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Report #2:

Experiment No 6: Pulse Amplitude Modulation (Sampling)

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December – 2023

Abstract

The aim of this experiment is to understand the Pulse Amplitude Modulation and how sampling works for specific sampling frequencies. We experiment with two types of sampling and discuss their differences. Moreover, we show the modulation and demodulation of various signals in both the frequency domain and time domain and discuss the results in comparison with the theoretical part. Also, we compare*signals*that* have aliasing with non-aliasing signals, and we discuss the importance of time multiplexing and its challenges.

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Theory

2.1 Pulse Amplitude Modulation (PAM) and Sampling Techniques

Pulse amplitude modulation (PAM) operates as a modulation technique where the amplitude of the pulsating carrier signal adjusts based on the immediate value of the message signal.

Pulse amplitude modulation involves the discrete sampling of the analog modulating signal, with each signal being sampled at consistent intervals. During sampling, the continuous-time signal undergoes a transformation into a discrete-time signal while maintaining continuous amplitude. This initial stage stands as the primary step in transitioning a signal from an analog to a digital format[1].

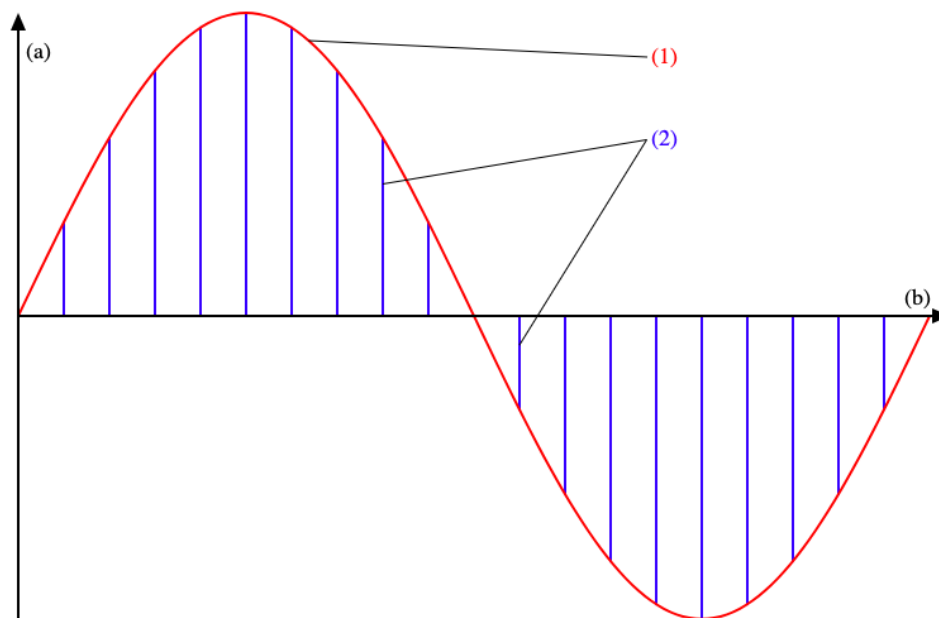


Figure 1: Pulse amplitude modulation Signal

As figure above, presented in blue color, the amplitude of every sample correlates directly with the message signal represented in red color.

Three sampling techniques exist: flat-top sampling, natural sampling, and ideal sampling. Practically unattainable, ideal sampling leads us to employ both flat-top and natural sampling

methods within our laboratory. Natural Pulse Amplitude Modulation (PAM) involves the multiplication of an analog signal with an impulse train. The depicted figure 2 showcases the resulting image where the upper segment of the pulses aligns with the modulating wave. Flat-topped PAM finds extensive application due to its ability to eliminate noise-induced distortions during signal transmission, a common issue in Natural PAM. Figure 3 illustrates the flat tops of the samples, highlighting the distinctive feature of this modulation technique.[2][3]

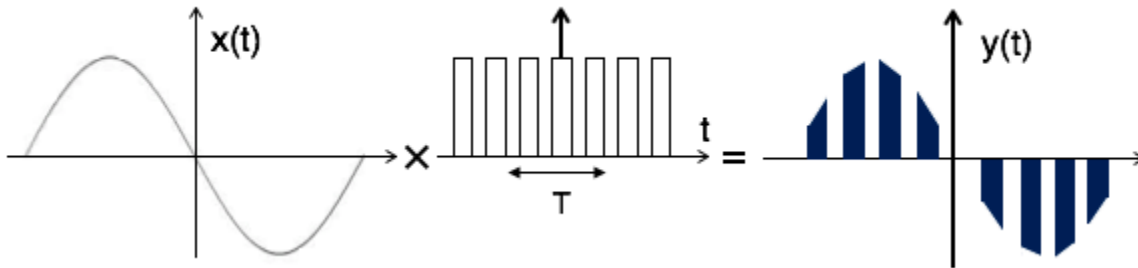


Figure 2: Natural Sampling

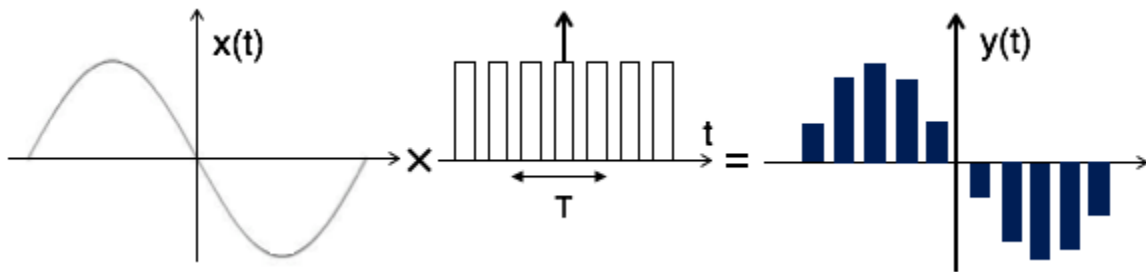


Figure 3: Flat top PAM

The duty cycle quantifies the proportion of time within a cycle that a wave remains in the ON-state. It's computed by dividing the ON-state duration (PW: Pulse width) by the signal's period(T_c). For instance, a 70% duty cycle signifies that the signal remains ON for 70% of the cycle and OFF for the remaining 30%.

$$\text{Equation 1) Duty Cycle} = (PW/T_c) * 100\%$$

$$\text{Equation 2) Zero Crossing} = (n * f_m) / \text{Duty cycle}$$

2.2 Demodulation Aliasing and Nyquist Rate.

To successfully convert a continuous signal into a sampled one, the sampling frequency should be at least twice the frequency of the message signal to properly retrieve the message signal. The sampling frequency serves as the minimum rate necessary for distortion-free sampling, preventing aliasing and enabling accurate reconstruction of the message signal. For proper reconstruction of the message signal, a crucial condition must be met by ensuring the following equation holds true[3].

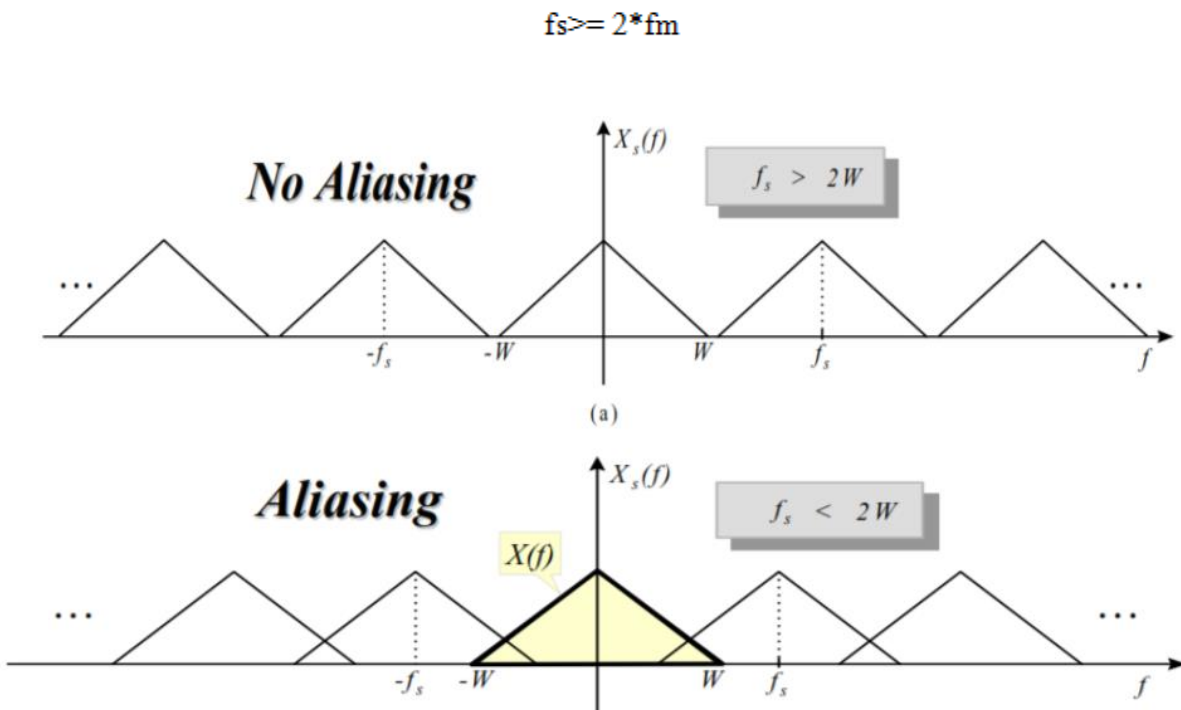


Figure 4: Aliased & Non-Aliased Signals

As depicted in the preceding figure, the region where overlap occurs due to undersampling signifies the presence of aliasing effects. Upon confirming the absence of aliasing, the signal undergoes processing through a low-pass filter, facilitating the retrieval of the original message signal.

2.3 Pulse Amplitude Modulation Time Multiplexing and Crosstalk.

Multiplexing involves transmitting multiple data signals through a shared communication channel, assigning distinct time slots within the overall time frame for each signal. Ensuring synchronization is critical, allowing each source to transmit solely during its allocated time slot to prevent collisions. Synchronization problems or constraints in channel bandwidth may lead to cross talk, resulting in noise interference [4].

Procedure and Data Analysis

3.1 Time and Frequency Characteristics of pulse train



Figure 5: Setup of PAM

First Initially, we assembled the components and established wire connections following the configuration illustrated in the preceding figure. Using the function generator, we selected a pulse train set at 1 kHz frequency, V_{ss} set to 10V, and with a 10% duty cycle.

This configuration enables us to generate a specific waveform characterized by its frequency, voltage amplitude, and the duration of its active state within each cycle. Adjusting these parameters allows for controlled signal output, crucial for various experiments in signal processing and modulation studies.

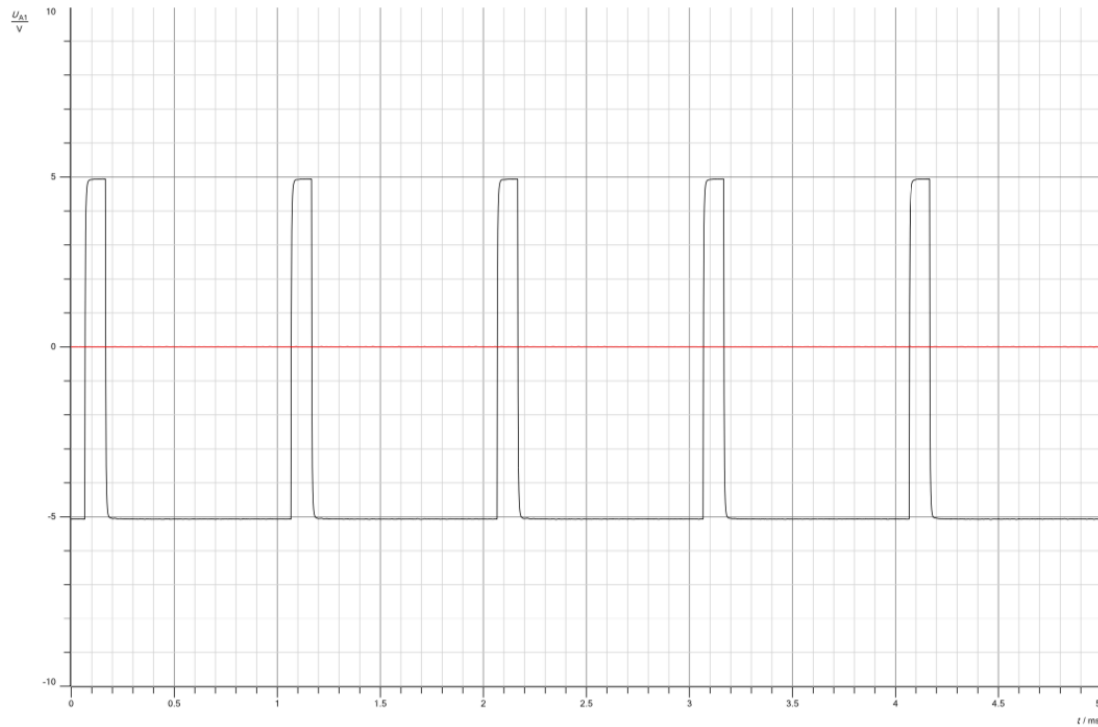


Figure 6: Pulse Train with 10% Duty Cycle (In Time Domain)

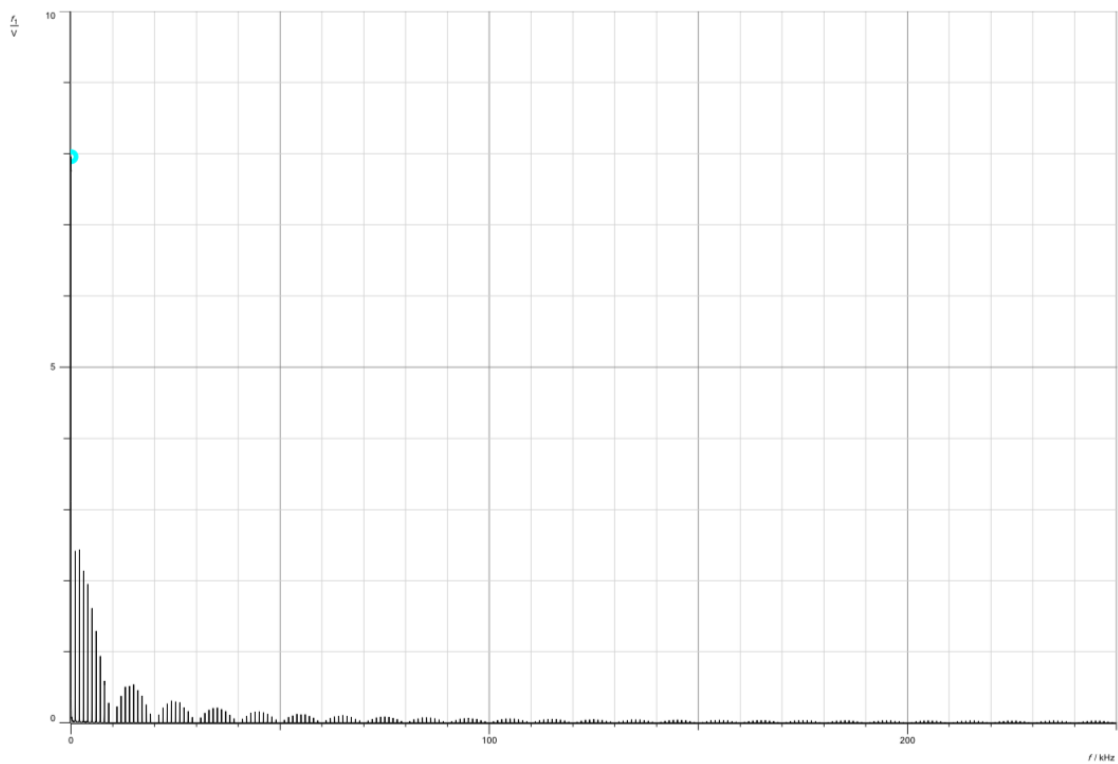


Figure 7: Puls Train with 10% Duty Cycle. (In Frequency Domain)

As depicted in the above figure, the envelope of the pulse spectrum exhibits zero crossings every 10 kHz intervals. This translates to the initial zero crossing transpiring at 10 kHz, followed by subsequent points at 20 kHz, 30 kHz, and onward. The accompanying table illustrates these zero crossings for various duty cycle values. The table below clearly demonstrates that a higher duty cycle corresponds to lower occurrences of zero crossings. This relationship aligns mathematically, as the zero-crossings display an inverse proportionality to the duty cycle, as evidenced in equation-two within the theoretical framework.

| Duty Cycle(%) | 20 | 30 | 40 | 50 | 90 |
|--------------------|----|------|-----|----|-----|
| Zero Crossing(khz) | 5 | 3.33 | 2.5 | 2 | 1.1 |

Table1: Zero Crossings for Different Duty Cycles

Pulse trains necessitate broader transmission bandwidths to encompass their extensive frequency range. Increased frequency coverage correlates with enhanced transmission accuracy and quality. As illustrated in the aforementioned figure, it's evident that the signal envelope takes on a sinc-shaped form.

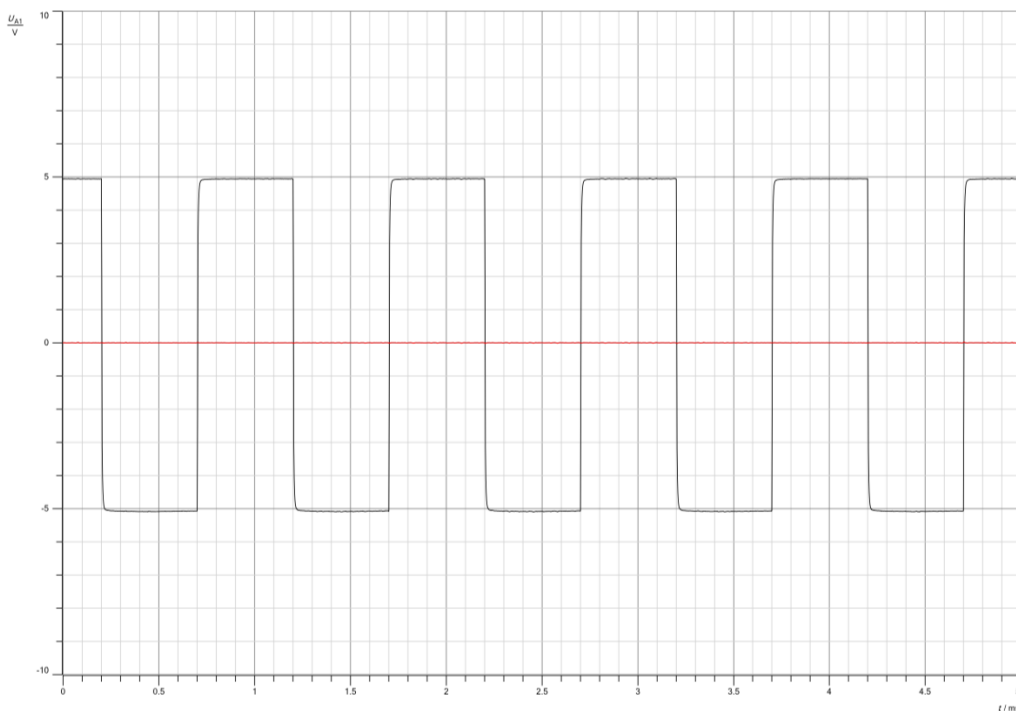


Figure 8: Pulse Train with 10% Duty Cycle (In Time Domain)

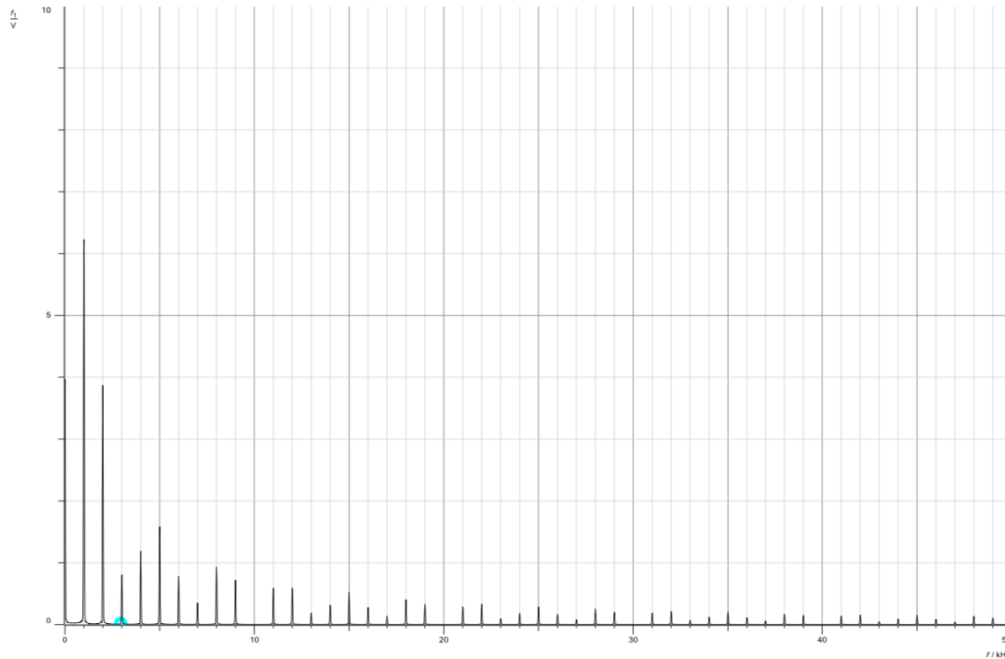


Figure 9: Pulse Train with 30% Duty Cycle. (In Frequency Domain).

The figures above demonstrate that altering the duty cycle directly affects the duration the signal spends in the ON-state. A comparison between figures 6 and 8 highlights that a higher duty cycle results in a longer pulse-width. Additionally, examining the frequency domain figures reveals that elevating the duty cycle amplifies the pulses amplitudes.

3.2 Characteristics of Pulse Amplitude Modulation (PAM).

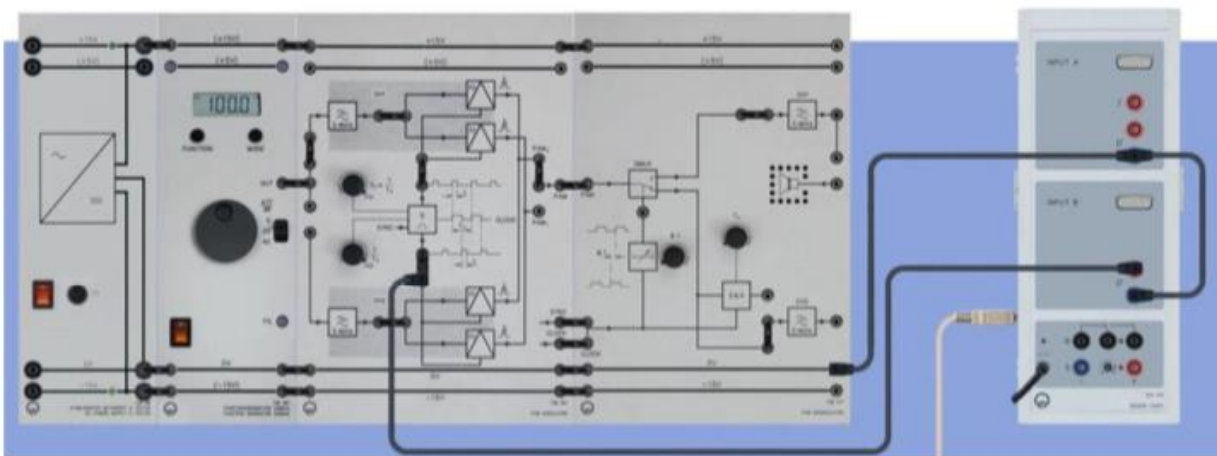


Figure 10: Setup of Pulse amplitude modulation

In this configuration, we maximize both the sampling-frequency-knob and the duty-cycle settings. We link the clock-generator to generate time-samples. By manipulating the pulse frequencies, we set one at 5kHz and then the other at 15kHz, as confirmed by the measurements obtained from the FFT analyzer.

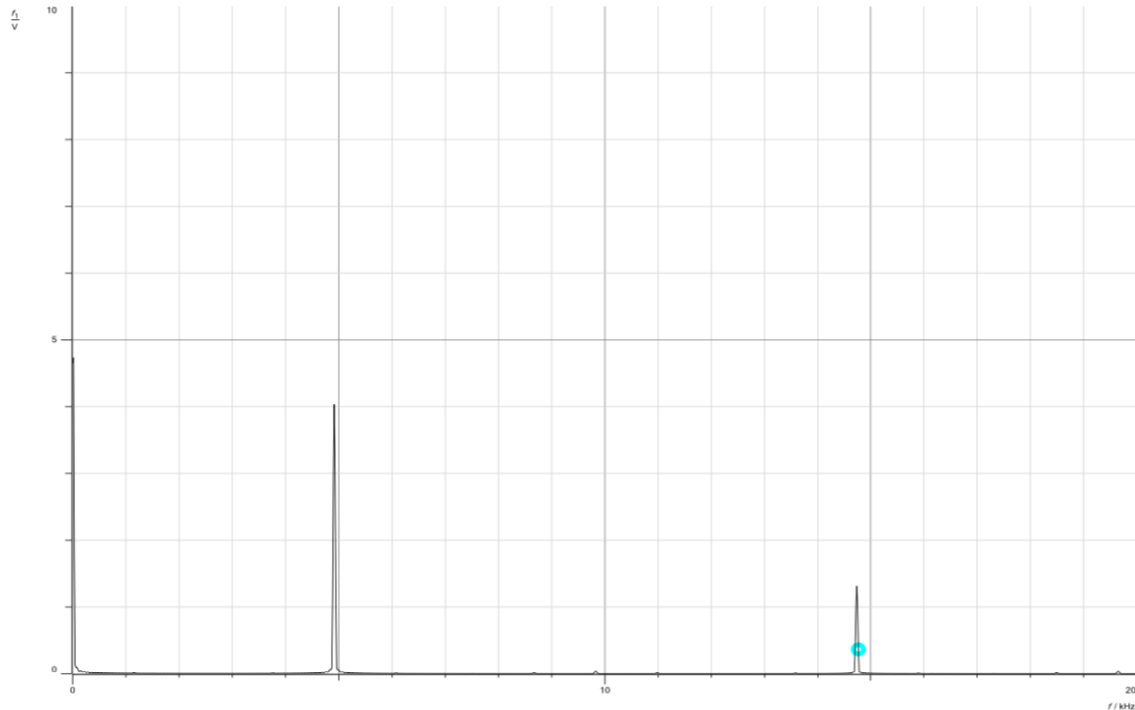


Figure 11: Pulse frequencies set at 5kHz & 15kHz

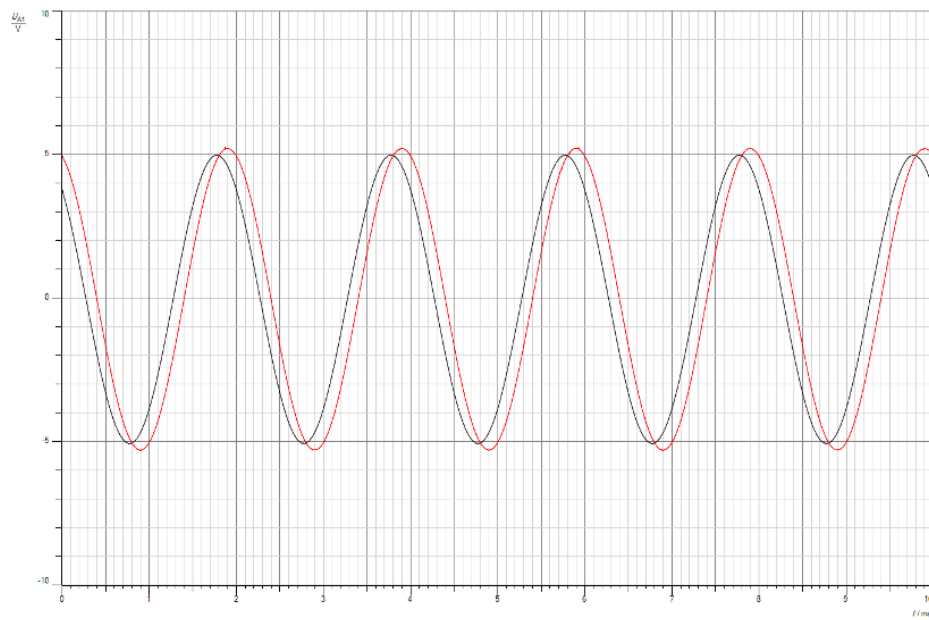


Figure 12: Signal before and after the channel filter

In this investigation, we examine the impact of the channel filter(CH1). The black-signal represents the state before the filter, while the red signal represents the state after the filter. Observing the results, it is evident that the filter induces a minor shift while maintaining consistent amplitude and frequency.

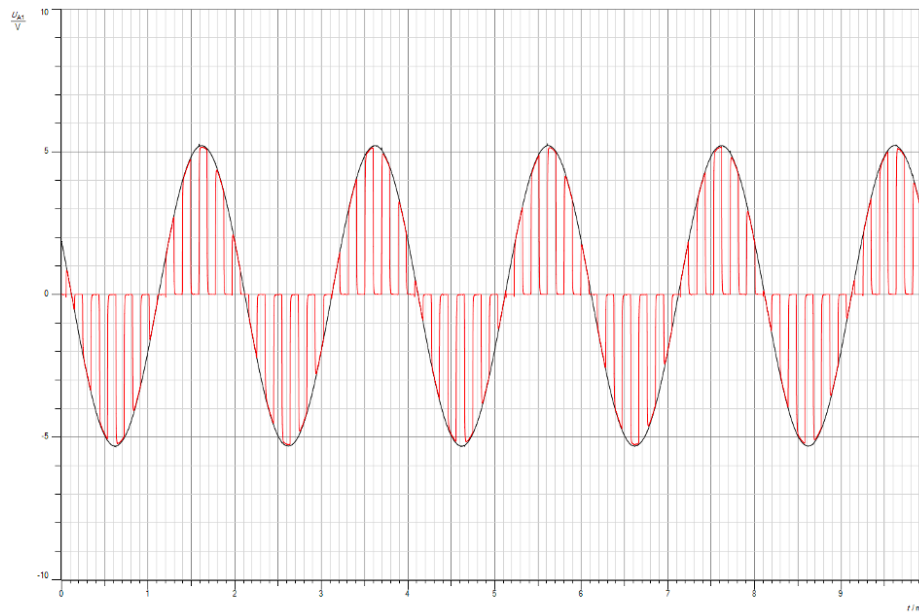


Figure 13: Signal of Pulse amplitude modulated(PAM)

In the above figure, The sampling method observed here appears to be natural sampling, evident from the sampled signals' amplitudes aligning with the signal's amplitude. While ideal or instantaneous sampling is optimal, it's unachievable in practice due to its theoretical nature. Consequently, our lab employs both natural and flat-topped sampling methods to address the limitations of real-world applications.

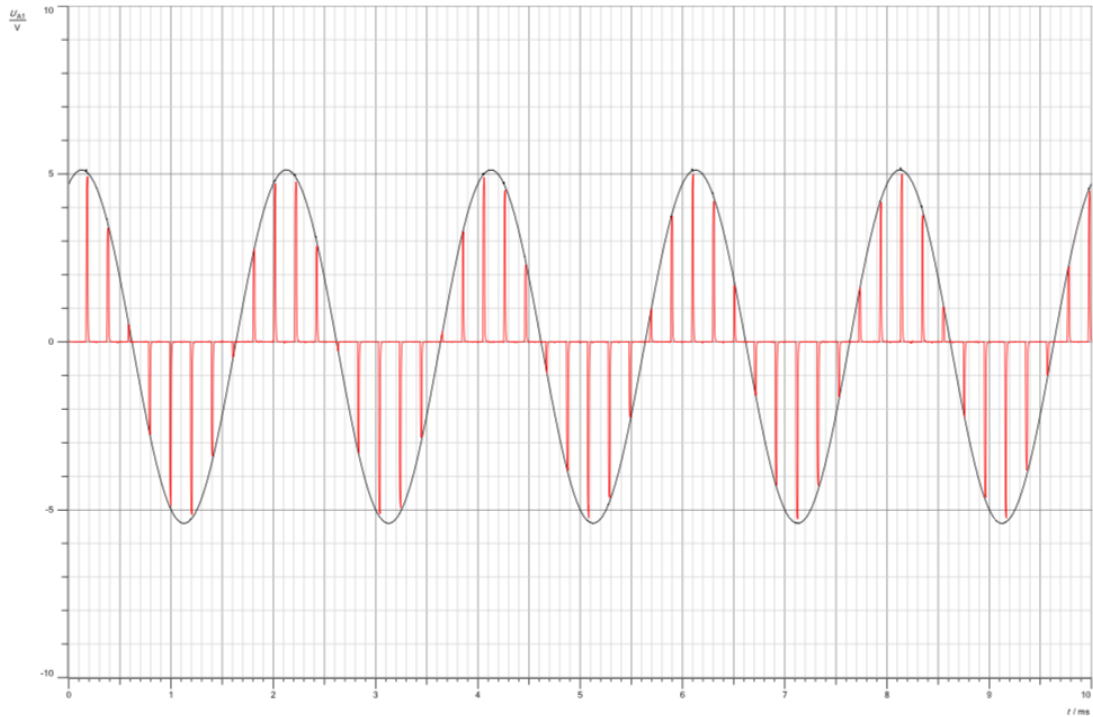


Figure 14: PAM signal with minimum duty cycle

Figure 12 and Figure 13 offer a comparison illustrating the impact of the duty cycle on the sampled signal. Decreasing the duty cycle visibly reduces the pulse width within the sampled signal, showcasing a direct correlation between the duty cycle and the resulting pulse width.

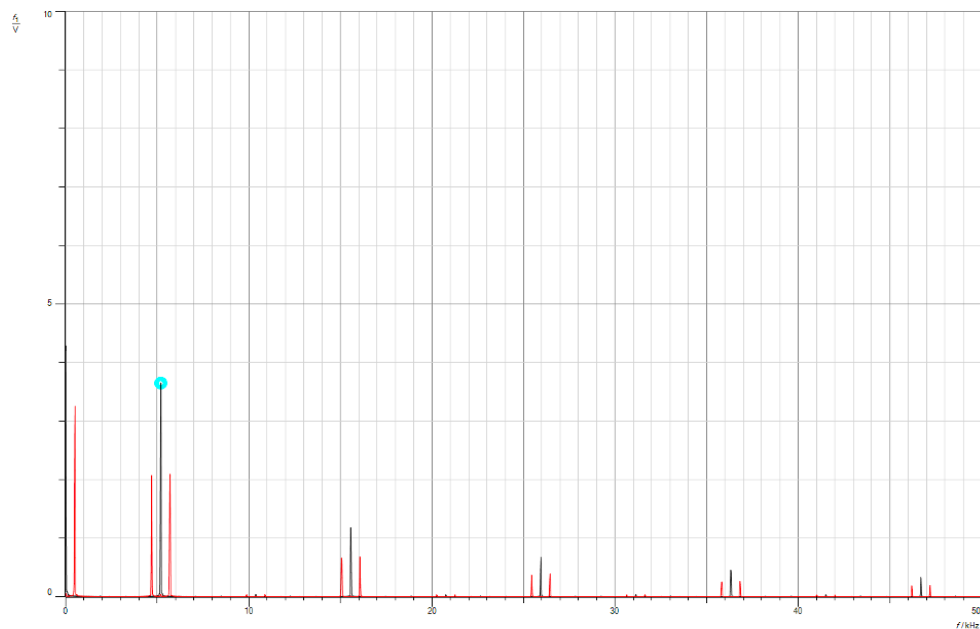


Figure 15: PAM1 output and clock generator

From the figure above, the observed sequence showcases the message signal at 5 kHz, followed by 15 kHz, and then 25 kHz, with a marginal variance in pulse frequency between each transition.

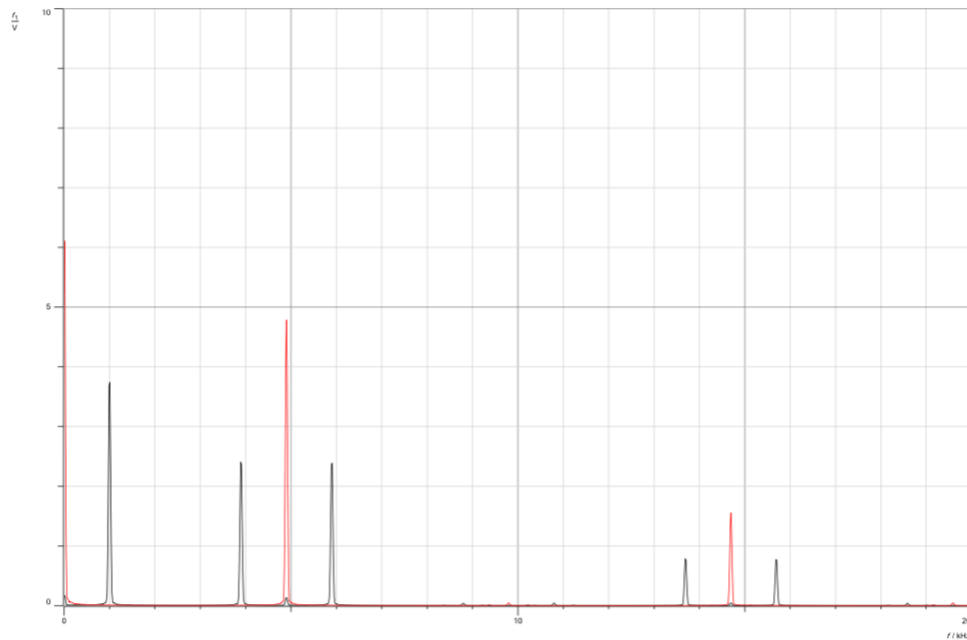


Figure 16: Message signal with frequency = 1khz

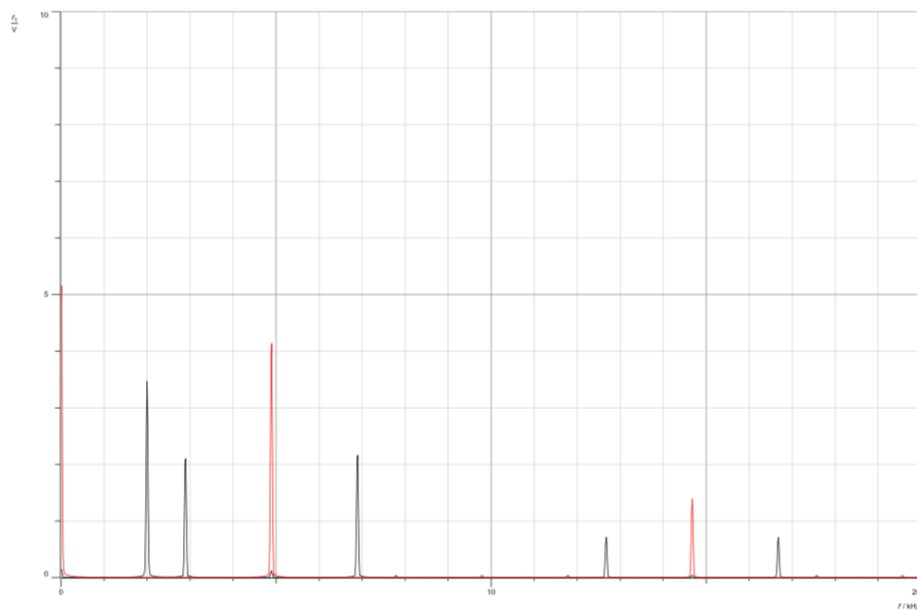


Figure 17: Message signal with frequency= 2khz

Changing The alterations in the message signal frequency are evident in the frequency domain representation. Zero crossings are contingent on both the the duty cycle and the message frequency, exhibiting an increase when the message frequency rises. Additionally, the absence of any interfering signals in the depicted figures indicates the absence of aliasing in the message signals.



Figure 18: Message signal with Duty Cycle: 10%

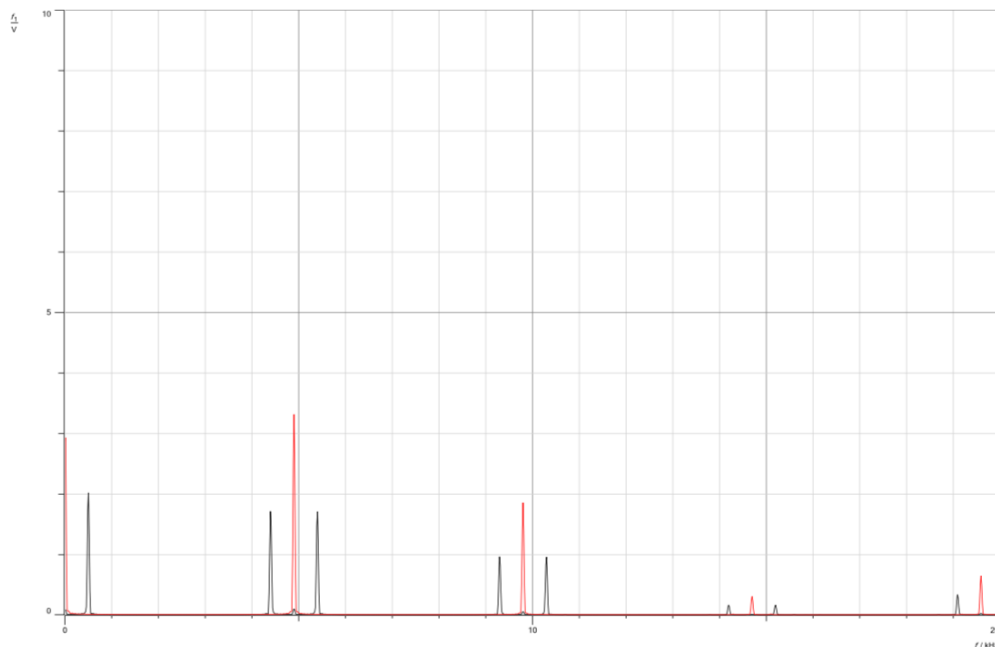


Figure 19: Message signal with Duty Cycle 30%

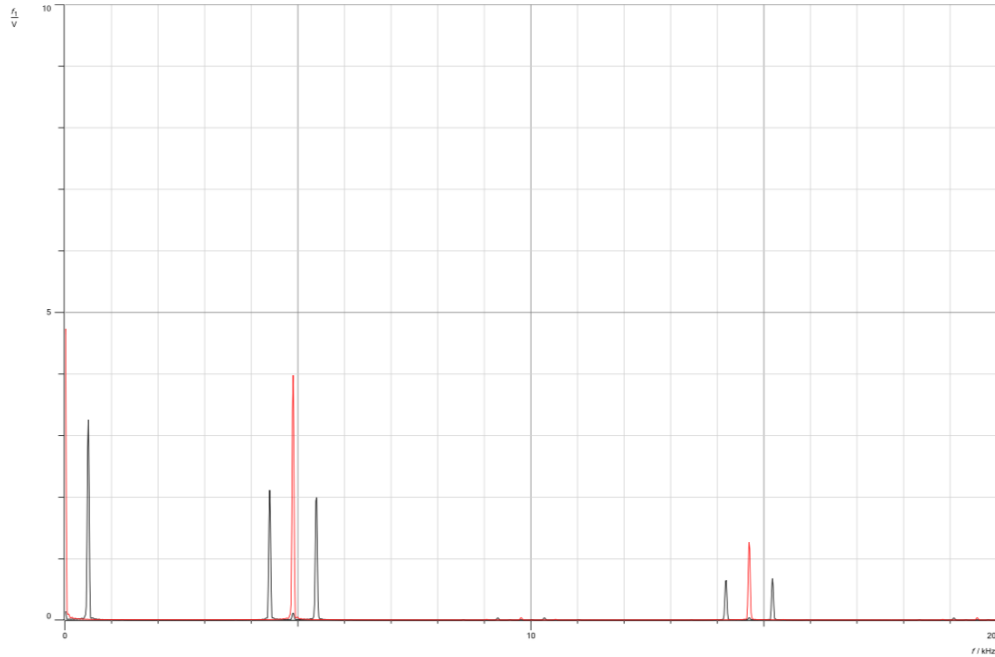


Figure 20: Message signal with Duty Cycle 50%

Based on the presented figures, it is apparent that varying the duty cycle results in changes to the amplitude of the signals. The progression from a 10% duty cycle to 30% and then to 50% demonstrates a corresponding increase in amplitude.

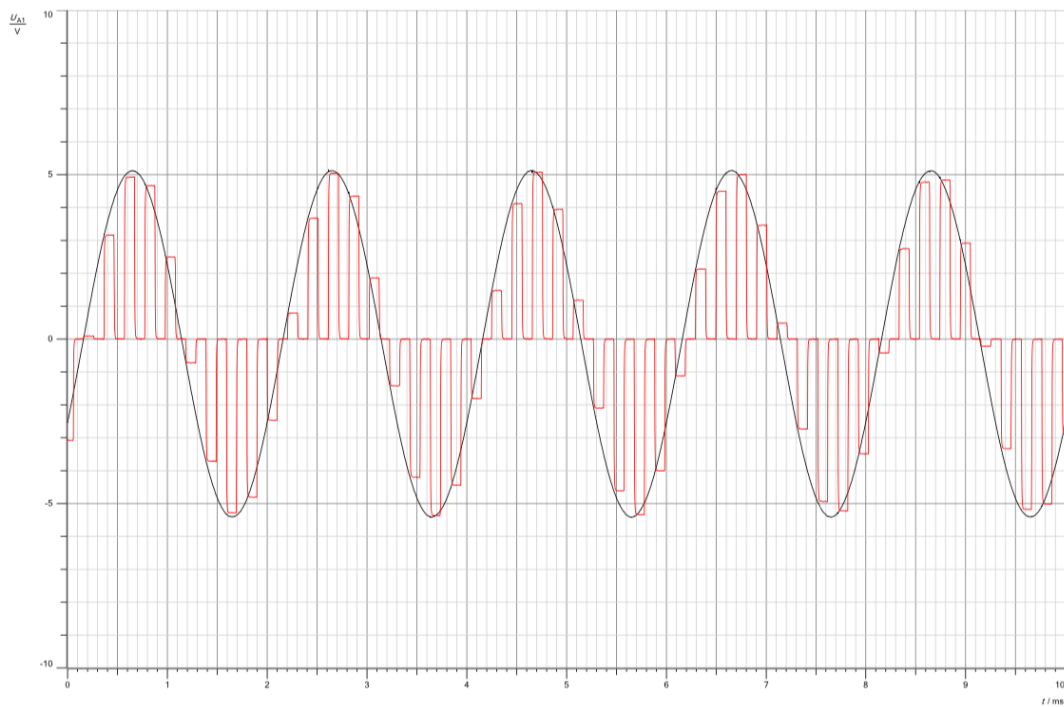


Figure 21: PAM2 modulated signal with max duty cycle.

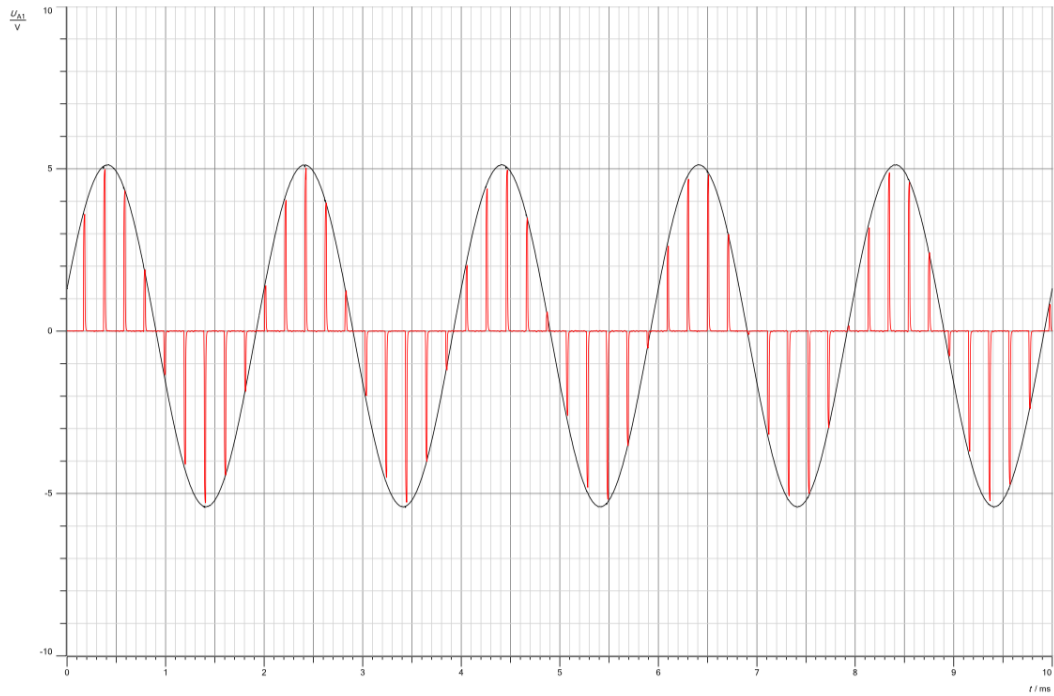


Figure 22: PAM2 with minimum duty cycle.

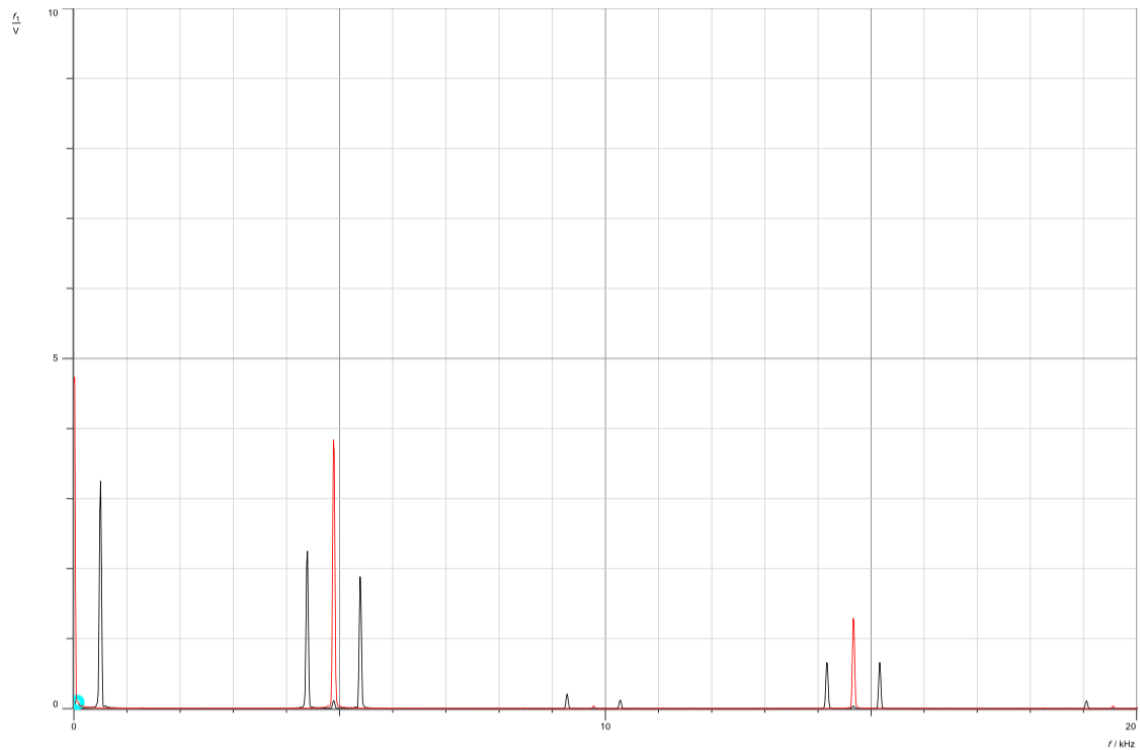


Figure 23: PAM2 with maximum duty cycle in frequency domain.

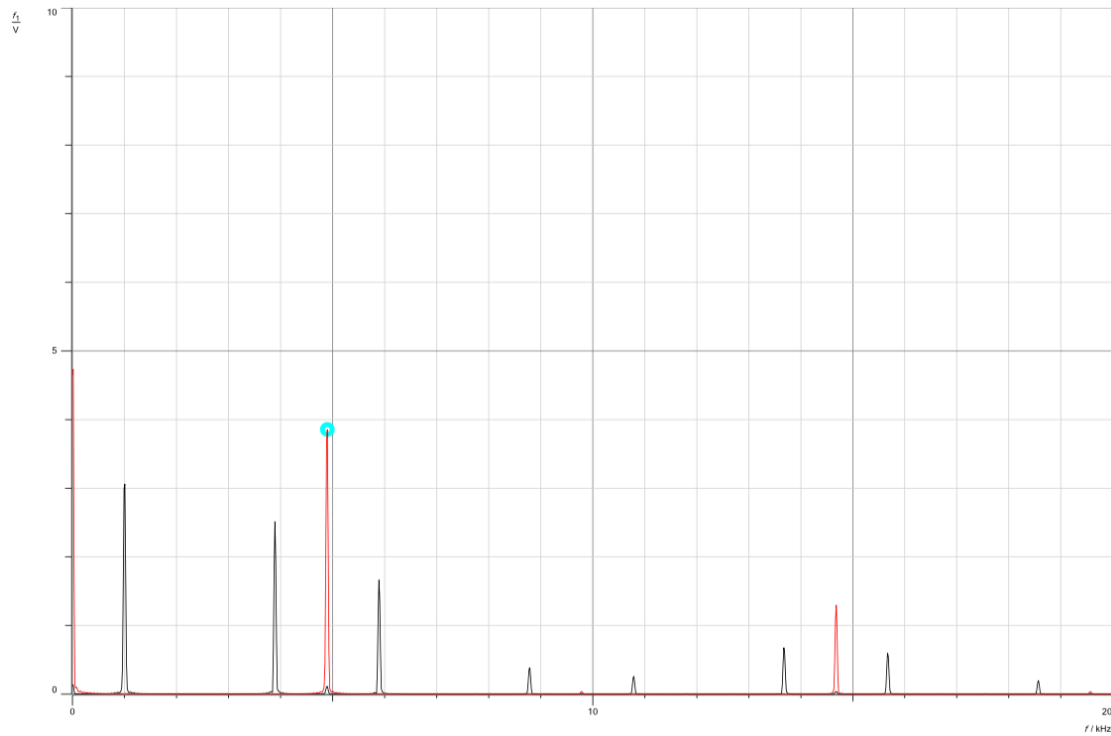


Figure 24: PAM2 signal with message frequency= 1khz

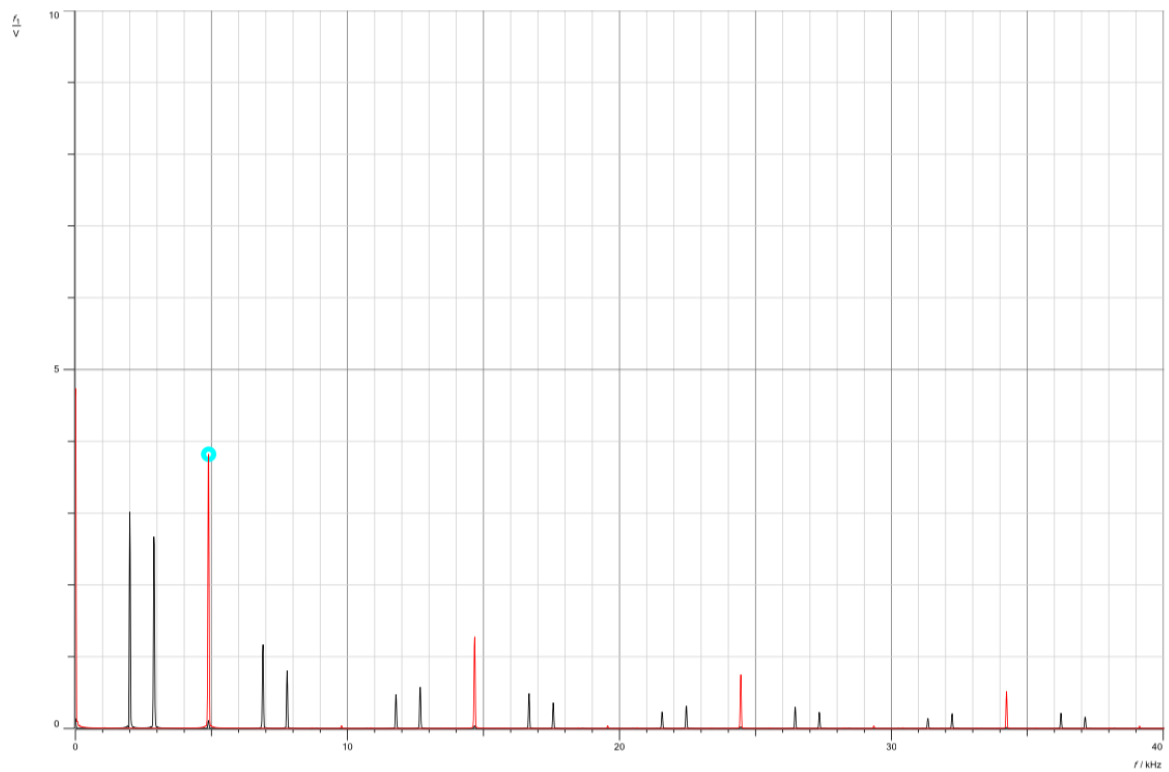


Figure 25: PAM2 signal with message frequency = 2khz.

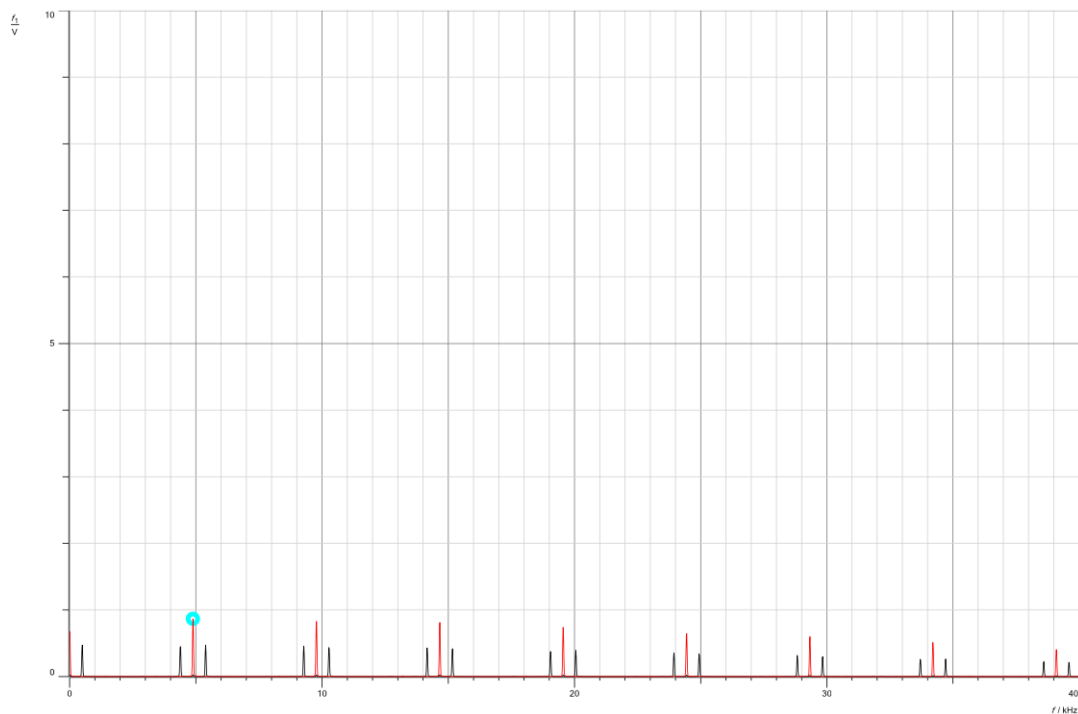


Figure 26: PAM2 with duty cycle 10% & fm= 500hz.

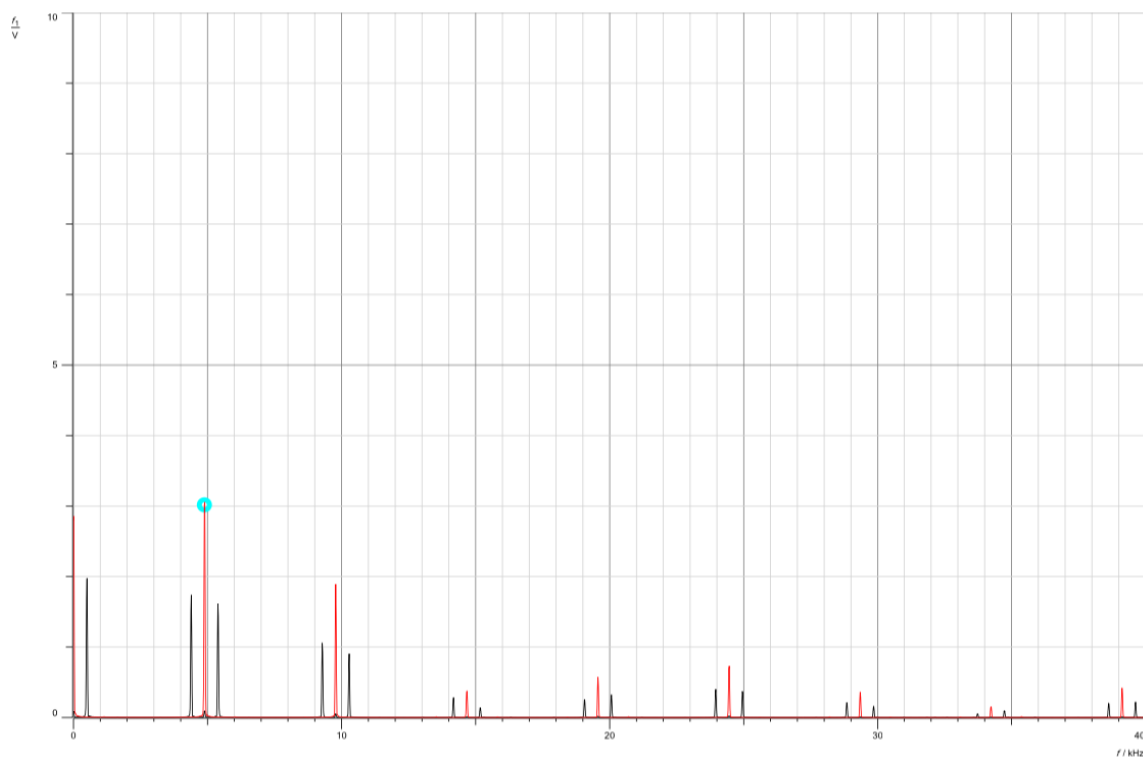


Figure 27: PAM2 with duty cycle= 30% & fm= 500hz.

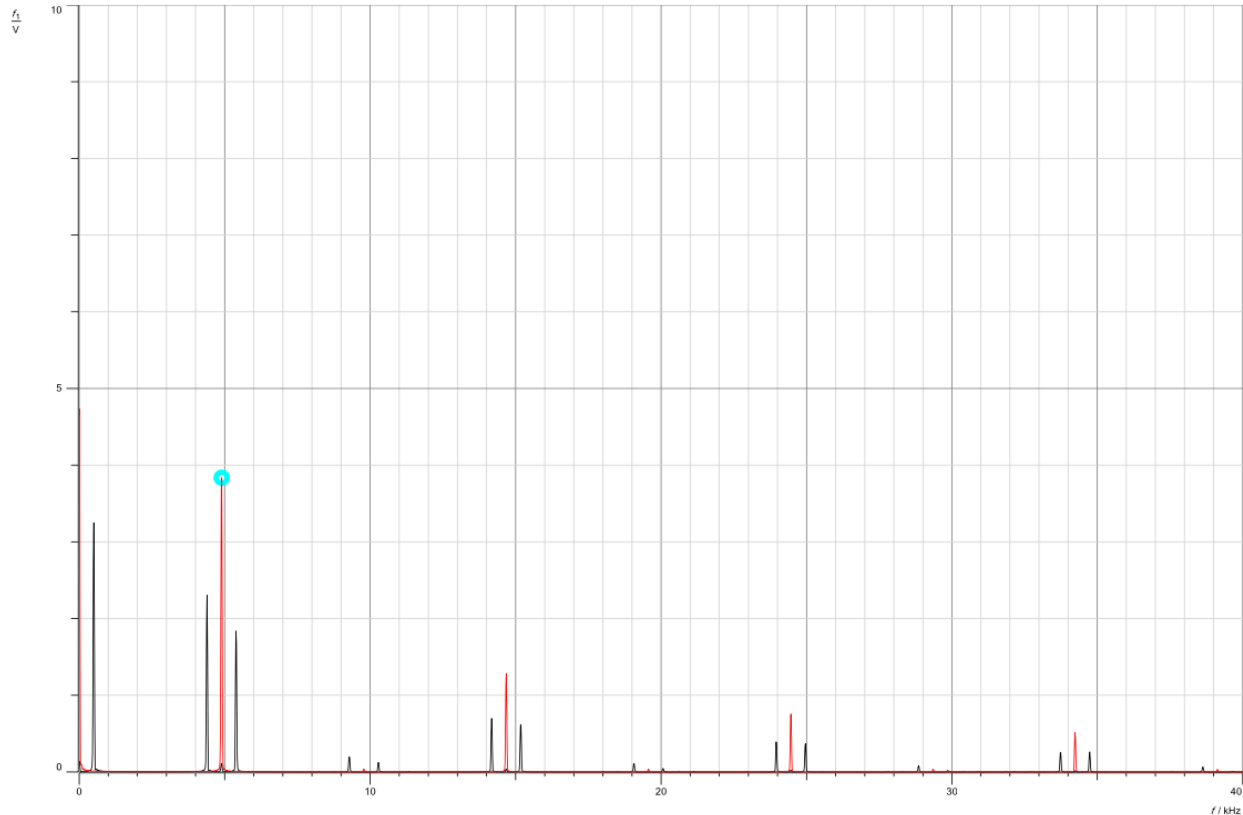


Figure 28: PAM2 with duty cycle= 50% & fm= 500hz.

The comparison between PAM1 and PAM2 in the presented figures highlights their distinctions: PAM1 employs natural sampling, whereas PAM2 utilizes flat-top sampling. Despite this difference, both sampling methods exhibit a consistent impact from the message, duty-cycle and frequency. Notably, the figures illustrate that as the duty-cycle rises, the zero-crossings decrease, regardless of whether it's in natural or flat-topped sampling. Furthermore, variations in the frequency of the message signal directly influence the magnitude of zero-crossings. A higher frequency within the message signal results in larger zero-crossings. Equation2 in the theoretical section also underscores this relationship.

Ideal sampling relies on an impulse as a clock generator to enable infinite sampling, deviating from the conventional ON and OFF switch mechanism. However, implementing this concept is unattainable in practical scenarios due to real-world limitations. As depicted in the figures, the observed sampling methods utilized are flat-top and natural sampling, being more feasible options given the constraints of reality.

3.3 Characteristics of Pulse Amplitude Demodulation.

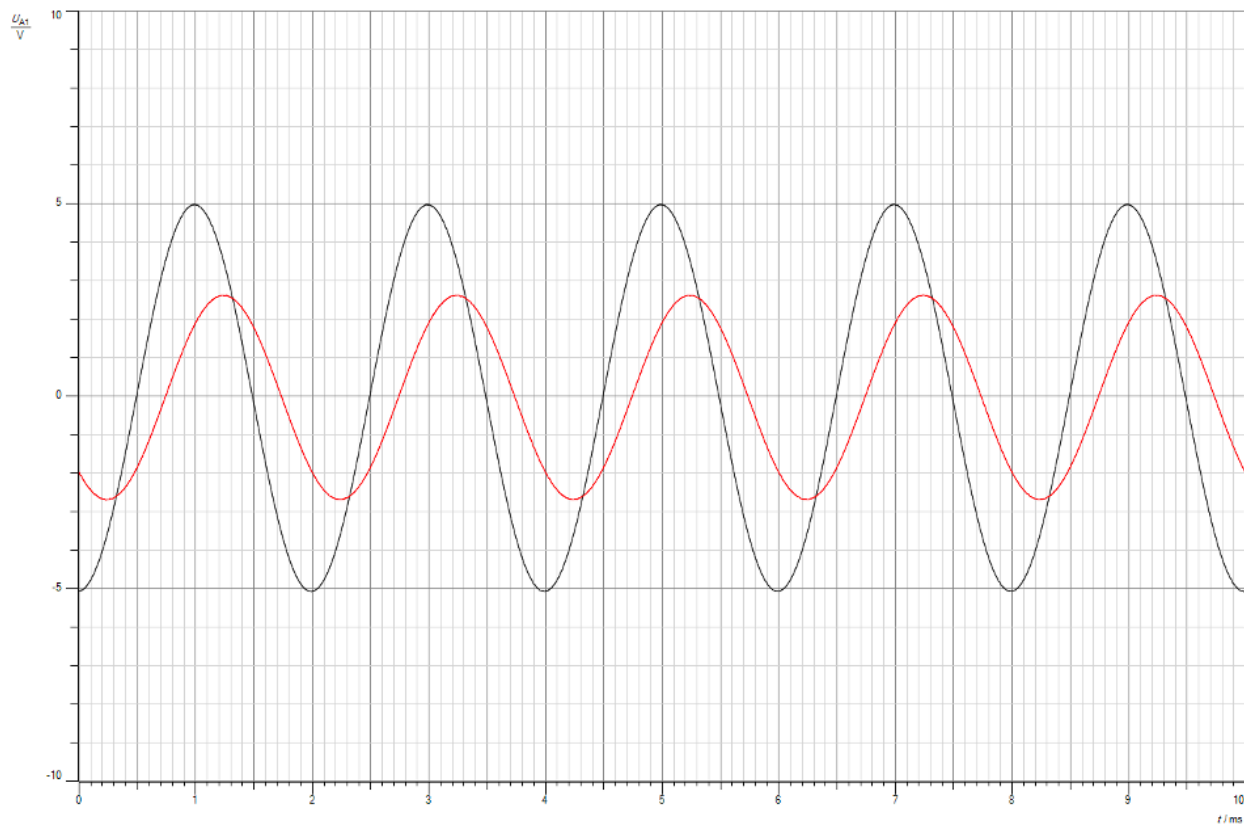


Figure 29: Demodulated signal

In the figure above, the black-signal represents the message signal, whereas the red-signal represents the demodulated signal. Notably, the demodulated signal effectively recovers the message signal, albeit with a varied amplitude. This discrepancy is anticipated due to the inherent gain factors associated with filters in the demodulation process.

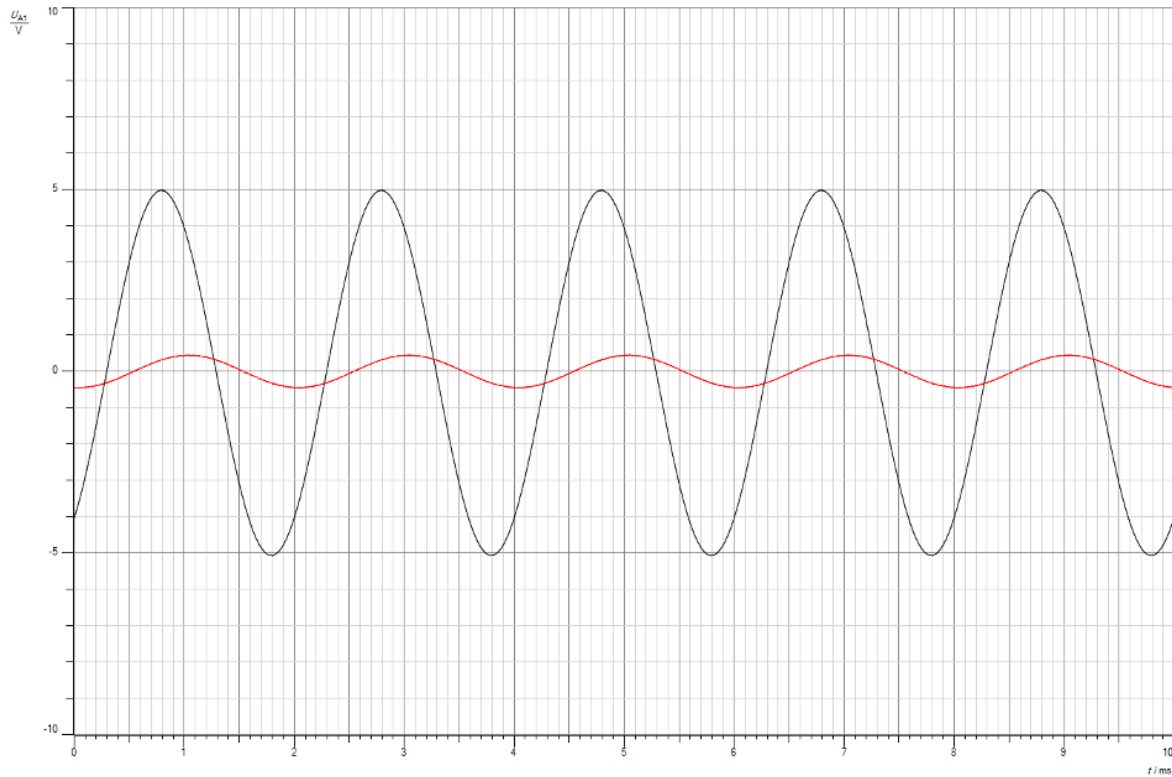


Figure 30: Demodulated signal with 10% duty cycle.

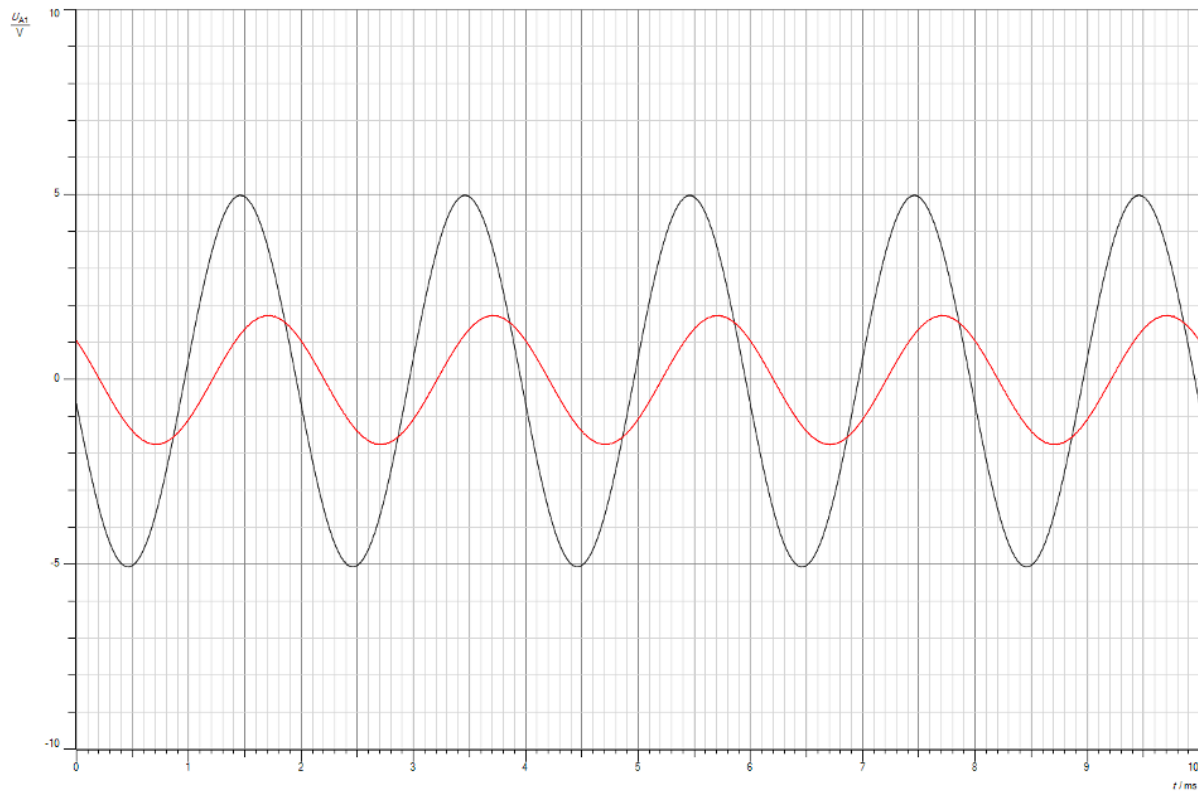


Figure 31: Demodulated signal with 30% duty cycle.

The figures above a clear relationship between the duty cycle variation and the resulting amplitude within the demodulated signal. With an increase in the duty cycle, there is a corresponding rise in the demodulated signal's amplitude.

3.4 Aliasing in the Time and the Frequency Domain.

Initially, we configure the clock generator frequency at 5 kHz with a 50% duty cycle. and the function generator is set to the following: Sine wave, Freq = 3000hz, and $V_{ss}=5v$. Then we connect the UA1 to the output signal of channel 1 filter, and UB1 to the PAM1 modulator. Finally, we place UB1 to the output of the demodulator filter of CH1.

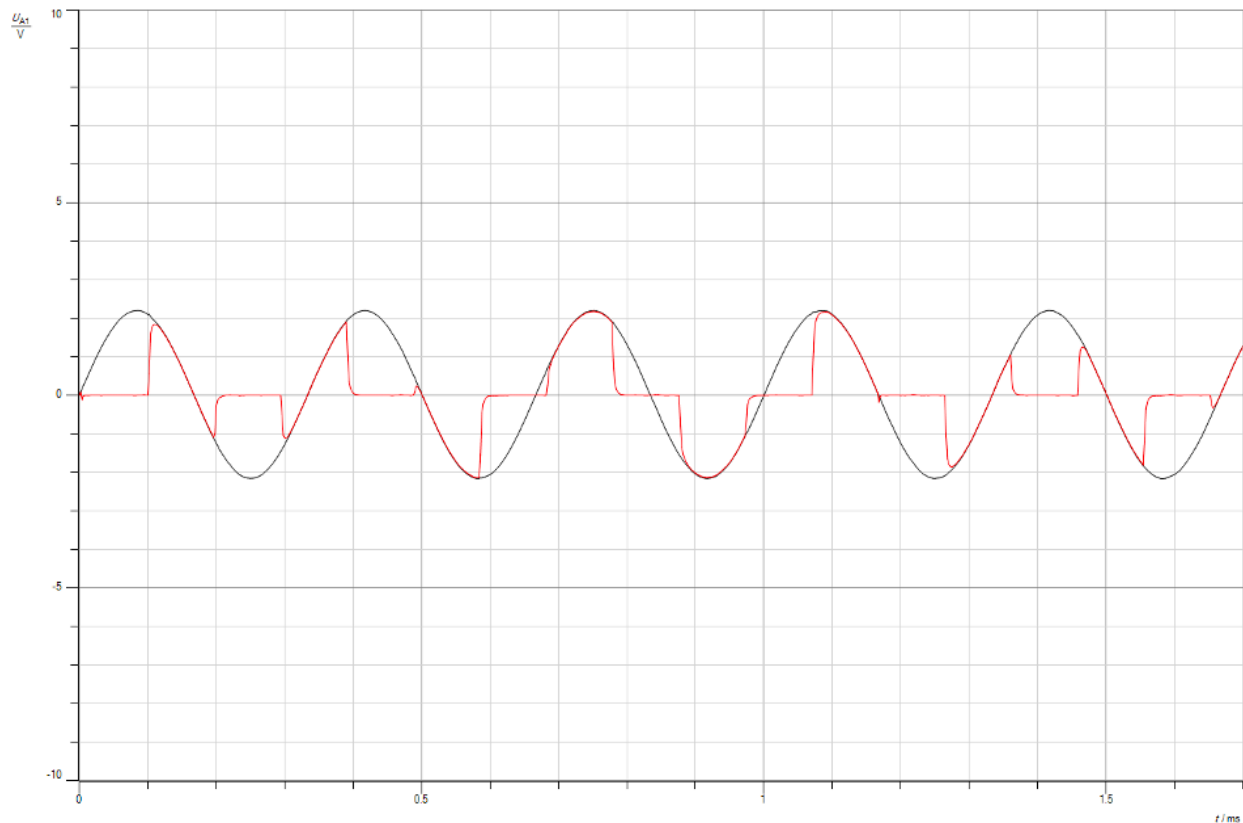


Figure 32: Signal with PAM1 modulator.

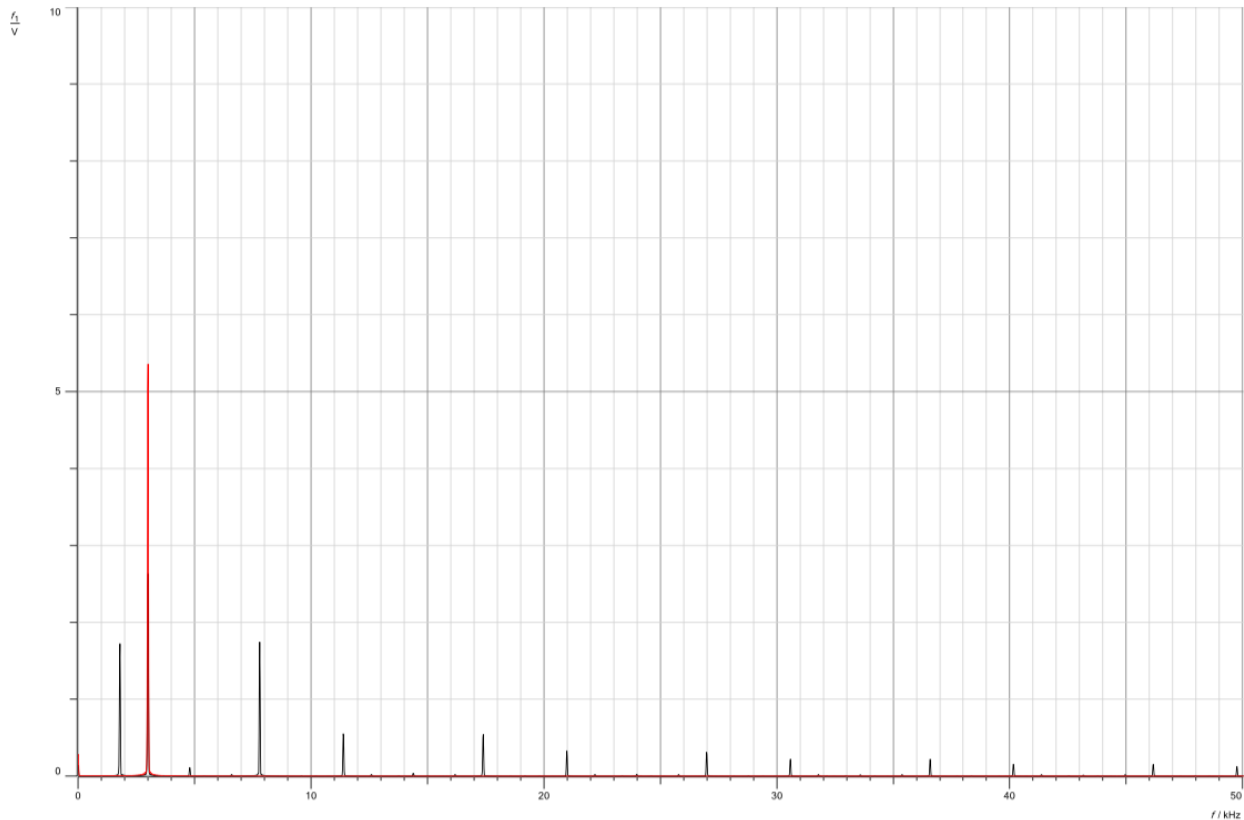


Figure 33: Signal with Aliasing

As shown in the figure, the message signal, indicated in red, operates at a 3kHz frequency. Notably, an additional impulse is discernible around ~2kHz within the same space. This occurrence signifies aliasing, a result of the sampling frequency being lower than twice the message frequency. As previously discussed, adhering to the Nyquist rate is crucial to prevent aliasing in such scenarios.

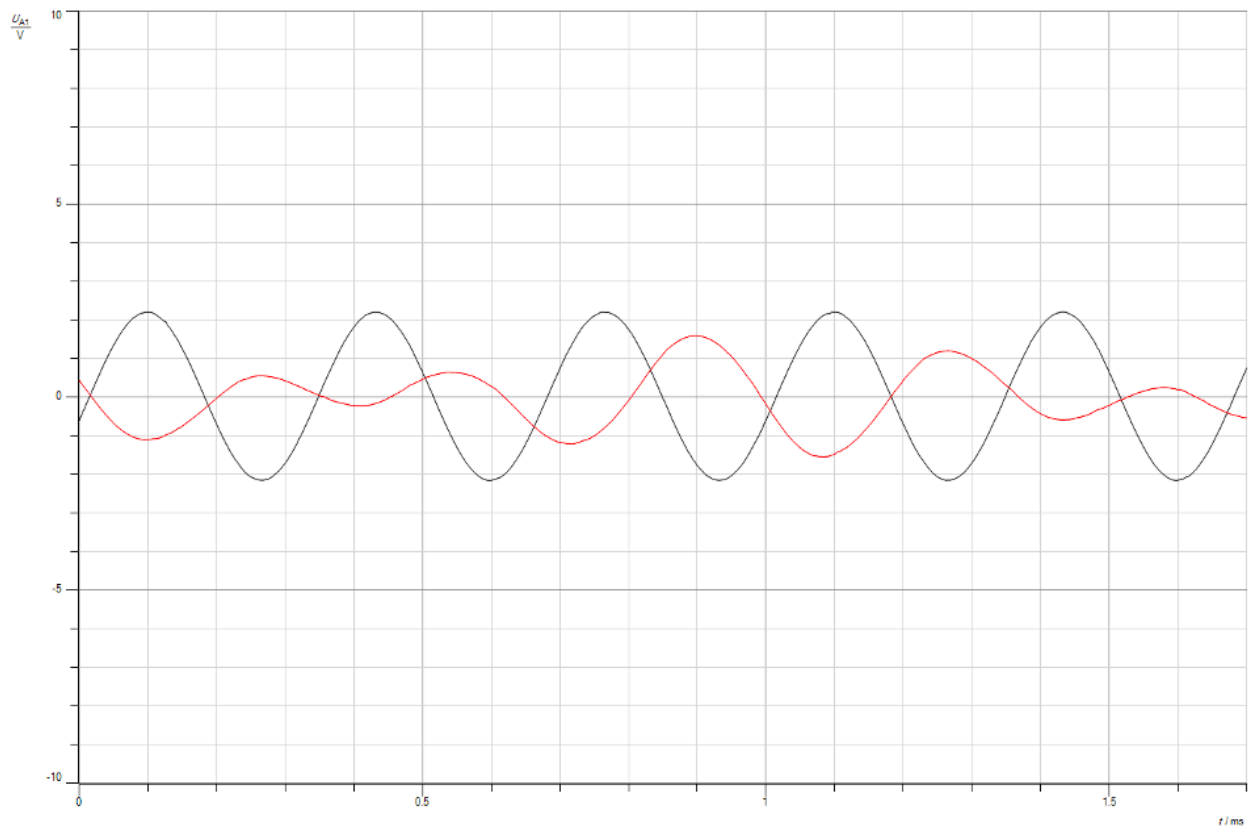


Figure 34: Signal with demodulator filter of CH1

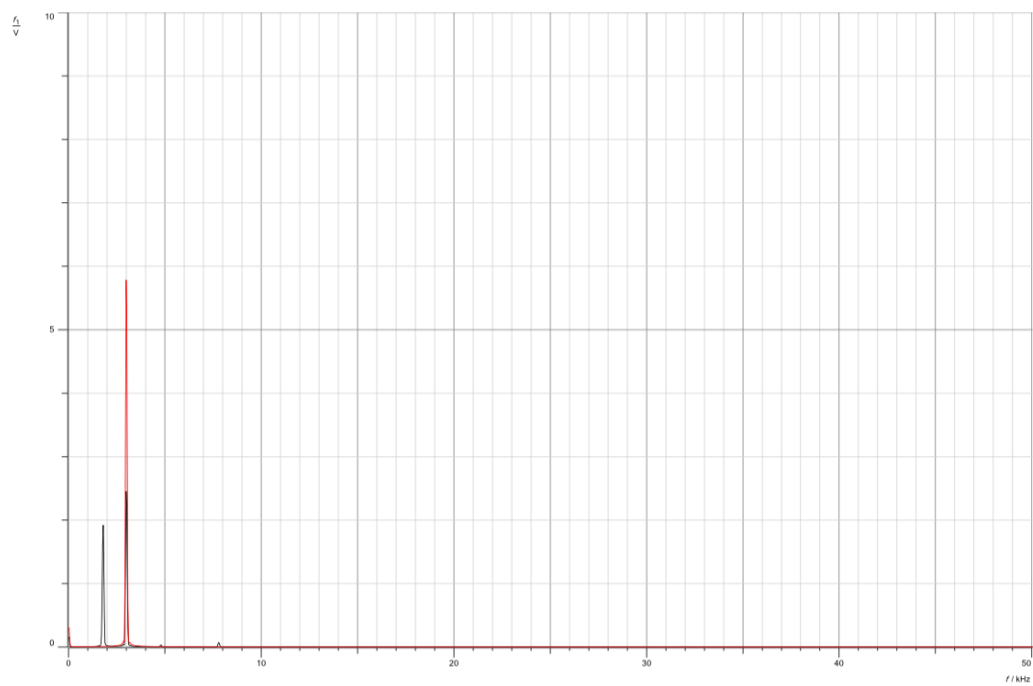


Figure 35: Demodulated signal in frequency domain

In this scenario, the message signal maintains a 3kHz frequency, and the demodulated signal indeed aligns with that frequency. Despite this alignment, the presence of aliasing indicates an inaccurate retrieval of the signal, leading to deviations and inconsistencies.

3.5 PAM Time Multiplex.

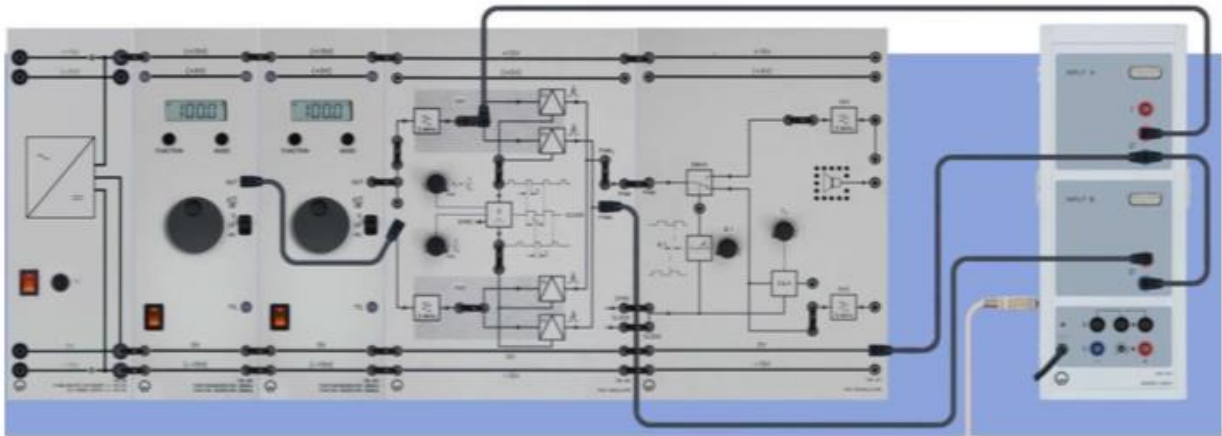


Figure 36: PAM Time Multiplex Setup

In this configuration, it's essential to maximize the sampling frequency (f_p) and duty cycle settings. Additionally, the function generator settings should be adjusted as follows: Set to Sine wave, with a frequency (f_{M2}) of 300 Hz, and a VSS (voltage) of 10V.

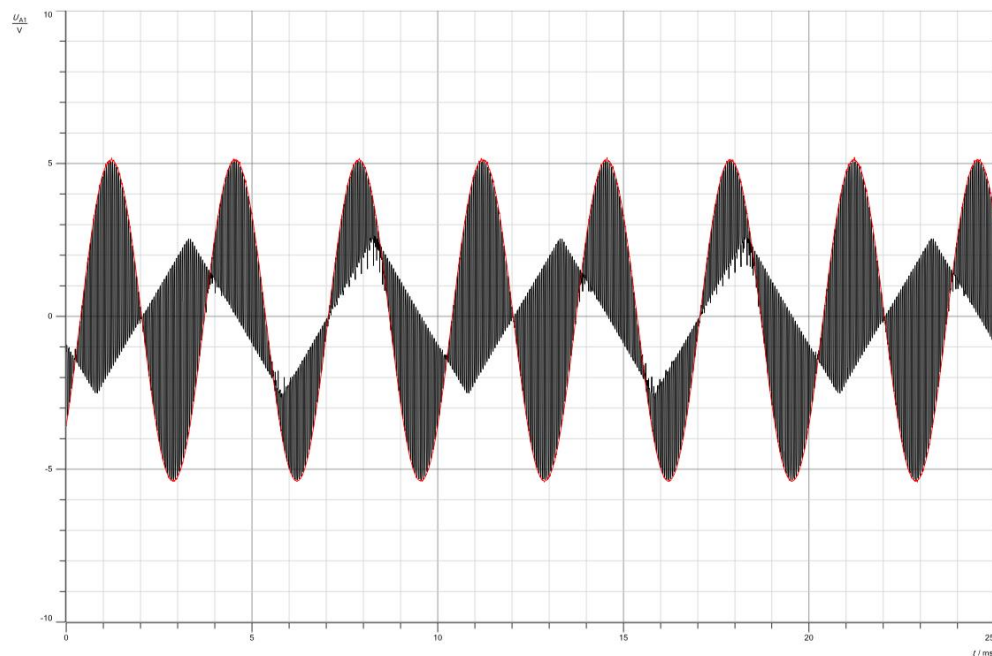


Figure 37: Triangular message channel CH1

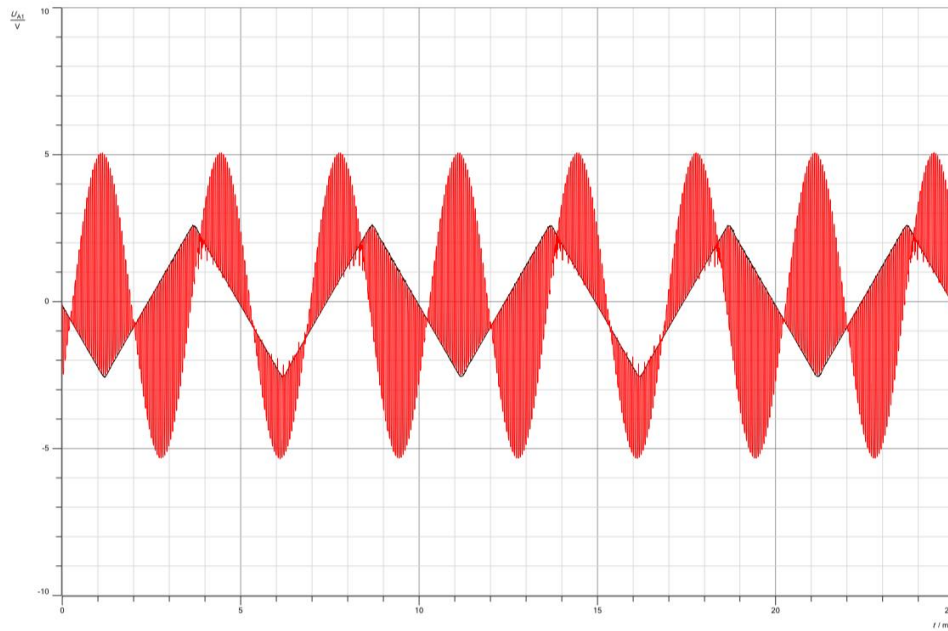


Figure 38: Sine message channel CH1

Here we can see two signals on the same time domain. One is triangular and the other is sinusoidal. Now we set the function generator to Triangle, $F_{m1}=200\text{hz}$, and $V_{ss} = 10\text{V}$. The second function generator is set to Sine, $F_{m2}=300\text{hz}$, and $V_{ss}=10$.

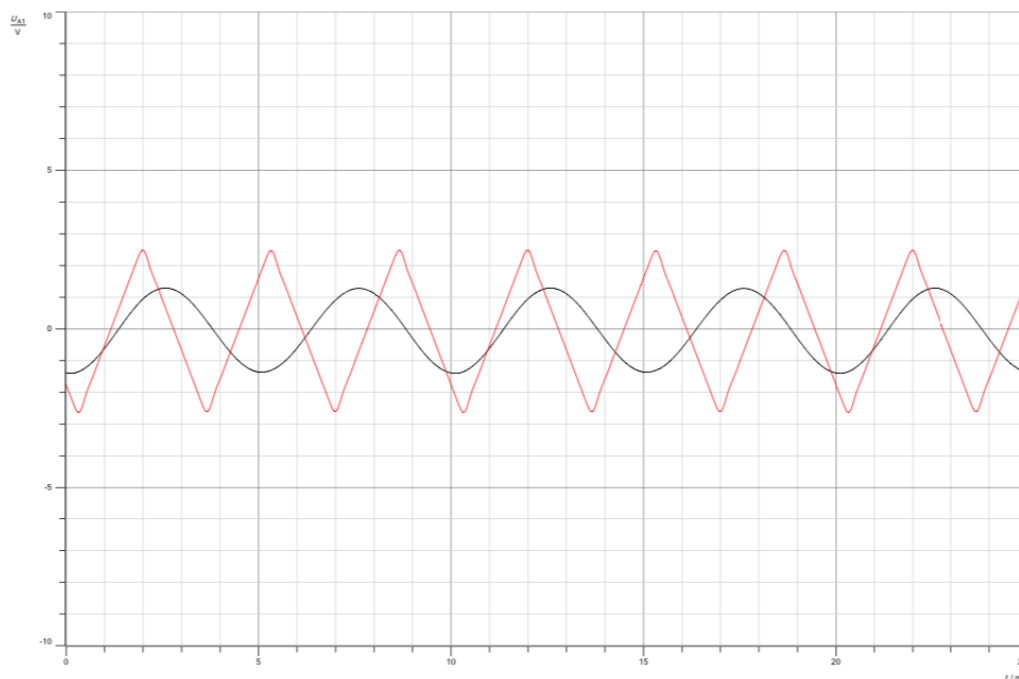


Figure 39: Demodulated Signals

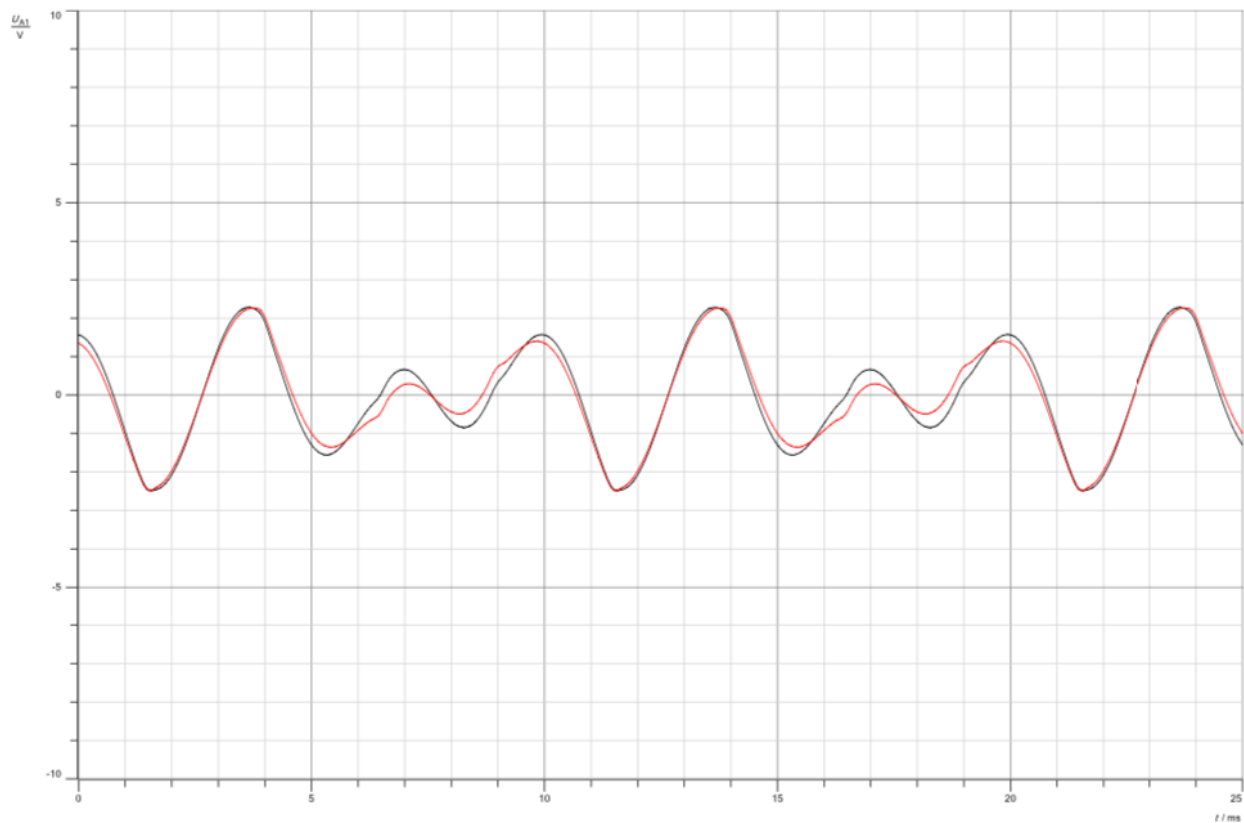


Figure 40: Effect of delta (middle)

Here In this observation, two signals —triangular and sinusoidal— are depicted within the same time-domain. The settings for the function generators are adjusted as follows: The first function generator is configured for a triangular waveform with a frequency (F_{m1}) of 200Hz and a voltage (V_{ss}) of 10V. Meanwhile, the second function generator is set to produce a sinusoidal waveform with a frequency (F_{m2}) of 300Hz, and a voltage (V_{ss}) of 10V.

Conclusion

In this lab, pulse amplitude modulation (sampling) and demodulation, as well as, aliasing effect, time multiplex and cross talk were covered. The modulation process in both the time and frequency domains were discussed; specifically, the effect of the duty cycle and message frequency on the Pulse amplitude modulated signal. We have learned about the different types of sampling techniques, which are neutral, ideal and flat-topped sampling. We have also discussed the difference between practical implementations and theoretical implementations.

References

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