

# Assignment3

Anton Linnér

2023-10-04

\section(Random number generation from bivariate EVD) \subsection(Parametric bivariate EV models) In the package `evd` the nine models and their respective dependence and asymmetry parameters are:

- Logistic. Dependence parameter  $\mathbf{r}$  between  $(0,1]$ . Smaller  $\mathbf{r}$  implies higher dependence.
- Asymmetrix logistic. Dependence parameter  $\mathbf{r}$ , as in (symmetric) Logistic. Asymmetry parameters are  $\mathbf{t}_1$  and  $\mathbf{t}_2$ . Indence if any of  $\mathbf{t}_1, \mathbf{t}_2$  are 0 or  $\mathbf{r} = 1$ . For complete dependence  $\mathbf{t}_1 = \mathbf{t}_2 = 1$  and  $\mathbf{r} \rightarrow 0$ .
- Husler-Reiss. Dependence parameter  $\mathbf{r} \in (0, \text{inf})$ . Full dependence as  $\mathbf{r} \rightarrow \text{inf}$ , and independence as  $\mathbf{r} \rightarrow 0$
- Negative logistic. Dependence parameter  $\mathbf{r} > 0$ . Higher  $\mathbf{r}$  implies higher dependence.
- Asymmetric negative logistic. Dependence parameter  $\mathbf{r} > 0$  and asymmetry parameters  $\mathbf{t}_1, \mathbf{t}_2 \in (0, 1]$ . Indence if any of  $\mathbf{t}_1, \mathbf{t}_2, \mathbf{r}$  approaches 0. Complete dependence if  $\mathbf{t}_1, \mathbf{t}_2 = 1, 1$  and  $\mathbf{r} \rightarrow \text{inf}$ .
- Bilogistic. Parameters  $\alpha, \beta$ . When  $\alpha = \beta$  the model is equivalent to logistic with dependence parameter  $\mathbf{r} = \alpha$ . As in logistic, when  $\alpha = \beta = \mathbf{r} \rightarrow 0$  the model tends to complete dependence. Independence as either both tends to 1, or one is fix and other tends to 1.
- Negative bilogistic Parameters  $\alpha, \beta$ . When  $\alpha = \beta$  the model is equivalent to negative bilogistic with dependence parameter  $\mathbf{r} = 1/\alpha$ . When  $\alpha = \beta \rightarrow 0$  the model tends to complete dependence. Independence as either both tends to  $\text{inf}$ , or one is fix and other tends to  $\text{inf}$ .
- Coles-Tawn. Parameters  $\alpha, \beta > (0, 0)$ . As  $\alpha = \beta \rightarrow \text{inf}$  the model shows complete dependence. Independence as either both tends to 0, or one is fix and other tends to 0.
- Asymmetric mixed distribution. Parameters  $\alpha, \beta$  fulfill the following conditions:  $\alpha$  and  $\alpha + 3\beta > 0$ , and  $\alpha + 2\beta, \alpha + \beta \leq 1$  As  $\beta$  is fix, the strength of dependence increases with  $\alpha$ . Complete dependence is not achievable. Independence as  $\alpha = \beta = 0$ .

```
sim1 = rbvevd(200, dep=1, model = "hr") #HR
plot(sim1)
```

