Circles

10^{th} Maths - Chapter 10

This is Problem-3 from Exercise 1

1. A tangent PQ at a point P of a circle of radius 5 cm meets a line through the centre O at a point Q so that OQ = 12 cm. Length PQ is

Solution:

The input parameters for this problem are available in Table (1)

Symbol	Value	Description
r	5	Radius of the Circle
О	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$	Centre of the circle
OP	5	Length of OP
OQ	12	Lenght of OQ
PQ	?	Length of PQ

Table 1

Since PQ is a tanget then

$$\mathbf{OP} \perp \mathbf{PQ}$$
 (1)

Then $\triangle \mathbf{OPQ}$ is a right angle triangle

$$\mathbf{OQ}^2 = \mathbf{OP}^2 + \mathbf{PQ}^2 \tag{2}$$

$$\mathbf{PQ} = \sqrt{\mathbf{OQ}^2 - \mathbf{OP}^2} \tag{3}$$

$$\mathbf{PQ} = \sqrt{114 - 25} \tag{4}$$

$$\mathbf{PQ} = \sqrt{119} \tag{5}$$

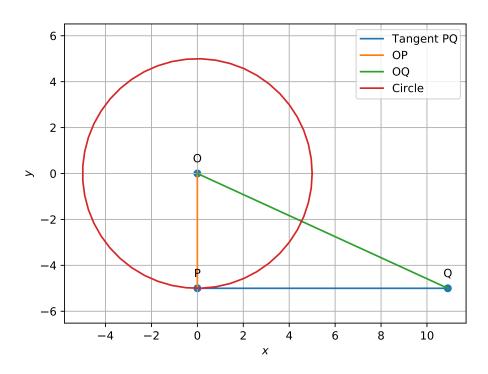


Figure 1