarks: If f returns a result, the result is ignored.

The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

12.3 Novel generalized numeric operations from <numeric>

12.3.1 Header <numeric> synopsis

```
template < class Execution Policy,
         class InputIterator, class T>
  T reduce(ExecutionPolicy &&exec,
           InputIterator first, InputIterator last, T init);
template<class ExecutionPolicy,</pre>
         class InputIterator, class T, class BinaryOperation>
  T reduce(ExecutionPolicy &&exec,
           InputIterator first, InputIterator last, T init,
           BinaryOperation binary_op);
template<class ExecutionPolicy,</pre>
         class InputIterator, class OutputIterator>
 OutputIterator
    exclusive_scan(ExecutionPolicy &&exec,
                   InputIterator first, InputIterator last,
                   OutputIterator result);
template < class Execution Policy,
         class InputIterator, class OutputIterator,
         class T>
  OutputIterator
    exclusive_scan(ExecutionPolicy &&exec,
                   InputIterator first, InputIterator last,
                   OutputIterator result,
                   T init):
template<class ExecutionPolicy,</pre>
         class InputIterator, class OutputIterator,
         class T, class BinaryOperation>
  OutputIterator
    exclusive_scan(ExecutionPolicy &&exec,
                   InputIterator first, InputIterator last,
                   OutputIterator result,
                   T init, BinaryOperation binary_op);
template<class ExecutionPolicy,</pre>
         class InputIterator, class OutputIterator>
 OutputIterator
    inclusive_scan(ExecutionPolicy &&exec,
                   InputIterator first, InputIterator last,
                   OutputIterator result);
template<class ExecutionPolicy,</pre>
         class InputIterator, class OutputIterator,
         class BinaryOperation>
 OutputIterator
    inclusive_scan(ExecutionPolicy &&exec,
                   InputIterator first, InputIterator last,
                   OutputIterator result,
                   BinaryOperation binary_op);
template < class Execution Policy,
         class InputIterator, class OutputIterator,
         class T, class BinaryOperation>
 OutputIterator
    inclusive_scan(ExecutionPolicy &&exec,
                   InputIterator first, InputIterator last,
                   OutputIterator result,
```

```
T init, BinaryOperation binary_op);
}
12.3.2 Reduce [reduce]
template < class Execution Policy,
          class InputIterator>
  typename iterator_traits<InputIterator>::value_type
    reduce(ExecutionPolicy &&exec,
            InputIterator first, InputIterator last);
  1. Effects: The algorithm's execution is parallelized as determined by exec.
  2. Returns: The result of the sum T(0) + *iter_0 + *iter_1 + *iter_2 + ... for every iterator
     iter_i in the range [first,last).
     The order of operands of the sum is unspecified.
  3. Requires: Let T be the type of InputIterator's value type, then T(0) shall be a valid expression. The
     operator+ function associated with T shall have associativity and commutativity.
     operator+ shall not invalidate iterators or subranges, nor modify elements in the range [first,last).
  4. Complexity: O(last - first).
  5. Remarks: The signature shall not participate in overload resolution if
     is_execution_policy<ExecutionPolicy>::value is false.
```

- 1. Effects: The algorithm's execution is parallelized as determined by exec.
- 2. Returns: The result of the generalized sum init + *iter_0 + *iter_1 + *iter_2 + ... or binary_op(init, binary_op(*iter_0, binary_op(*iter_2, ...))) for every iterator iter_i in the range [first,last).

The order of operands of the sum is unspecified.

3. Requires: The operator+ function associated with InputIterator's value type or binary_op shall have associativity and commutativity.

Neither operator+ nor binary_op shall invalidate iterators or subranges, nor modify elements in the range [first,last).

- 4. Complexity: O(last first).
- 5. Remarks: The signatures shall not participate in overload resolution if is_execution_policy<ExecutionPolicy>::value is false.

```
template < class Execution Policy,
         class InputIterator, class OutputIterator,
         class T>
  OutputIterator
    exclusive_scan(ExecutionPolicy &&exec,
                    InputIterator first, InputIterator last,
                    OutputIterator result,
                    T init);
template < class Execution Policy,
         class InputIterator, class OutputIterator,
         class T, class BinaryOperation>
  OutputIterator
    exclusive_scan(ExecutionPolicy &&exec,
                    InputIterator first, InputIterator last,
                    OutputIterator result,
                    T init, BinaryOperation binary_op);
  1. Effects: For each iterator i in [result, result + (last - first)), performs *i = prefix_sum,
     where prefix_sum is the result of the corresponding sum init + *iter_0 + *iter_1 + *iter_2 +
     ... or binary_op(init, binary_op(*iter_0, binary_op(*iter_1, binary_op(*iter_2, ...)))
     for every iterator iter_j in the range [first,first + (i - result) - 1).
     The order of operands of the sum is unspecified.
     The algorithm's execution is parallelized as determined by exec.
  2. Returns: The end of the resulting range beginning at result.
  3. Requires: The operator+ function associated with InputIterator's value type or binary_op shall
     have associativity.
     Neither operator+ nor binary_op shall invalidate iterators or subranges, nor modify elements in the
     ranges [first,last) or [result,result + (last - first)).
  4. Complexity: O(last - first).
  5. Remarks: The signatures shall not participate in overload resolution if
     is_execution_policy<ExecutionPolicy>::value is false.
  6. Notes: The primary difference between exclusive_scan and inclusive_scan is that exclusive_scan
     excludes the ith input element from the ith sum.
template < class Execution Policy,
         class InputIterator, class OutputIterator>
  OutputIterator
    inclusive_scan(ExecutionPolicy &&exec,
                    InputIterator first, InputIterator last,
                    OutputIterator result);
template < class Execution Policy,
         class InputIterator, class OutputIterator,
         class BinaryOperation>
  OutputIterator
```

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inclusive_scan(ExecutionPolicy &&exec,

OutputIterator result,

InputIterator first, InputIterator last,

```
BinaryOperation binary_op);
template < class Execution Policy,
         class InputIterator, class OutputIterator,
         class T, class BinaryOperation>
  OutputIterator
    inclusive scan(ExecutionPolicy &&exec,
                    InputIterator first, InputIterator last,
                    OutputIterator result,
                    T init, BinaryOperation binary_op);
  1. Effects: For each iterator i in [result, result + (last - first)), performs *i = prefix_sum,
     where prefix_sum is the result of the corresponding sum
     *iter_0 + *iter_1 + *iter_2 + ... or
     binary_op(*iter_0, binary_op(*iter_1, binary_op(*iter_2, ...))) or
     binary_op(init, binary_op(*iter_0, binary_op(*iter_1, binary_op(*iter_2, ...))))
     for every iterator iter_j in the range [first,first + (i - result) - 1).
     The order of operands of the sum is unspecified.
     The algorithm's execution is parallelized as determined by exec.
```

- 2. Returns: The end of the resulting range beginning at result.
- 3. Requires: The operator+ function associated with InputIterator's value type or binary_op shall have associativity.

Neither operator+ nor binary_op shall invalidate iterators or subranges, nor modify elements in the ranges [first,last) or [result,result + (last - first)).

- 4. Complexity: O(last first).
- 5. *Remarks:* The signatures shall not participate in overload resolution if is execution policy<ExecutionPolicy>::value is false.
- 6. *Notes:* The primary difference between exclusive_scan and inclusive_scan is that inclusive_scan includes the ith input element in the ith sum.

13 Existing Algorithms Left Unchanged by this Proposal

This proposal leaves some algorithms of <memory>, <algorithm>, and <numeric> unchanged because they either 1. have no parallelism, 2. have explicitly sequential semantics, 3. have an uncertain parallel implementation and for which we feel parallelization would be low priority.

For example, instead of parallelizing the standard heap algorithms, a better strategy may be to provide concurrent priority queues as a data structure as some have suggested.

13.1 Unchanged specialized algorithms from <memory>

- $\bullet\,$ No parallelism
 - addressof

13.2 Unchanged algorithms from <algorithm>

- No parallelism
 - iter_swap
 - $-\min$
 - max
 - minmax
- Uncertain / low priority
 - is_permutation
 - search
 - search_n
 - push_heap
 - pop_heap
 - make_heap
 - sort_heap
 - is_heap
 - is_heap_until
 - next_permutation
 - prev_permutation
- Explicitly sequential
 - copy_backward
 - move_backward
 - random_shuffle
 - shuffle

13.3 Unchanged generalized numeric operations from <numeric>

- Explicitly sequential
 - accumulate
 - partial_sum
 - iota