



$2 \uparrow\uparrow 4 = 2^{2^{2^2}} = 65536$   
 $2 \uparrow\uparrow\uparrow 4 = 2 \uparrow\uparrow (2 \uparrow\uparrow (2 \uparrow\uparrow 2))$

$G = 3 \uparrow \dots \uparrow 3$   
 $3 \uparrow \dots \uparrow 3$   
 $\vdots$   
 $3 \uparrow \dots \uparrow 3$   
 $3 \uparrow\uparrow\uparrow 3$

64 layers

Diagram illustrating the construction of a 64-layer GNN. The input graph is a 3D cube. The graph structure is expanded into a sequence of layers, showing the iterative application of the graph operation  $G = 3 \uparrow \dots \uparrow 3$  (repeated 3 times) and the final layer  $3 \uparrow \uparrow \uparrow \uparrow 3$  (repeated 3 times), resulting in a total of 64 layers.

Diagram illustrating the construction of a 64-layer GNN. The left side shows a 3D cube structure with vertices and edges, colored in purple and yellow. The right side shows a graph structure with 64 layers. The top layer is labeled  $G = 3 \uparrow \dots \uparrow 3$ . Below it, there are three more layers, each labeled  $3 \uparrow \dots \uparrow 3$ . The bottom layer is labeled  $3 \uparrow \uparrow \uparrow \uparrow 3$ . A large bracket on the right indicates that there are 64 layers in total.

$2 \uparrow \uparrow 4 = 2^{2^2} = 65536$   
 $2 \uparrow \uparrow \uparrow 4 = 2 \uparrow \uparrow (2 \uparrow \uparrow 2 \uparrow \uparrow 2)$

$G = 3 \uparrow \dots \uparrow 3$   
 $3 \uparrow \dots \uparrow 3$   
 $\vdots$   
 $3 \uparrow \dots \uparrow 3$   
 $3 \uparrow \uparrow \uparrow 3$

64 layers

$2 \uparrow\uparrow 4 = 2^{2^{2^2}} = 65536$   
 $2 \uparrow\uparrow\uparrow 4 = 2 \uparrow\uparrow (2 \uparrow\uparrow (2 \uparrow\uparrow 2))$

Diagram illustrating the construction of a 64-layer GNN. The graph structure is shown as a stack of layers, with the top layer labeled  $G = 3 \uparrow \dots \uparrow 3$  and the bottom layer labeled  $3 \uparrow \uparrow \uparrow \uparrow 3$ . The layers are grouped by braces, indicating a total of 64 layers.

Diagram illustrating the construction of a 64-layer GNN. The input graph is a 3D cube. The graph structure is expanded into a sequence of layers, showing the iterative application of the  $G$  operation. The layers are grouped into three sets of three layers each, plus a final layer, totaling 64 layers.

Diagram illustrating the construction of a 64-layer GNN. The structure is defined by the following equations and layer counts:

$$2 \uparrow \uparrow 4 = 2^{2^{2^2}} = 65536$$

$$2 \uparrow \uparrow \uparrow 4 = 2 \uparrow \uparrow (2 \uparrow \uparrow (2 \uparrow \uparrow 2))$$

The diagram shows a stack of layers, with the total number of layers being 64. The layers are grouped into four sets of 16 layers each, each set corresponding to one of the equations above.

Diagram illustrating the construction of a 64-layer GNN. The input graph is a 3D cube. The layers are grouped into four sets of 16 layers each, with the first set labeled  $2 \uparrow\uparrow 4 = 2^{2^2} = 65536$  and the last set labeled  $2 \uparrow\uparrow\uparrow 4 = 2 \uparrow\uparrow (2 \uparrow\uparrow (2 \uparrow\uparrow 2))$ .