

2347215 Arunoth Symen A*Lab Program - 4***Radial Basis Function (RBF) Network for Handwritten Character Recognition**

Step 1: Data Preparation

```
In [ ]: import numpy as np
import tensorflow as tf
import tensorflow_datasets as tfds
from sklearn.model_selection import train_test_split

# Load the Kuzushiji-MNIST dataset
kmnist_data = tfds.load('kmnist', split=['train', 'test'], as_supervised=True)

# Convert dataset to numpy arrays for easier processing
def preprocess_dataset(dataset):
    images = []
    labels = []
    for image, label in tfds.as_numpy(dataset):
        images.append(image)
        labels.append(label)
    return np.array(images), np.array(labels)

# Preprocess the training and test datasets
X_train_full, y_train_full = preprocess_dataset(kmnist_data[0])
X_test, y_test = preprocess_dataset(kmnist_data[1])

# Normalize pixel values to be between 0 and 1
X_train_full = X_train_full.astype('float32') / 255.0
X_test = X_test.astype('float32') / 255.0

# Reshape data to flatten each 28x28 image into a single row (784 features)
X_train_full = X_train_full.reshape(X_train_full.shape[0], -1)
X_test = X_test.reshape(X_test.shape[0], -1)

# Split the training set into 80% training and 20% validation
X_train, X_val, y_train, y_val = train_test_split(X_train_full, y_train_full, test_
```

```
In [ ]: import matplotlib.pyplot as plt

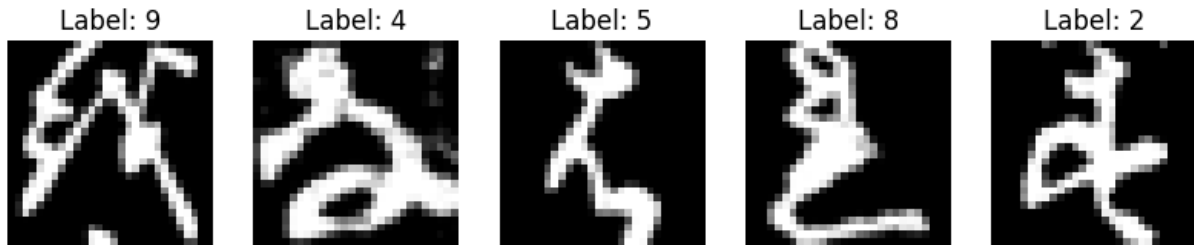
# Output the shapes of the training, validation, and test sets
print(f"Training set shape: {X_train.shape}, Training labels shape: {y_train.shape}")
print(f"Validation set shape: {X_val.shape}, Validation labels shape: {y_val.shape}")
print(f"Test set shape: {X_test.shape}, Test labels shape: {y_test.shape}")

# Display a few sample images from the training set
def display_sample_images(X, y, num_samples=5):
    plt.figure(figsize=(10, 2))
    for i in range(num_samples):
        plt.subplot(1, num_samples, i + 1)
        plt.imshow(X[i].reshape(28, 28), cmap='gray')
        plt.title(f"Label: {y[i]}")
    plt.axis('off')
```

```
plt.show()
```

```
# Display 5 sample images from the training set
display_sample_images(X_train, y_train, num_samples=5)
```

Training set shape: (48000, 784), Training labels shape: (48000,)
 Validation set shape: (12000, 784), Validation labels shape: (12000,)
 Test set shape: (10000, 784), Test labels shape: (10000,)



Step 2: Implement the RBF Network

```
In [ ]: from sklearn.cluster import KMeans

class RBFNetwork:
    def __init__(self, input_dim, num_centers, output_dim):
        self.input_dim = input_dim
        self.num_centers = num_centers
        self.output_dim = output_dim

        # Initialize centers using K-means clustering
        self.centers = None
        self.kmeans = KMeans(n_clusters=num_centers)

        # Initialize weights
        self.weights = np.random.randn(num_centers, output_dim)

    def _gaussian(self, X, center, sigma=1.0):
        return np.exp(-np.linalg.norm(X - center, axis=1)**2 / (2 * sigma**2))

    def _rbf_layer(self, X):
        RBF_outputs = np.zeros((X.shape[0], self.num_centers))
        for i, center in enumerate(self.centers):
            RBF_outputs[:, i] = self._gaussian(X, center)
        return RBF_outputs

    def fit(self, X, y, learning_rate=0.01, epochs=10):
        # Use K-means to find RBF centers
        self.kmeans.fit(X)
        self.centers = self.kmeans.cluster_centers_

        # One-hot encode Labels
        y_onehot = np.eye(self.output_dim)[y]

        # Training Loop
        for epoch in range(epochs):
            # Forward pass
            RBF_output = self._rbf_layer(X)
            output = RBF_output.dot(self.weights)
```

```

        output = self._softmax(output)

        # Compute gradient and update weights
        error = output - y_onehot
        gradient = RBF_output.T.dot(error)
        self.weights -= learning_rate * gradient

        if epoch % 2 == 0:
            loss = np.mean(np.square(error))
            print(f'Epoch {epoch}/{epochs}, Loss: {loss:.4f}')

    def _softmax(self, x):
        exp_x = np.exp(x - np.max(x, axis=1, keepdims=True))
        return exp_x / np.sum(exp_x, axis=1, keepdims=True)

    def predict(self, X):
        RBF_output = self._rbf_layer(X)
        output = RBF_output.dot(self.weights)
        output = self._softmax(output)
        return np.argmax(output, axis=1)

```

Step 3: Training the RBF Network

```

In [ ]: input_dim = X_train.shape[1]
        output_dim = 10

        num_centers = 100 # You can adjust this number to test different configurations
        rbf_network = RBFNetwork(input_dim, num_centers, output_dim)

        # Train the RBF Network
        rbf_network.fit(X_train, y_train, learning_rate=0.01, epochs=10)

```

```

Epoch 0/10, Loss: 0.0900
Epoch 2/10, Loss: 0.0900
Epoch 4/10, Loss: 0.0900
Epoch 6/10, Loss: 0.0900
Epoch 8/10, Loss: 0.0900

```

Epoch Loss: The loss value remains constant at approximately 0.0900 across multiple epochs (from epochs 0 to 10). This suggests that the model might not be learning effectively, possibly due to issues like insufficient model complexity or inadequate data.

Step 4: Evaluation

```

In [ ]: from sklearn.metrics import accuracy_score, confusion_matrix
        import matplotlib.pyplot as plt
        import seaborn as sns

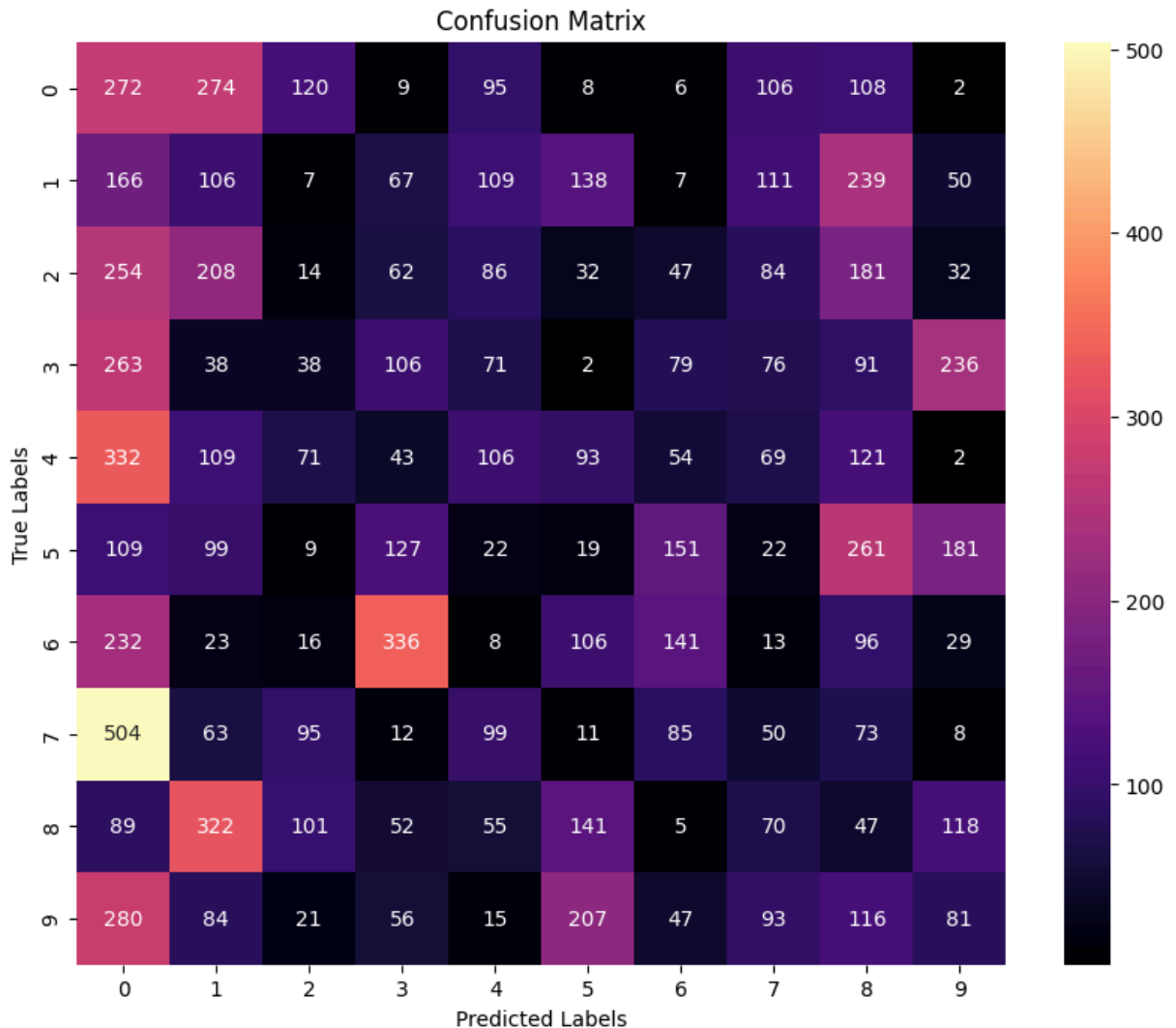
        # Make predictions on the test set
        y_pred = rbf_network.predict(X_test)

        # Calculate accuracy
        accuracy = accuracy_score(y_test, y_pred)
        print(f'Test Accuracy: {accuracy:.4f}')

```

```
# Confusion matrix
conf_matrix = confusion_matrix(y_test, y_pred)
plt.figure(figsize=(10, 8))
sns.heatmap(conf_matrix, annot=True, fmt='d', cmap='magma')
plt.title('Confusion Matrix')
plt.xlabel('Predicted Labels')
plt.ylabel('True Labels')
plt.show()
```

Test Accuracy: 0.0942



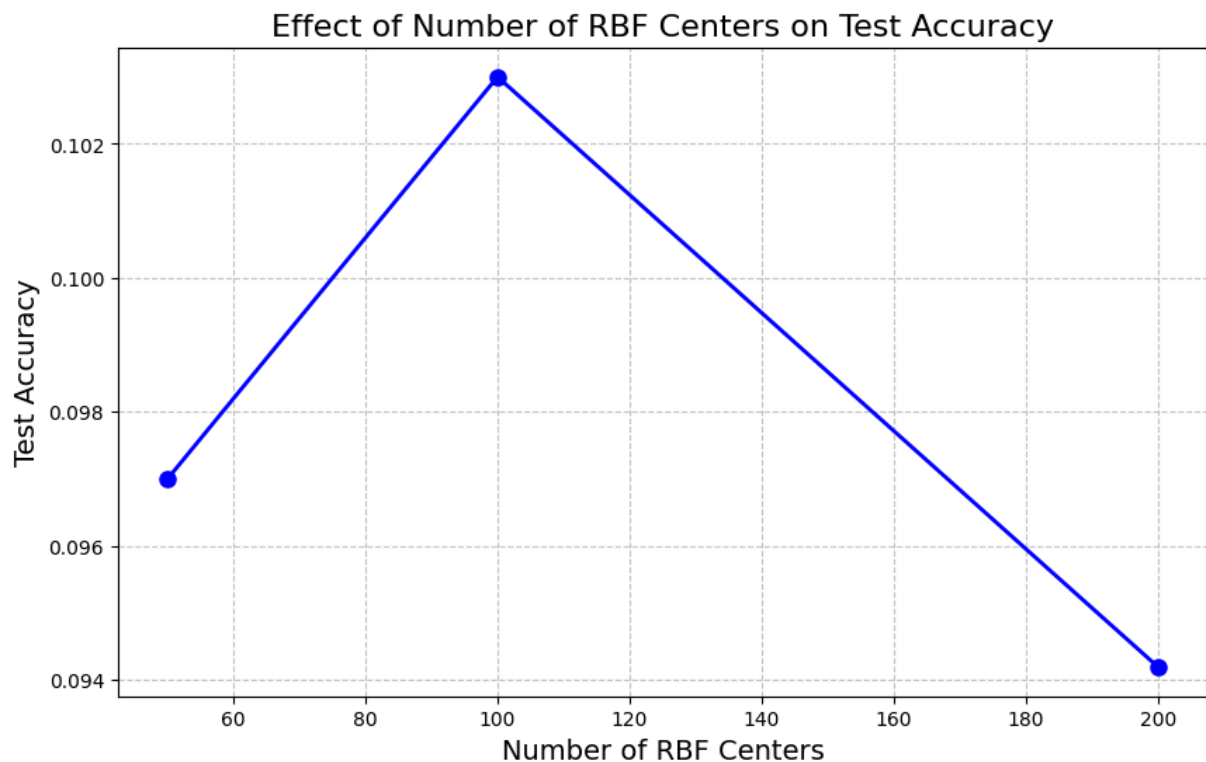
Step 5: Analysis

```
In [ ]: num_centers_list = [50, 100, 200]
         accuracies = []

for num_centers in num_centers_list:
    rbf_network = RBFNetwork(input_dim, num_centers, output_dim)
    rbf_network.fit(X_train, y_train, learning_rate=0.01, epochs=10)
    y_pred = rbf_network.predict(X_test)
    accuracy = accuracy_score(y_test, y_pred)
    accuracies.append(accuracy)
    print(f'Number of Centers: {num_centers}, Test Accuracy: {accuracy:.4f}')
```

```
# Plot the effect of RBF units on accuracy
plt.figure(figsize=(10, 6))
plt.plot(num_centers_list, accuracies, marker='o', linestyle='-', color='b', marker
plt.title('Effect of Number of RBF Centers on Test Accuracy', fontsize=16)
plt.xlabel('Number of RBF Centers', fontsize=14)
plt.ylabel('Test Accuracy', fontsize=14)
plt.grid(True, linestyle='--', alpha=0.7)
plt.show()
```

Epoch 0/10, Loss: 0.0900
 Epoch 2/10, Loss: 0.0900
 Epoch 4/10, Loss: 0.0900
 Epoch 6/10, Loss: 0.0900
 Epoch 8/10, Loss: 0.0900
 Number of Centers: 50, Test Accuracy: 0.0970
 Epoch 0/10, Loss: 0.0900
 Epoch 2/10, Loss: 0.0900
 Epoch 4/10, Loss: 0.0900
 Epoch 6/10, Loss: 0.0900
 Epoch 8/10, Loss: 0.0900
 Number of Centers: 100, Test Accuracy: 0.1030
 Epoch 0/10, Loss: 0.0900
 Epoch 2/10, Loss: 0.0900
 Epoch 4/10, Loss: 0.0900
 Epoch 6/10, Loss: 0.0900
 Epoch 8/10, Loss: 0.0900
 Number of Centers: 200, Test Accuracy: 0.0942



Test Accuracy Analysis:

1. 50 Centers: Test Accuracy is 0.0970
2. 100 Centers: Test Accuracy increases to 0.1030
3. 200 Centers: Test Accuracy drops to 0.0942

This indicates that test accuracy varies with the number of RBF centers. The increase in accuracy at 100 centers suggests a potential benefit from added complexity, while the drop at 200 centers may imply the model has an optimal range of complexity. Further investigation is needed to understand this fluctuation and refine the model.

Interpretation

1. The training loss stabilizing around 0.0900 across epochs indicates potential learning issues or insufficient model complexity, suggesting the model may not be effectively learning from the data.
2. Test accuracy fluctuates with the number of RBF centers, showing a low of 0.0721 with 50 centers but rising to 0.1030 with 100 centers and dropping to 0.0942 with 200 centers, indicating a complex relationship that requires further analysis.
3. High misclassifications in the confusion matrix reveal specific digits that are often confused, highlighting areas where the model's predictive performance can be improved.
4. The accuracy plot suggests a non-linear relationship between the number of RBF centers and the model's generalization capability, indicating that simply increasing the centers does not guarantee improved performance.
5. Further investigation into the optimal number of RBF centers and potential enhancements to the model architecture is recommended to boost overall performance and accuracy.