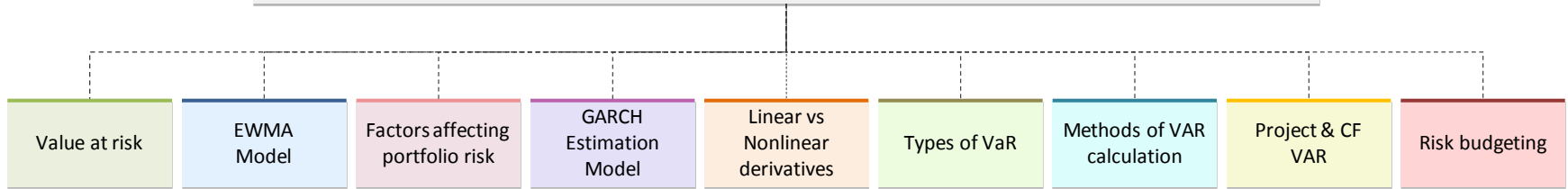


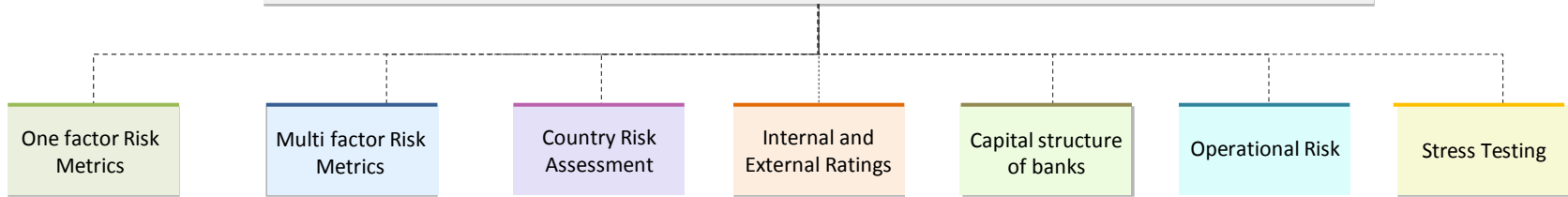
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## Valuation and Risk Models

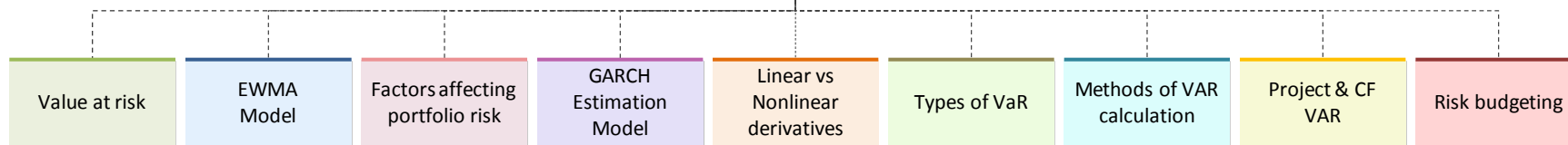
## Valuation and Risk Models (1/2)



## Valuation and Risk Models (2/2)



## Valuation and Risk Models (1/2)



### How to measure VAR

- **VaR** (daily VaR) (in%) =  $Z_{X\%} * \sigma$ 
  - $Z_{X\%}$ : the normal distribution value for the given probability (x%) (normal distribution has mean as 0 and standard deviation as 1)
  - $\sigma$ : standard deviation (volatility) of the asset (or portfolio)
- **VAR (X%) dollar basis** = VAR (X%) \* asset value
- **VAR for n days** using 1day VAR:  

$$VAR(X\%)_{n\text{-days}} = (VAR(X\%)_{1\text{-days}}) * \sqrt{n}$$

$$\sigma_{\text{port}} = \sqrt{(w_a^2 \sigma_a^2 + w_b^2 \sigma_b^2 + 2w_a w_b * \sigma_a * \sigma_b * \text{correlation}(a,b))}$$

$$VAR_{\text{port}} \text{ (daily VaR) (in\%)} = \sqrt{(w_a^2 (\%VaR_a)^2 + w_b^2 (\%VaR_b)^2 + 2w_a w_b * (VaR_a) * (\%VaR_b) * \sigma_{ab})}$$

$$\text{\$ VAR portfolio} = \sqrt{(\$VAR_a^2 + \$VAR_b^2 + 2\$VAR_a * \$VAR_b * \sigma_{a,b})}$$

$$\text{VAR of uncorrelated positions: } VAR_{\text{portfolio}} = \sqrt{VAR_1^2 + VAR_2^2}$$

**Q.**

A portfolio is composed of 2 securities. Calculate VAR at 95% confidence level.  
 Investment in security A & B are USD 1.5 mn and 3 mn respectively. Volatility of security A & B are 7% & 3% respectively. Correlation A & B is 10%

**Ans.**

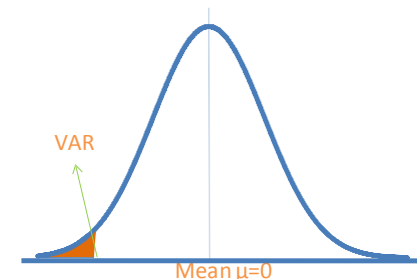
$$\begin{aligned} \sigma_{\text{portfolio}} &= \sqrt{(1/3)^2 (7\%)^2 + (2/3)^2 (3\%)^2 + 2 * (1/3) * (2/3) * 10\% * 7\% * 3\%} = 0.0316 \\ VAR &= 1.65 * 0.0316 * 4,500,000 = 234,630 \end{aligned}$$

**Value at Risk (VaR)** has become the standard measure that financial analysts use to quantify this risk. VAR represents maximum potential loss in value of a portfolio of financial instruments with a given probability over a certain horizon.

**Example:** The daily 5% VAR is \$10,000, it indicates that there is only 5% chance that on any given day, the portfolio will experience a loss of \$10,000 or more.

#### VAR Benefits:

- Aggregates all the risks in a portfolio into a single number provides an approach to arrive at economical capital.
- Relates capital with the expected losses
- Scaled to time



Approximately Normal Curve Representing VAR

The area under the normal curve for confidence value is:

Confidence (X%)	$Z_{X\%}$
90%	1.28
95%	1.65
97.5%	1.96
99%	2.32

**Q.**

If the assets has a daily  $\sigma$  of returns equal to 1.4% and asset has a current value of \$5.3 mn, calculate the VAR ( 5%) on both percentage & dollar basis.

**Ans.**

$$Z_{5\%} * \sigma = 1.65 * 1.4\% = 2.31\%, \text{ and } 0.0231 * \$5,300,000 = \$122,430$$

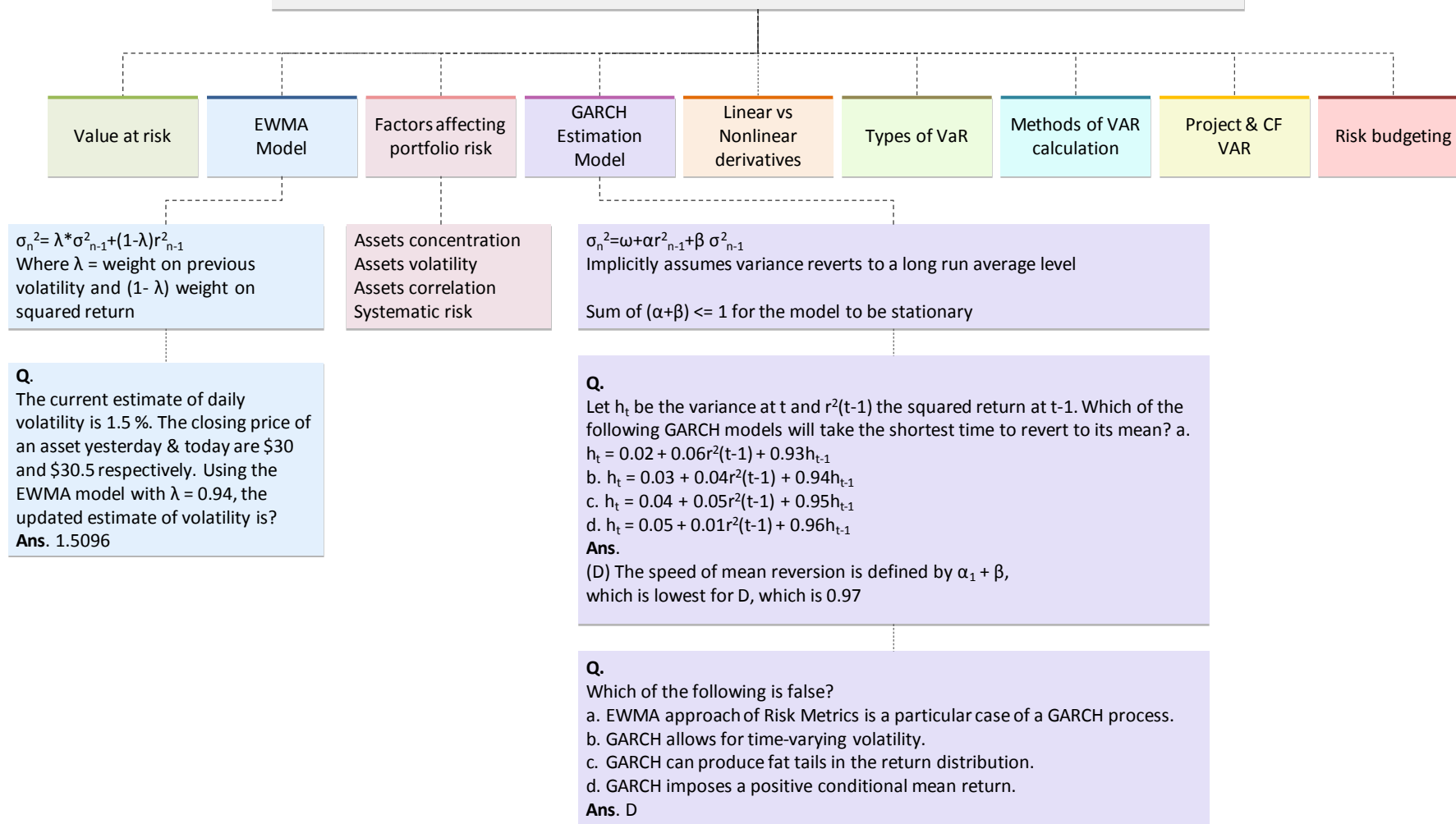
**Q.**

If the value of stock is 100 and the value of the put option at 110 is 20. 10 units change in the underlying brings in change of 4 units change in the option premium. If the annual volatility is 0.25. Calculate daily VaR at 97.5% assuming 250 days?

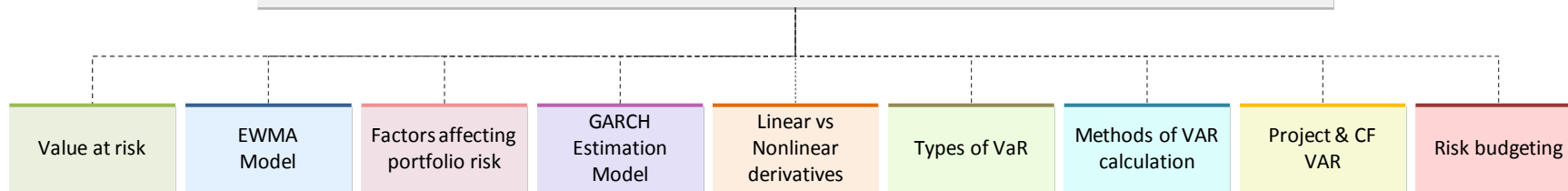
**Ans.**

$$\begin{aligned} \text{Delta} &= 0.4 & \text{STDEV(annual)} &= 0.25 \\ \text{Days} &= 50 \text{ daily} & \text{STDEV} &= 0.015811 \\ Z \text{ at } 97.5\% &= 1.96 \\ \text{Options Value} &= 20 \text{ units} & \text{VAR for option} &= 0.247923 \text{ units} \end{aligned}$$

## Valuation and Risk Models (1/2)



## Valuation and Risk Models (1/2)



Relationship b/w an underlying factor and the derivative's value are linear in nature

### VaR for Linear and Non Linear Derivatives

1. **Linear Assets:** When the value of the delta is constant for all changes in the underlying. Example: Forwards, futures.

Delta (1<sup>st</sup> derivative or duration in bonds) can be used to estimate the VAR for linear derivatives. **The delta-normal approach** (generally) does not work for portfolios of nonlinear securities.

**VAR Linear Derivative = Delta \* VAR Underlying risk factor**

2. **Non Linear Assets:** When the value of the delta keeps on changing with the change in the underlying asset. Examples: Options, Credit Derivatives, Swaps.

**Taylor Approximation:** large changes can be explained by the 2<sup>nd</sup> derivative i.e. gamma expected change in the delta of an option (or convexity in bonds). Taylor approximation is ineffective for callable bonds & mortgage backed securities.

**Q.**

A bond of \$10 mn, with modified duration of 3.6 yrs and annualized yield of 2%. calculate the 10 day holding period VaR of the position with 99% confidence interval, assuming there are 252 days in a year.

**Ans.**

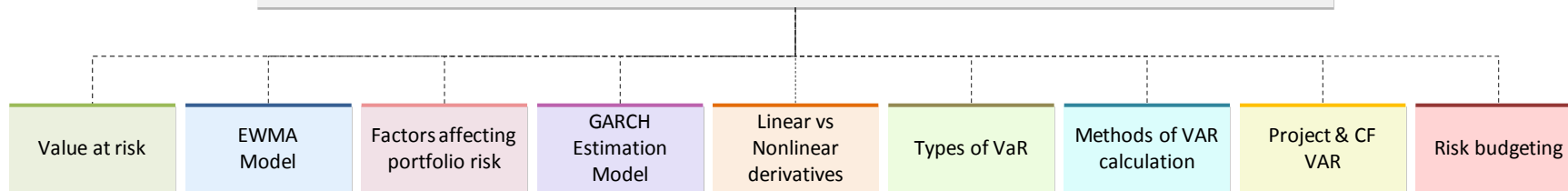
$$\text{VAR} = \$10,000,000 * 0.02 * 3.6 * [\sqrt{10} / (\sqrt{252})] * 2.33 = \$334,186$$

**Q.**

A 6 month call option with a strike price of \$10 is currently trading for \$1.41, the market price of the underlying stock is \$11. A 1% decrease in the stock to \$10.89 results in a 6.35% decrease in the call option with a value of \$1.32. If the annual volatility of the stock is  $s = 0.1975$  and the risk free rate of return is 5%, calculate the 1-day 5% VAR for this call option. **Ans.**

The daily volatility is  $= 1.25\% (0.1975 / \sqrt{250})$ ;  $\text{VAR}_{\text{stock}}(5\%) = 1.65 * 1.25\% = 2.06\%$ ;  
Delta of the call  $= 0.0635 / .01 = 6.35$ ;  $\text{VAR}_{\text{call}} = \Delta \text{VAR}_{\text{stock}} = 6.35 * 2.06\% = 13.1\%$ ,

## Valuation and Risk Models (1/2)



**Diversified VAR:** accounts for diversification effects.  
 $DVAR_p = z * \text{std dev} * \text{portfolio value}$   
 $= \sqrt{VAR_1^2 + VAR_2^2}$

**Undiversified VAR:** sum of the individual VARs for each risk factor. It assumes that all prices will move in the worst direction simultaneously, which is unrealistic.  
 $VAR_p$   
 $= \sqrt{VAR_1^2 + VAR_2^2 + 2VAR_1VAR_2}$   
 $= VAR_1 + VAR_2$

**Marginal VAR** is the change in VaR of the portfolio with one unit change in the components  
 $= DVAR * \beta_A / \text{portfolio value}$

**Incremental VAR:** The change in VAR from the addition of a new position in a portfolio.

**Component VAR** is the Amount a portfolio VAR would change by deleting either of the assets from a portfolio =  $DVAR * \beta_A * \text{weight of asset A}$ .

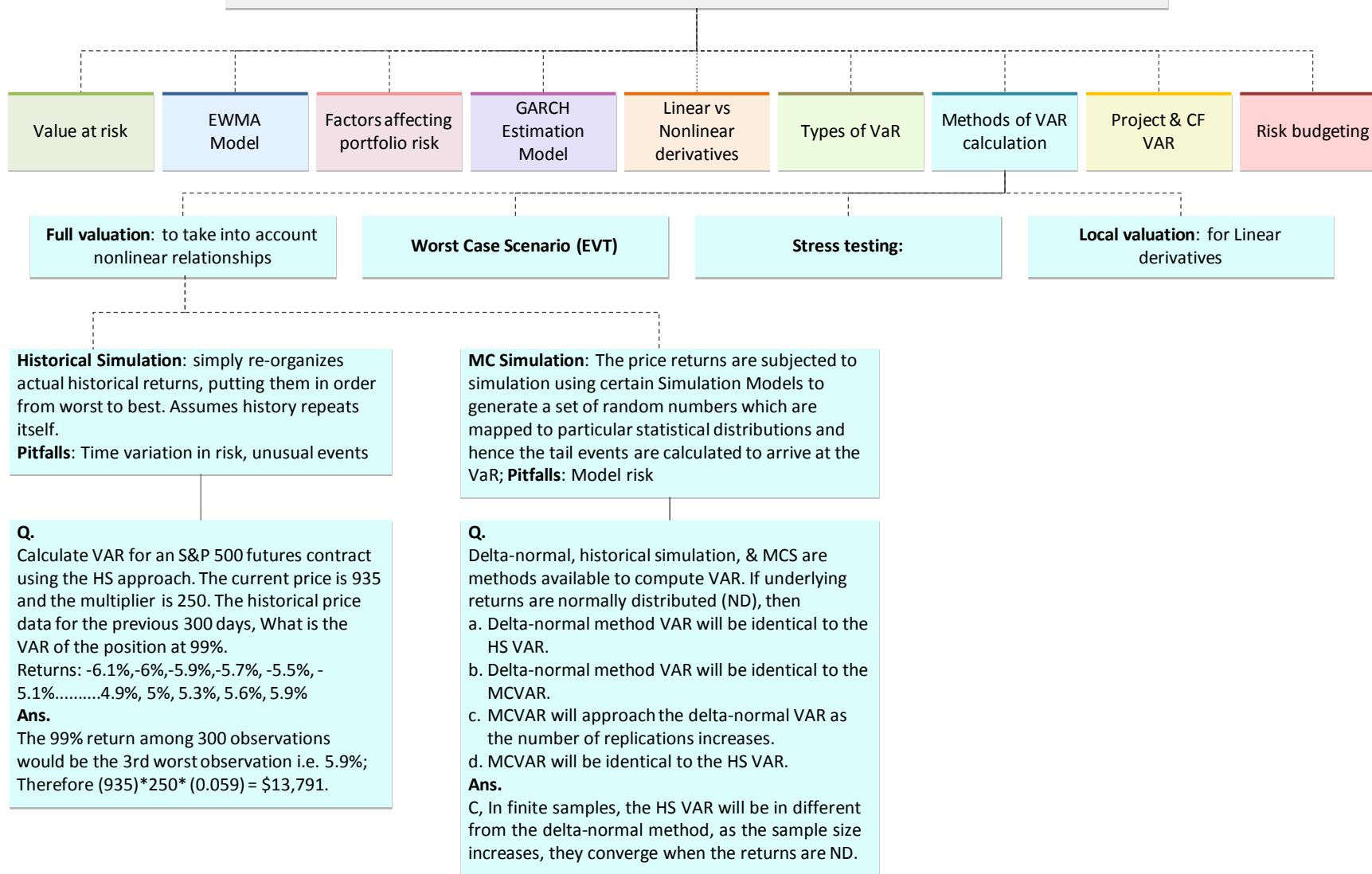
**Q.**  
 Weight of asset A & B are 0.6 & 0.4 in a portfolio. The value of the total portfolio is USD1 million and its  $\sigma$  is 0.060606; if the betas of asset A and asset B are 1.3 and 0.8 respectively, the respectively. What is the MVAR of Asset B and CVAR of Asset B at a 95%.

**Ans.**  
 $DVAR = 1.95 * 0.060606 * 1,000,000 = 99,999.90$   
 $MVAR = 99,999.90 * .8 / 1,000,000 = \$0.08$  CVAR  
 $= 99,999.90 * .8 * 0.4 = \$32,000.$

**Q.**  
 A portfolio has an equal amount invested in X and Y. The expected excess return of X is 9% and that of Y is 12%. The MVAR are 0.06 and 0.075 respectively. What should manager do to move towards the optimal portfolio?

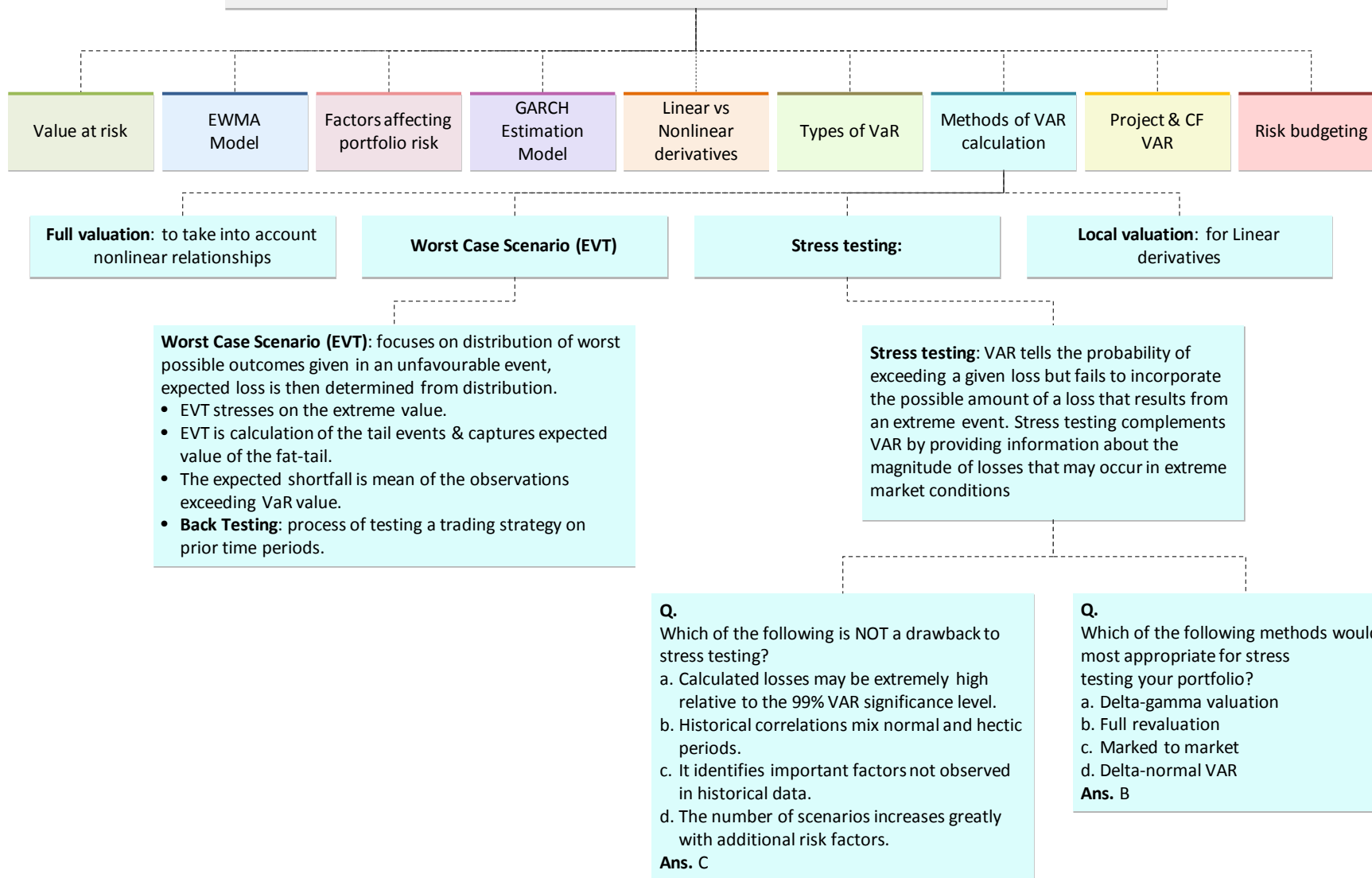
**Ans.**  
 The Expected excess Return ratio for X and Y are 1.5 and 1.6 respectively. Therefore portfolio weight in Y should increase to move the portfolio towards the optimal portfolio.

## Valuation and Risk Models (1/2)

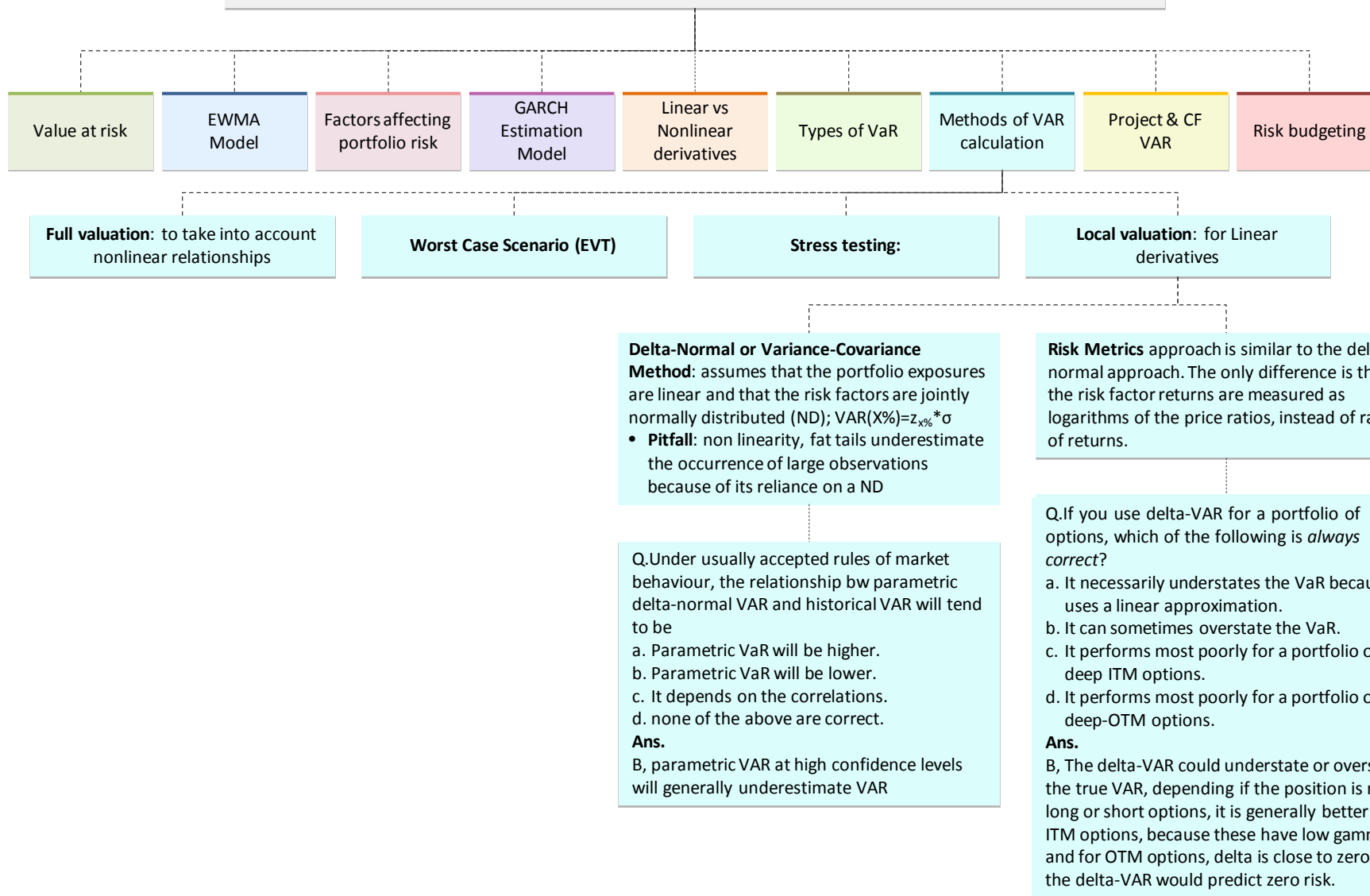




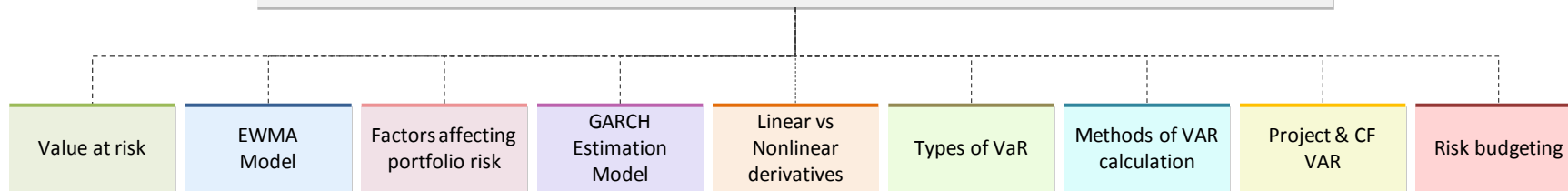
## Valuation and Risk Models (1/2)



## Valuation and Risk Models (1/2)



## Valuation and Risk Models (1/2)



**Cash Flow at Risk:** It is a measure of the expected cash flow at loss beyond a confidence level. If beta ( $\beta$ ) of an asset is  $\beta_x$  with the portfolio then the cash flow at risk (**CFAR**) =  $\beta_x \times \text{CFAR of portfolio}$ .

**Project VAR:** when considering a new project, you can explicitly calculate the dollar cost of the increase in CFAR and include it as an additional cost of the project.

**Q.**

A firm with existing projects have expected cash flow of \$100 mn and cash flow volatility of \$60 mn. New project with a cost of \$30 mn and cash flow volatility of \$20 mn. The correlation between two cash flows is 0.3. Calculate the volatility of the firm's projects with new projects at 95% confidence level and the additional project cost due to the increased cash flow volatility, if the cost of cash flow volatility is \$0.12.

**Ans.**

$\delta \text{ projects} = \sqrt{60^2 + 30^2 + 2 \times (.3) \times 60 \times 20} = \$68.7 \text{ mn}$

CFAR (at 5%) existing =  $1.65 \times 60 = \$99 \text{ mn}$

CFAR (at 5%) with new project =  $1.65 \times 68.7 = \$113.4 \text{ mn}$

The additional project cost due to increased cash flow volatility is:  $(\$113.4 \text{ mn} - \$99 \text{ mn}) \times .12 = \$1.73 \text{ mn}$

**Q.**

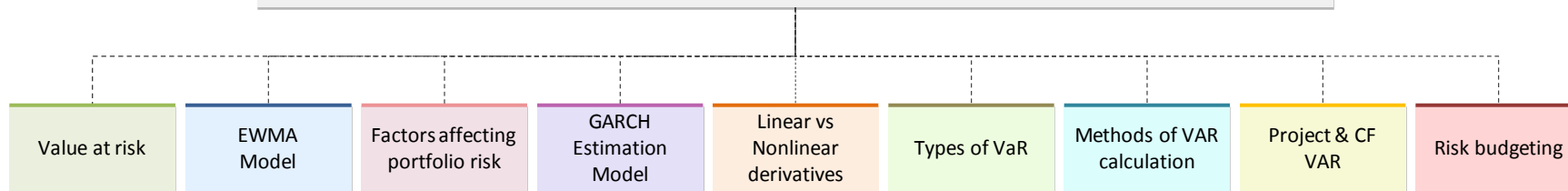
A trader has an allocation equal to 8% of the firm's capital; the beta of trader's return with the return of the firm is 0.90. The contribution of the trader to the Firm's VAR of \$120 million is:

- \$7.8 mn
- \$8.6mn
- \$9.6 mn
- \$10.8mn

**Ans.**

$0.08 \times 0.9 \times 120 \text{ million} = 8.64 \text{ million}$

## Valuation and Risk Models (1/2)



Risk Budgeting involves choosing and managing exposure to risk, 1<sup>st</sup> step is to determine the total amount of risk, as measured by VAR, Next is the optimal allocation of assets for that risk exposure.

**Funding Risk:** is the risk that the value of the assets will not be sufficient to cover the liabilities of the fund

**Q.**  
A Fund has \$200 mn in assets and \$180mn in liabilities. Expected return on the surplus, scales by assets is 4%, i.e. surplus is expected to grow by \$8 mn over 1st year. The volatility of surplus is 10%. Use  $Z = 1.65$ , what is the deficit with the loss associated with the VAR.  
**Ans.**  
Surplus =  $(200 - 180) = \$20$  mn, expected to grow by \$8 mn to a value of \$28 mn;  
 $VaR = 1.65 * 20 * 0.1 = \$33$  mn  
The deficit is:  $(33 - 28) = 5$  mn

**Risk Budgeting with Active Managers:** is done using Tracking error (Active Returns - benchmark return) & Information ratio (TE / volatility of managers TE)  
**Weight of portfolio managed by manager i**  
 $= IR_i * (\text{portfolio's tracking error volatility}) / IR_i * (\text{manager's tracking error volatility})$

**Q.**  
Determine the optimal weight ratio

	TE vol	Ratio	IR
Manager A	5%		0.70
Manager B	5%		0.50
Benchmark	0%		0.00
Portfolio	3%		0.82

**Ans.**  
A=51%, B=37% and remaining 12% in benchmark

## Valuation and Risk Models (2/2)

### One factor Risk Metrics

$$DV_{01} = \frac{-\Delta(\text{bond value})}{10000 \times \Delta(\text{interest rate})}$$

$$\text{convexity} = \frac{-1}{(\text{bond value})} \frac{d(\text{bond value})}{d(\text{interest rate})}$$

### Multi factor Risk Metrics

$$DV_{01}^k = \frac{-1}{10,000} \times \frac{\Delta(\text{bond value})}{\Delta(\text{key rate})}$$

$$D^k = \frac{-1}{(\text{bond value})} \times \frac{\Delta(\text{bond value})}{\Delta(\text{key rate})}$$

### Country Risk Assessment

### Internal and External Ratings

### Capital structure of banks

### Operational Risk

### Stress Testing

#### • Guidelines:

1. Politics can defy logic
2. Know your data sources
3. Question official statistics
4. Benefit from power of observation
5. Too much quantitative measures can be dangerous

#### Indicators used by rating agencies:

1. Macroeconomic performance
2. Public/external debt
3. External financing needs
4. Openness to trade and investment
5. Social pressures
6. Regime legitimacy

#### Country risk assessment in practice:

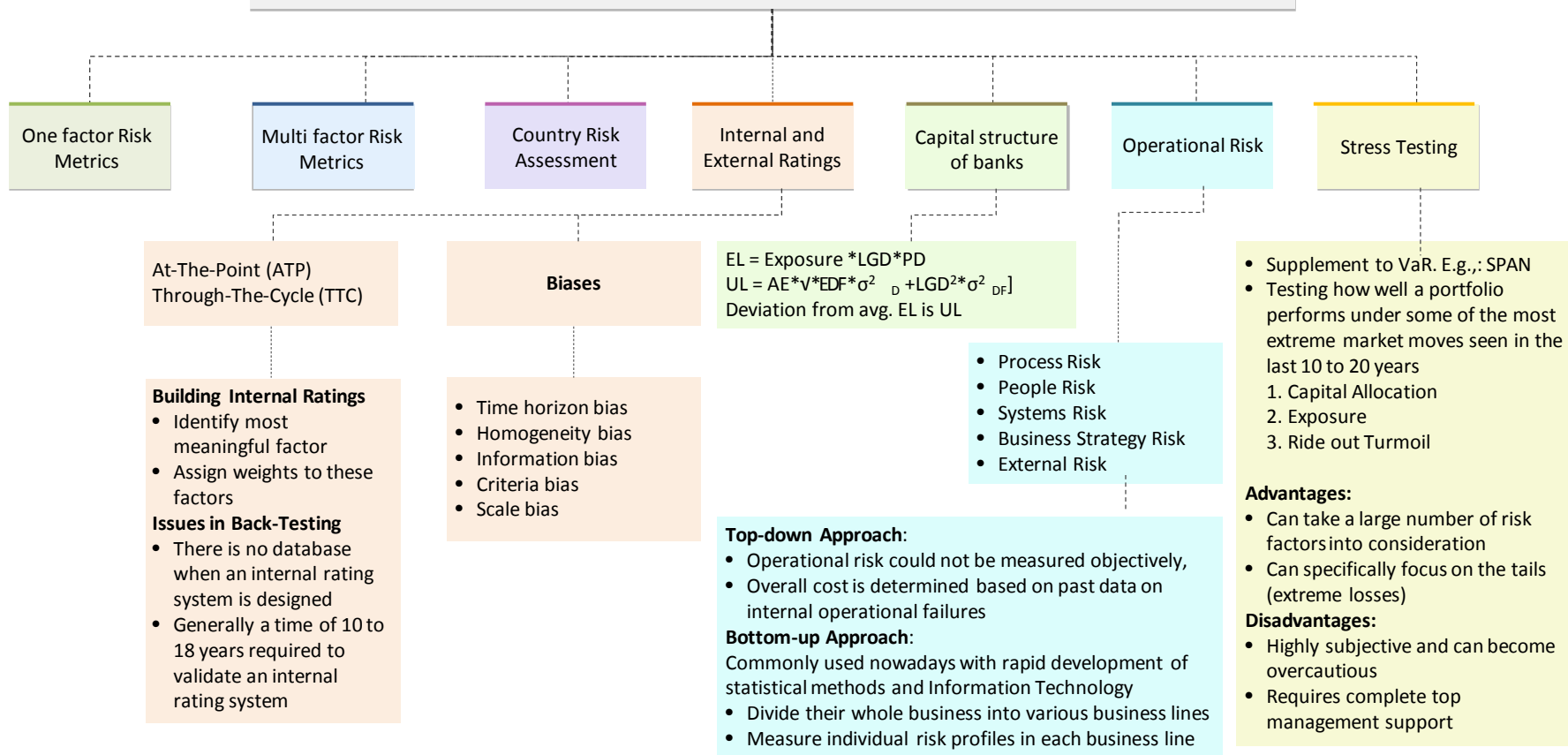
##### •Country risk management framework

1. Identify exposures
2. Analyze exposures
3. Analyze risk management techniques
4. Select appropriate risk management technique
5. Implement chosen technique
6. Monitor results/ revise program

#### Selecting tools:

1. Grade based rating scheme; listing risk and mitigants; measuring event probability (A,B..E); Categorize by number and color
2. Measuring economic measures for economic growth, economic health and power sector

## Valuation and Risk Models (2/2)



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# Thank you!

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