
Example 6.17 Using frequency sampling method, design a bandpass filter with the following specifications.

sampling frequency $F = 8000\text{Hz}$

cut off frequencies $f_{c1} = 1000\text{Hz}$

$f_{c2} = 3000\text{Hz}$

Determine the filter coefficients for $N = 7$.

Solution

$$\begin{aligned}\omega_{c1} &= 2\pi f_{c1} T = \frac{2\pi f_{c1}}{F} = \frac{2\pi(1000)}{8000} \\ &= \frac{\pi}{4}\end{aligned}$$

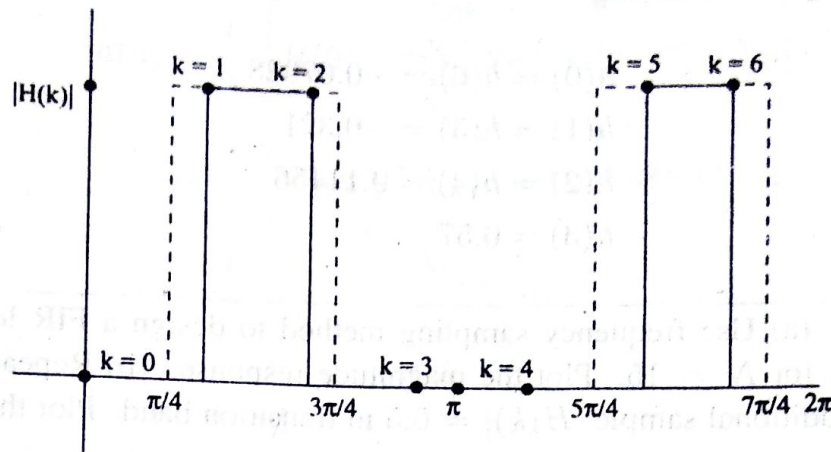


Fig. 6.61 Ideal magnitude response with samples for example 6.17

$$\begin{aligned}\omega_{c2} &= 2\pi f_{c2}T = \frac{2\pi f_{c2}}{F} = \frac{2\pi(3000)}{8000} \\ &= \frac{3\pi}{4}\end{aligned}$$

$$H(k) = H_d(e^{j\omega}) \Big|_{\omega = \frac{2\pi}{7}k} \quad k = 0, 1, \dots, 6$$

$$\begin{aligned}|H(k)| &= 0 && \text{for } k = 0, 3 \\ &= 1 && \text{for } k = 1, 2 \\ \theta(k) &= -\left(\frac{N-1}{N}\right)\pi && \text{for } 0 \leq k \leq \frac{N-1}{2} \\ &= -\frac{6}{7}\pi k && \text{for } 0 \leq k \leq 3 \\ H(k) &= 0 && \text{for } k = 0, 3 \\ &= e^{-j6\pi k/7} && \text{for } k = 1, 2\end{aligned}$$

The filter coefficients are given by

$$\begin{aligned}h(n) &= \frac{1}{N} \left[H(0) + 2 \sum_{k=1}^{\frac{N-1}{2}} \text{Re}(H(k)e^{j2\pi kn/N}) \right] \\ &= \frac{1}{7} \left[2 \sum_{k=1}^3 \text{Re}(e^{-j6\pi k/7} e^{j2\pi kn/7}) \right] \\ &= \frac{1}{7} \left[2 \sum_{k=1}^2 \cos \frac{2\pi k}{7} (3-n) \right] \\ &= \frac{2}{7} \left[\cos \frac{2\pi}{7} (3-n) + \cos \frac{4\pi}{7} (3-n) \right]\end{aligned}$$

$$h(0) = h(6) = -0.07928$$

$$h(1) = h(5) = -0.321$$

$$h(2) = h(4) = 0.11456$$

$$h(3) = 0.57$$