Vector Algebra

12^{th} Maths - Chapter 10

This is Problem-3 from Exercise 10.4

1. A girl walks 4 km towards west, then she walk 3 km in a direction 30° east of north and stops. Determine the girl's displacement from her initial point of departure.

Solution: Let initial point, middle point, final point be A, B and C respectively. Let initial point be the origin,

$$\mathbf{A} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \tag{1}$$

Now, girl walks 4km towards west A-B then,

$$\mathbf{A} \cdot \mathbf{B} = \begin{pmatrix} -4\\0 \end{pmatrix} \tag{2}$$

Then girl walks 3 km in the direction 30° east of north

$$\mathbf{B-C} = \begin{pmatrix} 3\cos 60^{\circ} \\ 3\sin 60^{\circ} \end{pmatrix} \tag{3}$$

$$= \begin{pmatrix} \frac{3}{2} \\ \frac{3\sqrt{3}}{2} \end{pmatrix} \tag{4}$$

By triangle law of vector addition, we have

$$\mathbf{A} \cdot \mathbf{C} = \mathbf{A} \cdot \mathbf{B} + \mathbf{B} \cdot \mathbf{C} \tag{5}$$

$$= \begin{pmatrix} -4\\0 \end{pmatrix} + \begin{pmatrix} \frac{3}{2}\\\frac{3\sqrt{3}}{2} \end{pmatrix} \tag{6}$$

$$= \begin{pmatrix} \frac{-5}{2} \\ \frac{3\sqrt{3}}{2} \end{pmatrix} \tag{7}$$

Hence, the girl's displacement from her initial point of departure is

$$\begin{pmatrix} \frac{-5}{2} \\ \frac{3\sqrt{3}}{2} \end{pmatrix} \tag{8}$$

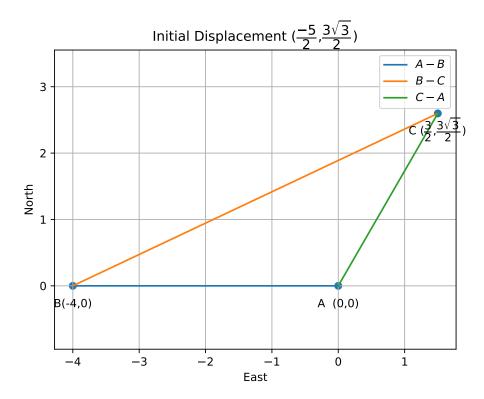


Figure 1