

# **CS 287 Lecture 20 (Fall 2019)**

## **Model-based RL**

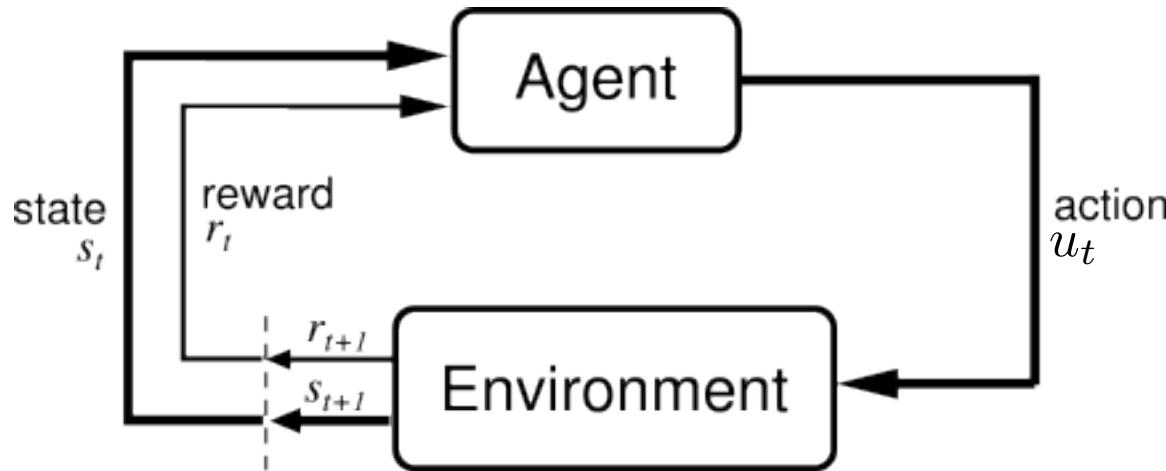
Pieter Abbeel  
UC Berkeley EECS

# Outline

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- Model-based RL
- Ensemble Methods
  - Model-Ensemble Trust Region Policy Optimization
  - Model-based RL via Meta Policy Optimization
- Asynchronous Model-based RL
- Vision-based Model-based RL

# Reinforcement Learning



# “Algorithm”: Model-Based RL

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- For iter = 1, 2, ...
  - Collect data under current policy
  - Learn dynamics model from past data
  - Improve policy by using dynamics model
    - e.g SVG(k) requires dynamics model, but can also run TRPO/A3C in simulator

# Why Model-Based RL?

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- Anticipate data-efficiency
  - Get model out of data, which might allow for more significant policy updates than just a policy gradient
- Learning a model
  - Re-usable for other tasks [assuming general enough]

# “Algorithm”: Model-Based RL

```
for iter = 1, 2, ...
```

- Collect data under current policy
- Learn dynamics model from past data
- Improve policy by using dynamics model

Anticipated benefit?

– much better sample efficiency

So why not used all the time?

-- training instability

→ ME-TRPO

-- not achieving same asymptotic performance as model-free methods

→ MB-MPO

# Overfitting in Model-based RL

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- Standard overfitting (in supervised learning)
  - Neural network performs well on training data, but poorly on test data
    - E.g. on prediction of  $s_{\text{next}}$  from  $(s, a)$
- New overfitting challenge in Model-based RL
  - policy optimization tends to exploit regions where insufficient data is available to train the model, leading to catastrophic failures
  - = “model-bias” (Deisenroth & Rasmussen, 2011; Schneider, 1997; Atkeson & Santamaria, 1997)
  - Proposed fix: Model-Ensemble Trust Region Policy Optimization (ME-TRPO)

# Model-Ensemble Trust-Region Policy Optimization

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**Algorithm 1** Vanilla Model-Based Deep Reinforcement Learning

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- 1: Initialize a policy  $\pi_\theta$  and a model  $\hat{f}_\phi$ .
  - 2: Initialize an empty dataset  $D$ .
  - 3: **repeat**
  - 4:   Collect samples from the real environment  $f$  using  $\pi_\theta$  and add them to  $D$ .
  - 5:   Train the model  $\hat{f}_\phi$  using  $D$ .
  - 6:   **repeat**
  - 7:     Collect fictitious samples from  $\hat{f}_\phi$  using  $\pi_\theta$ .
  - 8:     Update the policy using BPTT on the fictitious samples.
  - 9:     Estimate the performance  $\hat{\eta}(\theta; \phi)$ .
  - 10:    **until** the performance stop improving.
  - 11: **until** the policy performs well in real environment  $f$ .
- 

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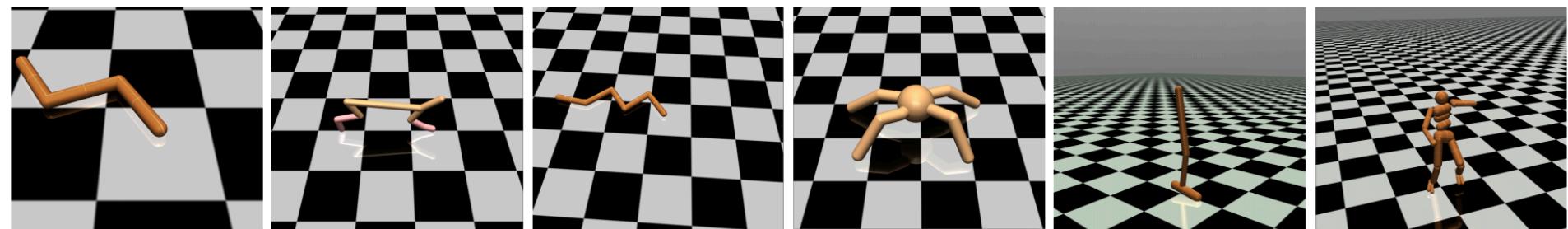
**Algorithm 2** Model Ensemble Trust Region Policy Optimization (ME-TRPO)

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- 1: Initialize a policy  $\pi_\theta$  and all models  $\hat{f}_{\phi_1}, \hat{f}_{\phi_2}, \dots, \hat{f}_{\phi_K}$ .
  - 2: Initialize an empty dataset  $\mathcal{D}$ .
  - 3: **repeat**
  - 4:   Collect samples from the real system  $f$  using  $\pi_\theta$  and add them to  $\mathcal{D}$ .
  - 5:   Train all models using  $\mathcal{D}$ .
  - 6:   **repeat** ▷ Optimize  $\pi_\theta$  using all models.
  - 7:     Collect fictitious samples from  $\{\hat{f}_{\phi_i}\}_{i=1}^K$  using  $\pi_\theta$ .
  - 8:     Update the policy using TRPO on the fictitious samples.
  - 9:     Estimate the performances  $\hat{\eta}(\theta; \phi_i)$  for  $i = 1, \dots, K$ .
  - 10:   **until** the performances stop improving.
  - 11: **until** the policy performs well in real environment  $f$ .
-

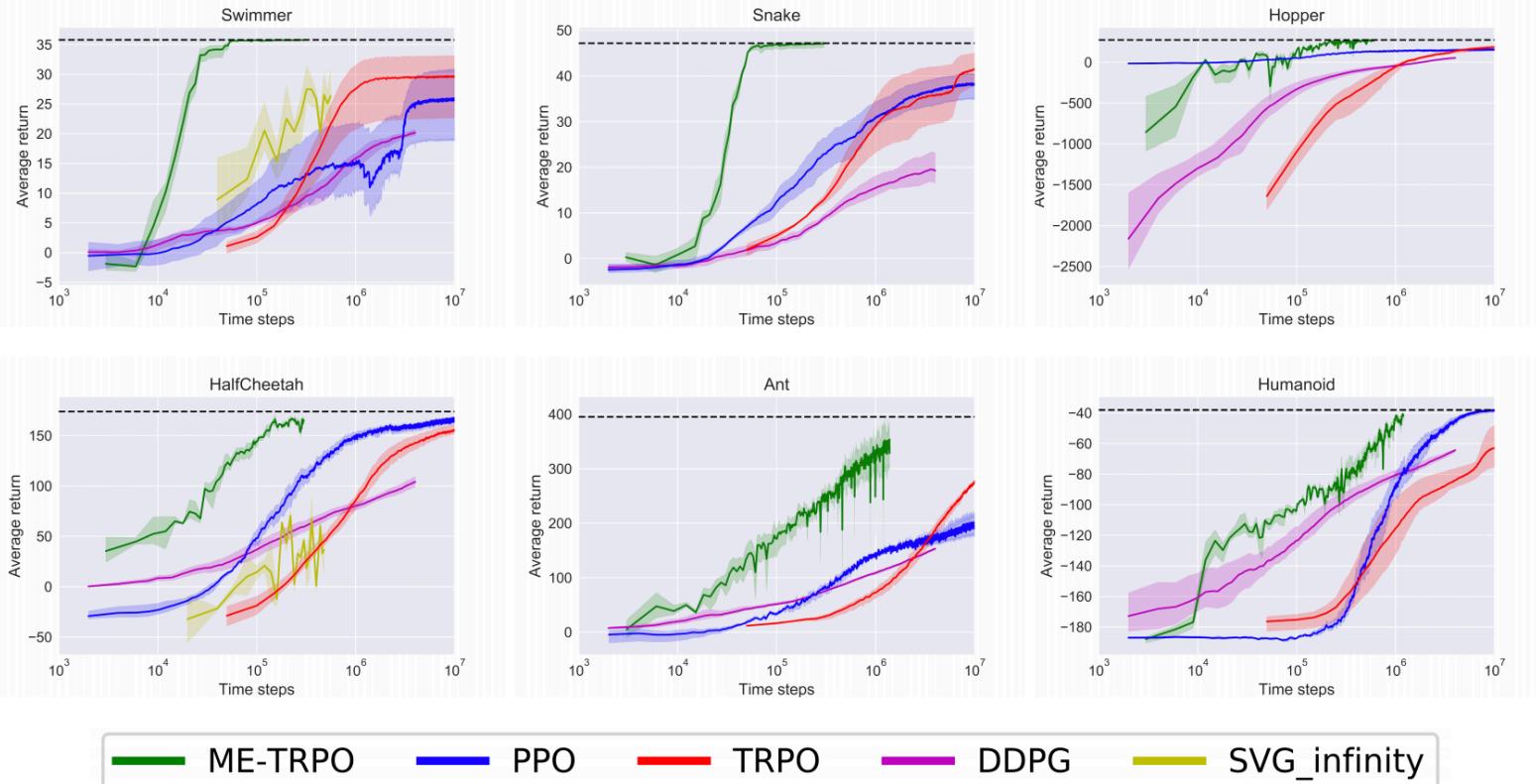
# ME-TRPO Evaluation

- Environments:



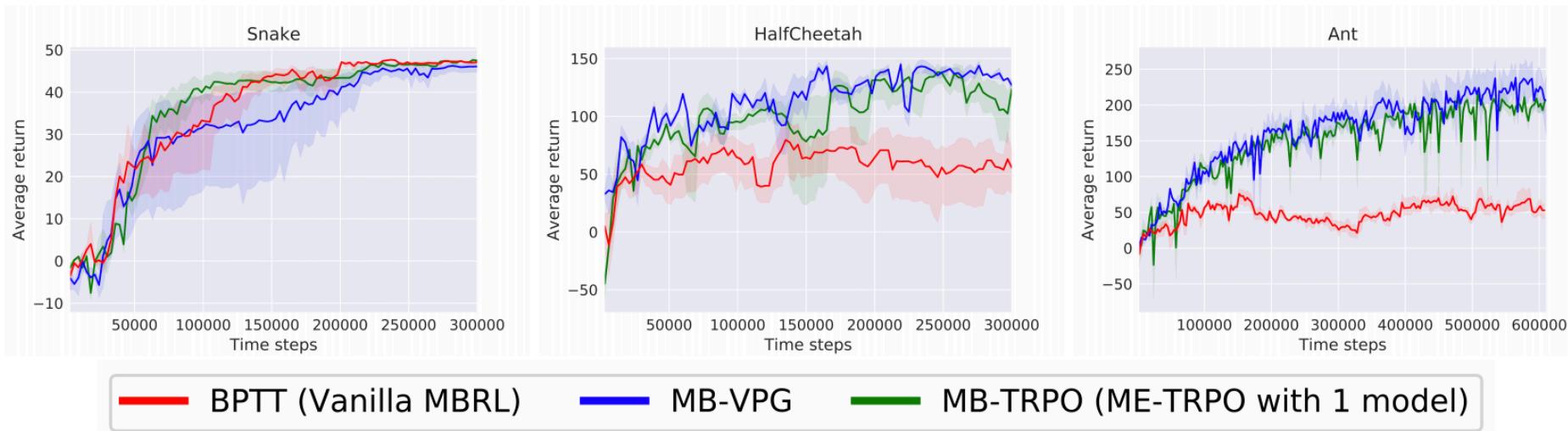
# ME-TRPO Evaluation

## ■ Comparison with state of the art



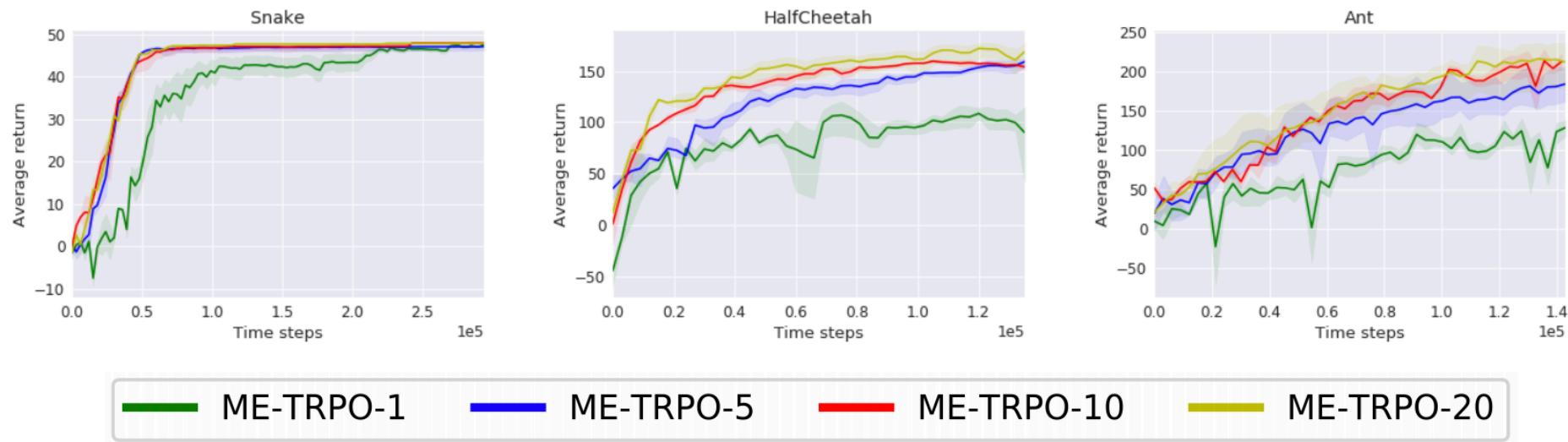
# ME-TRPO -- Ablation

TRPO vs. BPTT in standard model-based RL



# ME-TRPO -- Ablation

Number of learned dynamics models in the ensemble



# “Algorithm”: Model-Based RL

```
for iter = 1, 2, ...
```

- Collect data under current policy
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Anticipated benefit?

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→ ME-TRPO

-- **not achieving same asymptotic performance as model-free methods**

→ MB-MPO

# Model-based RL Asymptotic Performance

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- Because learned (ensemble of) model imperfect
  - Resulting policy good in simulation(s), but not optimal in real world
- Attempted Fix 1: learn better dynamics model
  - Such efforts have so far proven insufficient
- Attempted Fix 2: model-based RL via meta-policy optimization (MB-MPO)
  - Key idea:
    - Learn ensemble of models representative of generally how the real world works
    - Learn an \*\*\*adaptive policy\*\*\* that can quickly adapt to any of the learned models
    - Such adaptive policy can quickly adapt to how the real world works

# Model-Based RL via Meta Policy Optimization (MB-MPO)

```
for iter = 1, 2, ...
```

- collect data under current adaptive policies  $\pi_{\theta'_1}, \dots, \pi_{\theta'_K}$
- learn **ENSEMBLE** of K simulators from all past data
- **meta-policy optimization over ENSEMBLE**
  - → new **meta-policy**  $\pi_\theta$
  - → new **adaptive policies**  $\pi_{\theta'_1}, \dots, \pi_{\theta'_K}$

# Model-based via Meta-Policy Optimization MB-MPO

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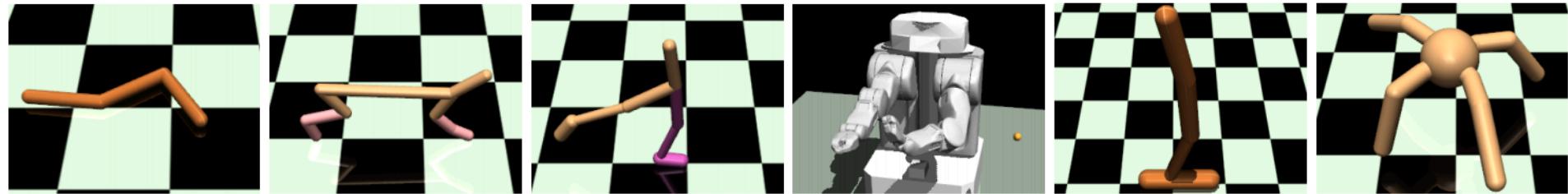
## Algorithm 1 MB-MPO

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**Require:** Inner and outer step size  $\alpha, \beta$

- 1: Initialize the policy  $\pi_{\theta}$ , the models  $\hat{f}_{\phi_1}, \hat{f}_{\phi_2}, \dots, \hat{f}_{\phi_K}$  and  $\mathcal{D} \leftarrow \emptyset$
- 2: **repeat**
- 3:   Sample trajectories from the real environment with the adapted policies  $\pi_{\theta'_1}, \dots, \pi_{\theta'_K}$ . Add them to  $\mathcal{D}$ .
- 4:   Train all models using  $\mathcal{D}$ .
- 5:   **for all** models  $\hat{f}_{\phi_k}$  **do**
- 6:     Sample imaginary trajectories  $\mathcal{T}_k$  from  $\hat{f}_{\phi_k}$  using  $\pi_{\theta}$
- 7:     Compute adapted parameters  $\theta'_k = \theta + \alpha \nabla_{\theta} J_k(\theta)$  using trajectories  $\mathcal{T}_k$
- 8:     Sample imaginary trajectories  $\mathcal{T}'_k$  from  $\hat{f}_{\phi_k}$  using the adapted policy  $\pi_{\theta'_k}$
- 9:   **end for**
- 10:   Update  $\theta \rightarrow \theta - \beta \frac{1}{K} \sum_k \nabla_{\theta} J_k(\theta'_k)$  using the trajectories  $\mathcal{T}'_k$
- 11: **until** the policy performs well in the real environment
- 12: **return** Optimal pre-update parameters  $\theta^*$

# MB-MPO Evaluation



# MB-MPO Evaluation

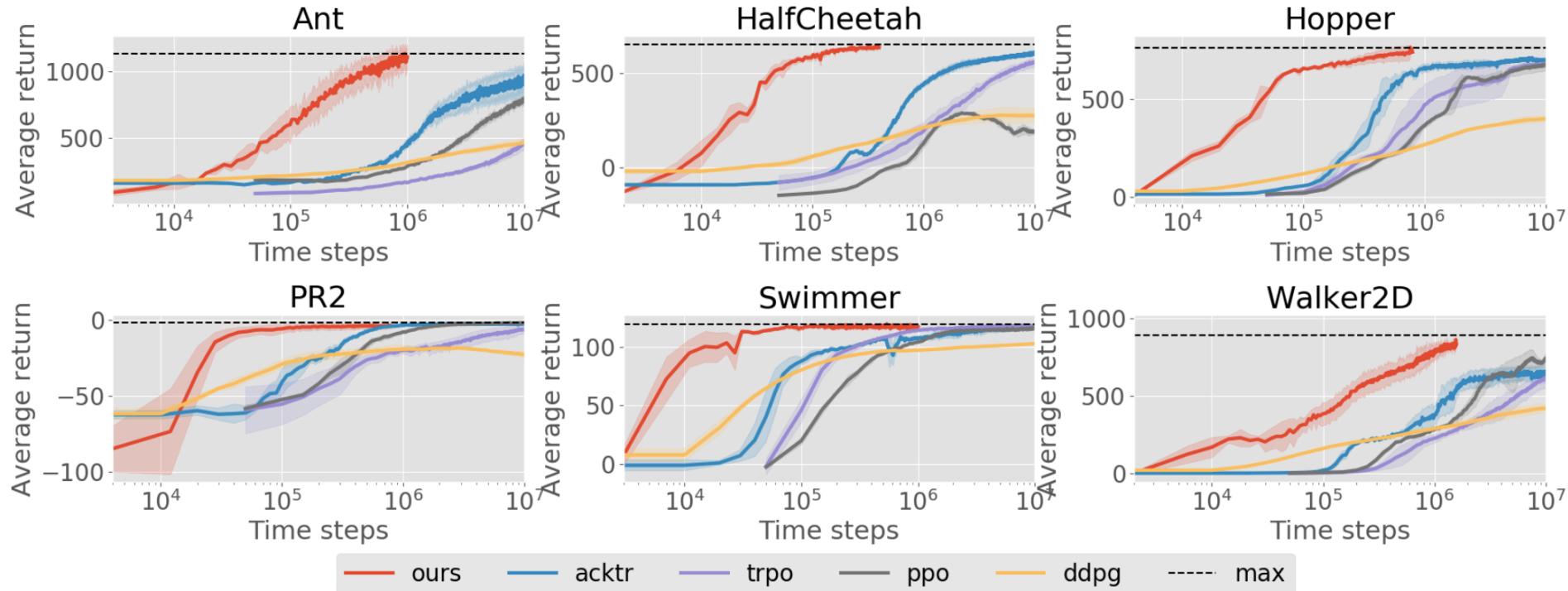


# MB-MPO Evaluation



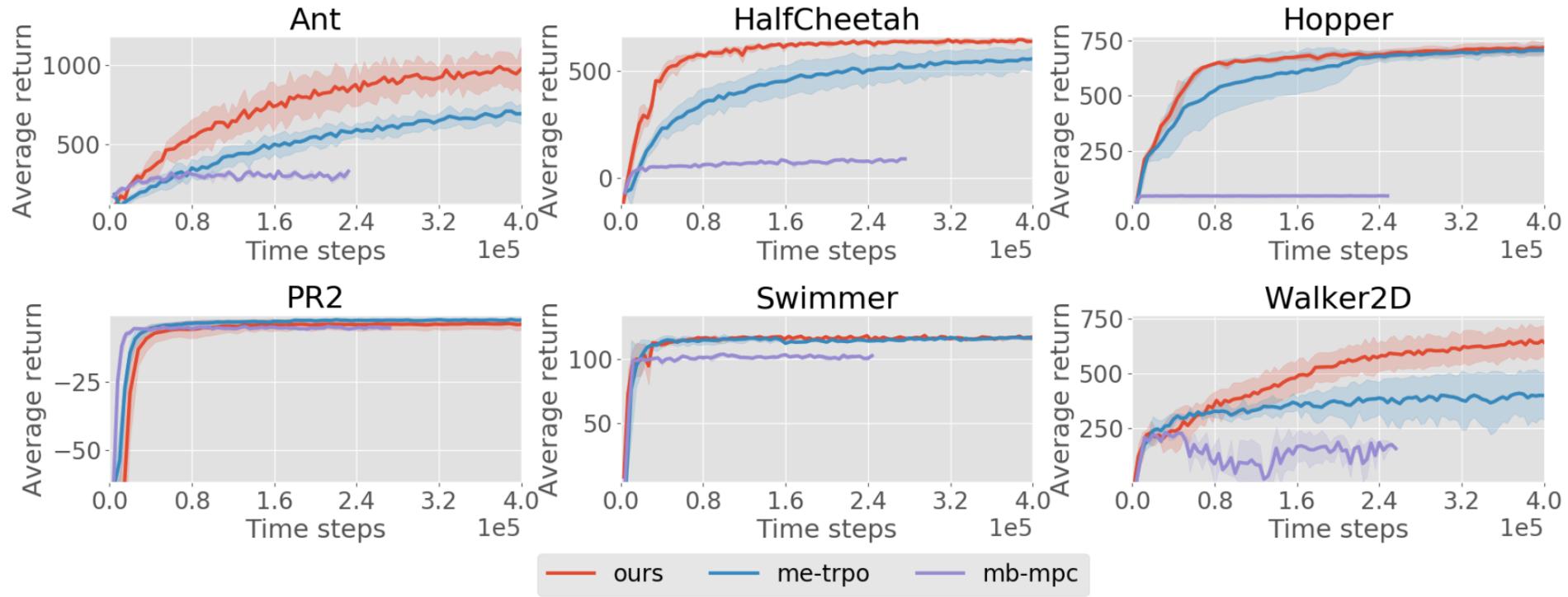
# MB-MPO Evaluation

- Comparison with state of the art model-free



# MB-MPO Evaluation

- Comparison with state of the art model-based





# So are we done?

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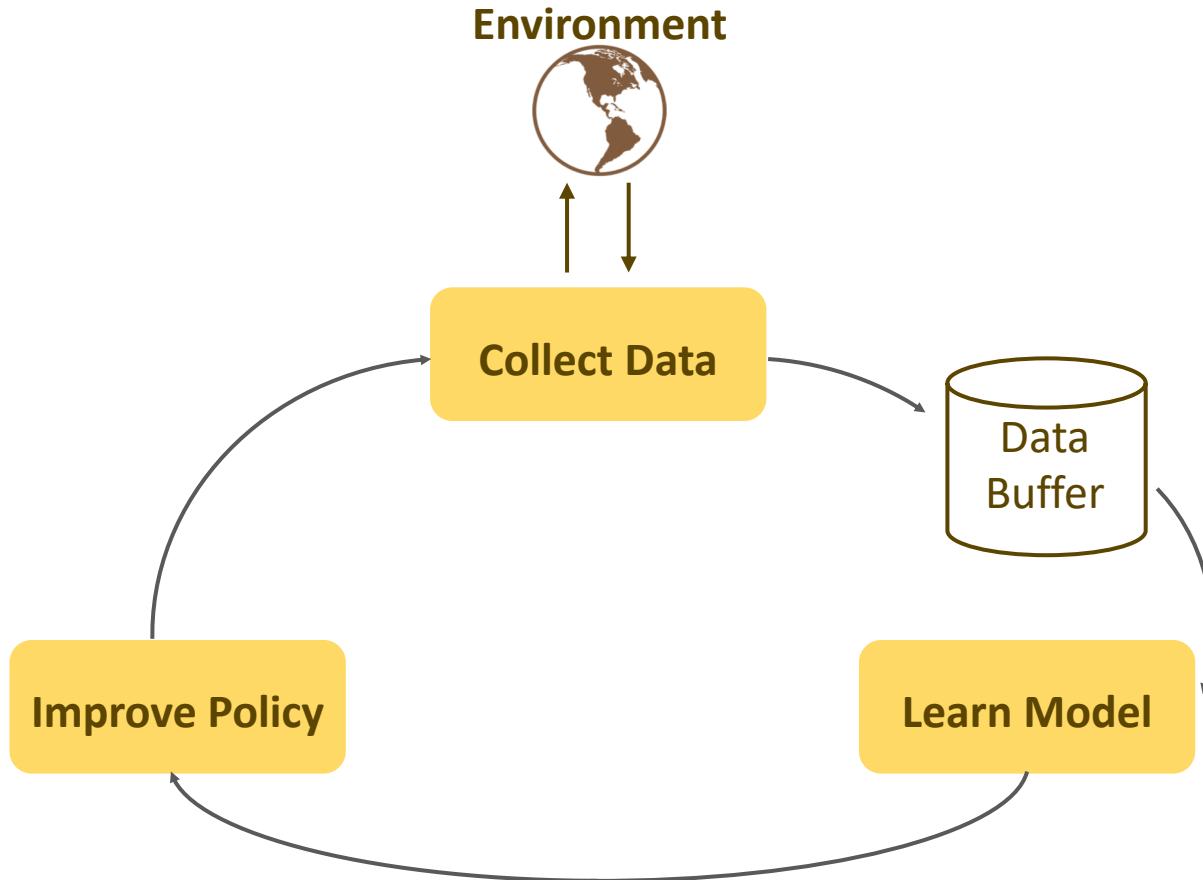
- No...

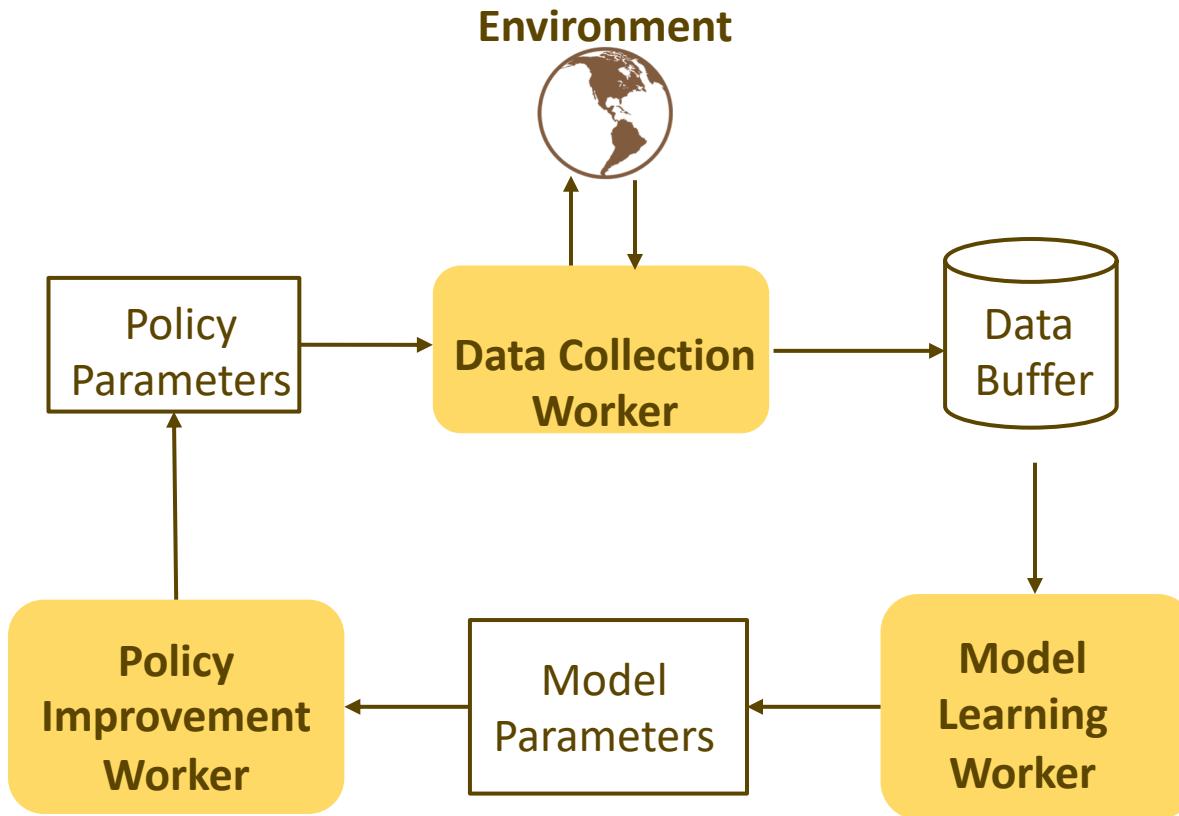
- Not real-time --- exacerbated by need for extensive hyperparameter tuning
- Limited to short horizon
- From state (though some results have started to happen from images)

# So are we done?

---

- No...
  - *Not real-time --- exacerbated by need for extensive hyperparameter tuning*
  - Limited to short horizon
  - From state (though some results have started to happen from images)





# Questions to be answered

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1. Performance?

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2. Effect on policy regularization?

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4. Robustness to hyperparameters?

# Questions to be answered

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1. Performance?
2. Effect on policy regularization?
3. Effect on data exploration?
4. Robustness to hyperparameters?
5. Robustness to data collection frequency?

# Experiments

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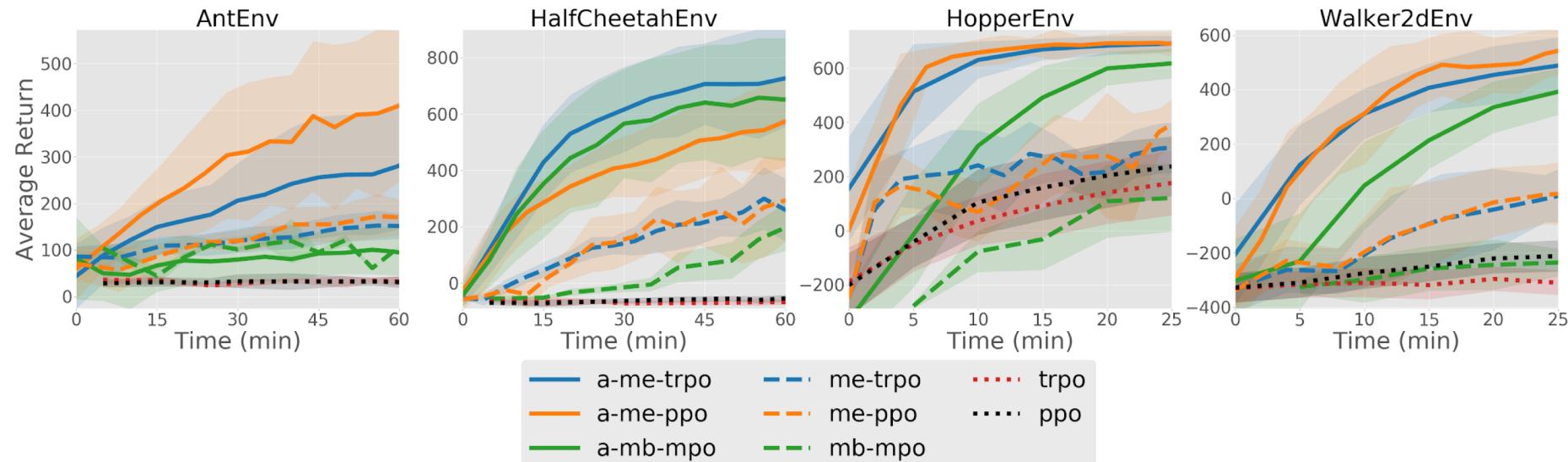
## 1. How does the asynch-framework perform?

Asynch: ME-TRPO, ME-PPO, MB-MPO

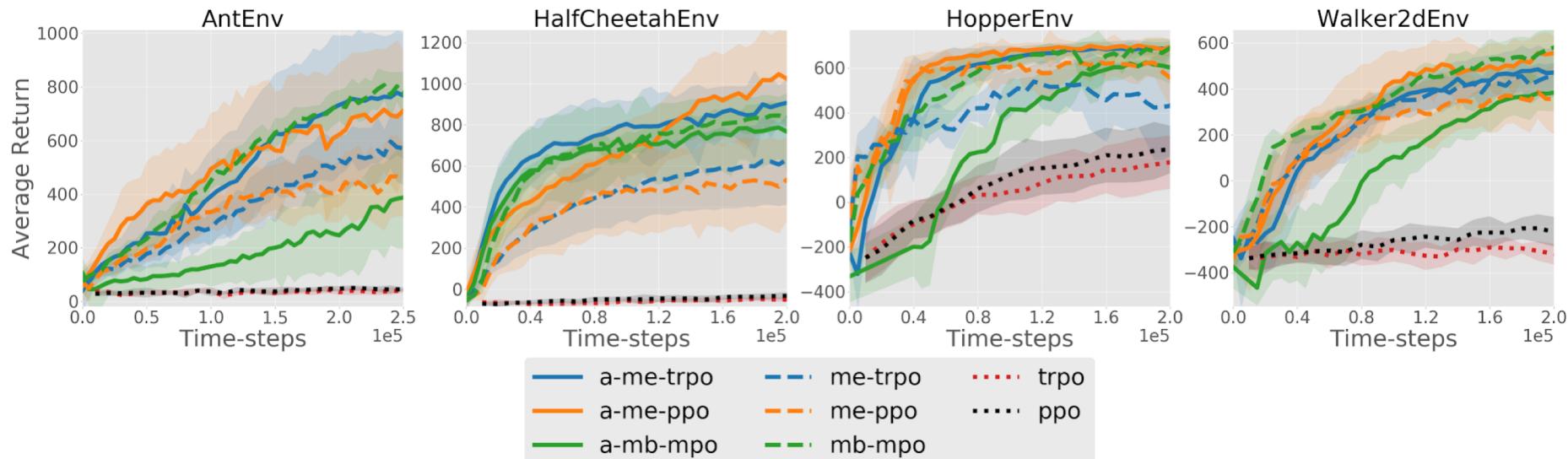
Baselines: ME-TRPO, ME-PPO, MB-MPO; TRPO, PPO

- a. Average Return vs. Time
- b. Average Return vs. Sample complexity (Timesteps)

# Performance Comparison: Wall-Clock Time



# Performance Comparison: Sample Complexity

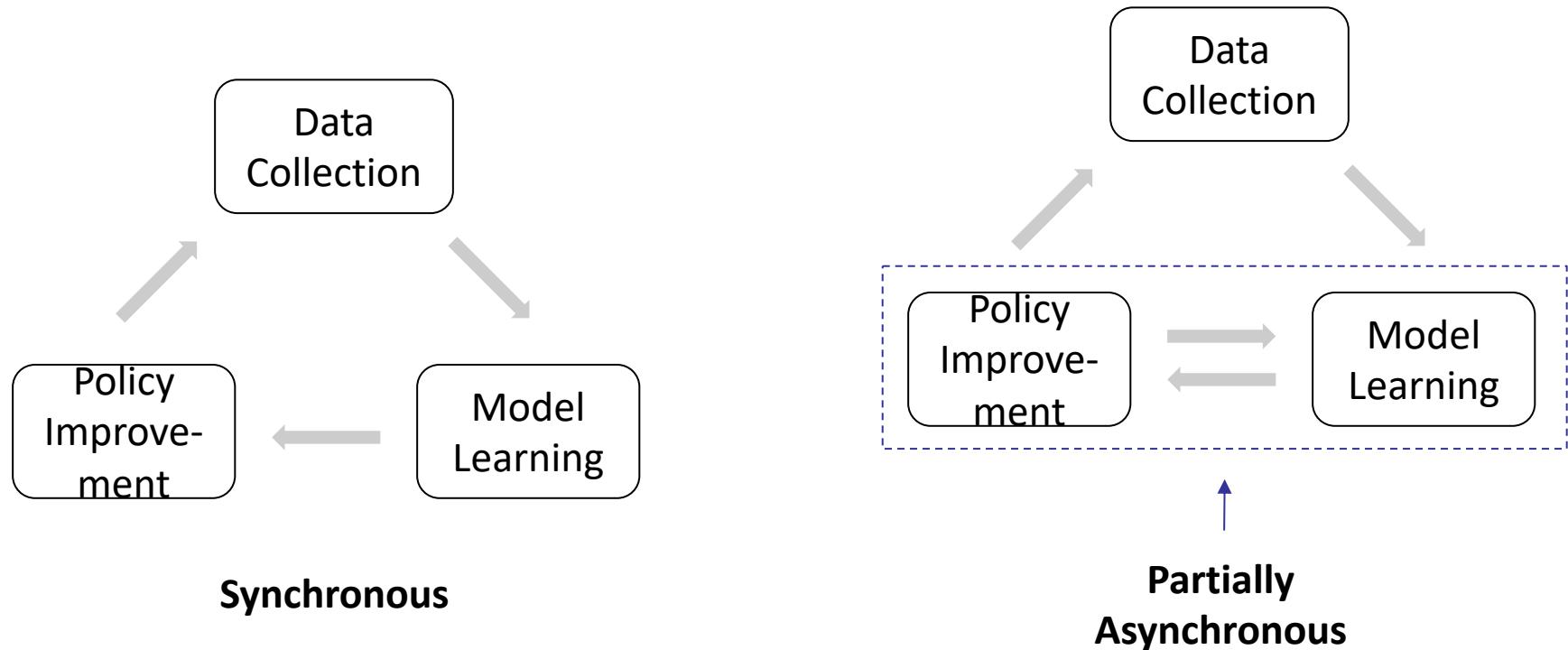


# Experiments

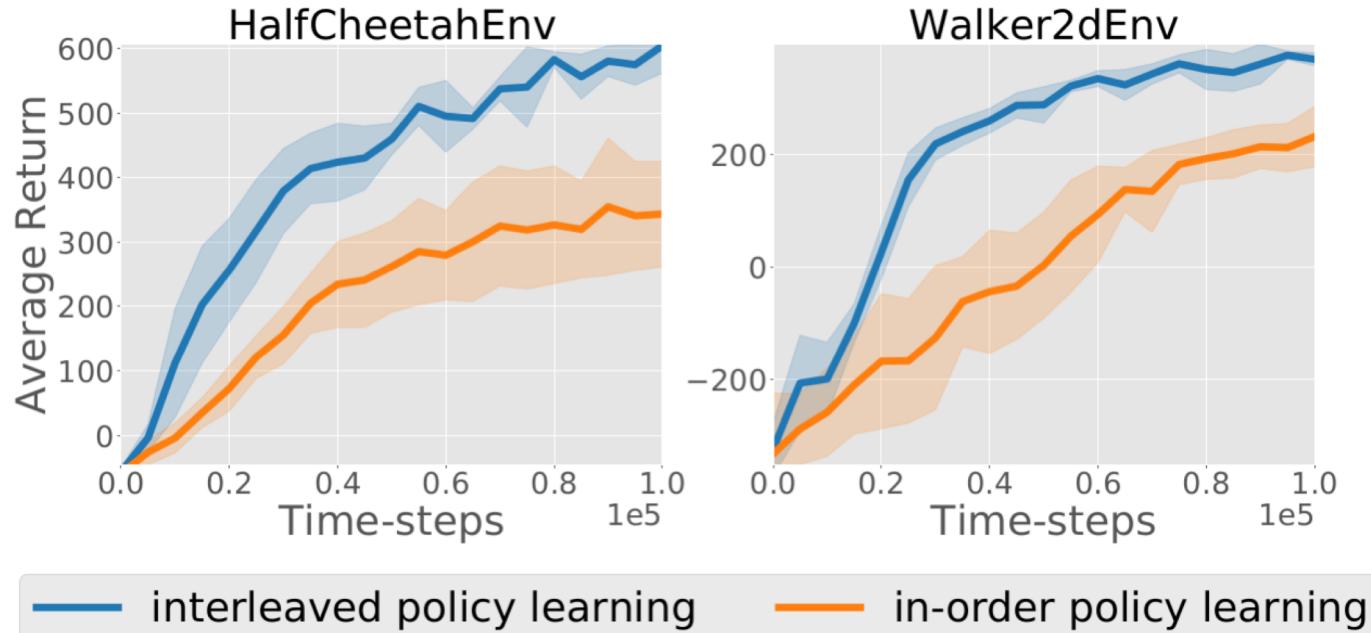
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1. Performance comparison
2. **Are there benefits of being asynchronous other than speed?**
  - a. Policy learning regularization
  - b. Exploration in data collection

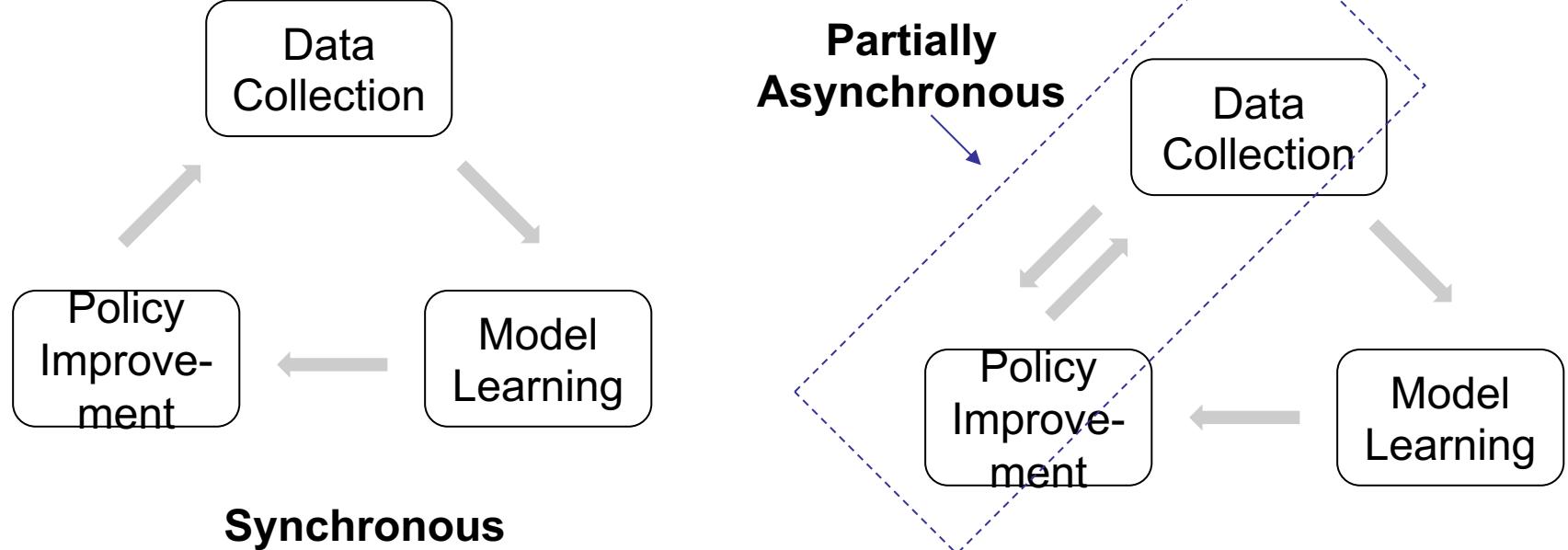
# Policy Learning Regularization



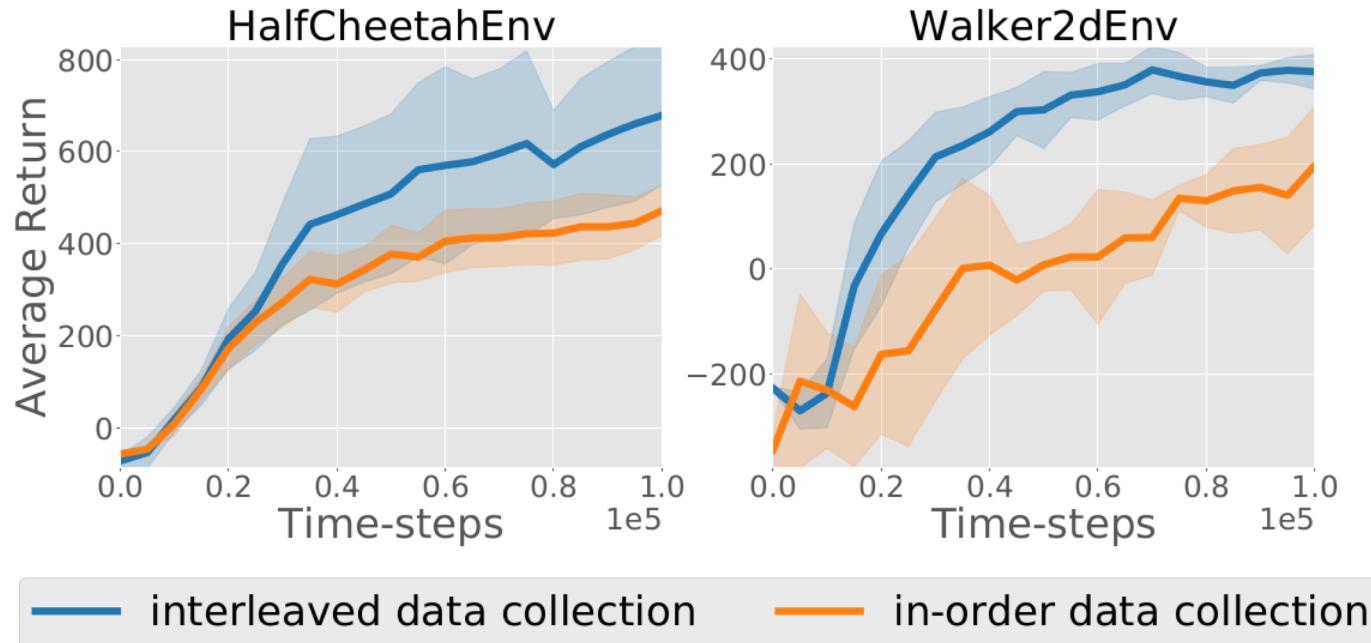
# Policy Learning Regularization



# Improved Exploration for Data Collection



# Improved Exploration for Data Collection

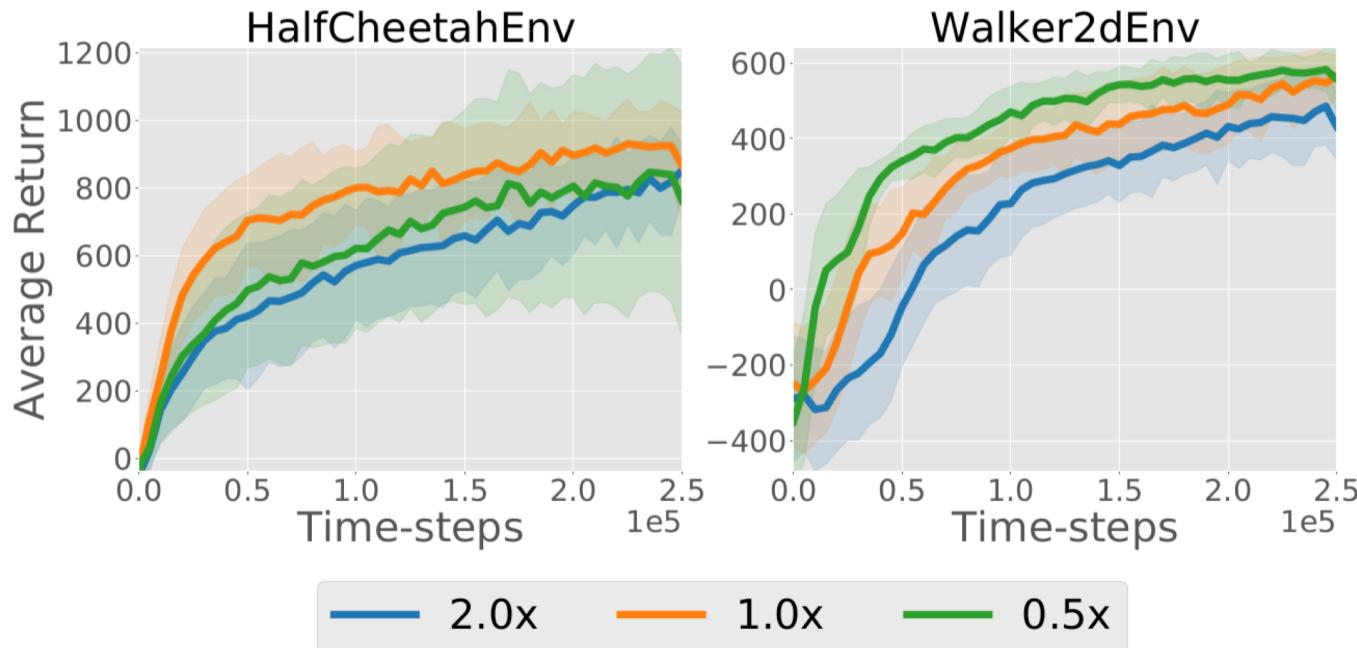


# Experiments

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1. Performance comparison
2. Asynchronous effects
3. **Is the asynch-framework robust to data collection frequency?**

# Ablations: Sampling Speed

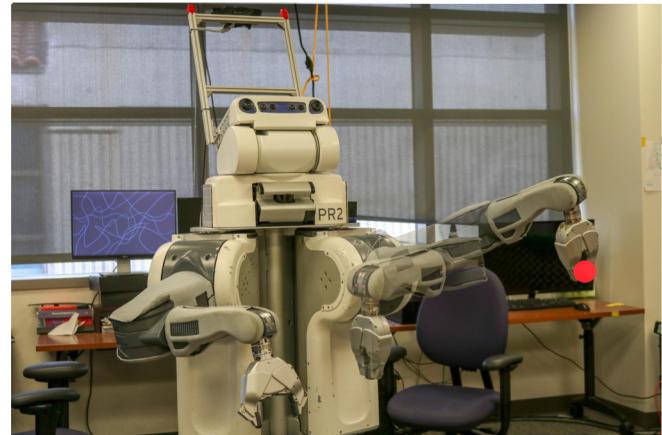
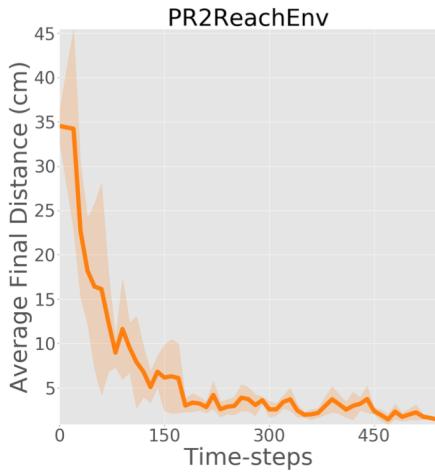
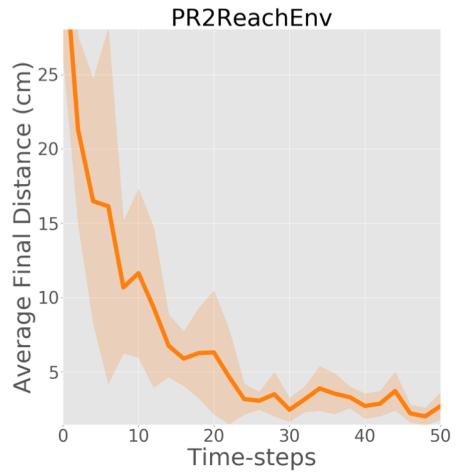


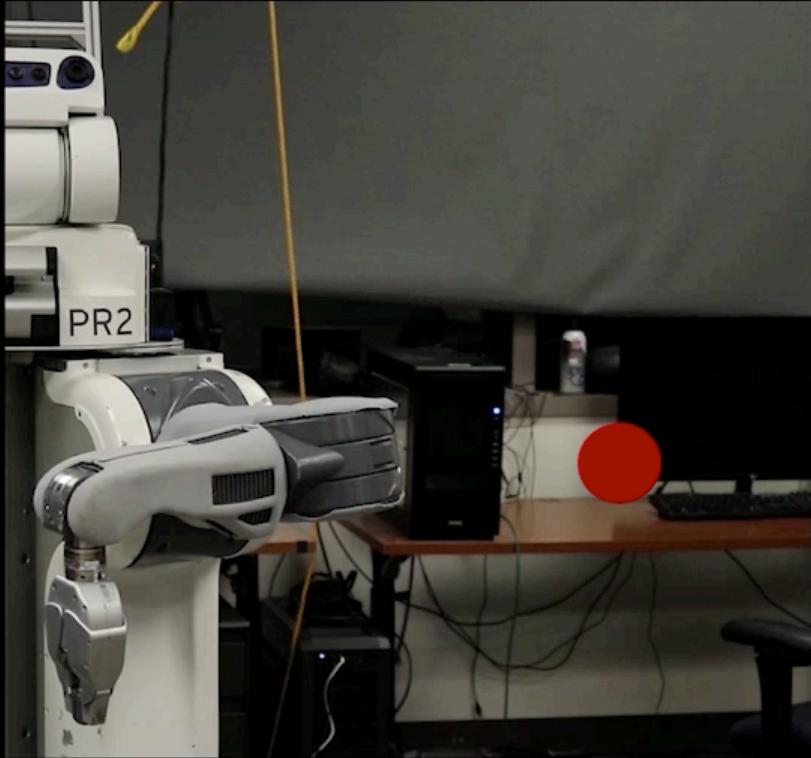
# Experiments

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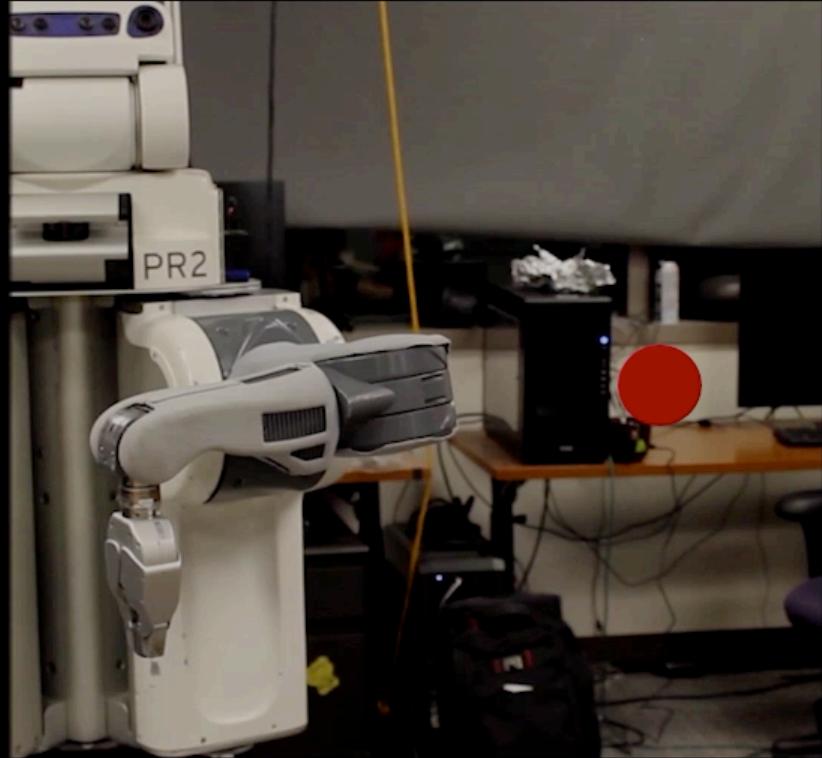
1. Performance comparison
2. Asynchronous effects
3. Ablations
4. **Does the aynch-framework work in real robotics tasks?**
  - a. Reaching a position
  - b. Inserting a unique shape into its matching hole in a box
  - c. Stacking a modular block onto a fixed base

# Real Robot Tasks: Reaching Position





Synchronous

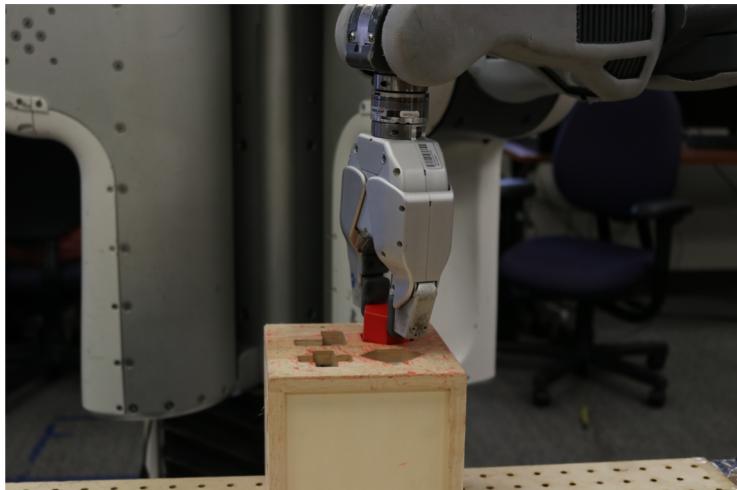
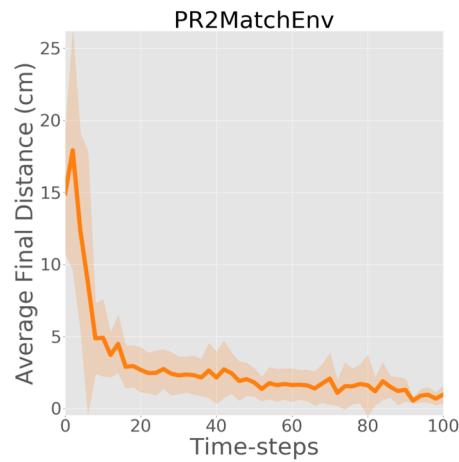
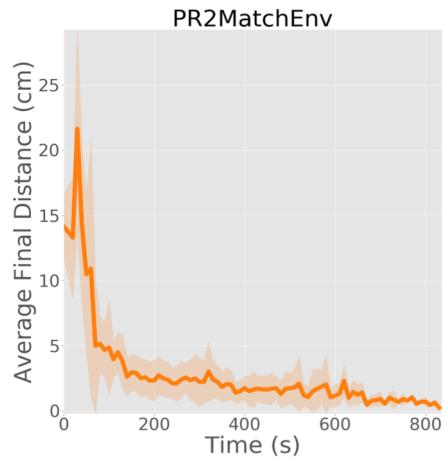


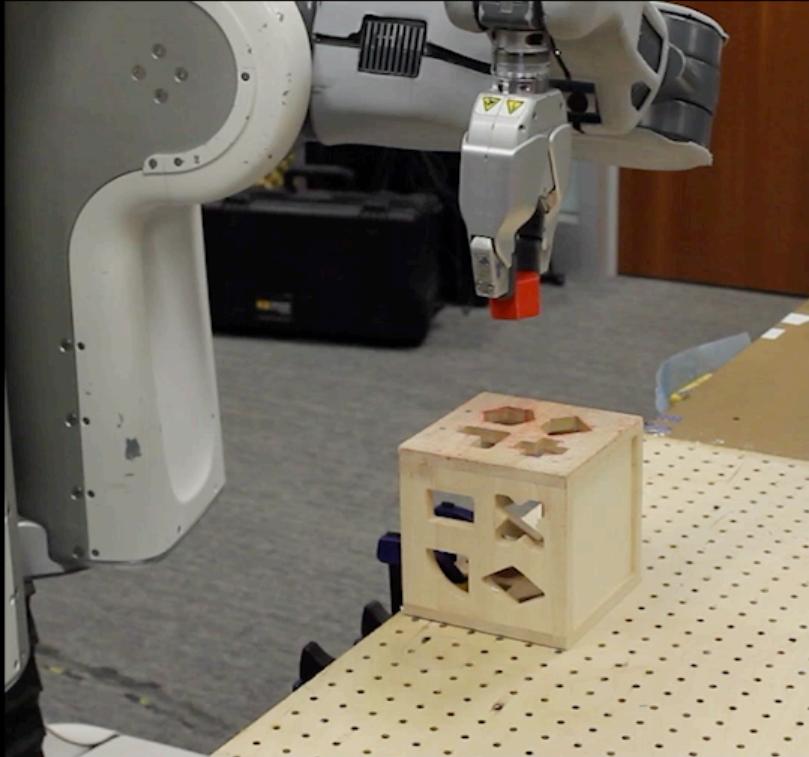
Asynchronous

Wall Clock Time: 0 seconds

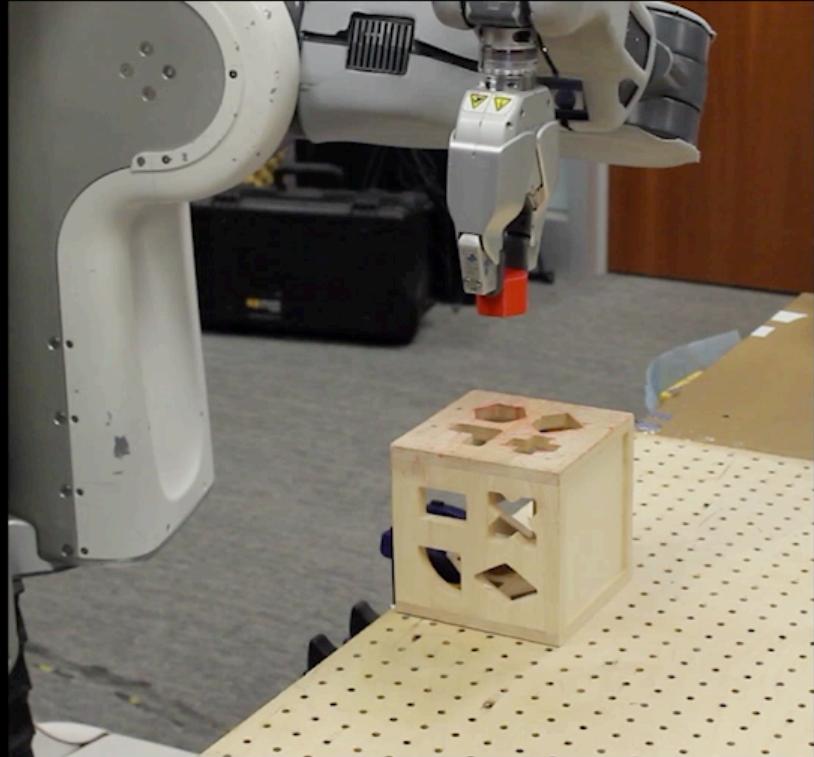
x2

# Real Robot Tasks: Matching Shape





Synchronous

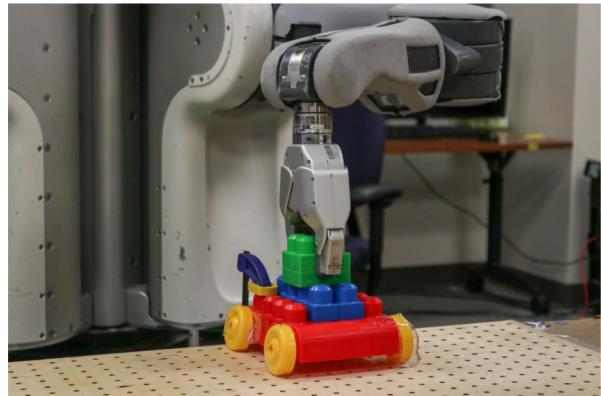
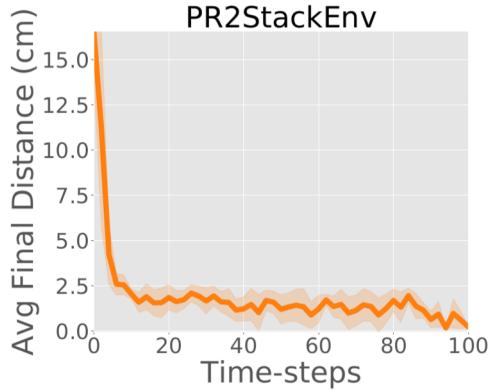
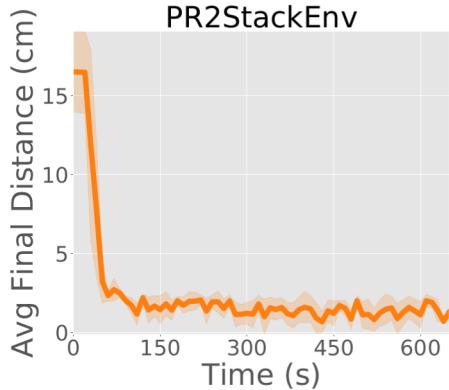


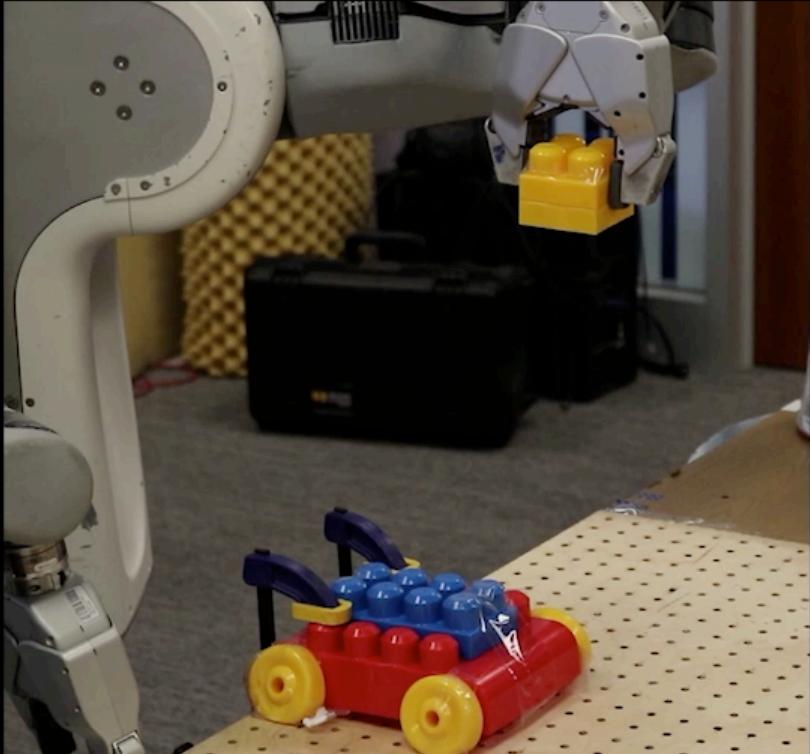
Asynchronous

Wall Clock Time: 0 minutes

x2

# Real Robot Tasks: Stacking Lego





Synchronous



Asynchronous

Wall Clock Time: 0 minutes

x2

# Summary of Asynchronous Model-based RL

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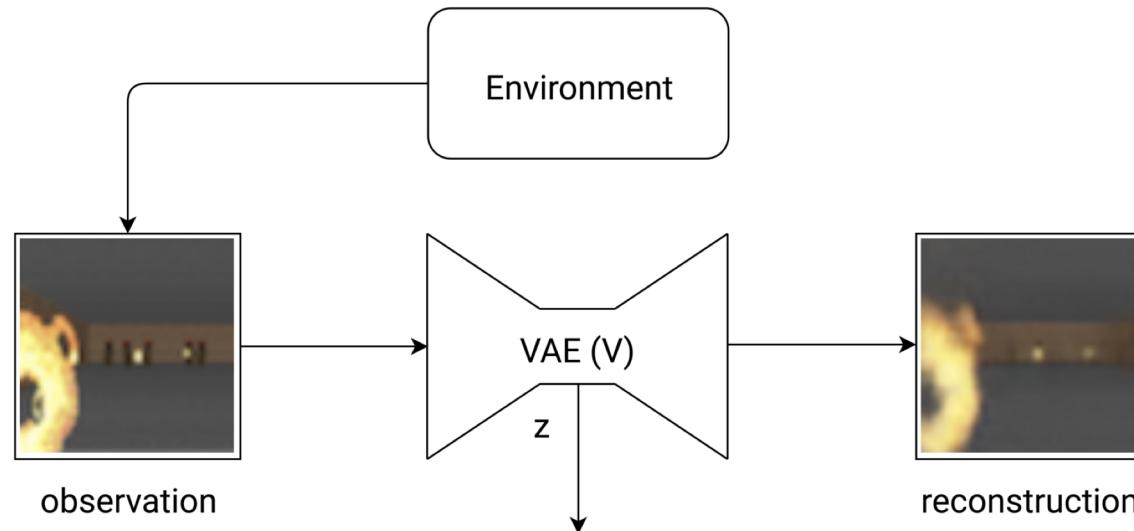
- Problem
  - Need fast and data efficient methods for robotic tasks
- Contributions
  - General asynchronous model-based framework
  - Wall-clock time speed-up
  - Sample efficiency
  - Effect on policy regularization & data exploration
  - Effective on real robots

# Outline

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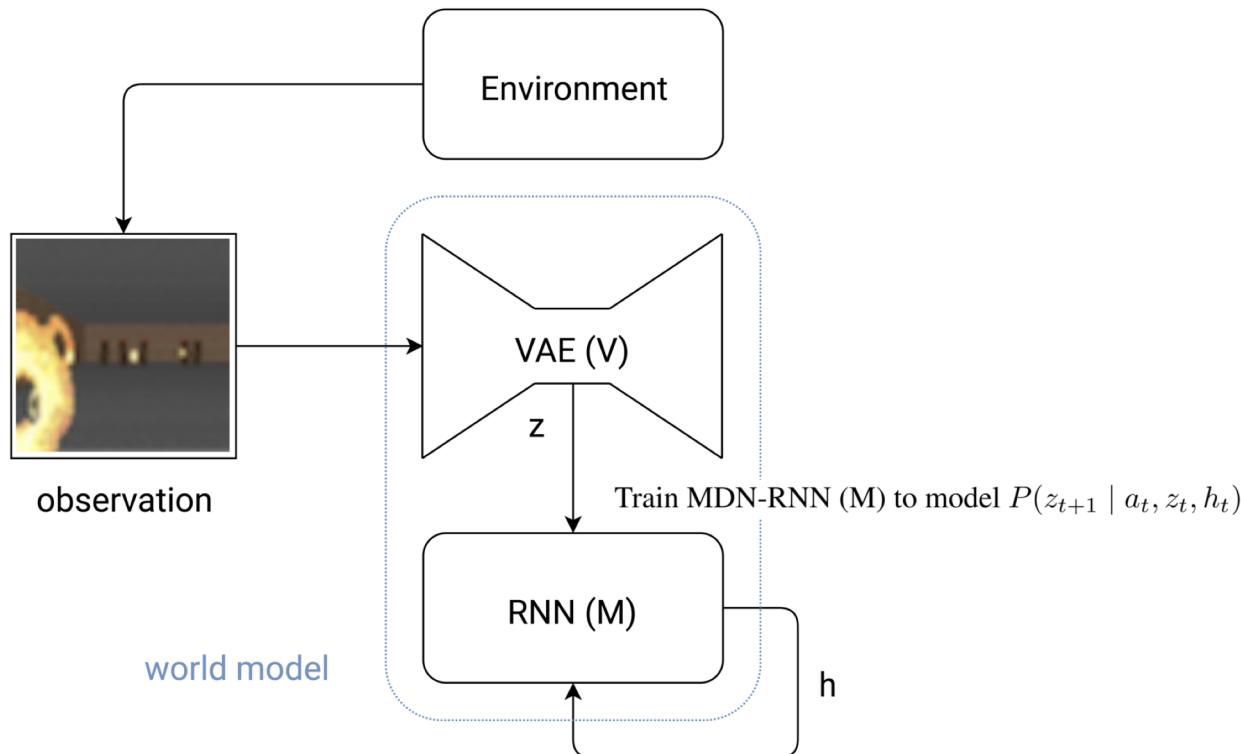
- Model-based RL
- Ensemble Methods
  - Model-Ensemble Trust Region Policy Optimization
  - Model-based RL via Meta Policy Optimization
- Asynchronous Model-based RL
- Vision-based Model-based RL

# World Models

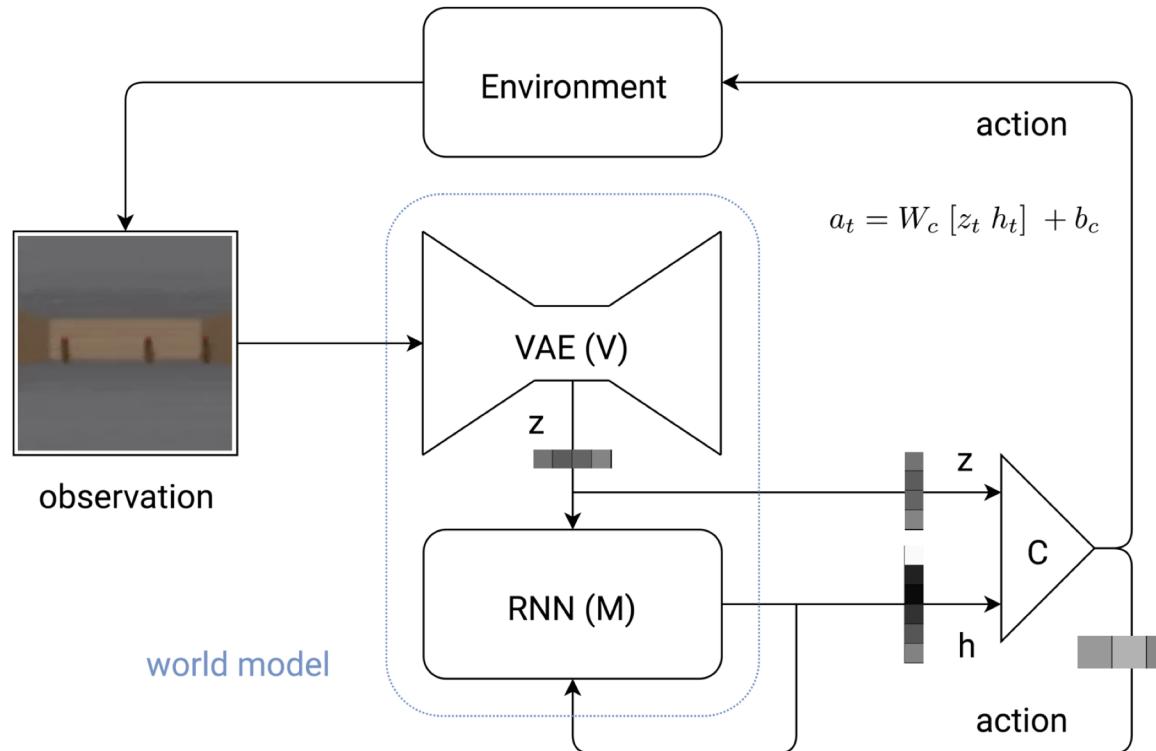


Train VAE (V) to encode frames into  $z$

# World Models

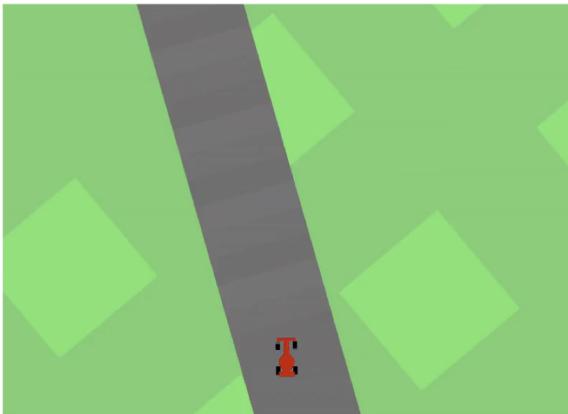


# World Models



# World Models

## CarRacing-v0



- ▶ Randomly generated tracks
- ▶ Stay on tiles, travel around track
- ▶ Average Score > 900 (100 trials) to “solve” task

Procedure:

1. Collect 10,000 rollouts from a random policy.
2. Train VAE (V) to encode frames into  $z \in \mathcal{R}^{32}$ .
3. Train MDN-RNN (M) to model  $P(z_{t+1} | a_t, z_t, h_t)$ .
4. Evolve linear controller (C) to maximize the expected cumulative reward of a rollout.  $a_t = W_c [z_t \ h_t] + b_c$

MODEL	PARAMETER COUNT
VAE	4,348,547
MDN-RNN	422,368
CONTROLLER	867



Source: Taste of Home  
([www.tasteofhome.com](http://www.tasteofhome.com))

# World Models

Action-Conditional Video  
Prediction using Deep Networks  
in Atari Games (2015)

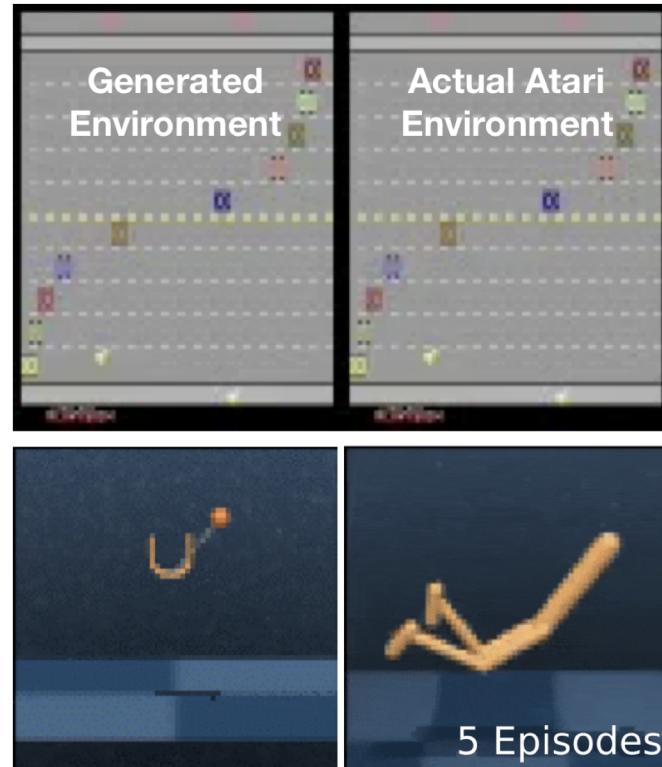
**Junhyuk Oh**, Xiaoxiao Guo, Honglak Lee,  
Richard Lewis and Satinder Singh

Model-Based Reinforcement  
Learning for Atari (2018)

Błażej Osiski, Łukasz Kaiser, Mohammad Babaeizadeh,  
George Tucker, Dumitru Erhan, Ryan Sepassi, Chelsea Finn,  
Sergey Levine, Piotr Kozakowski, Konrad Czechowski,  
Piotr Miłos and Henryk Michalewski

Learning Latent Dynamics for  
Planning from Pixels (2018)

**Danijar Hafner**, Timothy Lillicrap, Ian Fischer, Ruben Villegas,  
David Ha, Honglak Lee and James Davidson



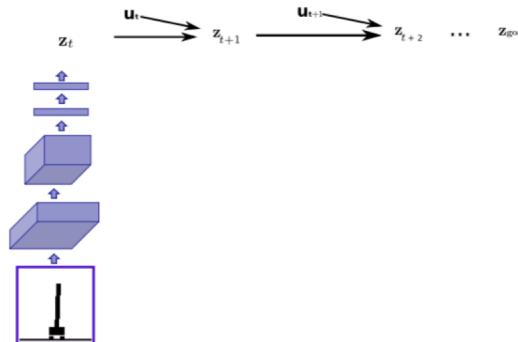
# Embed to Control

## Embed to Control: Model based RL from raw images



Can we perform model based RL starting from raw images ?

- Standard algorithms would fail in pixel space
- We want to **unsupervisedly** learn latent space  $z_t$  for control from images  $x_t$



Related attempts:

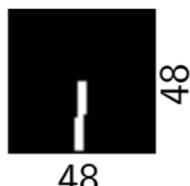
- ▶ [Lange et al.:Deep Learning of Visual Control Policies, 2010]
- ▶ [Wahlstroem et al.: From Pixels to Torques, 2015]

# Embed to Control

Systems we consider

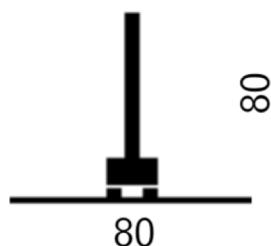


Pendulum  
 $z \in \mathbb{R}^3$



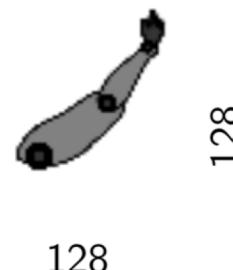
48  
48

Cart-Pole  
 $z \in \mathbb{R}^8$



80  
80

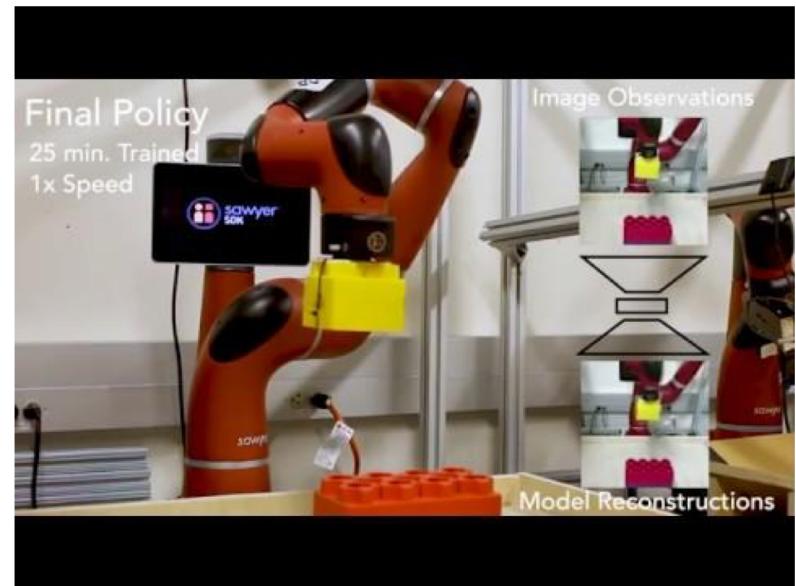
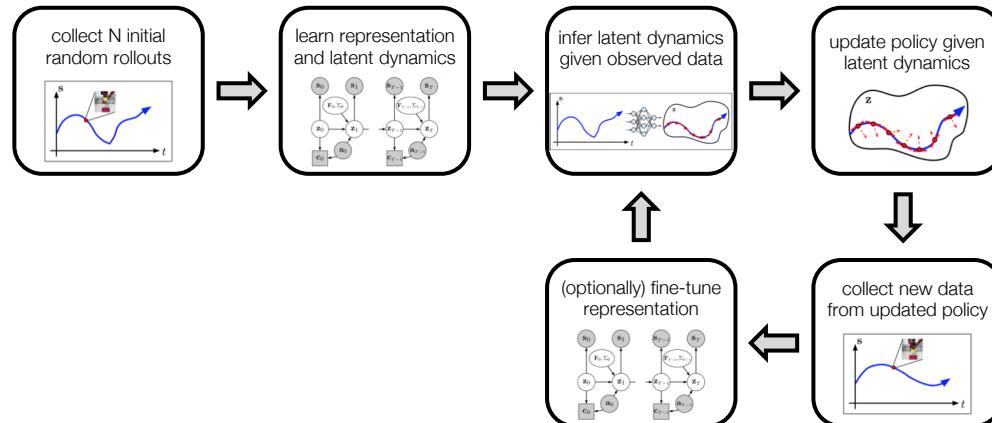
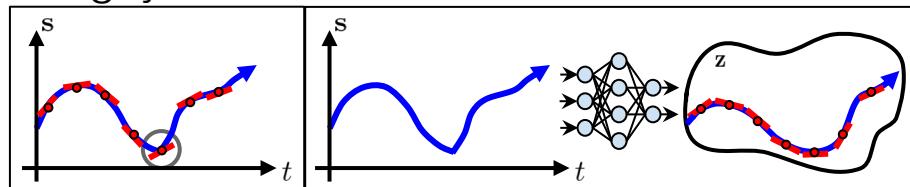
Three-Link-Arm  
 $z \in \mathbb{R}^8$



128  
128

# SOLAR: Deep Structured Representations for Model-Based Reinforcement Learning

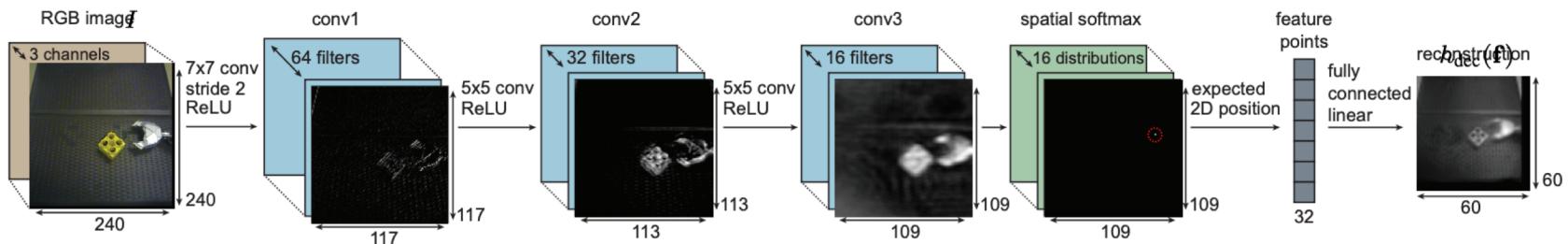
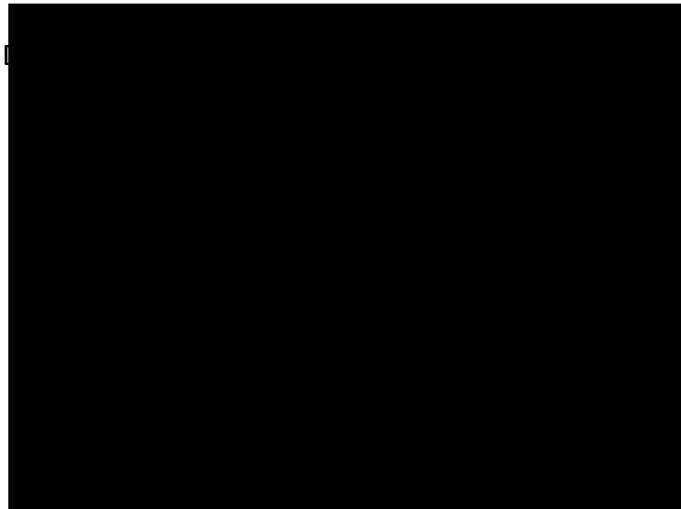
Marvin Zhang\*, Sharad Vikram\*, Laura Smith, Pieter Abbeel, Matthew Johnson, Sergey Levine



<https://goo.gl/AJKoCL>

# Deep Spatial Autoencoders

- Deep Spatial Autoencoders for Visuomotor Learning, Finn, Tan, Duan, (https://arxiv.org/abs/1509.06113)
  - Train deep spatial autoencoder
  - Model-based RL through iLQR in the latent space



# Robotic Priors / PVEs

- PVEs: Position-Velocity Encoders for Unsupervised Learning of Structured State Representations

Rico Jonschkowski, Roland Hafner, Jonathan Scholz, and Martin Riedmiller (<https://arxiv.org/pdf/1705.09805.pdf>)

- Learn an embedding without reconstruct<sup>+</sup>

$$\mathbf{s}_t^{(p)} = \phi(\mathbf{o}_t)$$

$$\mathbf{s}_t^{(v)} = \alpha(\mathbf{s}_t^{(p)} - \mathbf{s}_{t-1}^{(p)})$$

$$L_{\text{conservation}} = \mathbf{E}\left[\left(\|\mathbf{s}_t^{(v)}\| - \|\mathbf{s}_{t-1}^{(v)}\|\right)^2\right]$$

$$L_{\text{variation}} = \mathbf{E}\left[e^{-\|\mathbf{s}_a^{(p)} - \mathbf{s}_b^{(p)}\|}\right]$$

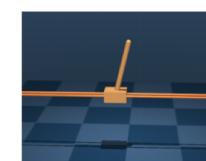
$$\begin{aligned} L_{\text{controlability (i)}} &= e^{-\text{Cov}(\mathbf{a}_{t,i}, \mathbf{s}_{t+1,i}^{(a)})} \\ &= e^{-\mathbf{E}\left[\left(a_{t,i} - \mathbf{E}[a_{t,i}]\right)\left(s_{t+1,i}^{(a)} - \mathbf{E}[s_{t+1,i}^{(a)}]\right)\right]} \end{aligned}$$

$$L_{\text{slowness}} = \mathbf{E}\left[\|\mathbf{s}_t^{(p)} - \mathbf{s}_{t-1}^{(p)}\|^2\right]$$

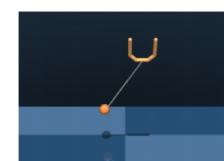
$$L_{\text{inertia}} = \mathbf{E}\left[\|\mathbf{s}_t^{(v)} - \mathbf{s}_{t-1}^{(v)}\|^2\right] = \mathbf{E}\left[\|\mathbf{s}_t^{(a)}\|^2\right]$$



(a) Inverted pendulum



(b) Cart-pole

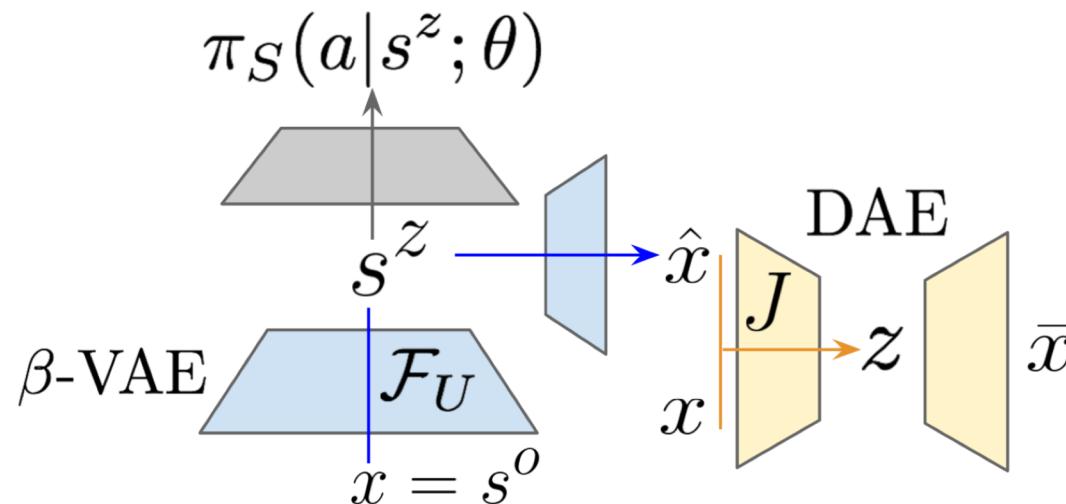


(c) Ball in cup

# Disentangled Representation Learning Agent (Darla)

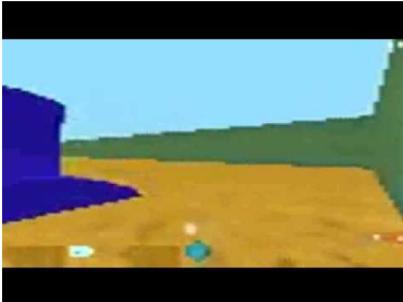
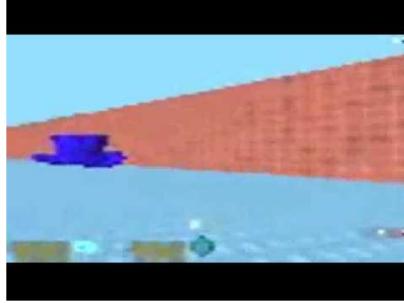
DARLA: Improving Zero-Shot Transfer in Reinforcement Learning

Irina Higgins, Arka Pal, Andrei A. Rusu, Loic Matthey, Christopher P Burgess, Alexander Pritzel, Matthew Botvinick, Charles Blundell, Alexander Lerchner (<https://arxiv.org/abs/1707.08475>)



# DeepMind Lab Transfer

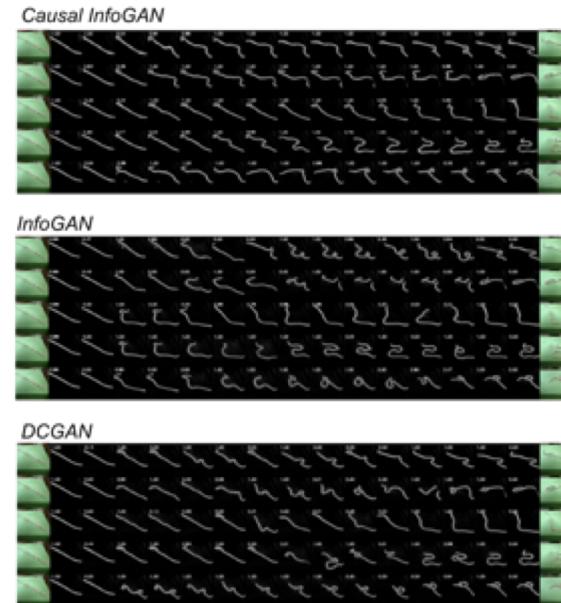
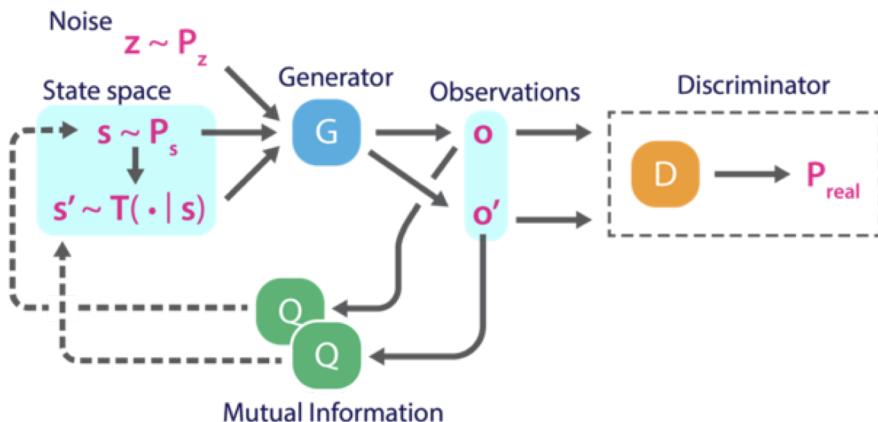
DARLA vs DQN baseline

		Train	Transfer
DQN			
DARLA			

# Causal InfoGAN

Learning Plannable Representations with Causal InfoGAN

Thanard Kurutach, Aviv Tamar, Ge Yang, Stuart Russell, Pieter Abbeel (<https://arxiv.org/pdf/1807.09341.pdf>)

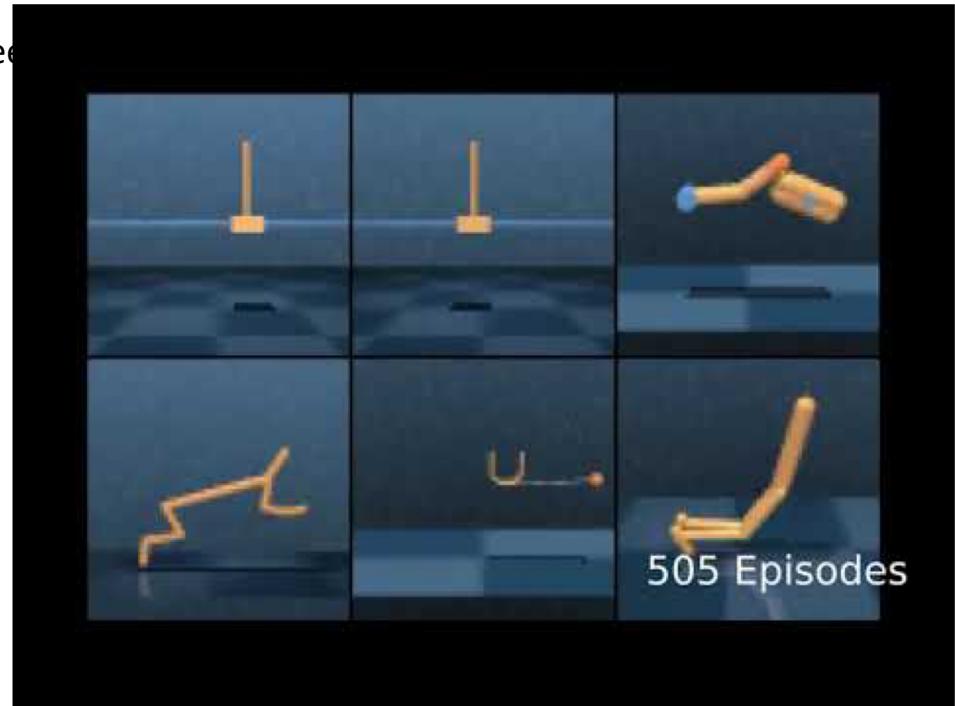


# PlaNet

Learning latent dynamics for planning from pixels

Danijar Hafner, T. Lillicrap, I Fischer, R Villegas, D Ha, H Lee

- Learn latent space dynamics model
- Multi-step prediction
- Planning in latent space



# Visual Foresight

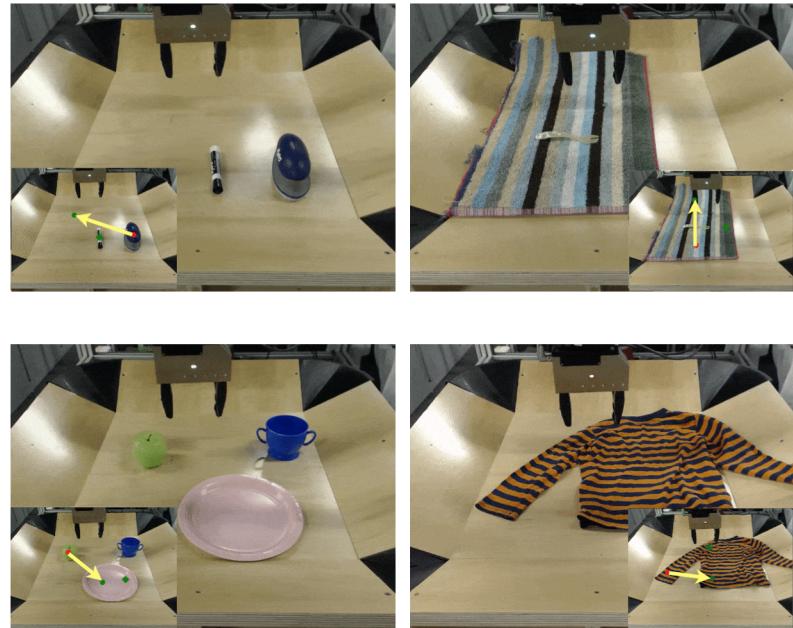
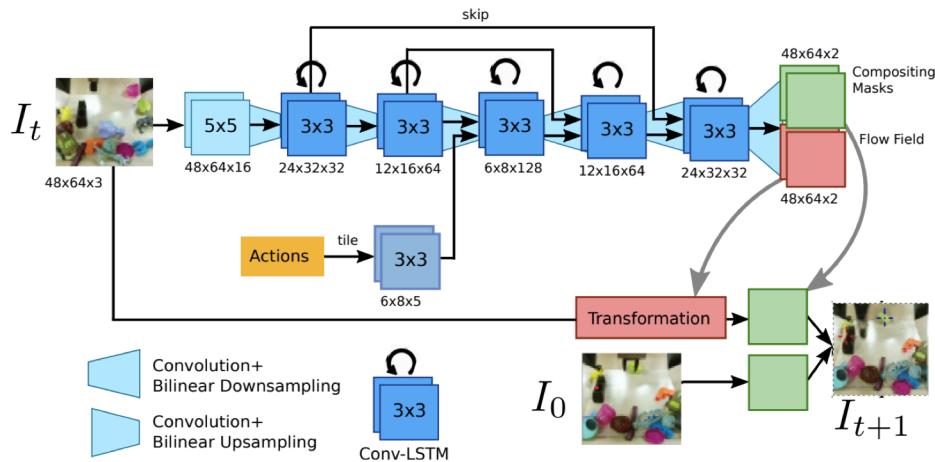
Deep Visual Foresight for Planning Robot Motion, Finn and Levine, ICRA 2017 <http://arxiv.org/abs/1610.00696>

Visual Foresight: Model-Based Deep Reinforcement Learning for Vision-Based Robotic Control, Frederik Ebert, Chelsea Finn,

Sudeep Dasari, Annie Xie, Alex Lee, Sergey Levine, <https://arxiv.org/abs/1812.00568>,

<https://bair.berkeley.edu/blog/2018/11/30/visual-rl/>

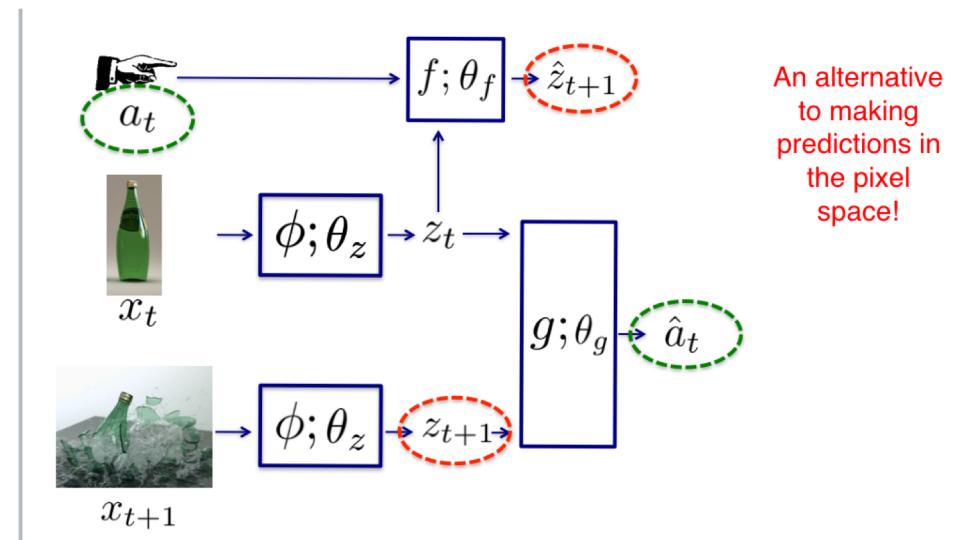
- Video prediction + Cross Entropy Maximization for MPC



# Forward + Inverse Dynamics Models

Learning to Poke by Poking: Experiential Learning of Intuitive Physics, Pulkit Agrawal, Ashvin Nair, Pieter Abbeel, Jitendra Malik, Sergey Levine, <https://arxiv.org/abs/1606.07419>

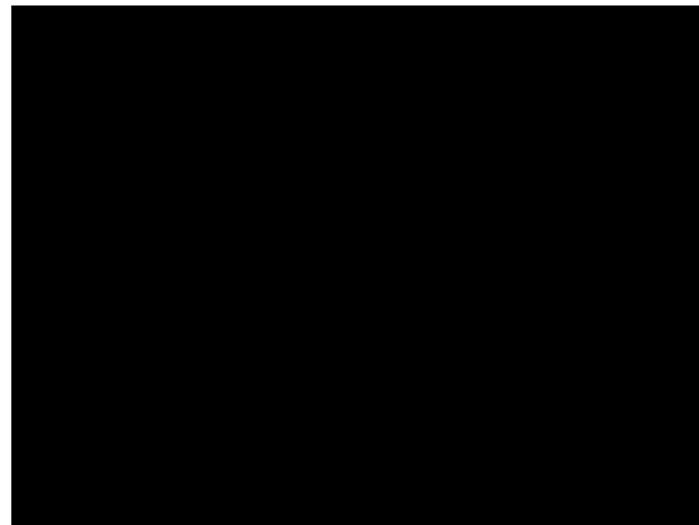
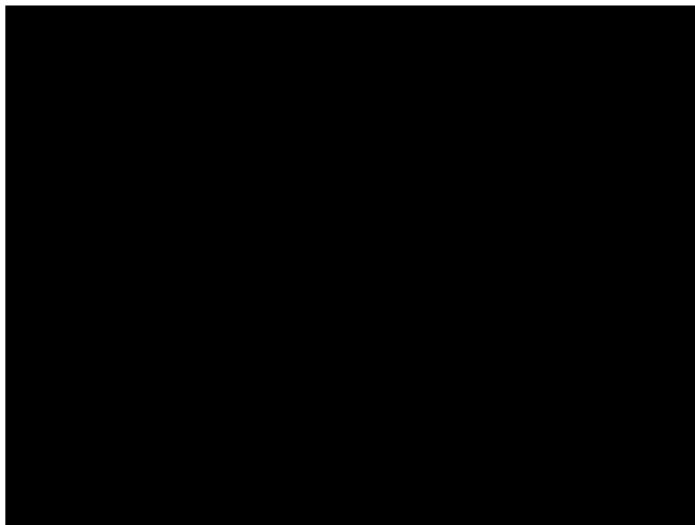
- Learning a forward model in latent space
- BUT: couldn't the latent features always be zero?
- SOLUTION: require the features from t and t+1 to be sufficient to predict  $a_t$



# Forward + Inverse Dynamics Models

Learning to Poke by Poking: Experiential Learning of Intuitive Physics, Pulkit Agrawal, Ashvin Nair, Pieter Abbeel, Jitendra Malik, Sergey Levine, <https://arxiv.org/abs/1606.07419>

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- BUT: couldn't the latent features always be zero?
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# Predictron

## The Predictron: End-To-End Learning and Planning

David Silver, Hado van Hasselt, Matteo Hessel, Tom Schaul, Arthur Guez, Tim Harley, Gabriel Dulac-Arnold, David Reichert, Neil Rabinowitz, Andre Barreto, Thomas Degrif (<https://arxiv.org/pdf/1612.08810.pdf>)

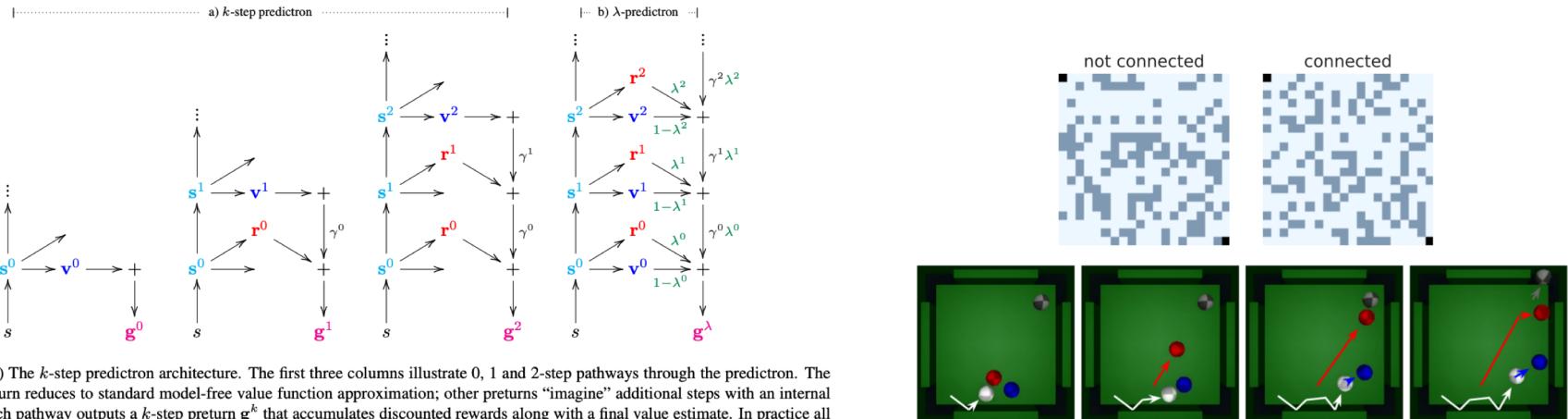


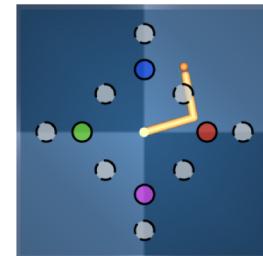
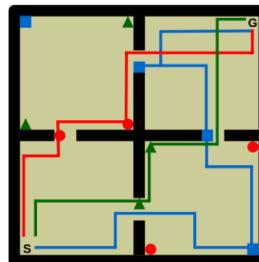
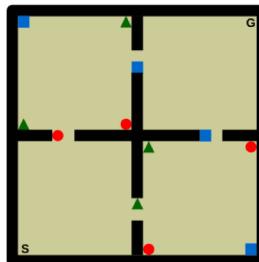
Figure 1. a) The  $k$ -step predictron architecture. The first three columns illustrate 0, 1 and 2-step pathways through the predictron. The 0-step preturn reduces to standard model-free value function approximation; other preturns “imagine” additional steps with an internal model. Each pathway outputs a  $k$ -step preturn  $g^k$  that accumulates discounted rewards along with a final value estimate. In practice all  $k$ -step preturns are computed in a single forward pass. b) The  $\lambda$ -predictron architecture. The  $\lambda$ -parameters gate between the different preturns. The output is a  $\lambda$ -preturn  $g^\lambda$  that is a mixture over the  $k$ -step preturns. For example, if  $\lambda^0 = 1, \lambda^1 = 1, \lambda^2 = 0$  then we recover the 2-step preturn,  $g^\lambda = g^2$ . Discount factors  $\gamma^k$  and  $\lambda$ -parameters  $\lambda^k$  are dependent on state  $s^k$ ; this dependence is not shown in the figure.

# Successor Features

Successor Features for Transfer in Reinforcement Learning

André Barreto, Will Dabney, Rémi Munos, Jonathan J. Hunt, Tom Schaul, Hado van Hasselt, David Silver (<https://arxiv.org/abs/1606.05312>)

$$\begin{aligned} Q^\pi(s, a) &= \mathbb{E}^\pi [r_{t+1} + \gamma r_{t+2} + \dots | S_t = s, A_t = a] \\ &= \mathbb{E}^\pi [\phi_{t+1}^\top \mathbf{w} + \gamma \phi_{t+2}^\top \mathbf{w} + \dots | S_t = s, A_t = a] \\ &= \mathbb{E}^\pi \left[ \sum_{i=t}^{\infty} \gamma^{i-t} \phi_{i+1}^\top | S_t = s, A_t = a \right]^\top \mathbf{w} = \psi^\pi(s, a)^\top \mathbf{w} \end{aligned}$$



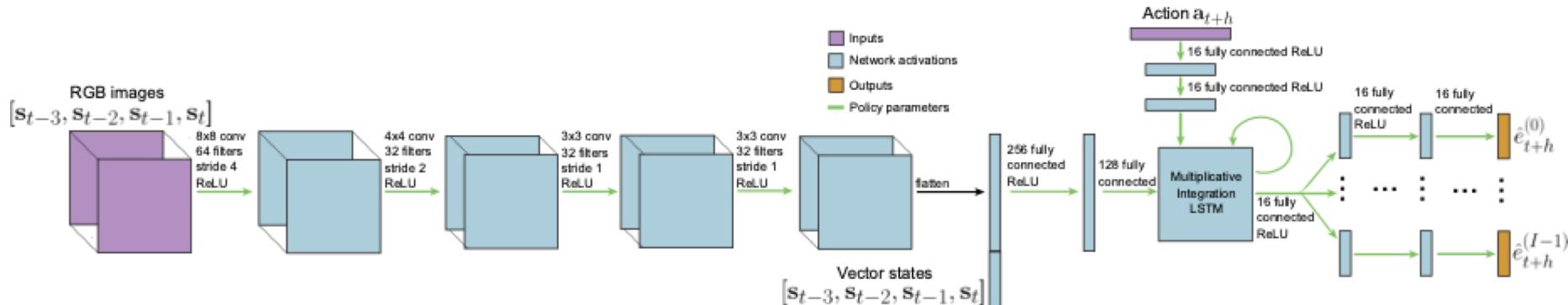
# Kahn et al.

Composable Action-Conditioned Predictors: Flexible Off-Policy Learning for Robot Navigation

Gregory Kahn\*, Adam Villaflor\*, Pieter Abbeel, Sergey Levine, CoRL 2018 (<https://arxiv.org/pdf/1810.07167.pdf>)

Self-supervised Deep Reinforcement Learning with Generalized Computation Graphs for Robot Navigation

Gregory Kahn, Adam Villaflor, Bosen Ding, Pieter Abbeel, Sergey Levine, ICRA 2018 (<https://arxiv.org/pdf/1709.10489.pdf>)



# Kahn et al.

Composable Action-Conditioned Predictors: Flexible Off-

Gregory Kahn\*, Adam Villaflor\*, Pieter Abbeel, Sergey Levine

Self-supervised Deep Reinforcement Learning with Generative Models

Gregory Kahn, Adam Villaflor, Bosen Ding, Pieter Abbeel, Sergey Levine



# Some Theory References on State Representations

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- From skills to symbols: Learning symbolic representations for abstract high-level planning:  
<https://jair.org/index.php/jair/article/view/11175>
- Homomorphism: <https://www.cse.iitm.ac.in/~ravi/papers/KBCS04.pdf>
- Towards a unified theory of state abstraction for mdps:  
<https://pdfs.semanticscholar.org/ca9a/2d326b9de48c095a6cb5912e1990d2c5ab46.pdf>
- Model reduction techniques for computing approximately optimal solutions for markov decision processes.<https://arxiv.org/abs/1302.1533>
- Adaptive aggregation methods for infinite horizon dynamic programming
- Transfer via soft homomorphisms. [http://www.ifaamas.org/Proceedings/aamas09/pdf/01\\_Full%20Papers/12\\_67\\_FP\\_0798.pdf](http://www.ifaamas.org/Proceedings/aamas09/pdf/01_Full%20Papers/12_67_FP_0798.pdf)
- Near optimal behavior via approximate state abstraction <https://arxiv.org/abs/1701.04113>
- Using PCA to Efficiently Represent State Spaces: <http://irll.eecs.wsu.edu/wp-content/papercite-data/pdf/2015icml-curran.pdf>

# A Separation Principle for Control in the Age of Deep Learning

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A Separation Principle for Control in the Age of Deep Learning

Alessandro Achille, Stefano Soatto (<https://arxiv.org/abs/1711.03321>)

*We review the problem of defining and inferring a “state” for a control system based on complex, high-dimensional, highly uncertain measurement streams such as videos. Such a state, or representation, should contain all and only the information needed for control, and discount nuisance variability in the data.*