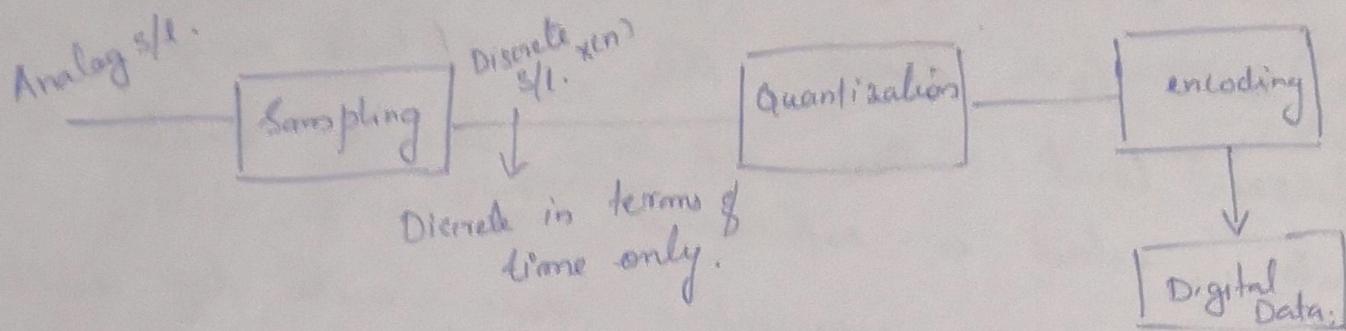


Quantization



we can represent analog signal as

$$x(t) = \sin 2\pi f t \rightarrow \text{here } t \text{ can take any values}$$

such as $\dots, -1, -1.1, -1.12, -1.13 \dots$

Discrete S/I

$$x(n) = \sin(2\pi f n T_s) \rightarrow \text{here } n \text{ take the values}$$

$n = 1, 2, 3 \dots$

But these discrete signals are continuous in amplitude.
In order to store in digital systems it is very compulsory
to map the amplitude into fixed magnitudes. For that
we do quantization.

Quantization is the process of converting continuous
amplitude S/I into discrete amplitude. we can
also say it as approximation or rounding off.

therefore output of quantizer will be a digital S/I
which is discrete in time and amplitude.

This quantised digital S/I will be encoded in the
next stage of digital communications.

Consider a continuous s/e with amplitude range $[x_{\min}, x_{\max}] \Rightarrow$ dynamic range.

We have to divide this amplitude range into reference levels. These are the discrete amplitude levels; which is represented by no: of bits.

Suppose we are representing these levels by 2 bits $\therefore n = 2$ bit.

\therefore no: of quantized level (Δ^2)

$$L = 2^2 = 4 \text{ levels}$$

So total amplitude range is divided into 4 reference levels.

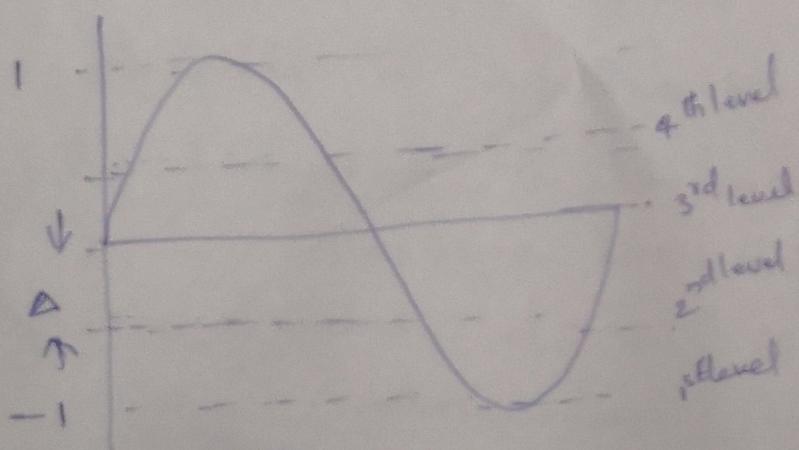
These 4 quantized levels are defined by step size Δ

($\Delta \rightarrow$ difference b/w 2 quantization levels).

Δ can be expressed as

$$\Delta = x_{\max} - x_{\min}$$

$$\frac{1}{L}$$



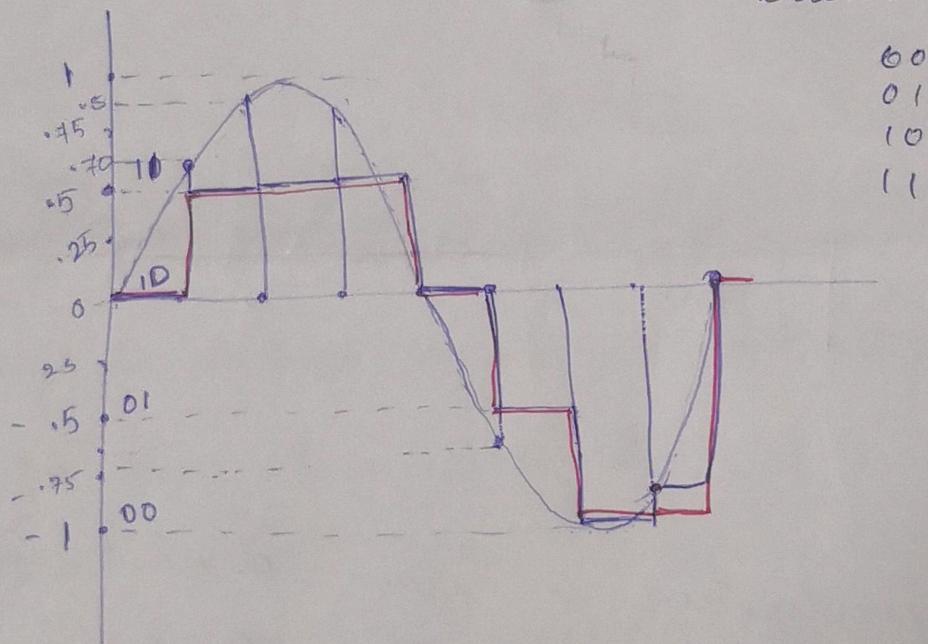
Step size

$$\Delta = \frac{1 - -1}{4} = \frac{2}{4} = \frac{1}{2}$$

$$\therefore \Delta = 0.5$$

So the ^{reference} difference levels are defined at .5 intervals of amplitude.
we have to choose the nearest reference levels to define quantized magnitudes of amplitude.

Here 4 levels are encoded by 2 bits



x = sample value

x_q = quantized value

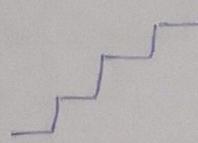
$$\text{Quantized error } \epsilon_q = x_q - x$$

Digital signal

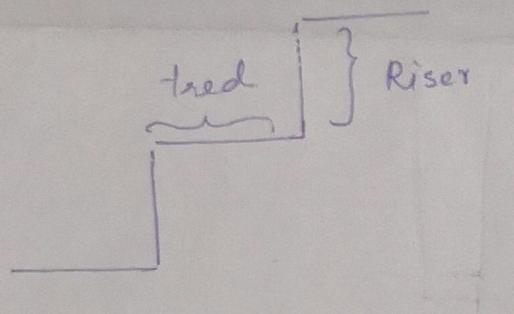
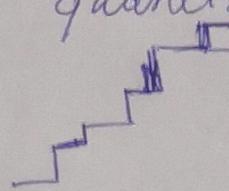
0	0.70	0.8	+0.75
0	0.5	0.5	-0.5
0	-0.2	-0.3	-0.25
10	10	10	01

Depending upon the length of the step size we can divide the quantization in to two classes.

1) uniform quantization : In this the step size Δ is constant along the quantization process



(2) Non uniform quantization: In this step size will vary

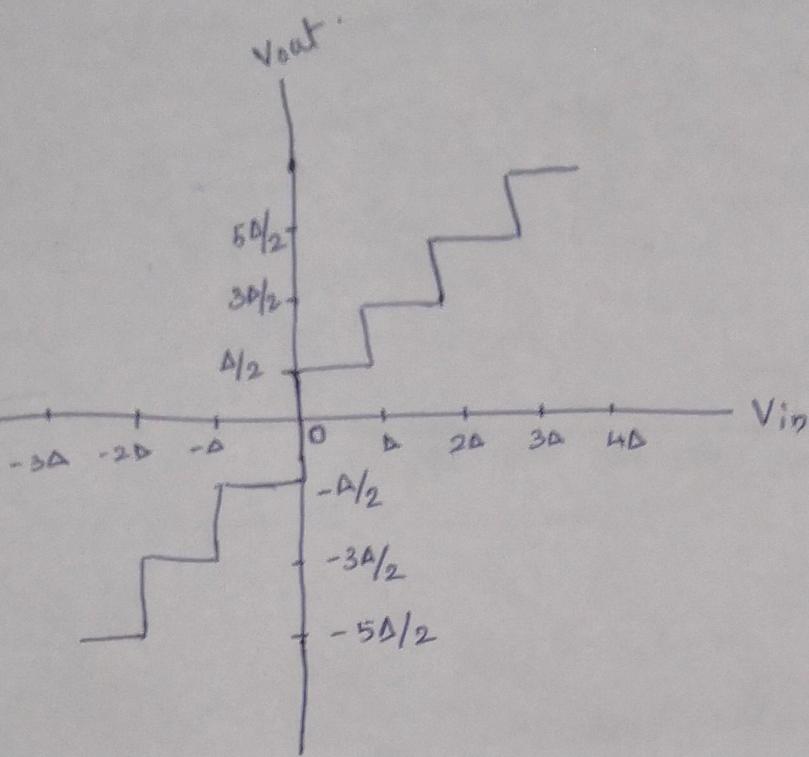


Uniform quantization is again divided in to two according to the characteristics drawn

Mid tread quantization \Rightarrow Origin lies at the centre of the tread.

Mid riser quantization \Rightarrow Origin lies at the centre of the riser.

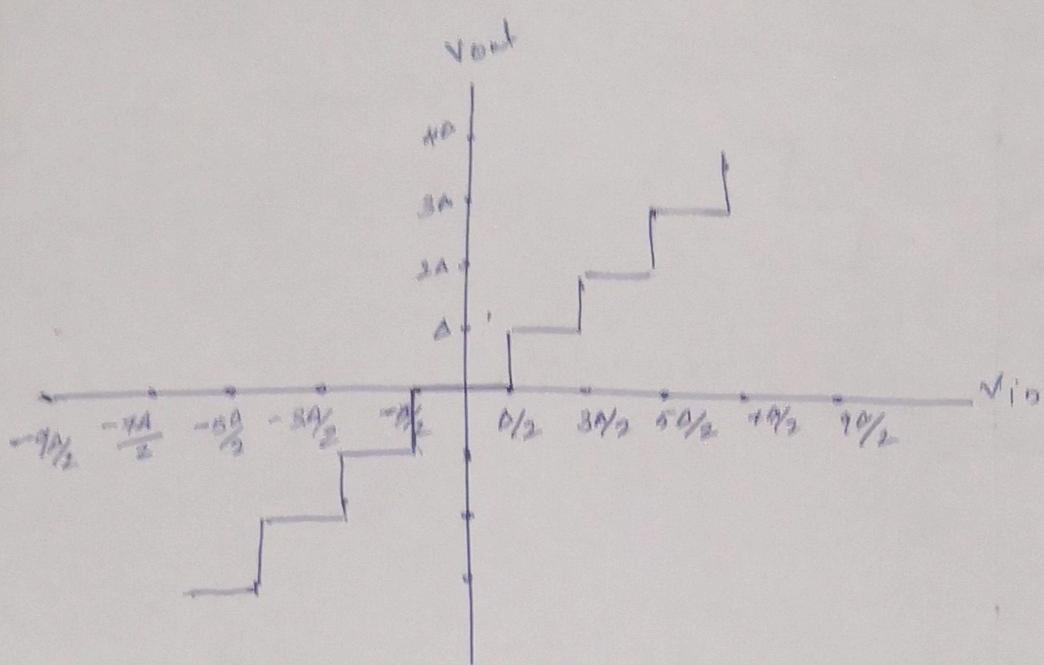
Midrise Quantisation



From the figure we can know that when input is between 0 and Δ output is $\Delta/2$ when input is between Δ and 2Δ output is $\frac{3\Delta}{2}$.

From the fig it is clear that it is rising at the zero i.e., at zero it has a transition. There is no level which is denoted by zero.

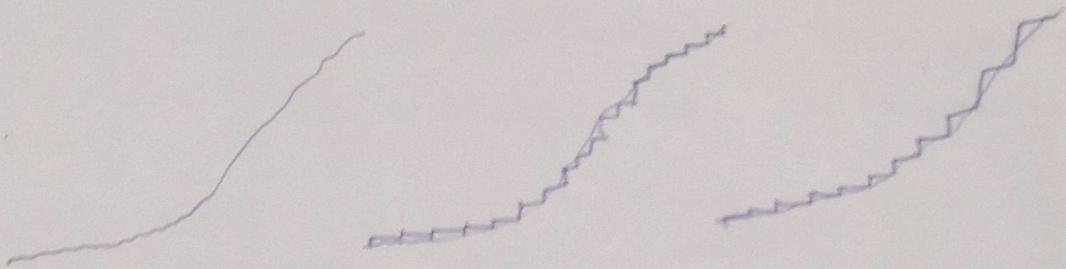
Mid Trd quantization



from the graph when V_{in} is between $-A/2$ and $A/2$
output is 0
~~when~~ so here 0 is a level of output.

Non uniform quantisation

Non uniform quantization means step size is variable. if we consider a signal which is varying slowly at a time and varying quickly some other time.



if we are using small steps everywhere we have to use more no. of bits to represent it.

so if we denote the smaller variations with small stepsize and faster variations with larger stepsize it will no. of levels will be reduced so no. of bits used to denote it can be reduced -

This is non uniform quantization.

Non uniform quantization is achieved by companding; which is a nonlinear mapping of input to the output.