Straight Lines

11^{th} Maths - Chapter 10

This is Problem-3 from Exercise 10.2

1. Find the equation of line passing through $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$ with slope m.

Solution: Line passing through point $\mathbf{A} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$ is given by,

$$\mathbf{n}^{\top} \left(\mathbf{x} - \mathbf{A} \right) = 0 \tag{1}$$

Where,

$$\mathbf{n} = \begin{pmatrix} m \\ -1 \end{pmatrix} \tag{2}$$

$$\mathbf{n}^{\top} = \begin{pmatrix} m & -1 \end{pmatrix} \tag{3}$$

Substituting \mathbf{A} and \mathbf{n} in equation (1)

$$\begin{pmatrix} m & -1 \end{pmatrix} \begin{pmatrix} \mathbf{x} - \begin{pmatrix} 0 \\ 0 \end{pmatrix} \end{pmatrix} = 0 \tag{4}$$

$$(m -1) \mathbf{x} - 0 = 0$$

$$(m -1) \mathbf{x} = 0$$

$$(6)$$

$$\begin{pmatrix} m & -1 \end{pmatrix} \mathbf{x} = 0 \tag{6}$$

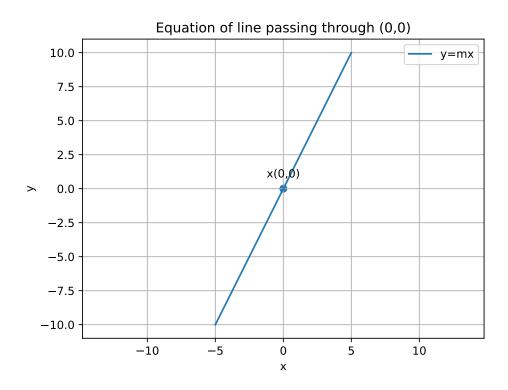


Figure 1