

# Advanced mixed-models workshop: Session 1

Dale Barr

University of Glasgow

Bremen March 2015

# Tentative schedule

## Today

	Start	End	Activity
1	09:00	10:30	Review / Overview
2	11:00	12:30	Dataset 1 (one factor)
3	13:30	15:00	Dataset 2 (multifactor)
4	15:30	17:00	Slack time / Q&A / BYOD*

## Tomorrow

	Start	End	Activity
1	09:00	10:30	Dataset 3 (GLMM)
2	11:00	12:30	Dataset 4 (multifactor GLMM)
3	13:00	15:00	Slack time / Q&A / BYOD*

\* Bring Your Own Data

# Repository for this workshop

If you have git installed, use:

```
git clone https://github.com/dalejbarr/bremen.git
```

or download full archive from:

<https://github.com/dalejbarr/bremen/archive/master.zip>

# General information on LMEMs

- Baayen (2008), *Analyzing Linguistic Data*
- Baayen, Davidson, & Bates (2008), *JML*
- Barr, Levy, Scheepers, Tily (2013), *JML*
- Barr (2013), *Frontiers in Psychology* (interactions)
- Bates et al. <http://arxiv.org/pdf/1406.5823.pdf> (technical)
- Bolker et al. (2009), *Trends in Ecology & Evolution*
- Westfall, Kenny, and Judd (2014), *JEP: General* (power)
- see also r-lang and r-sig-mixed-models mailing lists
- r-sig-mixed-models FAQ <http://glmm.wikidot.com/faq>
- add-on packages afex, pbkrcomp, lmerTest

# Simulated data

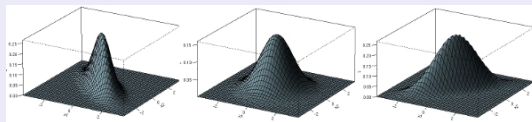
- single-factor within subject / between items
- IV: type of word, DV = lexical decision times

$$Y_{si} = \beta_0 + S_{0s} + I_{0i} + (\beta_1 + S_{1s})X_i + e_{si}$$

## Subjects

$$\langle S_{0i}, S_{1i} \rangle \sim N(\langle 0, 0 \rangle, \Sigma)$$

$$\Sigma = \begin{pmatrix} \tau_{00}^2 & \rho_I \tau_{00} \tau_{11} \\ \rho_I \tau_{00} \tau_{11} & \tau_{11}^2 \end{pmatrix}$$



## Items

$$I_{0i} \sim N(0, \omega_{00}^2)$$

# Define the data structures

```
library("MASS") # needed for mvrnorm

set.seed(11709)

nsubj <- 100
nitem <- 50 # must be an even number

#####
## create the data structures
subj <- data.frame(subject_id = 1:nsubj)

item <- data.frame(item_id = 1:nitem,
                   cond = rep(1:2, each = nitem / 2))

trial <- expand.grid(subject_id = 1:nsubj,
                    item_id = 1:nitem)
```

# Define parameters for data generation

```
#####  
## define parameters for data generation  
## first, fixed effects  
mu <- 800 # grand mean  
eff <- 80 # 80 ms difference  
effc <- c(-.5, .5) # deviation codes  
res_sd <- 200 # residual (standard deviation)  
iri <- 80 # by-item random intercept sd  
sri <- 100 # by-subject random intercept sd  
srs <- 40 # by-subject random slope sd  
rcor <- .2 # correlation between intercept and slope
```

# By-item random effects

```
## define item random effects variance  
## and sample items  
item$iri <- rnorm(nitem, mean = 0, sd = iri)  
  
## view the expected mean for each item  
## for a typical subject (random effs = 0)  
head(cbind(mu, eff[item$cond], item$iri,  
           mu + eff[item$cond] + item$iri), 3)
```

```
      mu  
[1,] 800 80 14.94782 894.9478  
[2,] 800 80 -86.30801 793.6920  
[3,] 800 80 -12.78345 867.2165
```



# By-subject random effects

```
## define subject random effects variance
## variance co-variance matrix
svcov <- matrix(c(sri^2,
                  rcor * sri * srs,
                  rcor * sri * srs,
                  srs^2), nrow = 2)

## sample subjects
srfx <- mvrnorm(nsubj, mu = c(0, 0), Sigma = svcov)

subj$sri <- srfx[, 1]
subj$srs <- srfx[, 2]

head(subj, 3)
```

	subject_id	sri	srs
1	1	-80.025967	-0.7625934
2	2	44.612596	54.5130100
3	3	8.744992	-20.4295562

# Pull it all together

```
dat <- merge(merge(subj, trial), item)
dat <- dat[order(dat$subject_id, dat$item_id), ] # sort
dat$err <- rnorm(nrow(dat), sd = res_sd) # trial-level noise
dat$Y <- with(dat,
  mu + sri + iri + (eff + srs) * effc[cond] + err)

head(dat)
```

	item_id	subject_id	sri	srs	cond	iri	err	Y
1	1	1	-80.02597	-0.7625934	1	14.94782	382.34441	1077.6476
173	2	1	-80.02597	-0.7625934	1	-86.30801	283.44878	877.4961
235	3	1	-80.02597	-0.7625934	1	-12.78345	30.35586	697.9277
390	4	1	-80.02597	-0.7625934	1	-13.91040	-282.01806	384.4269
414	5	1	-80.02597	-0.7625934	1	55.61871	-238.73081	497.2432
513	6	1	-80.02597	-0.7625934	1	-45.92916	73.42391	707.8501

# Decomposition matrix

$$Y_{si} = \beta_0 + S_{0s} + I_{0i} + (\beta_1 + S_{1s})X_i + e_{si}$$

Attaching package: 'dplyr'

The following object is masked from 'package:MASS':

```
select
```

The following object is masked from 'package:stats':

```
filter
```

The following objects are masked from 'package:base':

```
intersect, setdiff, setequal, union
```

Source: local data frame [16 x 11]

	sid	iid	c	Y	mu	sri	iri	eff	srs	x
1	1	1	1	1077.6476	800	-80.025967	14.94782	80	-0.7625934	-0.5
2	1	2	1	877.4961	800	-80.025967	-86.30801	80	-0.7625934	-0.5
3	1	26	2	637.6155	800	-80.025967	-65.44482	80	-0.7625934	0.5
4	1	27	2	808.4316	800	-80.025967	171.89799	80	-0.7625934	0.5
5	2	1	1	533.2496	800	44.612596	14.94782	80	54.5130100	-0.5
6	2	2	1	930.9572	800	44.612596	-86.30801	80	54.5130100	-0.5

# Fitting the model

```
library("lme4")  
dat$c <- dat$cond - mean(dat$cond)  
mod <- lmer(Y ~ c + (1 + c | subject_id) + (1 | item_id),  
            dat, REML = FALSE)
```

Loading required package: Matrix

Loading required package: Rcpp

# Viewing results

Linear mixed model fit by maximum likelihood ['lmerMod']

Formula:  $Y \sim c + (1 + c \mid \text{subject\_id}) + (1 \mid \text{item\_id})$

Data: dat

AIC	BIC	logLik	deviance	df.resid
67635.0	67680.6	-33810.5	67621.0	4993

Scaled residuals:

Min	1Q	Median	3Q	Max
-3.8927	-0.6637	-0.0136	0.6749	3.7872

Random effects:

Groups	Name	Variance	Std.Dev.	Corr
subject_id	(Intercept)	9467	97.30	
	c	1254	35.42	0.32
item_id	(Intercept)	7767	88.13	
Residual		40119	200.30	

Number of obs: 5000, groups: subject\_id, 100; item\_id, 50

Fixed effects:

	Estimate	Std. Error	t value
(Intercept)	793.29	16.06	49.38
c	112.10	25.81	4.34