## Miscellaneous Exercise on Chapter 2

Find the value of the following:

1. 
$$\cos^{-1}\left(\cos\frac{13\pi}{6}\right)$$

2. 
$$\tan^{-1}\left(\tan\frac{7\pi}{6}\right)$$

Prove that

3. 
$$2\sin^{-1}\frac{3}{5} = \tan^{-1}\frac{24}{7}$$

4. 
$$\sin^{-1}\frac{8}{17} + \sin^{-1}\frac{3}{5} = \tan^{-1}\frac{77}{36}$$

5. 
$$\cos^{-1}\frac{4}{5} + \cos^{-1}\frac{12}{13} = \cos^{-1}\frac{33}{65}$$
 6.  $\cos^{-1}\frac{12}{13} + \sin^{-1}\frac{3}{5} = \sin^{-1}\frac{56}{65}$ 

6. 
$$\cos^{-1}\frac{12}{13} + \sin^{-1}\frac{3}{5} = \sin^{-1}\frac{56}{65}$$

7. 
$$\tan^{-1}\frac{63}{16} = \sin^{-1}\frac{5}{13} + \cos^{-1}\frac{3}{5}$$

Prove that

8. 
$$\tan^{-1} \sqrt{x} = \frac{1}{2} \cos^{-1} \frac{1-x}{1+x}$$
,  $x \in [0, 1]$ 

9. 
$$\cot^{-1}\left(\frac{\sqrt{1+\sin x} + \sqrt{1-\sin x}}{\sqrt{1+\sin x} - \sqrt{1-\sin x}}\right) = \frac{x}{2}, x \in \left(0, \frac{\pi}{4}\right)$$

10. 
$$\tan^{-1}\left(\frac{\sqrt{1+x}-\sqrt{1-x}}{\sqrt{1+x}+\sqrt{1-x}}\right) = \frac{\pi}{4} - \frac{1}{2}\cos^{-1}x$$
,  $-\frac{1}{\sqrt{2}} \le x \le 1$  [Hint: Put  $x = \cos 2\theta$ ]

Solve the following equations:

11. 
$$2\tan^{-1}(\cos x) = \tan^{-1}(2 \csc x)$$
 12.  $\tan^{-1}\frac{1-x}{1+x} = \frac{1}{2}\tan^{-1}x, (x > 0)$ 

**13.** 
$$\sin(\tan^{-1} x), |x| < 1$$
 is equal to

(A) 
$$\frac{x}{\sqrt{1-x^2}}$$
 (B)  $\frac{1}{\sqrt{1-x^2}}$  (C)  $\frac{1}{\sqrt{1+x^2}}$  (D)  $\frac{x}{\sqrt{1+x^2}}$ 

**14.** 
$$\sin^{-1}(1-x) - 2\sin^{-1}x = \frac{\pi}{2}$$
, then x is equal to

(A) 
$$0, \frac{1}{2}$$
 (B)  $1, \frac{1}{2}$  (C)  $0$  (D)  $\frac{1}{2}$