EE5175: Image Signal Processing

Lab-8

- 1. Assume a Markov-1 process with covariance matrix R of size 8×8 and $\rho = 0.91$. Compute the Energy Packing Efficiency and De-correlation Efficiency of the Walsh-Haddamard Transform and Discrete Cosine Transform for the above process. What is your observation about the eigenvectors of R in relation to the DCT basis?
- 2. Find $\beta^2 R^{-1}$, where $\beta^2 = \frac{1-\rho^2}{1+\rho^2}$. Does $\beta^2 R^{-1}$ have a tridiagonal structure?. Is it close to the tridiagonal matrix Q given by,

$$\mathbf{Q} = \begin{bmatrix} 1 - \alpha & -\alpha & 0 & 0 & 0 & 0 & 0 & 0 \\ -\alpha & 1 & -\alpha & 0 & 0 & 0 & 0 & 0 \\ 0 & -\alpha & 1 & -\alpha & 0 & 0 & 0 & 0 \\ 0 & 0 & -\alpha & 1 & -\alpha & 0 & 0 & 0 \\ 0 & 0 & 0 & -\alpha & 1 & -\alpha & 0 & 0 \\ 0 & 0 & 0 & 0 & -\alpha & 1 & -\alpha & 0 \\ 0 & 0 & 0 & 0 & 0 & -\alpha & 1 & -\alpha \\ 0 & 0 & 0 & 0 & 0 & 0 & -\alpha & 1 - \alpha \end{bmatrix}$$

where $\alpha = \frac{\rho}{1 + \rho^2}$

Try diagonalizing $\beta^2 R^{-1}$ and Q using the DCT matrix. What is your observation.?

- 3. Compute SVD for the given 8×8 image **g** (provided in imageFile.mat and also given below) using the following steps:
 - (a) Perform eigen-value decomposition of $\mathbf{g}^T\mathbf{g}$ and $\mathbf{g}\mathbf{g}^T.$
 - (b) Find the singular value matrix Σ .
 - (c) Reconstruct the image using Σ and the eigen-vector matrices.
- 4. Remove one singular value at a time from Σ and reconstruct the image $(\widehat{\mathbf{g}_k})$. Compute $\|\mathbf{g} \widehat{\mathbf{g}_k}\|^2$ and compare it with the sum of the squares of the first k singular values.

| Image $\mathbf{g} =$ | 207 | 244 | 107 | 173 | 70 | 111 | 180 | 244 |
|----------------------|-----|-----|-----|-----|-----|-----|-----|-----|
| | 230 | 246 | 233 | 193 | 11 | 97 | 192 | 86 |
| | 3 | 40 | 202 | 189 | 24 | 195 | 70 | 149 |
| | 232 | 247 | 244 | 100 | 209 | 202 | 173 | 57 |
| | 161 | 244 | 167 | 167 | 177 | 47 | 167 | 191 |
| | 24 | 123 | 9 | 43 | 80 | 124 | 41 | 65 |
| | 71 | 204 | 216 | 180 | 242 | 113 | 30 | 129 |
| | 139 | 36 | 238 | 8 | 8 | 164 | 127 | 178 |

 $-\mathrm{end}-$