Electric Power System tutorial 2.
Powergrid and technology for renewable production

Content

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Problems from Electric Power Systems, by Ned Mohan

Example 5.4, power flow calculation

Consider the 345 kV transmission from example 5.4 in [1] as shown in Figure 15. You shall now calculate the power flow using Matlab/Simscape.

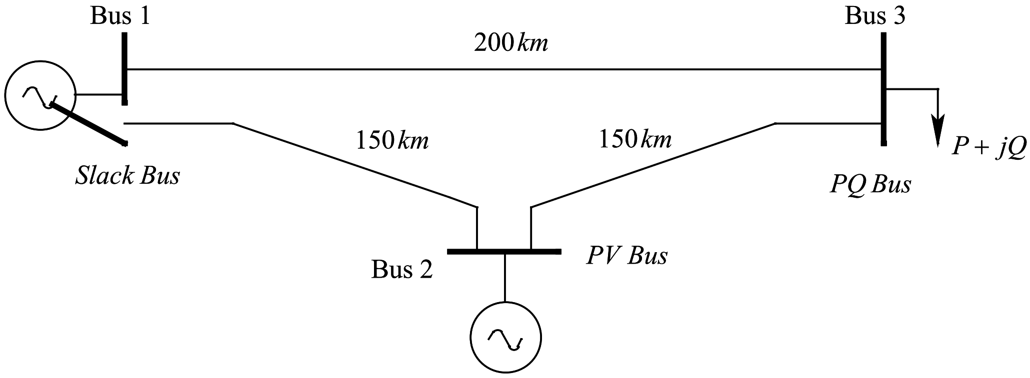


Figure 1 Transmission system 345 kV

Line data:

Series reactance $X_L = \omega L = 0.376\ \Omega/km$
Series resistance $R_L = 0.037\ \Omega/km$
Shunt susceptance $B = \omega C = 4.5\ \mu\Omega/km$

The actual impedance and susceptance of the line sections are defined related the actual line length. The three busses of the system are defined as:

$$U_b = 345\ kV$$
$$S_b = 100\ MVA$$
$$\omega = 2\pi f, f = 60\ Hz$$

- Bus1, slack bus: $V_1 = 1.0\angle 0°\ pu$
- Bus2, PV-bus: $V_2 = 1.05\ pu,\ P_2^{sp} = 2.0\ pu$
- Bus3, PQ-bus: $P_3^{sp} = -5.0\ pu, Q_3^{sp} = -1.0\ pu$

Simscape power flow setup

Simscape is an extension of Simulink to provide circuit simulation models in for example power systems. In Simscape we can build up circuits using models for the voltage sources, transmission lines and loads.

In this task you shall setup up the 3-bus transmission system as shown in Figure 1.

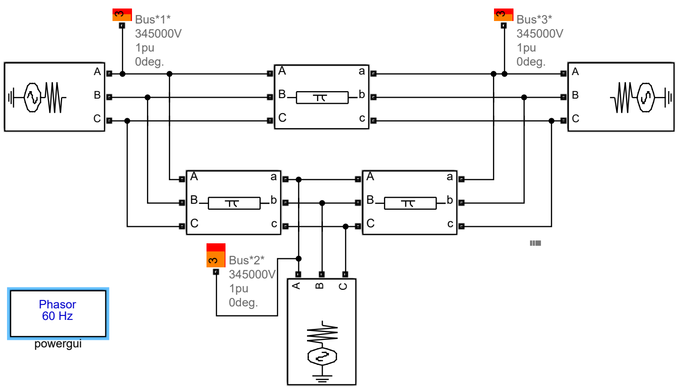


Figure 2 Three-bus transmission system example in Simscape

To invoke Simscape type **simscape** in the command window. The following window will appear, where **Electrical** shall be selected.

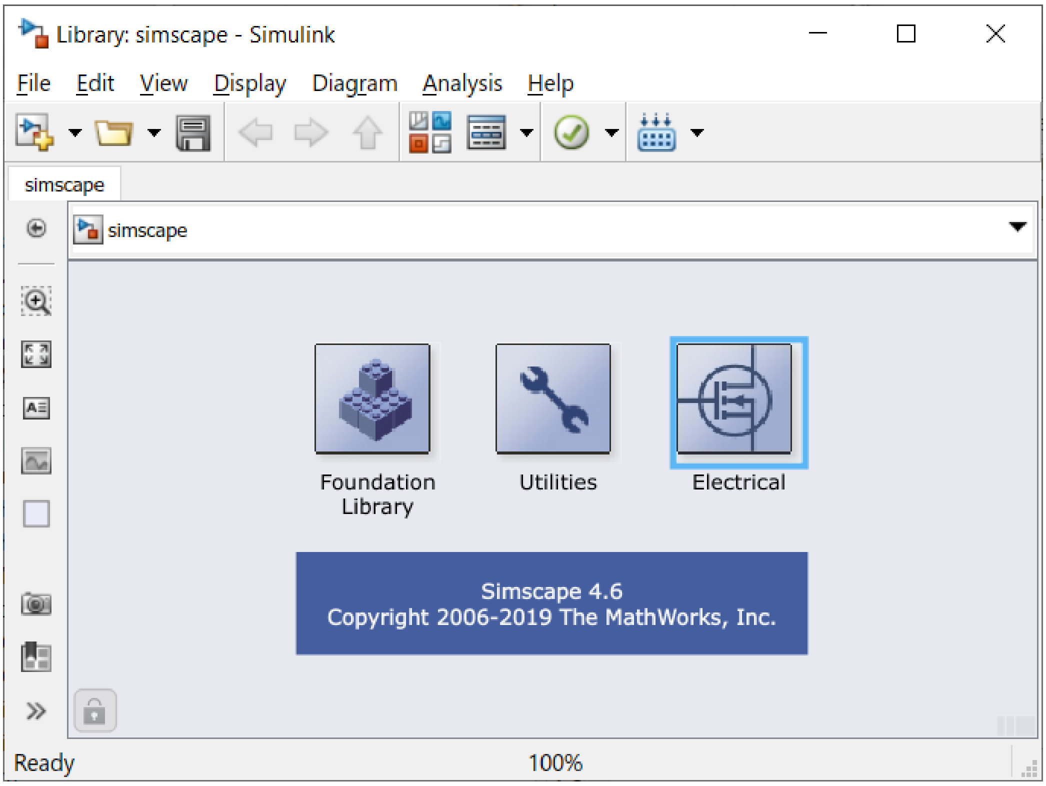


Figure 3 Simscape start window

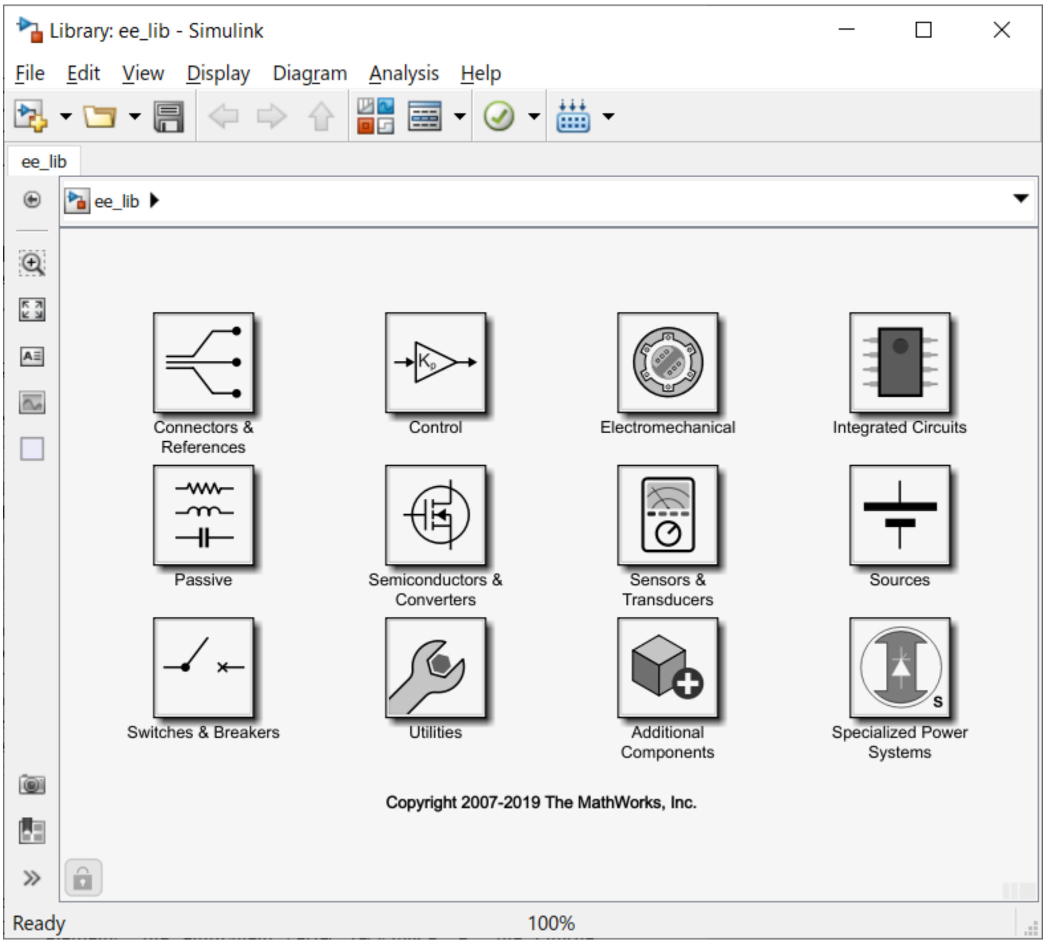


Figure 4 Simscape Electrical

Thereafter, **Specialized Power Systems** shall be selected, and in the next step the power flow components are found under **Fundamental blocks**.

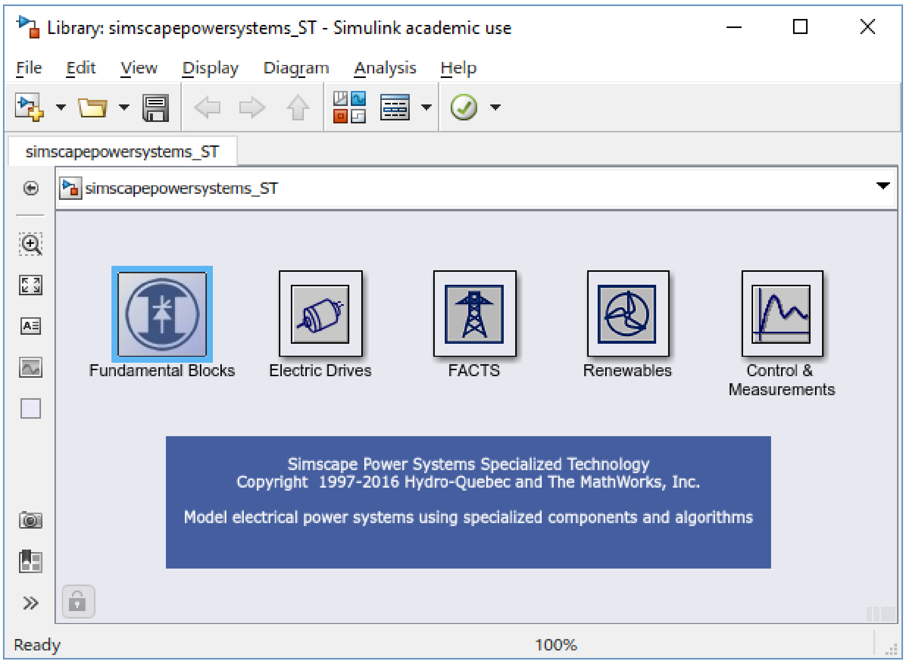


Figure 5 Simscape Specialized Power Systems

1. Create a blank model through the **New** button
2. Add the powergui block (found in Fundamental Blocks library) for simulation control and to obtain load flow calculation functionality.

   In the block parameters, set Simulation type to Phasor, 60 Hz.

Now you shall find components for the slack bus, the PV-bus, the PQ-bus and transmission lines.

- Slack-bus, PV-bus and PQ-bus (PQ-load) can all be modelled using the **Three-phase Source** (Figure 7) found among **Electrical Sources**.
- Transmission lines are modelled by **Three-phase PI-section Line** (Figure 8) also found among **Elements**.

Note: A quick way of adding new components is to, after pointing at the model area, typing the name of the component: e.g. Three-phase source. All models with the same first words will appear for selection.

Connection of blocks is done by tapping and dragging between terminals to join. Also, when placing a new block in line with another, light blue lines will appear as suggested connections. Tapping these will make them connect. Change of connections is done by dragging the end to a new point.

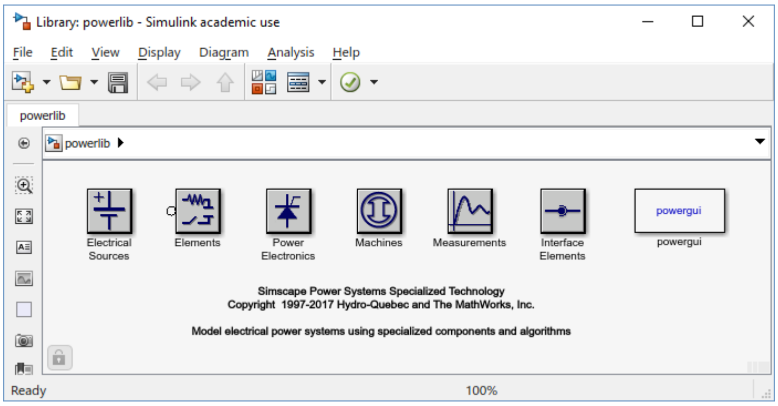
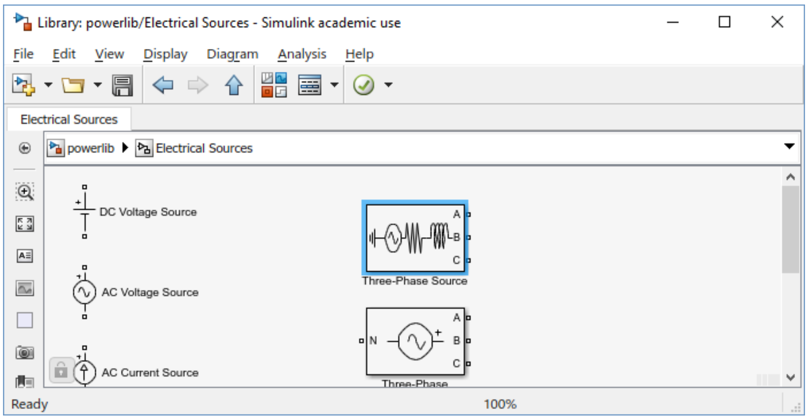

Library: powerlib - Simulink academic use
File Edit View Display Diagram Analysis Help
powerlib
Electrical Sources
Elements
Power Electronics
Machines
Measurements
Interface Elements
powergui
Simscape Power Systems Specialized Technology
Copyright 1997-2017 Hydro-Quebec and The MathWorks, Inc.
Model electrical power systems using specialized components and algorithms
Ready
100%

Figure 6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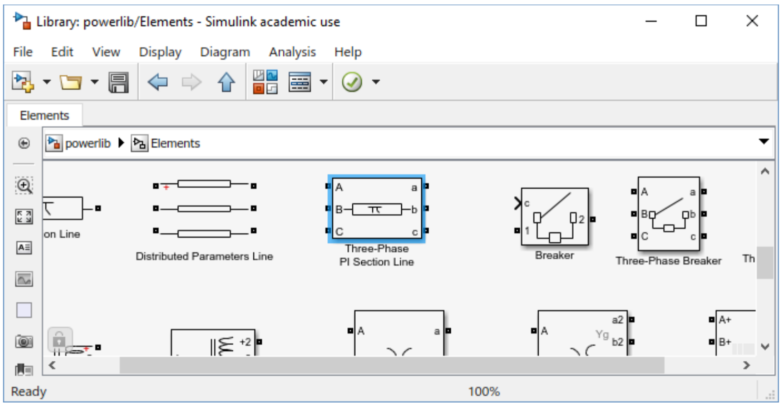
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Breaker
Three-Phase Breaker
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Setting of slack bus (swing bus)

The following parameters are defined for the slack bus in Figure 9:

1. Configuration: Yg (Star connected to ground)
2. Ph-ph voltage: 345 kV
3. Ph angle: 0 deg
4. Freq: 60 Hz
5. Impedance internal (small but non-zero to enhance solution):
   0.01 ohm, L=0, Vbase=345 kV
6. Load flow: swing
7. The voltage reference will be set later in a separate, so-called **bus block**.

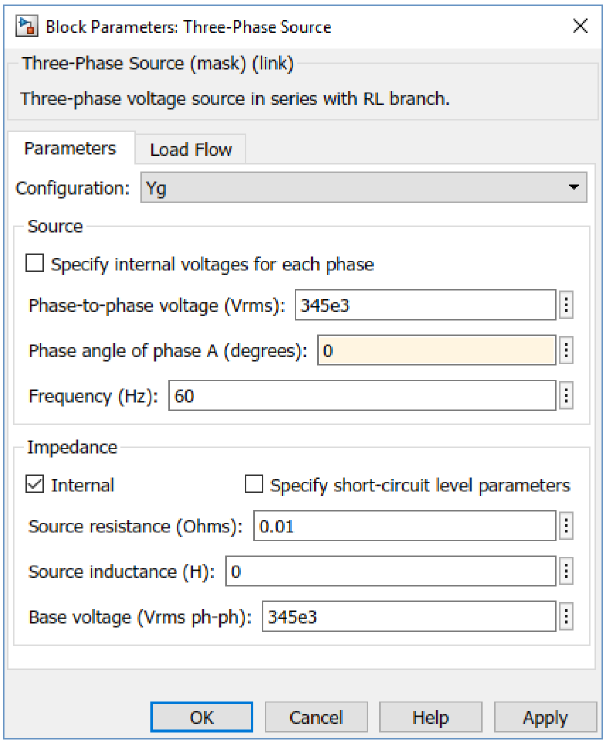


Figure 9 Slack bus parameters

Setting of PV-bus

The PV-bus (2) is setup same as the slackbus except for the Load flow Tab (Figure 10):

1. Configuration: Yg (Star connected to ground)
2. Ph-ph voltage: 345 kV
3. Ph angle: 0 deg
4. Freq: 60 Hz
5. Impedance internal: 0.01 ohm, L=0, Vbase=345 kV
6. Load flow: PV, P=200 MW, Qmin=-inf, Qmax=inf
7. The voltage reference will be set later in a separate, so-called **bus block**.

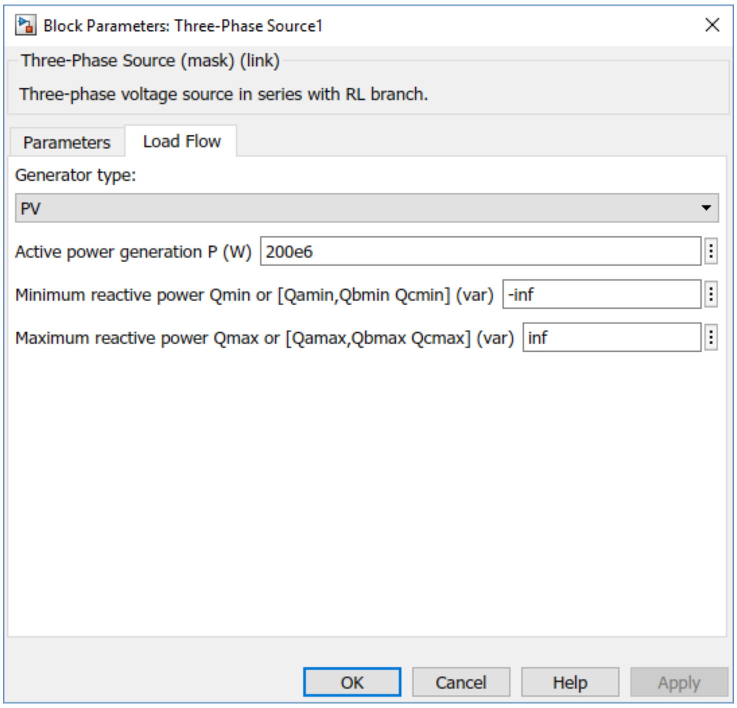


Figure 10 Load flow settings for the PV-bus

Setting of PQ-bus

The PQ-load is setup for 500 MW, 100 MVar loading by negative numbers for the Three-phase source component as shown by Figure 11. Other parameters of the Three-phase source are set same as for the slack-bus.

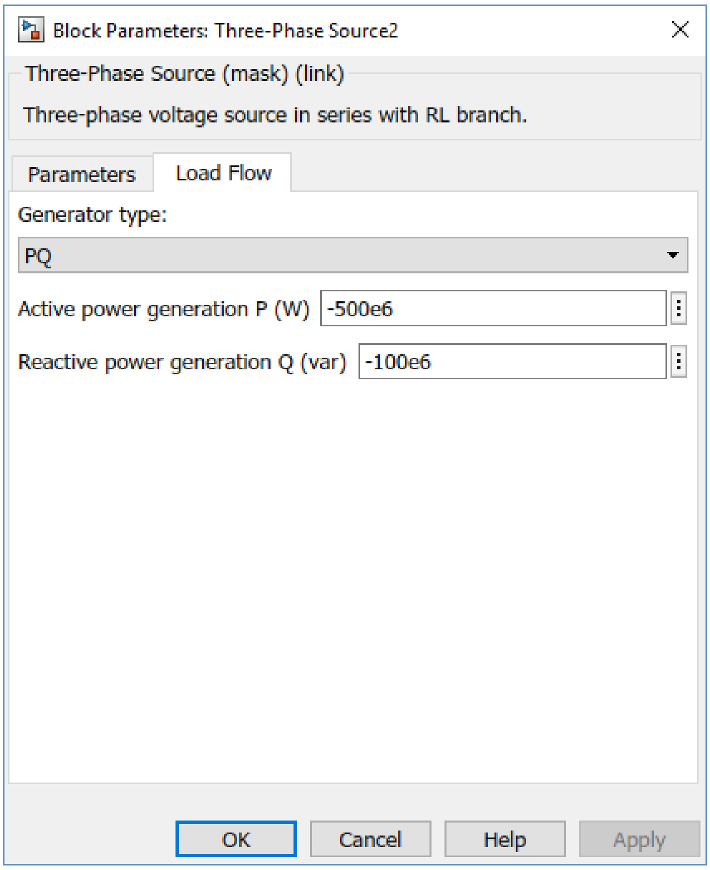


Figure 11 PQ-bus load flow settings

Setting of transmission lines

The transmission line data in this model is given as resistance, inductance and capacitance per km. Consequently, the series reactance and shunt susceptance values defined in example 5.4 above shall be converted to inductance and capacitance for a 60 Hz system frequency. The data in the model is given as positive and zero sequence values, which could be set equal as shown by Figure 12.
Since all the lines have the same line parameters except for the length, setup one line first and copy the whole line block to the other locations. Thereafter setting the length parameters.

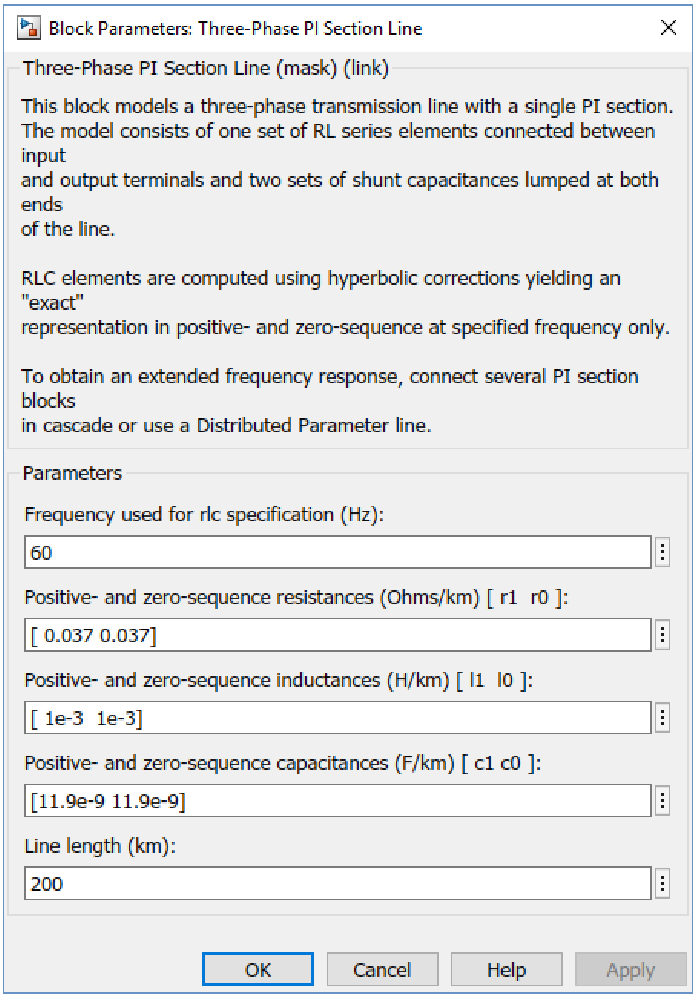
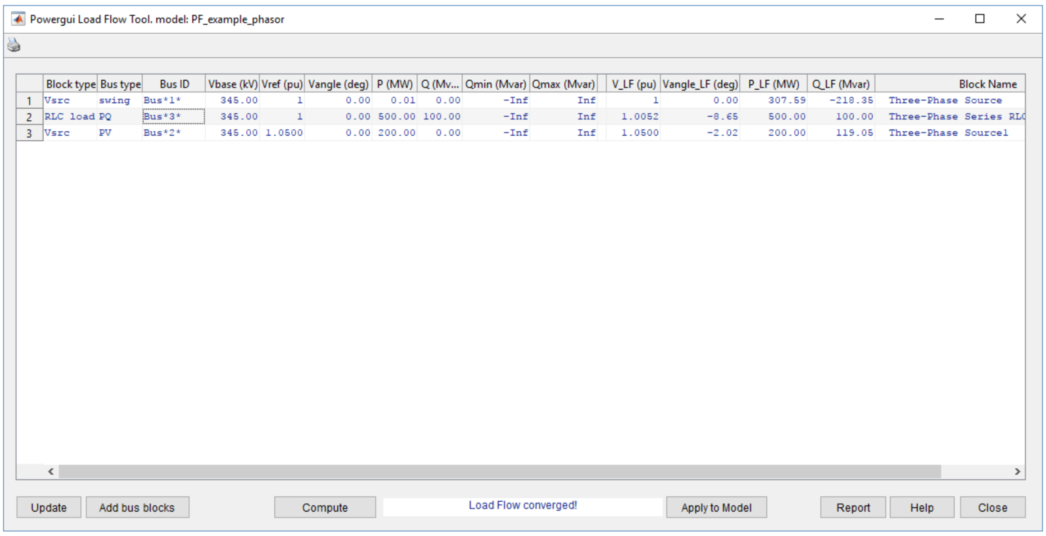


Figure 12 Transmission line parameters

Load flow calculation

By clicking the powergui block and selecting the **Tools** menu, a Load flow calculation tool can be entered.

1. Check **Load flow settings** for 60 Hz, S_{base}=100 MVA, voltage and power units as kV and MW.
2. Click the **Load Flow** button to bring up a window as in Figure 13.
3. Clicking the button **Add bus blocks**, results in the Load flow bus labels (red flags) being inserted next to each bus according to Figure 2.
4. Go back to the model page and edit the Load Flow Bus blocks.
    a. In the blocks related to the slack-bus (Bus 1) and PV-bus (Bus-2) the target voltage and angle settings are given (only voltage for the PV-bus) See Figure 14. $V_1 = 1.0\angle 0°\ pu$, $V_2 = 1.05\ pu$
    b. Check the bus blocks numbering as defined earlier for this example: slack-bus (Bus 1), PV-bus (Bus-2) and PQ-bus (Bus-3).
5. In the powergui Load Flow Tool now press Compute to perform the load flow calculation.
6. Click Apply to Model to save the load flow as initial conditions for the voltage sources of the system.
7. Generate a Load flow report through the **Report** button. Select MATLAB *.rep file for fastest response.
8. Close the Load flow tool.
9. Save the model file again to retain the updated initial conditions.



	Block type	Bus type	Bus ID	Vbase (kV)	Vref (pu)	Vangle (deg)	P (MW)	Q (Mv...	Qmin (Mvar)	Qmax (Mvar)	V_LF (pu)	Vangle_LF (deg)	P_LF (MW)	Q_LF (Mvar)	Block Name
1	Vsrc	swing	Bus*1*	345.00	1	0.00	0.01	0.00	-Inf	Inf	1	0.00	307.59	-218.35	Three-Phase Source
2	RLC load	PQ	Bus*3*	345.00	1	0.00	500.00	100.00	-Inf	Inf	1.0052	-8.65	500.00	100.00	Three-Phase Series RLC
3	Vsrc	PV	Bus*2*	345.00	1.0500	0.00	200.00	0.00	-Inf	Inf	1.0500	-2.02	200.00	119.05	Three-Phase Source1

Figure 13 Load flow window

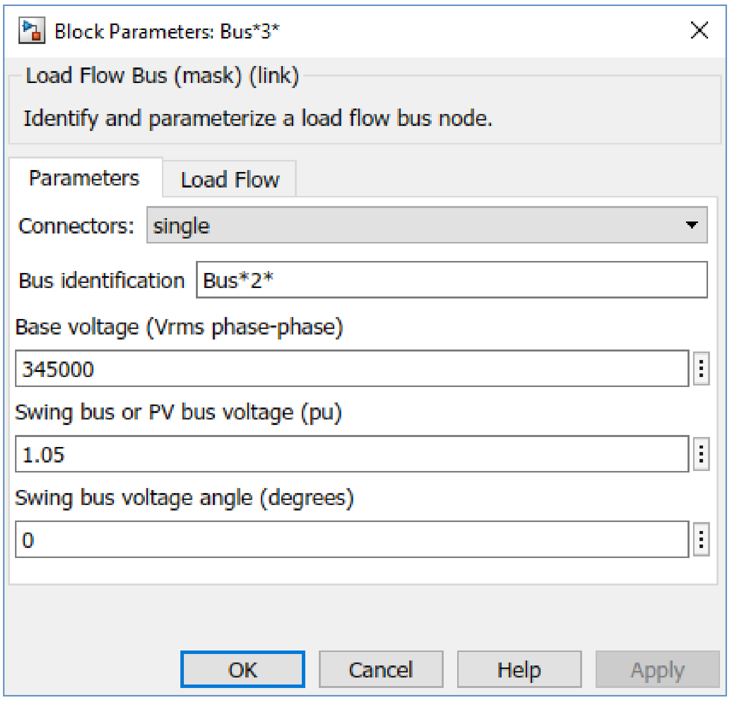


Figure 14 Load flow bus-2 block settings

Supplementary questions

2. Determine the active power loading of the individual lines as given by the load flow report.

sending bus – receiving bus	P into line [MW]	Q into line, sending end [Mvar]	Q into line, receiving end [Mvar]	Total Q into line [Mvar]
1-3				
1-2				
2-3				

3. Determine which lines are loaded above and below SIL.
4. With the background of loading compared to SIL explain the levels of total Q of the lines.

10.20

In the power flow of example 5.4, what will the voltage be at bus-3 if the power demand (P and Q) at bus-3 is increased by 100%?

Dynamic simulation

By changing the model used for the PQ-load from the Three-phase source to a **Three-phase Dynamic Load**, stepping of the load during a time simulation can be done. In Figure 16 below the Simscape setup using a dynamic load is shown.

Save your previous model to a new name for preparation of this modified setup. Retain the previous model for load flow calculations without the dynamic simulation.

Parameters of the dynamic load shall be setup,

1. defining the base voltage and frequency,
2. as well as the initial P and Q.
3. Initial voltage and angle is not required to fill, since using the Load flow tool will do this.
4. Furthermore, external control of PQ shall be selected.

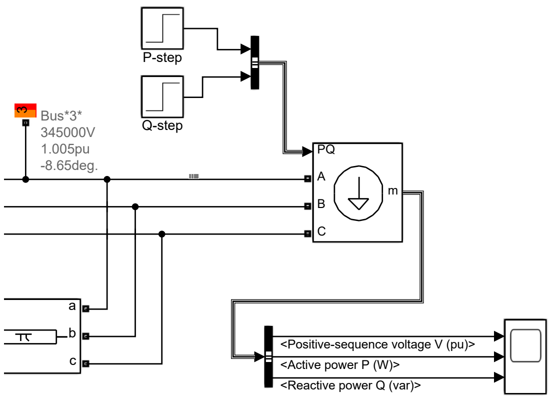


Figure 15 PQ-load replaced by Dynamic load

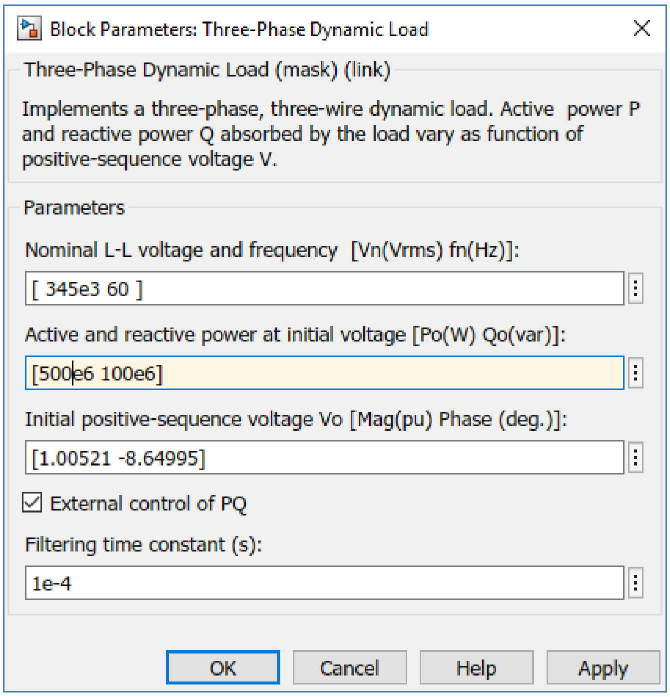


Figure 16 Dynamic load settings

To complete the setup, the external PQ input and the measurement of resulting voltage and PQ-flow, shall be defined. The complete Simulink library is reached through the button  .

1. Add two **Step** blocks (found in Simulink/Sources, or by typing Step after pointing at the model area).
    a. Setup the Step blocks for a step at 1s, where P changes from 500 to 1000 MW, and Q from 100 to 200 Mvar.
2. Add a **Bus Creator** (in Simulink/Commonly used blocks) to make a 2-dimensional bus for interfacing the dynamic load PQ input.
3. Add a **Bus Selector** to separate the three signals obtained at the m-output.
    a. Double click the Bus Selector to perform setup. You can see the three available signals to the left. By marking them and clicking select they will move to the right-hand side. Delete any initial undefined signals on the right side.
4. Add a **Scope** (in Simulink/Commonly used blocks) for plotting.
    a. Double click to setup. Selecting **File/Number of input ports/More…** brings up the following window.
    b. Set number of input ports to 3
    c. Maximize axes: Auto

   d. Axes scaling: Auto
   e. Click layout to define the layout of the 3 sub-plots.

5. Under the menu Model Configuration Parameters and the tab **Solver**,
   a. Simulation stop time: 2 s.
6. Open the powergui Load Flow Tool and press Compute to perform the load flow calculation related to the initial conditions with PQ-load of 500 MW and 100 Mvar.
   a. Compare the results with earlier Simscape load flow.
   b. Click Apply to Model to save the load flow as initial conditions for the new Dynamic Load.
   c. Close the Load flow tool.
7. Start simulation through button.
8. On the Scope graphs you may now determine the final voltage level after the PQ-load increase.

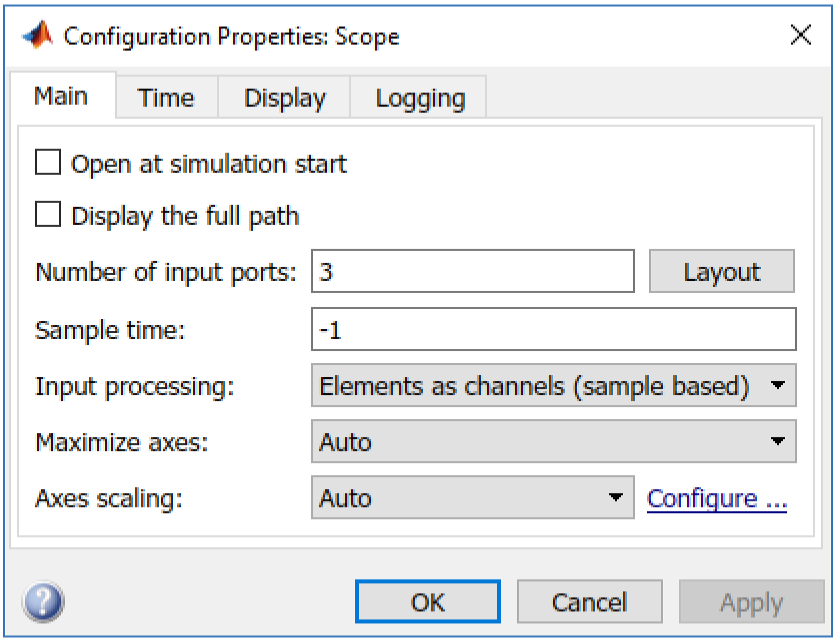


Figure 17 Scope sub-plot layout and settings

10.21

For the problem 10.20, with bus-3 loading increased by 100%, what reactive power compensation needs to be provided at bus-3 to bring its voltage to 1 pu?
Use Simscape model for load flow calculation without dynamic simulation,

1. changing bus-3 **Three phase source** from PQ-bus to a PV-bus
2. with 1000 MW load
3. and 1 pu voltage setting. This is given in the Load flow bus-3 block.

4. Use the Load flow tool to find the net reactive power for this voltage level.
5. Save a Load flow report from the Load flow tool.
6. Determine reactive power compensation at bus-3 that would be required in combination with the original inductive Q-load of 200 Mvar.

Supplementary questions

1. Determine the surge impedance and surge impedance loading (SIL) for the transmission lines.
2. Determine the active power loading of the individual lines as given by the load flow report.

sending bus – receiving bus	P into line [MW]	Q into line, sending end [Mvar]	Q into line, receiving end [Mvar]	Total Q into line [Mvar]
1-3				
1-2				
2-3				

3. Determine which lines are loaded above and below SIL.
4. With the background of loading compared to SIL explain the levels of total Q of the lines.
5. Compare the line loading and Q consumption with the supplementary questions to the original load flow calculation.

10.22 Series compensation

In the circuit with a dynamic load 10.20, insert a series capacitor in series with the 200 km line to effectively reduce the line impedance to 50%. The series capacitor is modeled by a **Three-Phase series RLC branch**, where only C is used. What improvement is obtained in the voltage stability when the load at bus 3 steps up by 100%.

Example 5.4, admittance matrix setup

Consider the 345 kV transmission from example 5.4 in [1] as shown in Figure 15. You shall setup the admittance matrix for this 3-bus system.

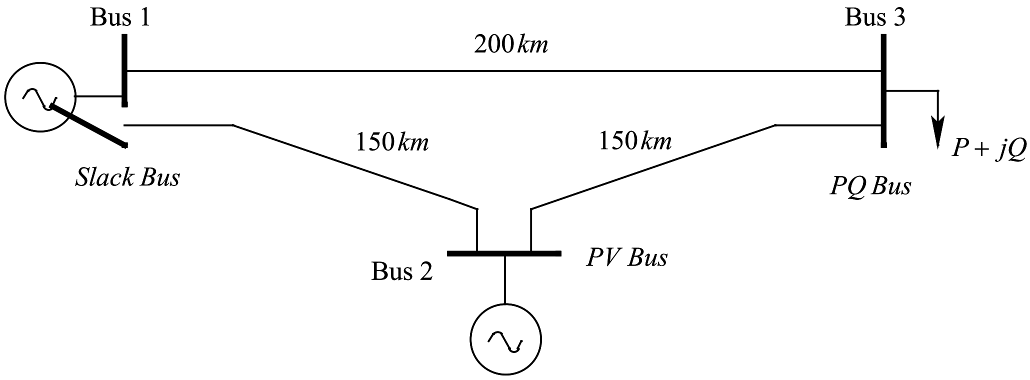


Figure 18 Transmission system 345 kV

Line data:

series reactance = $0.376\ \Omega / km$,
series resistance = $0.037\ \Omega / km$,
shunt susceptance $B(=\omega C) = 4.5\,\mu\square\ / km$

The actual impedance and susceptance of the line sections are defined related the actual line length:

$$Z_{12} = (0.037 + j0.376) \cdot Length_{(1-2)}\ ohm$$

$$B_{12} = 4.5 \cdot Length_{(1-2)}\ \mu ohm$$

Convert the parameters to pu using

$$Z_{base} = \frac{U_{ph}^2}{S_{ph}} = \frac{U_{LL}^2}{S_{3ph}} = \frac{U_{base}^2}{S_{base}} = \frac{345kV^2}{100MVA} = 1190\ ohm$$

$$Y_{base} = \frac{1}{Z_{base}}$$

Setup the admittance matrix elements as defined below.

Make a MATLAB script file containing all calculations, rather than making calculations directly in the command window. This gives better flexibility to adjust and redo calculations when needed.

$$\begin{bmatrix} \overline{I}_1 \\ \overline{I}_2 \\ .. \\ .. \\ .. \\ \overline{I}_n \end{bmatrix} = \begin{bmatrix} Y_{11} & Y_{12} & .. & .. & .. & Y_{1n} \\ Y_{21} & Y_{22} & .. & .. & .. & Y_{2n} \\ .. & .. & .. & .. & .. & .. \\ .. & .. & .. & .. & .. & .. \\ .. & .. & .. & .. & .. & .. \\ Y_{n1} & Y_{n2} & .. & .. & .. & Y_{nn} \end{bmatrix} \begin{bmatrix} \overline{V}_1 \\ \overline{V}_2 \\ .. \\ .. \\ .. \\ \overline{V}_n \end{bmatrix}$$

Elements in the diagonal are defined as:

$$Y_{kk} = Y_{kG} + \sum_{\substack{m \\ m \neq k}} \frac{1}{Z_{km}}$$

Where Y_{kG} is the total admittance to ground at bus (node) k. For each line, the total B is split equally between the ends of the line.

$$Y_{kG} = j \sum_{\substack{m \\ m \neq k}} \frac{B_{km}}{2}$$

For elements out of the diagonal, the negated admittance of the line between bus k and bus m is given by:

$$Y_{km} = -\frac{1}{Z_{km}}$$

Example 5.4, power flow solution

Using the admittance matrix defined in the previous task, you shall now solve the power flow for this three-bus system. The three busses of the system are defined as:

- Bus1, slack bus: $V_1 = 1.0\angle 0° \; pu$
- Bus2, PV-bus: $V_2 = 1.05 \; pu, \; P_2^{sp} = 2.0 \; pu$
- Bus3, PQ-bus: $P_3^{sp} = -5.0 \; pu, Q_3^{sp} = -1.0 \; pu$

The solution to the system implies knowing all three bus voltages to both magnitude and phase. Related to the conditions for the busses defined above we are missing three variables: Angle(V2), magnitude and angle of V3.

You will use MATLAB fsolve to solve the power flow of this system.

fsolve

Solve system of nonlinear equations

Nonlinear system solver

Solves a problem specified by

$$F(x) = 0$$

for x, where $F(x)$ is a function that returns a vector value.

x is a vector or a matrix; see Matrix Arguments.

Here F(x) are a set of equations that defined the solution. In our case we have three conditions which we want to arrive at as defined for the busses above:

$$P_2 = P_2^{sp} = 2\,pu$$
$$P_3 = P_3^{sp} = -5\,pu$$
$$Q_3 = Q_3^{sp} = -1\,pu$$

So, we have three equations to solve to get the three unknowns! The unknowns are defined as x(1)=angle(V2), x(2)=magnitude(V3), x(3)=angle(V3).

To use fsolve you will make the following function call in MATLAB to obtain the solution for the unknown x's:

```
x=fsolve(@PFsolve,x0,[],y,vref,pqref)
```

- Here, PFsolve is a function given for use together with fsolve for this example. See function listing below.
- x0 is a 3 element vector with the initial guess for the solution of x. Use 0 for initial angles and 1 for voltage, such as x0=[0 1 0].
- y is the admittance 3x3 matrix.
- vref defines the known voltages and is a vector of three elements. Set unknown element to zero.
- pqref is the reference for P and Q, also a vector of three elements. Set unknown element to zero and give elements where both P and Q are defined as P+jQ.

```
function [ dpq,pq,vk,ik ] = PFsolve( x,y,vref,pqref )
%PFsolve Summary of this function goes here
%   x: variables for solution
%   y: admittance matrix
%   vref: voltage references for slack-bus or PV-busses.
%       Complex value if angle is defined for slack-bus.
%   pqref: p-references for PV-busses and p+jq for PQ-
busses.

% Node voltages
vk(1,1)=vref(1);
vk(2,1)=vref(2)*exp(1j*x(1));
vk(3,1)=x(2)*exp(1j*x(3));
```

```
% Injected currents into nodes
ik=y*vk;

% Injected power into nodes
pq=vk.*conj(ik);

% Equations to solve for zero through variables in x
dpq(1)=real(pqref(2)-pq(2));
dpq(2)=real(pqref(3)-pq(3));
dpq(3)=imag(pqref(3)-pq(3));
end
```

After getting a solution (x) from fsolve, all the values for P, Q, voltage and current for the three busses, can be obtained through the function call of PFsolve directly, with the solution x as the first parameter:

```
[ dpq,pq,vk,ik ] = PFsolve( x,y,vref,pqref )
```

- dpq is the deviation from the ideal solution
- pq is the P+jQ injection in each bus
- vk is the bus voltage
- ik is the injected current in each bus

1. Fill the table with the load flow results obtained:

Bus no	Voltage magnitude [pu]	Voltage angle [deg]	Active power [pu]	Reactive power [pu]
1				
2				
3				

Table 1 Load flow results

2. Compare the results with earlier results from the MATLAB Simscape load flow calculation.
3. How much are the total active power line losses in the system given in MW?
4. How much are the total reactive power line losses in the system given in Mvar?

Literature:

[1] Electric Power Systems a first course, Ned Mohan, Wiley 2012