Python code and analysis

```
import numpy as np
2 import matplotlib.pyplot as plt
                           # the half width of the well in angstroms
a = 3.0
5 \text{ m} = 1.0
                           # mass of electron in 1 me units
6 \text{ V0} = 10.0
                           # height/depth of well in eV
_{7} \text{ hbar} = 1.0
                           # hbar
s delta = np. sqrt(2.0*m*V0*(a**2.0)/(hbar**2.0))
                                                          # Defined in the hand written solution
eta = np.arange(0.001,2*np.pi,0.01) # Defined in the hand written solutiom
10
def f(f, eta):
12
       This is the lhs in the transcendental equations.
13
       return np. sqrt(((delta/eta)**2.0)-1.0)
15
17 def f1(eta):
18
       The equation whose zeros are to be found to obtain the even solution.
19
20
       return f(eta) - np.tan(eta)
21
22
23 def f2(eta):
24
       The equation whose zeros are to be found to obtain the odd solution.
25
26
       return f(eta) + (1.0/np.tan(eta))
27
28
def firstDerivative_O4(function, x0, stepsize):
30
       Returns first derivative of the function "function" at the point x0 by considering points, one and two
31
        steps on either side of x0.
       The Accuracy is of order (stepsize) 4.
32
33
34
       return (function (x0 - 2.0* stepsize) - 8.0* function (x0 - stepsize) + 8.0* function (x0 + stepsize) -
       function (x0 + 2.0*stepsize))/(12.0*stepsize)
35
  def Newton_Raphson(f,x0,stepsize):
36
37
       Returns the zero of f. x0 is the guess. stepsize will be used for determining the first derivative of
38
39
       fprime = firstDerivative_O4(f,x0,stepsize)
40
       x1 = x0 - (f(x0)/fprime)
41
       while ((x0 - x1)) > = stepsize **(8.0)):
42
           x0 = x1
           fprime = firstDerivative_O4(f,x0,stepsize)
44
45
           x1 = x0 - f(x0)/fprime
       return x1
46
47
48
  def get_energy(eta):
49
       Gets energy value for given eta value.
50
51
       return (eta**2.0)*(hbar**2.0)/(2.0*m*(a**2.0))
52
54 ##### Main portion begins #####
even_guess = np.pi/4.0 # Guess for even solution odd_guess = 0.999*np.pi # Guess for odd solution
 \text{even\_sol} = \text{Newton\_Raphson}(\text{f1}, \text{even\_guess}, 10**(-3)) \ \# \ \text{Obtaining the solution using the Newton Raphson method} 
odd_sol = Newton_Raphson(f2, odd_guess, 10**(-3)) # Obtaining the solution using the Newton Raphson method
61 ### Printing the solutions
print ("eta for even sol : {etev:0.6 f}".format(etev=even_sol))
print("eta for odd sol : {etod:0.6f}".format(etod=odd_sol))
print ("Energy for even state is : {e2:0.6f}".format(e2=get_energy(even_sol)))
print ("Energy for odd state is : {e1:0.6f}".format(e1=get_energy(odd_sol)))
```

The outputs are shown below:

Even solution (η)	Odd solution (η)	Even energy (eV)	Odd energy (eV)
1.460	2.922	0.118	0.474



