

The impact of cosmic variance on simulating weak lensing surveys

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ABSTRACT

According to our current understanding, galaxy shapes and morphologies should depend on various factors such as the local environment. Realistic image simulations for calibration of weak lensing analysis methods that use training samples from the Hubble Space Telescope can therefore be affected by these trends, due to the limited volume of the universe that has been surveyed by Hubble. We will show how redshift slices in a volume-limited subsample of COSMOS can be classified as overdense or underdense (or neither), and how the statistical properties of various morphological parameters such as ellipticity, Sérsic n , Bulge-to-Total ratio and color differ in these bins. This study requires a careful distinction between environment effects from large-scale structure, which we do not wish to include in simulations, and general trends in the galaxy population with redshift. We conclude with some guidance for how upcoming surveys can use COSMOS data as the basis for weak lensing simulations without having their conclusions overly affected by cosmic variance. **I have some comments on this abstract, but prefer to do all revision of the abstract at the end once the paper is finalized.**

Key words: Gravitational lensing: weak — Cosmology: Large-scale structure of Universe — Galaxies: evolution.

1 INTRODUCTION

Weak gravitational lensing, the deflection of light by mass, is one of the cleanest ways to study the nature of dark energy by tracking the growth of structure in the Universe as a function of time (e.g., Bartelmann & Schneider 2001; Albrecht et al. 2006; Weinberg et al. 2013). As light from background sources passes by matter (including dark matter) on its way to us, the apparent shapes of the background galaxies get distorted, and the galaxies get slightly magnified as well. Because of its sensitivity to dark matter and dark energy, major surveys such as the Hyper Suprime-Cam (HSC; Miyazaki et al. 2006), Dark Energy Survey (DES; The Dark Energy Survey Collaboration 2005), the Kilo-Degree Survey (KIDS; de Jong et al. 2013), the Panoramic Survey Telescope and Rapid Response System (PanSTARRS; Kaiser et al. 2010), the Large Synoptic Survey Telescope (LSST; LSST Science Collaboration et al. 2009), Euclid¹ (Laureijs et al. 2011), and Wide-Field Infrared Survey Telescope (WFIRST; Green et al. 2012) are

planned for the next two decades to gather enormous quantities of weak lensing data that will lead to precise constraints on the growth of structure with time, and therefore cosmological parameters.

For the upcoming surveys to achieve their promise, their systematic error budgets must be below their statistical error budgets. Systematic error budgets for weak lensing surveys typically include astrophysical effects, such as intrinsic alignments of galaxy shapes with large scale density fields (e.g., Troxel & Ishak 2014) and the effect of baryons on the matter power spectrum (e.g., van Daalen et al. 2011), as well as observational uncertainties such as the ability to robustly infer shears from galaxy observed shapes or photometric redshifts from their observed colors. Given the expected sub-per cent errors on upcoming surveys, systematic errors must be reduced from their typical level in the current state-of-the-art measurements that typically achieve ~ 5 per cent statistical errors at best (e.g., Schrabback et al. 2010; Heymans et al. 2013; Jee et al. 2013; Mandelbaum et al. 2013).

One method that is commonly used to test for the presence of systematic errors in the shear estimation process is image simulation, where we can cleanly test whether our methods of shear estimation recover the ground truth.

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This is a valuable test, considering the numerous sources of additive and multiplicative bias such as a mismatch between galaxy model assumptions and actual galaxy light profiles (e.g., Voigt & Bridle 2010; Melchior et al. 2010), biases due to the effects of pixel noise on the shear estimates (Kacprzak et al. 2012; Melchior & Viola 2012; Refregier et al. 2012), and ellipticity gradients (Bernstein 2010). These biases often differ for galaxies with different morphologies (e.g., disks vs. ellipticals), sizes, S/N , and shape (Bridle et al. 2010; Kitching et al. 2012). A general requirement for simulations used to test shear recovery is that they should be as realistic as possible.

Realistic simulations may use samples based on images from the Hubble Space Telescope (*HST*). Software packages like GalSim² (Rowe et al. 2014) can generate images of galaxies from the *HST* as they would appear with an additional lensing shear and viewed by some lower resolution telescope. Examples of training samples from the *HST* include the COSMOS survey (used by the GREAT3 challenge, Mandelbaum et al. 2014) or the Ultra Deep Field (UDF, used by Jee et al. 2013). These two examples serve as the extremes in the *HST* samples used as the basis for image simulation, with COSMOS being shallower but representing the current widest contiguous area surveyed by the *HST*, and the latter being extremely deep but narrow.

For a variety of physical reasons, some of which are still not fully understood, the shape and morphology of galaxies depends on their local environment (e.g., Carollo et al. 2014; De Propriis et al. 2014). Hence, local overdensities or underdensities observed in these *HST* fields may (given the small size of the field) cause the properties of the galaxy population in redshift slices to be atypical depending on the environment in that slice. This would have the undesired consequence of including variation in galaxy properties due to the COSMOS (or other) survey cosmic variance in the simulated galaxy sample in that redshift slice, rather than only including ensemble effects that would appear in a large cosmological volume, such as true redshift evolution of galaxy properties. Our goal is to quantify the degree to which the morphology-density correlations in COSMOS cause noticeable changes in the galaxy populations in narrow redshift slices at a level that could result in difficulty using the sample to derive redshift-dependent shear calibrations. Upcoming surveys will study lensing as a function of redshift and therefore need to simulate galaxy samples at different redshifts in order to assess the shear calibration at each redshift.

The paper is structured as follows: in Sec. 2, we describe the data that we use for this study. In Sec. 3, we describe our methods for deriving the relevant galaxy properties like environment, morphology, and shape. Using these ingredients, we present our results in Sec. 4 and discuss their implications in Sec. 5.

2 DATA

COSMOS (Scoville et al. 2007; Koekemoer et al. 2007; Leauthaud et al. 2007) is a flux-limited, narrow deep field

survey covering a contiguous area of 1.64 deg² of sky, with images taken using the Advanced Camera for Surveys (ACS) Wide Field Channel (WFC) in the Hubble Space Telescope (*HST*).

We apply the following set of initial cuts to the data, all of which is defined in Leauthaud et al. (2007):

(i) **MU_CLASS=1**: Unlike SExtractor’s stellar index **CLASS_STAR** which is continuous, the **MU_MAX** method that compares the peak surface brightness to the background level, provides a clear differentiation of galaxies (**MU_CLASS=1**) from stars (**MU_CLASS=2**) and other spurious objects like cosmic rays (**MU_CLASS=3**)

(ii) **CLEAN=1**: Objects near bright stars or those containing saturated pixels were removed and the rest classify as *clean*.

(iii) **GOOD_ZPHOT_SOURCE =1**: This cut requires that the photometric redshifts be reliable and good enough to draw conclusions about the population. More details on what ‘good’ refers to can be found in Mandelbaum et al. (2011)

Precise shape measurements, when compared to ground-based surveys, can be made since the full width half-maximum (FWHM) of the point-spread function (PSF) is 0.12″. High resolution images taken through the wide F814W filter (broad I), after correcting for the PSF, have led to collection of postage stamp images³ for the GREAT3 challenge (Mandelbaum et al. 2014), using the procedure described in Mandelbaum et al. (2011). Parametric models to most of these galaxies including Sérsic n profile fits, 2 component bulge+disk fits, axis ratios etc were done for GREAT3 challenge (Mandelbaum et al. 2014) using the method described in Lackner & Gunn (2012). This is described briefly in Sec. 3.3. In addition to the ACS/WFC (F814W) imaging, the COSMOS field has also been imaged by Subaru Suprime-Cam ($B_j, V_j, g^+, r^+, i^+, z^+$, NB816), the Canada-French Hawaii Telescope (CFHT; u^*, i^*) and the KPNO/CTIO (K_s).

Photometric redshifts were determined by Ilbert et al. (2009). The accuracy of photometric redshifts for $m_{F814W} \leq 22.5$ is $\sigma_{\Delta z} = 0.007(1 + z_s)$ and at fainter magnitudes, i.e. $m_{F814W} \leq 24$, $\sigma_{\Delta z} = 0.012(1 + z_s)$. The photometric redshift values become noisy beyond z of 1 for our purposes and the various fits to the galaxies are also not very reliable beyond the apparent magnitude (m) value of 23.5. Thus, we will exclude all galaxies that have F814W magnitude greater than 23.5. However, we will use $m_{F814W} \leq 25.2$ sample in volume-limiting process (cf. §3.2) to calculate completeness. We take the $z < 1.0$ flux-limited sample to fit redshift distribution models (cf. §3.1) and then restrict ourselves to $z \leq 1$ sample for all further analysis.

Stellar mass estimates were obtained (Leauthaud et al. 2010) using the Bayesian code described in Bundy et al. (2006). Basically, a grid of models that vary in age, star formation history, dust content and metallicity are constructed to which the observed galaxy’s spectral energy distribution (SED) and the photometric redshift are referenced to. At each grid point, the probability that the SED fits the model are calculated and by marginalizing over all the parameters in the grid, the stellar mass probability distribution is ob-

² <https://github.com/GalSim-developers/GalSim>

³ <http://irsa.ipac.caltech.edu/data/COSMOS/images/galaxy-postage-stamps/>

tained. The median of this distribution is taken as the stellar mass estimate. A Chabrier IMF (Chabrier 2003) is assumed.

We will analyze how the galaxy morphology and intrinsic shape depends on the environment in which they reside.

3 METHODS

In order to study the variation in the intrinsic ellipticity distribution and other morphological indicators with environment, there are three main steps to be carried out.

- (i) To identify overdense and underdense environments in our survey from the redshift distribution of galaxies (§3.1),
- (ii) To limit the sample such that Malmquist bias is minimized before comparing galaxies in different redshift slices (§3.2),
- (iii) To estimate the galaxy axis ratios and other morphological indicators such as Sérsic index and Bulge-to-Total ratios (§3.3).

3.1 Finding overdensities

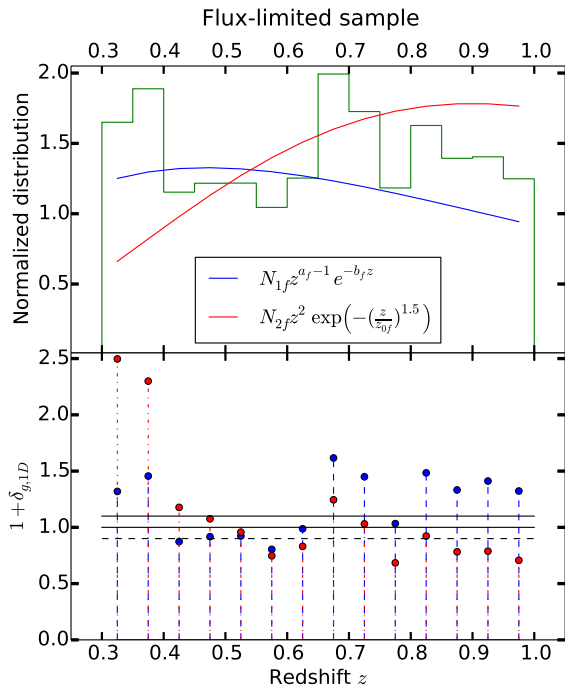


Figure 1. Upper panel: Redshift distribution of flux-limited ($m_{F814W} \leq 23.5$) sample with bins that are 0.05 wide. Two analytical functions with best fit parameters are plotted over it. Lower panel: Plot of $(1 + \delta_{g,1D}) = N/N_{\text{mod}}$ with each functional form as the model for each redshift bin. [Give parameter values.](#) [Set minor ticks.](#)

Weak lensing simulations will use galaxies selected in 2D redshift slices and we split our sample in a similar way to assign overdensities.

For our (flux-limited) sample of galaxies, up to $z = 1.0$, we fit parametric models to the histogram of photometric

redshift in order to assign values of overdensity. Figures show Chi-squared distribution given by

$$p_1(z) \sim z^{a-1} \exp(-bz) \quad (1)$$

and the function given by

$$p_2(z) \sim z^2 \exp\left(-\left(\frac{z}{z_0}\right)^{1.5}\right) \quad (2)$$

that was first presented by Baugh & Efstathiou (1993) as fits to the redshift histograms. The normalization constants depend not only on the parameters but also on the lower and the upper limit of the redshifts considered. Here a, b and z_0 are free parameters that are to be determined. For low z , the volume is too small to rely the overdensity values from our model fits and hence the fit is made for $z \geq 0.3$. Our binning width, Δz must be small enough so as to be able to identify localized overdensities/underdensities but large enough to not let our conclusions be affected by the errors in photometric redshift. We choose our bins to be 0.05 wide starting from $z = 0.3$.

Overdensity (as predicted by a given model) in a redshift bin is defined as the ratio of the difference between the value given by the histogram and the value predicted by the model to the latter:

$$\delta_{g,1D} = \frac{(N - N_{\text{mod}})}{N_{\text{mod}}}. \quad (3)$$

Note that $\delta_{g,1D}$ is model dependent. If a model and the distribution agree, then $\delta_{g,1D} = 0$ for that model at all the redshifts.

Our decision criterion is as follows. We leave a 10% margin of safety i.e., if $|\delta_{g,1D}| < 0.1$, we say that the model and the actual distribution agree. We label a redshift bin overdense if at least one of the models predicts the value of $\delta_{g,1D} > 0.1$ while the other predicts $\delta_{g,1D} > -0.1$, i.e., neutral or overdense and vice versa for the underdense regions. We label a redshift bin ‘neutral’ if both the models predicted the value of $\delta_{g,1D}$ within the margin of safety or if one of them predicts the bin to be overdense while the other predicts it to be underdense.

We thus identify the regions $z = 0.30 - 0.40, 0.65 - 0.75, 0.80 - 0.85$ as overdense, $z = 0.55 - 0.65, 0.75 - 0.80$ as underdense and $z = 0.40 - 0.55$ as unclassified.

Our classification is not very rigorous since it considers only the counts in redshift slices and compares with models that only approximately describe the redshift distribution of galaxies. Moreover, the photometric redshifts become less accurate as we go to higher redshifts (cf. §2) and no information about structure in transverse direction has been taken into account. Thus, it is important to cross-check with a more careful study of the density fields in the same field of view. Kovač et al. (2010), using a sample of $\sim 10,000$ zCOSMOS spectra sources with $I_{AB} < 22.5$, have reconstructed the three dimensional overdensity field up to $z \sim 1$. In spite of the above mentioned shortcomings, our classification of overdensities and underdensities agrees with this work done, except for the last two high redshift bins. We believe that this disagreement is due to the errors in our photometric redshifts and the overdensity reported in $z = 0.875 - 1$ slice is observed by us in $z = 0.80 - 0.85$ slice.

However, the other point to keep in mind here is that

what we are doing most closely follows the way the COSMOS galaxies would be used when constructing a simulation to test weak lensing measurement methods: the sample would be divided into redshift slices using the photometric redshifts, and the shear calibration would be estimated for all galaxies in that slice. Thus, it is the apparent over- and under-densities in such a procedure that we care about here (where our main concern is testing systematics in weak lensing survey simulations, rather than learning about galaxy formation and evolution).

3.2 Volume limiting

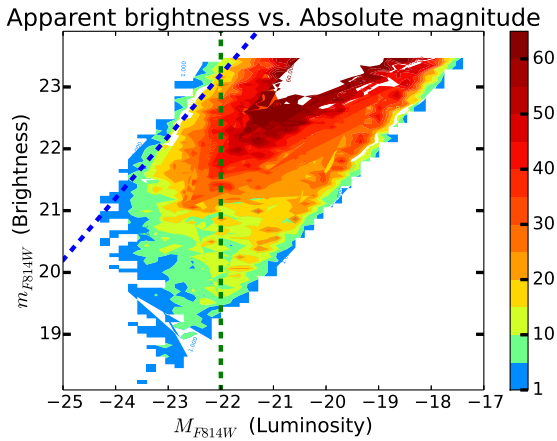


Figure 2. 2-D histogram of galaxies in apparent magnitude (m_{F814W}) and absolute magnitude (M_I) space.

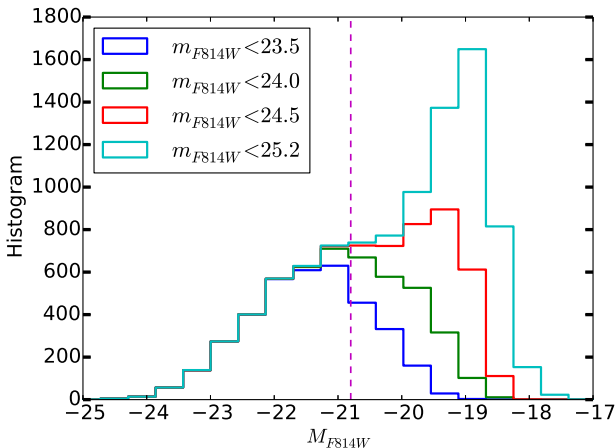


Figure 3. Distribution of M_I for various flux-limited samples are plotted together. The vertical line corresponds to the luminosity cut of -20.8 , below which the $m_{F814W} < 23.5$ sample has 95.3% of the galaxies in the $m_{F814W} < 25.2$ sample.

COSMOS is a flux-limited survey and is therefore affected by Malmquist bias, i.e. at higher redshifts, the brighter galaxies are preferentially observed. Our analysis involves comparing galaxies in different redshift slices to

find significant differences in morphology, if any, so with a flux-limited sample, we would be comparing only the bright galaxies at high redshifts with bright and faint galaxies at low redshifts. For a fair comparison, we must restrict ourselves to bright galaxies at all redshifts and this is achieved by volume-limiting the sample. We generate, using the method below, a volume-limited sample that is complete upto $z = 1$ by applying a cut on luminosity such that only galaxies intrinsically brighter than a certain threshold is considered. This threshold is set on M_I , which are K -corrected i^+ -band magnitudes from Subaru or from the PSF-matched CHFT i^* -band images. **Is it i band, or I band? Check which one and then be self-consistent throughout the text. I think they call it I_{814} , so I . But you are still being ambiguous in sometimes calling it I and other times $F814W$. Pick one. Actually, is this the catalog entry called “ M_I ”? If so, it really is a different band - it’s the k -corrected I -band data from Subaru or CFHT, so it’s appropriate to call it M_I and explain briefly that it’s from the Subaru data (but m_{F814W} , since MAG_AUTO is from $F814W$).** Since the parent sample contains fainter galaxies, upto $m_{F814W} = 25.2$, we compare the distribution of the $m_{F814W} = 23.5$ sample with the samples containing fainter galaxies for high redshift bins, to see where the sample is no longer complete.

At $M_I \sim -22.0$, we see the sample is beginning to be biased in the $0.9 < z < 1.0$ bin due to the flux limit. We obtain 97.84% completeness in this bin for M_I , where completeness is defined as the ratio between the number of galaxies in $m_{F814W} \leq 23.5$ and in $m_{F814W} \leq 25.2$ samples. Thus the sample $z \leq 1$ and $M_I < -22$ is at least 97.84% complete. Figs. 2 & 3 show that at $M_I < -22$, we are not affected by flux limit yet.

The region between $0.85 < z < 1.0$ is only moderately overdense and we do not seem to have as many underdense regions to compare with. It would rather be advantageous to disregard this region and redo the volume limiting procedure. We relax our luminosity cut so that the sample is volume-limited *not* until $z = 1$ but until $z = 0.85$. We choose to impose the cut at $M_I = -20.8$, with 95.3% completeness in the $0.8 < z \leq 0.85$ bin. This increases the sample size significantly, from 7,418 galaxies to 11,169. We call this sample $S1$.

However, previous studies **cite** have shown that absolute luminosities evolve with redshift. Thus, we must also let the luminosity cut evolve with the redshift. There has been no published literature on the LF for the I -band, particularly for the COSMOS survey. We used the published result (Faber et al. 2007) for the ‘rate’ of evolution of B-band magnitudes for DEEP2 and COMBO-17 surveys, which is $\Delta M_B^* \sim -1.23$ mag per unit redshift, for both blue and red galaxies combined together. Typically, estimates of evolution in K-band are lesser than the estimates of evolution in B and V bands. Assuming that the evolution is a smooth function of the wavelength, the evolution in I-band is expected to be lesser than that of the B-band. Therefore, by considering no evolution and an upper bound on the evolution, we can interpolate what the results would be like for the true I -band evolution.

Thus, we construct a second volume-limited sample $S2$, this time by letting the luminosity cut evolve. Starting from $M_I = -20.8$ for the $0.8 < z \leq 0.85$ bin, we add to it 1.23 times the difference between the bincenters to obtain the

Redshift	Environment	S1	S2	S3
0.3-0.4	Overdense	1726	2505	1260
0.4-0.475	Neutral	988	1317	710
0.475-0.55	Neutral	1410	1788	902
0.55-0.65	Underdense	1797	2193	1183
0.65-0.75	Overdense	4059	4476	2593
0.75-0.8	Underdense	1159	1196	675
0.8-0.85	Overdense	2428	2428	1630

Table 1. List of different redshift bins, their environmental classification and the number of galaxies binwise for volume-limited samples constructed in three different ways: using hard luminosity cut (S1), letting the luminosity cut evolve with redshift (S2) and imposing stellar-mass cuts (S3).

luminosity cut for the other (lower) redshift bins. At lower redshifts, we allow for fainter galaxies that wouldn't have passed the cut in S1 and hence has more galaxies.

Alternatively, one could get around the problem of considering redshift evolution by imposing cuts on stellar mass instead of absolute luminosity in a particular band. In Fig. 4, we show the stellar mass function (SMF) of our sample for various F814W flux limit. Tomczak et al. (2014) report the SMFs for the ZFOURGE survey, which includes COSMOS. They considered for this work, a single stellar population following a Chabrier IMF (Chabrier 2003). We plot their SMF for *all* galaxies in Fig. 4 for reference. Their SMF is higher than ours since they reach K_s -band 5σ depth of 24.9. As in the case of M_I s, we compare the stellar mass in the $m_{F814W} \leq 23.5$ sample with that of the $m_{F814W} \leq 25.2$ sample. The sample $\log(M/M_\odot) > 10.15$ is about 95% complete in the redshift bin $[0.75 - 0.85]$ and has 10,341 galaxies in total. Thus, we construct a third volume-limited sample S3 by imposing the stellar mass cut mentioned above. The number of galaxies in redshift slices are tabulated in Table 1 for all 3 ways of obtaining a volume-limited sample. Stellar-mass limited sample happens to be the smallest one.

There is a minor pitfall with this method. We analyse only those galaxies for which postage stamp images exist. 12% of galaxies that pass our cuts do not have an associated postage stamp image. Yet, we use the full $m_{F814W} \leq 23.5$ sample, irrespective of the existence of postage stamps, for identifying overdensities and in the completeness calculation for volume-limiting. Postage stamps may not exist because, given the size of the galaxy, the size of the postage stamp we want to draw around it (including enough blank space) intersects with the edge of the CCD. If all galaxies were the same size, this would be a purely random effect, but in fact bigger galaxies are more likely to get excluded by this cut. Typically galaxies that are nearby and intrinsically very bright do not have postage stamps associated with them and this is an effect that is dominant at lower redshifts. Our completeness calculation is done at high redshifts and thus we believe that our conclusions are not affected by this bias.

The functional forms for the (flux-limited) redshift distribution that we used in §3.1 are not physically motivated. We fit them again to the redshift distribution of a volume-limited sample (S1). Referring to Fig. 5, the values of $\delta_{g,1D}$ for the $z = 0.40 - 0.55$ bin have increased and are within $\pm 10\%$ of 0. This is the reason why in §3.1 we classified them as neutral as opposed to underdense. We will see in §4 that

they are more similar to overdense regions as opposed to underdense regions. The other redshift slices seem to exhibit a consistent behavior.

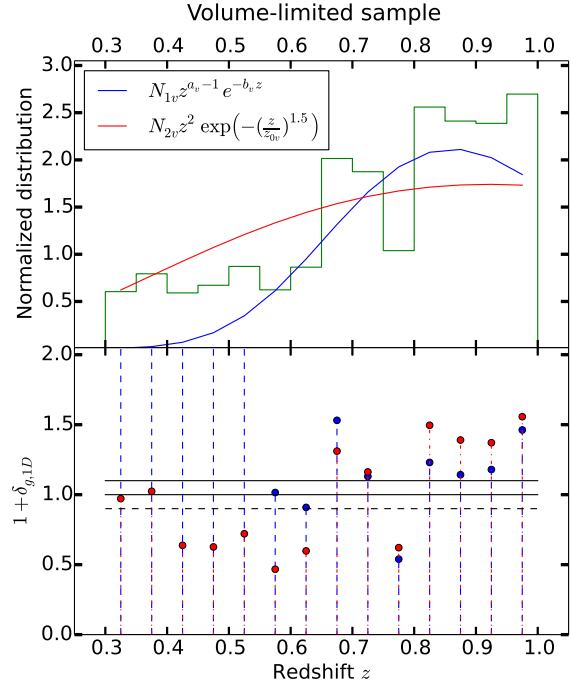


Figure 5. Upper panel: Redshift distribution of volume-limited ($M_I < -20.8$) S1 sample with bins that are 0.05 wide. Two analytical functions with best fit parameters are plotted over it. Lower panel: Plot of $(1 + \delta_{g,1D}) = N/N_{\text{mod}}$ with each functional form as the model for each redshift bin.

In the following section, we will compare and analyze the distribution of properties of the galaxies residing in the overdense regions.

3.3 Describing galaxy morphology and shape

If galaxies have elliptical isophotes, its shape and size could be defined by the axis ratio and the area enclosed by a boundary isophote. However, in real galaxy images, the boundary may not be well defined and the shape may not be well approximated by an ellipse. More importantly, the effect of smearing due to the point-spread function (PSF) is larger. Thus, we are in need of more sophisticated methods to measure the ellipticities.

One method to estimate the ellipticities is to estimate the axis-ratios by fitting parametric models to each image. The models that we fit to the images are

- (i) a Sérsic profile given by the expression

$$S = \Sigma_{1/2} \exp \left(-k(R/R_{\text{eff}})^{1/n} - 1 \right), \quad (4)$$

- (ii) two Sérsic component fits: de Vaucouleurs bulge ($n = 4$) + exponential disc profile ($n = 1$),

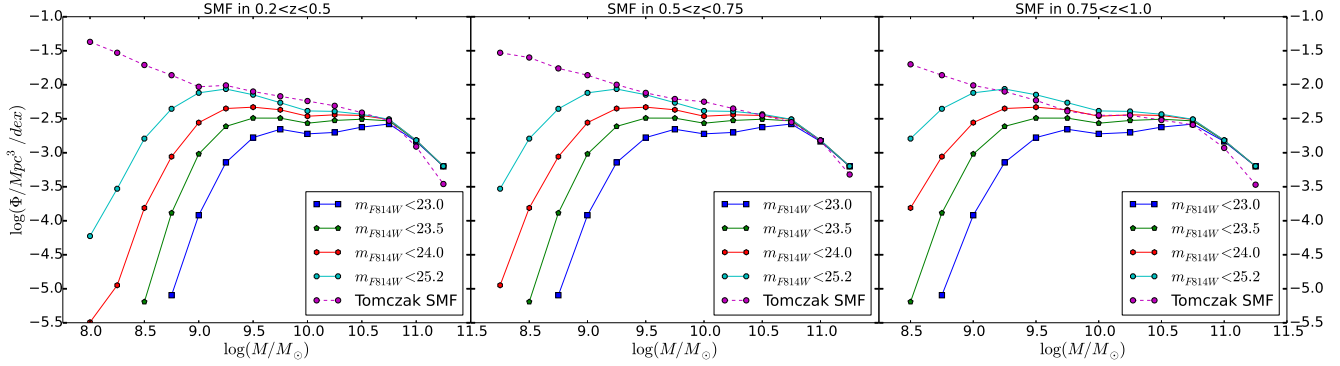


Figure 4. Stellar-mass distribution for various flux-limited samples in three redshift ranges are plotted. Bins have been chosen so as to make the comparison easier with a study of SMF in the same survey (Tomczak et al. 2014). At high mass, the distributions are the same for various flux limits indicating that the samples are complete in that mass range. The curves begin to separate at low masses on account of incompleteness, which determines where the mass cutoff should be to volume-limit the sample.

where

$$R^2 = ((x - x_0) \cos \Phi + (y - y_0) \sin \Phi)^2 + ((y - y_0) \cos \Phi - (x - x_0) \sin \Phi)^2 / q^2,$$

R_{eff} is the half-light radius of the profile, $\Sigma_{1/2}$ is the surface brightness at $R = R_{\text{eff}}$, (x_0, y_0) is the centroid of the image, Φ is the profile rotation angle, n is the Sérsic index, k is a n -dependent normalization factor and q is the axis ratio of the elliptical isophotes. Thus, the Sérsic profile has 7 free parameters. The bulge+disk model has 10 free parameters since the Sérsic indices are fixed as 1 and 4 and both the profiles are required to have the same centroid (x_0, y_0) . Best-fit parameters were found, by minimizing the weighted sum of the difference between the image and the PSF-convolved model using Levenberg-Marquardt minimization, `mpfit2fun` in IDL (Markwardt 2009). More details about the fit can be found in Lackner & Gunn (2012).

The quantities that we would use from the single Sérsic profile fits are the Sérsic index and axis ratio and from the bulge+disk fits will be the Bulge-to-Total ratio given by $\Sigma_{1/2}(n=4)/(\Sigma_{1/2}(n=4) + \Sigma_{1/2}(n=1))$. **I think it would be useful to take the entire sample that we use for science, and show the overall distributions of axis ratio, distortion (one curve for Claire’s and one curve for re-Gaussianization), Sérsic index, and Bulge-to-Total . This would be a nearly full-page four panel figure, but I think it’s worthwhile to illustrate the nature of the sample. For example, it will clearly show why we cannot use the distributions of Sérsic index and Bulge-to-Total , because of the hard cutoffs.**

An alternative method involves correcting the observed image for the PSF and computing the covariances from which the ellipticity of the galaxy can be obtained. The PSF correction scheme used on the observed images is that of ‘re-Gaussianization’ method described in §2.4 of Hirata & Seljak (2003) (hereafter HS03). This method models the true PSF $g(\mathbf{x})$ as a Gaussian $G(\mathbf{x})$ and the residual $\epsilon(\mathbf{x}) = g(\mathbf{x}) - G(\mathbf{x})$ is assumed to be small. Thus, the Gaussian-convolved intrinsic image of f , is $I' = G \otimes f = I - \epsilon \otimes f$, where I is the observed image. The crucial idea here is that, when ϵ is small, we get a reasonably accurate estimate of I' even if we use an approximate form for f . The form assumed for f is that of a Gaussian with covari-

ance $M_f^{(0)} = M_I - M_g$, where M_I and M_g are the adaptive covariances of the measured object and PSF respectively, described in §2.1 of HS03, which is in turn based on Bernstein & Jarvis (2002). Once we obtain the covariance matrices of the intrinsic image f , one can compute the ellipticities of the galaxies, which we will refer to as ‘ellipticities based on moments’.

4 RESULTS

Having identified the overdense and underdense regions in a volume-limited sample (§3.1, §3.2), we will now see in this section if the morphological parameters of the galaxies, listed in §3.3, have any dependence on the environment that they reside in. We have 3 different ways of volume-limiting our sample

- (i) no redshift evolution of luminosity cut (S1),
- (ii) use B -band evolution rate for I -band luminosities (S2),
- (iii) impose stellar mass cuts instead of luminosity (S3)

and we will present our results in each of the 3 cases.

4.1 Axis-ratios

We can understand the influence of environment on the ellipticities of the galaxies simply by comparing the distribution of the axis ratios for the overdense and underdense samples. Then, we proceed to consider the root mean square ellipticity, a statistic that can characterize the shape of the population/sample of galaxies.

4.1.1 Comparing distributions

We use two statistical tests namely the Kolmogorov-Smirnov test and Anderson-Darling test to compare distributions. The Anderson-Darling test is carried out using the `adk` package⁴ in R.

We first compare the distribution of the axis ratio in *all*

⁴ <http://www.inside-r.org/packages/cran/adk/docs/adk.test>

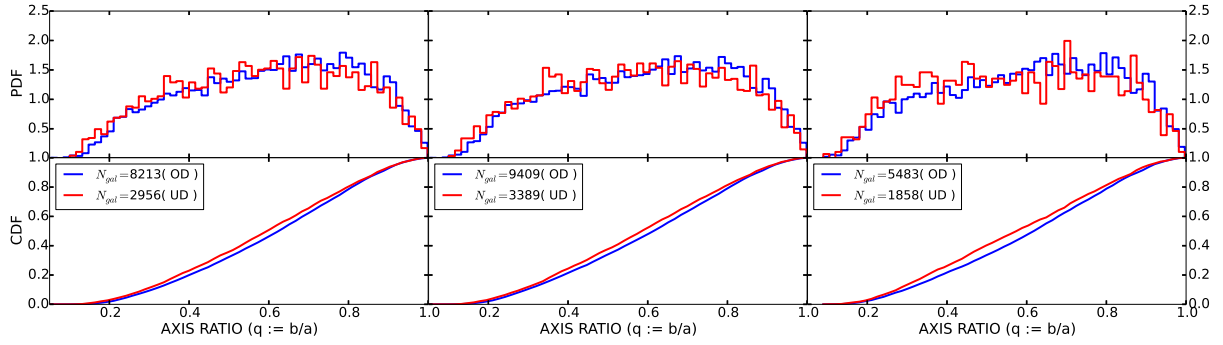


Figure 6. The distributions of axis ratios of galaxies in *all* overdense (OD) and *all* underdense (UD) regions in the case of luminosity-selected sample (left), luminosity-selected with B-band evolution taken into account (center) and stellar-mass-selected sample (right). The upper panels show the histogram and the bottom panels show the empirical cumulative distribution function (ECDF). p -values are computed using these CDFs using the Kolmogorov-Smirnov and Anderson-Darling tests and are given in Table. 2. The difference between the CDFs turn out to be statistically significant. *This figure and the ones below appear to be right-justified (pushed up against the right margin) instead of centered. Can you look into fixing that? Also, the := is not very standard notation, I recommend just =. Finally, the spacing in the legends is funny; I would prefer to see things like “8213 (OD)” rather than the current “8213(OD)”. The former is also consistent with the next figure.*

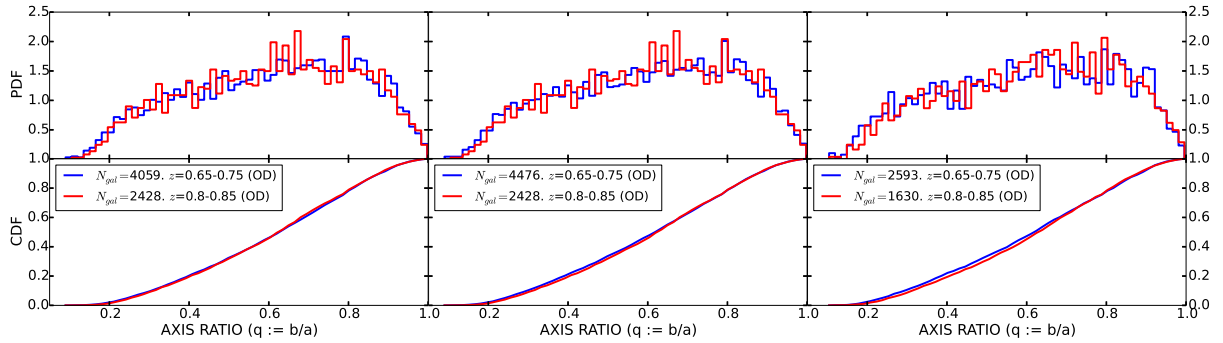


Figure 7. Comparison in similar environments: Axis ratios of galaxies in two overdense redshift bins, $z = 0.65 - 0.75$ and $z = 0.80 - 0.85$ are compared. p -values from the KS and AD test are given in Table. 2

Redshift bins	S1	S2	S3
All overdense vs.	1.1×10^{-4}	2.6×10^{-5}	1.9×10^{-6}
All underdense	1×10^{-5}	$< 1 \times 10^{-5}$	$< 1 \times 10^{-5}$
$z : [0.65, 0.75]$ (OD) vs.	0.613	0.431	0.231
$z : [0.80, 0.85]$ (OD)	0.494	0.237	0.130
$z : [0.65, 0.75]$ (OD) vs.	5.8×10^{-4}	1.5×10^{-5}	3.5×10^{-6}
$z : [0.55, 0.65]$ (UD)	9.8×10^{-4}	$< 1 \times 10^{-5}$	$< 1 \times 10^{-5}$

Table 2. p -values from the Kolmogorov-Smirnov (top) and Anderson-Darling (bottom) obtained by comparing the distributions of axis ratios are given for three cases: *all* overdense (OD) vs. *all* underdense (UD), two overdense bins, not very separated in redshift and a pair of adjacent overdense and underdense bins. S1, S2, S3 refer to the volume-limited sample in three different ways. The Anderson-Darling p -values are correct only upto 5 decimal places.

overdense bins and *all* underdense bins in Fig. 6. *How was the volume-limiting carried out for this? You should say the answer to this question for all figures. The caption mentions it. I'm afraid that's not enough. Some people are going to*

Redshift bins	S1	S2	S3
All overdense vs.	5.6×10^{-4}	1.0×10^{-4}	3.3×10^{-6}
All underdense	3×10^{-5}	1×10^{-5}	$< 1 \times 10^{-5}$
$z : [0.65, 0.75]$ (OD) vs.	0.9563	0.7476	0.5359
$z : [0.80, 0.85]$ (OD)	0.5162	0.3352	0.2290
$z : [0.65, 0.75]$ (OD) vs.	6.0×10^{-3}	2.5×10^{-4}	2.4×10^{-4}
$z : [0.55, 0.65]$ (UD)	1.2×10^{-2}	2.5×10^{-4}	5×10^{-5}

Table 3. p -values from the Kolmogorov-Smirnov (top) and Anderson-Darling (bottom) obtained by comparing the ellipticities computed using second moments are given for three cases: *all* overdense (OD) vs. *all* underdense (UD), two overdense bins, not very separated in redshift and a pair of adjacent overdense and underdense bins. S1, S2, S3 refer to the volume-limited sample in three different ways. *Should I write only two significant digits for higher p -values? The Anderson-Darling p -values are correct only upto 5 decimal places.*

read linearly and you want the info in the main text, too. Unless otherwise mentioned, the axis ratios refer to the values obtained using the method of Lackner & Gunn (2012).

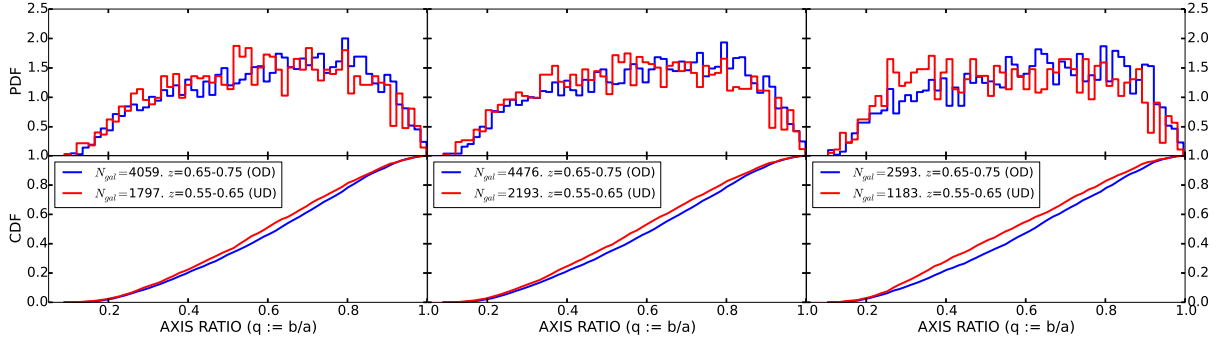


Figure 8. Comparison in contrasting environments: Axis ratios of galaxies in an underdense redshift bin, $z = 0.55 - 0.65$ are compared with those in an overdense bin, $z = 0.65 - 0.75$. p -values from the KS and AD test are given in Table. 2

The cumulative distinction functions are also plotted alongside in order to be able to visualize the ‘distance’ between the distributions. Referring to the first two rows in Table 2, we see that the p -values from both the KS and AD tests are well below 0.05, so we reject the ‘null hypothesis’ that the overdense and underdense regions have same axis ratio distributions at 95% significance level.

One might imagine that the disagreement between the distributions is, at least partly, due to the fact that the overdense and underdense sample have different redshift distributions. To show that that is not the case, we will compare distributions between two overdense / underdense redshift bins, where we expect to find similarity, and between an overdense and underdense regions, where we expect the distributions to differ. Figures 7 and 8 are examples showing that the distributions are indeed similar when the environments are similar and different when the environments are different, confirming our expectation. Similar conclusion can be arrived at by comparing other redshift bins.

Such a trend is also observed in axis ratios based on second moments. If Q_{ij} represents the generic matrix element of the matrix of second moments, then define a complex number, sometimes known as the *distortion*, as

$$e = e_1 + ie_2 = \frac{Q_{11} - Q_{22} + 2iQ_{12}}{Q_{11} + Q_{22}}. \quad (5)$$

Then, one definition of ellipticity is the magnitude of this complex number which is $\sqrt{e_1^2 + e_2^2}$.

After neglecting a small fraction ($\sim 0.0065\%$) of galaxies (36 out of 55991 galaxies between $0.3 \leq z < 0.85$ with $\log(M/M_\odot) > 10.15$) for which the moments do not converge, we make comparisons to the above between the distribution of ellipticities computed from the second moments and the results are tabulated in Table 3. Once again, we see that the distributions are consistent with each other when the environment is similar and are inconsistent when the environments are contrasting.

4.1.2 RMS ellipticities

For the luminosity-selected sample without any evolution, RMS ellipticities of galaxies in each redshift bin are shown in Figure 9. As one can see, the underdense regions have significantly higher values for RMS ellipticities when compared to the overdense regions. Note in particular that we’ve been

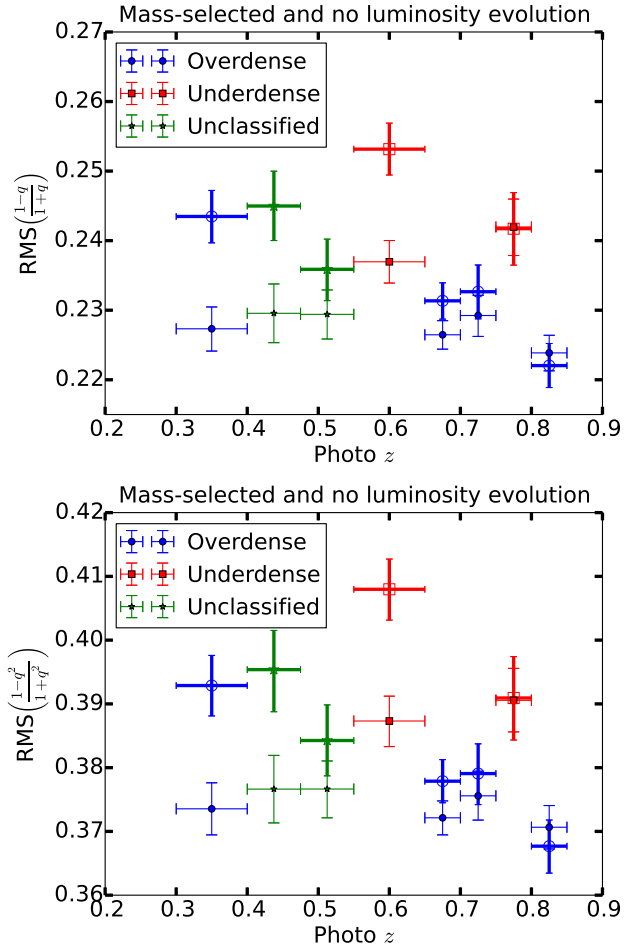


Figure 9. Left: RMS ellipticities with ellipticity defined as $\frac{1-q}{1+q}$. Right: RMS ellipticities with ellipticity defined as $\frac{1-q^2}{1+q^2}$. The horizontal errorbars simply correspond to the binwidth while the vertical ones are 1σ errorbars obtained by bootstrapping. I’m thinking these are so similar we just need to show one figure, and can say the results for the other in words. The same goes for the next figure.

able to capture the narrow overdense bin $0.75 \leq z < 0.80$. There is (almost) no redshift dependence in the figure.

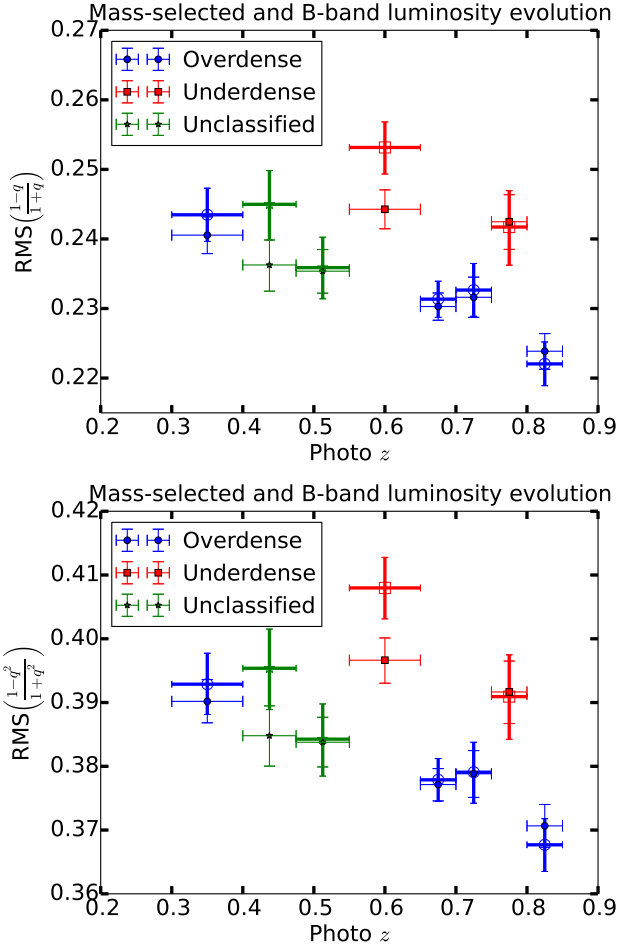


Figure 10. Left: RMS ellipticities with ellipticity defined as $\frac{1-q}{1+q}$. Right: RMS ellipticities with ellipticity defined as $\frac{1-q^2}{1+q^2}$. The horizontal errorbars simply correspond to the binwidth while the vertical ones are 1σ errorbars obtained by bootstrapping. The solid points correspond to the sample where the luminosity cut evolves by -1.23 per unit redshift (S2) and the unfilled points correspond to the sample obtained from stellar mass cuts (S3).

The dependence on the local environment seems to make sense. Overdense regions typically have young, spiral galaxies which have high q and hence low RMS ellipticity. On the contrary, the underdense regions typically have old, elliptical galaxies and thus low q and high RMS ellipticity.

From Figs. 1 and 5, the region $0.4 \leq z < 0.55$ show signs of being marginally underdense but have low RMS ellipticities too that agree with the rest of the overdense regions.

When the B-band luminosity evolution is taken into account in selecting the sample, a systematic increase in the ellipticity at lower redshifts can be observed. We plot these alongside with stellar-mass selected samples, where a similar trend is found, in Fig. 10. Also, the RMS values of the ellipticities calculated from the second moments within each redshift bin are given in Fig. 11.

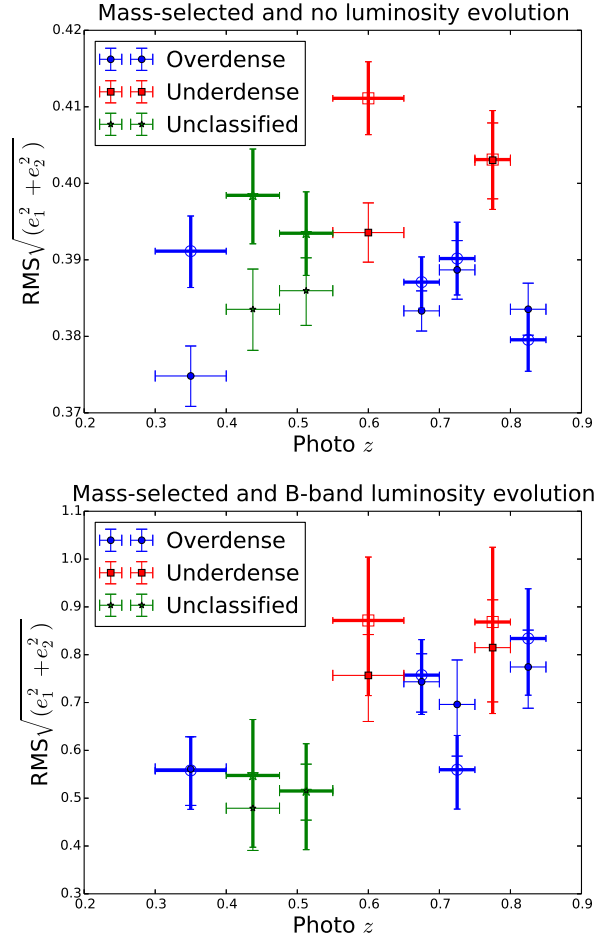


Figure 11. RMS ellipticities with ellipticity defined as $\sqrt{e_1^2 + e_2^2}$, where e_1 and e_2 are the real and imaginary components of the distortion defined in Eq. 5. The horizontal errorbars simply correspond to the binwidth while the vertical ones are 1σ errorbars obtained by bootstrapping. The solid points correspond to the luminosity selected sample (S1 sample on the left and S2 sample on the right) and the unfilled points correspond to the sample obtained from stellar mass cuts (S3).

4.2 Other morphological parameters

For other morphological parameters such as the Sérsic index and Bulge-to-Total ratio, we do not compare the distributions themselves directly. For Sérsic profile fits, it gets tricky since we truncate the Sérsic index at 6. For Bulge-to-Total ratios, we force the value to be between 0.05 and 0.95. We will understand the dependence of these quantities on environment by computing the median values in different redshift bins. We choose median over mean since it is more robust to the truncation effects. Fig. 12 show the median of the Sérsic index with and without taking into account of the luminosity evolution. Median values obtained using stellar mass selected samples are plotted alongside for reference. We observe that the overdense regions tend to have higher Sérsic index than the adjacent underdense ones. Fig. 13 show the variation of median Bulge-to-Total ratio with redshift. We see that the bulge component is more in overdense regions than in the underdense regions. These two observations are

consistent with each other since higher Sérsic index implies higher bulge component which are typical in young galaxies found in overdense regions.

In Fig. 12, we see that the Sérsic indices of mass selected sample ($S3$) are systematically greater than those of the luminosity selected samples ($S1, S2$). This is consistent with the Bulge-to-Total values being higher in $S3$ than in $S1$ or $S2$ in Fig. 13. This is not just an edge effect but can be seen from the distributions themselves that the mass selected sample doesn't include as many disk-like galaxies as in luminosity selected samples.

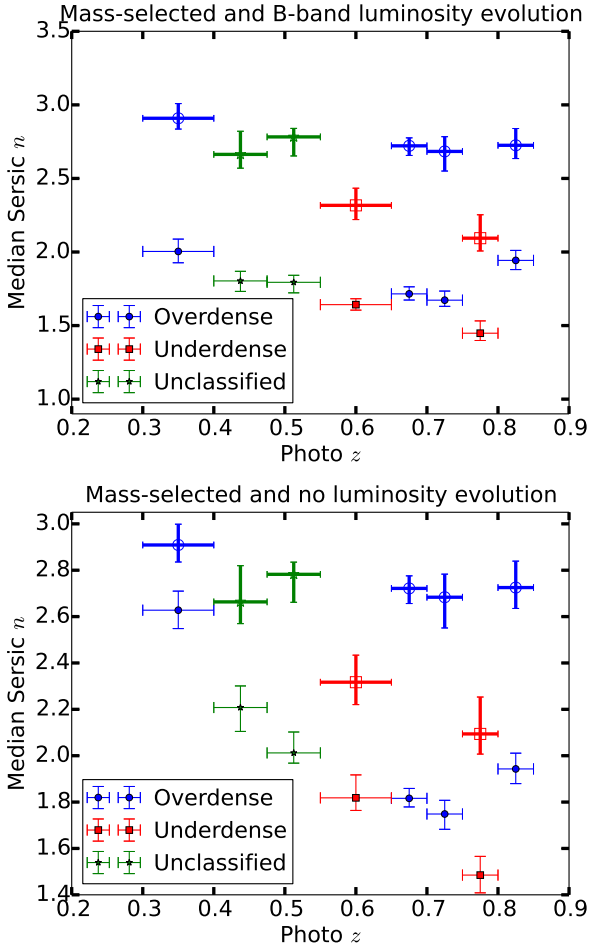


Figure 12. Median values of the Sérsic indices for volume-limited samples $S1$ and $S3$ are plotted (filled centers and thin errorbars) in left and right panels respectively for each redshift bin. Median values for the $S2$ sample are plotted in both the panels (open centers and thick errorbars) in both the panels. The horizontal errorbars simply correspond to the binwidth while the vertical ones are 1σ errorbars obtained by bootstrapping. **Only need to have a legend on one panel, since the legends on both panels are the same. Same comment applies to next figure.**

5 CONCLUSIONS

In this study, we have shown that morphological parameters of galaxies depend on the local environments along the

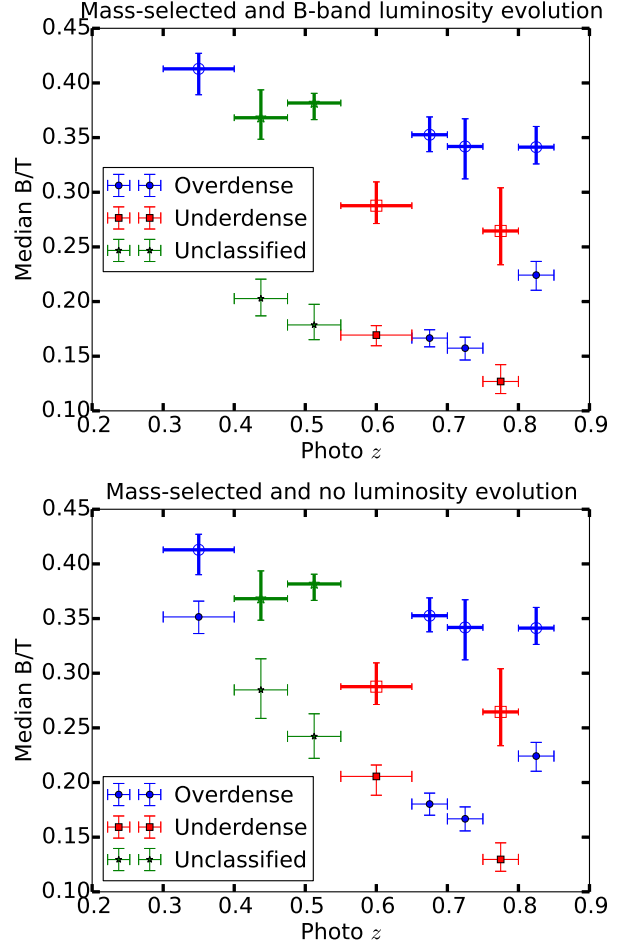


Figure 13. Median values of the Bulge-to-Total ratios for volume-limited samples $S1$ and $S3$ are plotted (filled centers and thin errorbars) in left and right panels respectively for each redshift bin. Median values for the $S2$ sample are plotted in both the panels (open centers and thick errorbars) in both the panels. The horizontal errorbars simply correspond to the binwidth while the vertical ones are 1σ errorbars obtained by bootstrapping. **These look so similar that I am questioning the need to have both. Perhaps remove one and mention that they are nearly identical in the text.**

line of sight in a manner than affect Weak Lensing simulations. In studies of Weak Lensing, one simulates galaxy images in a redshift slice by learning from the images in the same redshift bin of a training sample like COSMOS, which we have used for our analysis here. The survey volume is broken up into multiple redshift slices and are classified as ‘overdense’, ‘underdense’ or ‘neutral’ according to their local environment. This is done by comparing the 1-D redshift distribution to some of the parametric models available in the literature. The incompleteness in the sample is minimized by constructing a volume limited sample either by imposing stellar mass cuts ($S3$) or by imposing a luminosity cut. Further, depending on whether we have the cut fixed or evolve with redshift, we get two more volume limited samples $S1$ and $S2$ respectively. Morphological parameters are obtained by fitting a single Sérsic profile to the images or by a two component (bulge+disk) fit. The morphological

quantities of interest include axis ratios or equivalently the ellipticities, Sérsic indices and Bulge-to-Total ratios.

For all the three volume-limited samples, we compare the distributions of the axis-ratios of the galaxies in overdense and underdense regions and conclude that the distributions are different after performing statistical tests on them. From the axis ratios, we compute ellipticities and find that the root mean squared value of the ellipticities of galaxies in a redshift bin vary significantly between the overdense and underdense regions. Such a behavior is also observed when ellipticities are computed using second moments instead of a parametric model fitting. Sérsic index and Bulge-to-Total ratios also exhibit similar trends with redshift based on the local environment.

Our result has serious implications for realistic image simulations for Weak Lensing. It suggests that the training sample is affected by cosmic variance so as to possibly bias the conclusions from the simulations. This is particularly a problem with narrow surveys where a single galaxy cluster or a void could affect the environment significantly. Thus, we are forced to use wider redshift bins, much larger than the uncertainties in the redshifts, so as to be able to wash out the environmental dependence. However, future surveys such as the Large Synoptic Survey Telescope (LSST; LSST Science Collaboration et al. 2009) will image larger areas of sky mitigating the dependence of local environment in image simulations.

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