



**Faculty of Engineering & Technology**  
**Electrical and Computer Engineering Department**  
**Communication Laboratory - ENEE4113**  
**Prelab Exp4 FM Modulation**

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**Section: 6**

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## Software Prelab:

Consider the frequency modulated signal:

$$s(t) = \cos(2\pi(20k)t + 6\sin(1000\pi t))$$

Build a Simulink model in a MATLAB Simulink that [Take plots in time and frequency domains]:

1. Extract the message signal  $m(t)$  from  $s(t)$ . [by hand solution].

Q1  $s(t) = \cos(2\pi(20k)t + 6\sin(1000\pi t))$

$\Rightarrow s_{FM}(t) = A \cos(2\pi f_c t + B \sin(2\pi f_m t))$

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$A = 1$

$f_c = 20,000$

$B = 6 \rightarrow B = \frac{k_f A_m}{f_m}$  (Assume  $k_f = 300$ )

$f_m = 500$

$6 = \frac{300 A_m}{500} \Rightarrow A_m = \frac{6(500)}{300} = 10$

$\Rightarrow m(t) = 10 \cos(2\pi(500)t)$  #

Fig1: Extract  $m(t)$  from  $s(t)$  by hand solution.

2. Plot 5 cycle from message signal  $m(t)$  and  $s(t)$  versus  $t$ . [by Simulink].

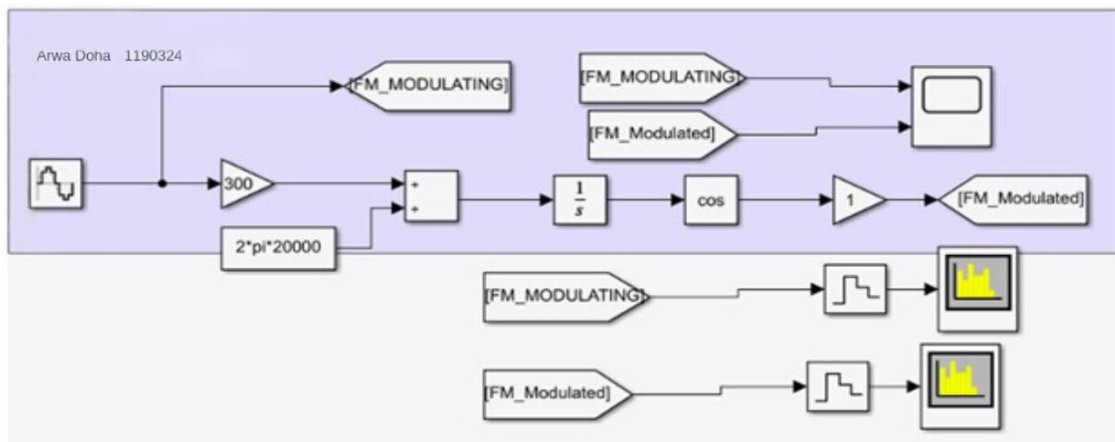


Fig2: Block diagram of 5 cycle from  $m(t)$  and  $s(t)$ .

In the time-domain waveform results for message Signal  $m(t)$  and Modulated Signal  $S(t)$ :

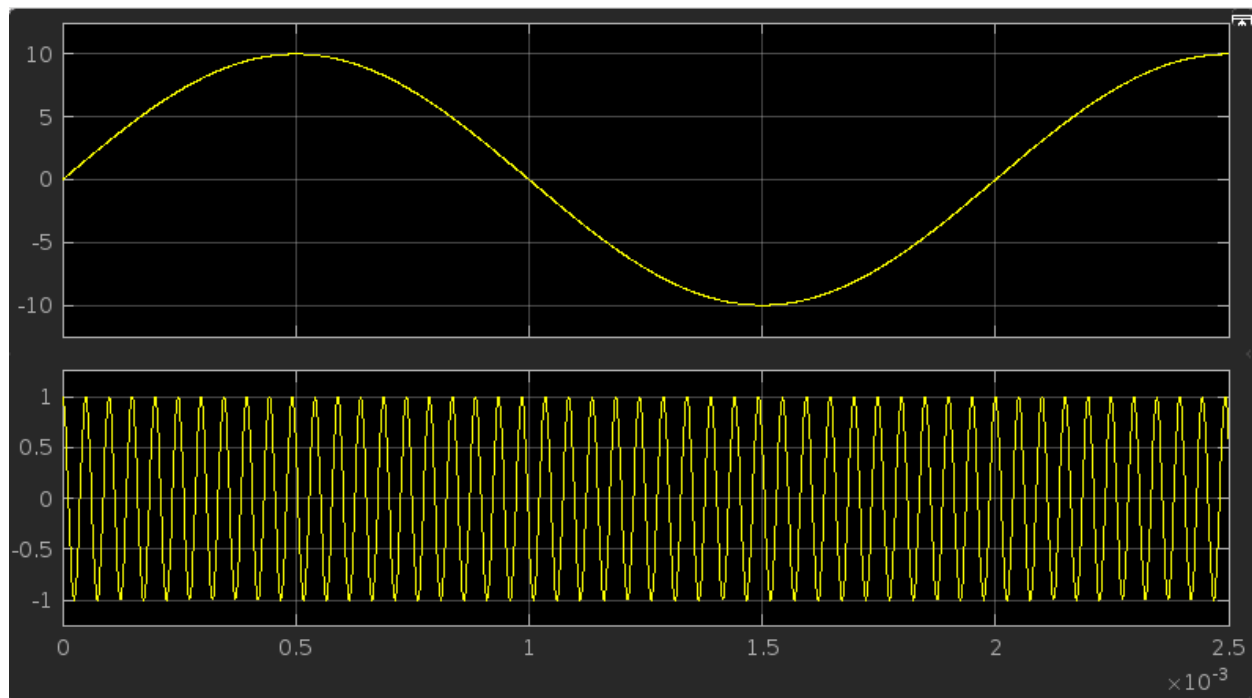


Fig3:  $m(t)$  &  $s(t)$  in time domin

In the freq-domain waveform results for message Signal  $m(t)$  and Modulated Signal  $S(t)$

For 5 cycles, but the high frequency of the modulated signal makes it challenging to discern in this representation.:

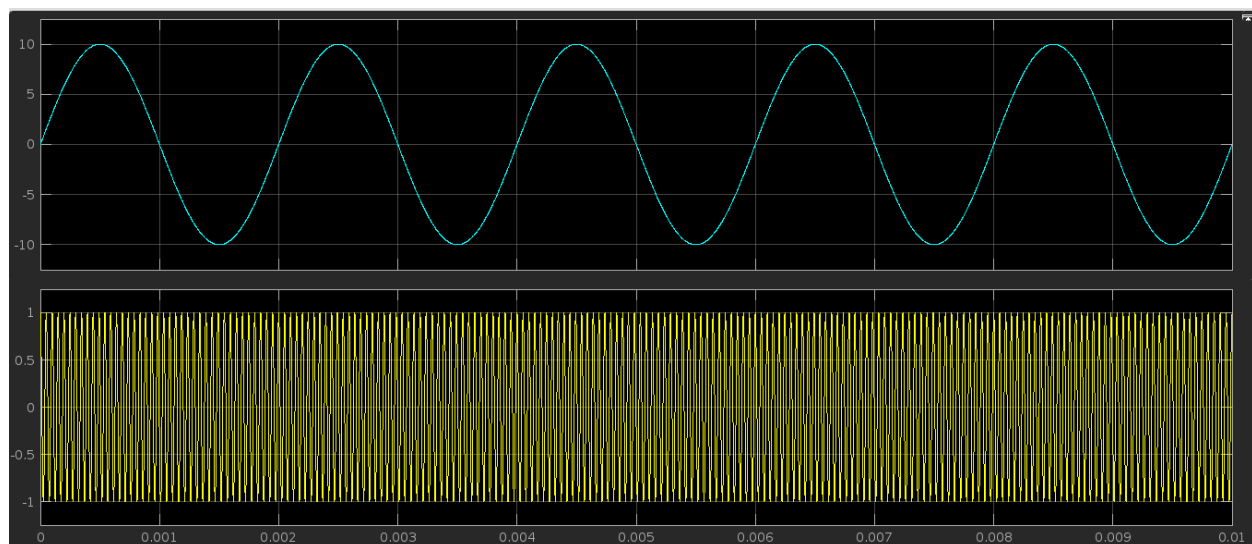


Fig4:  $m(t)$  &  $s(t)$  for 5 cycles in time domin

In the freq-domain waveform results for message Signal:  $M(F) = 5\delta(f-500) + 5\delta(f+500)$

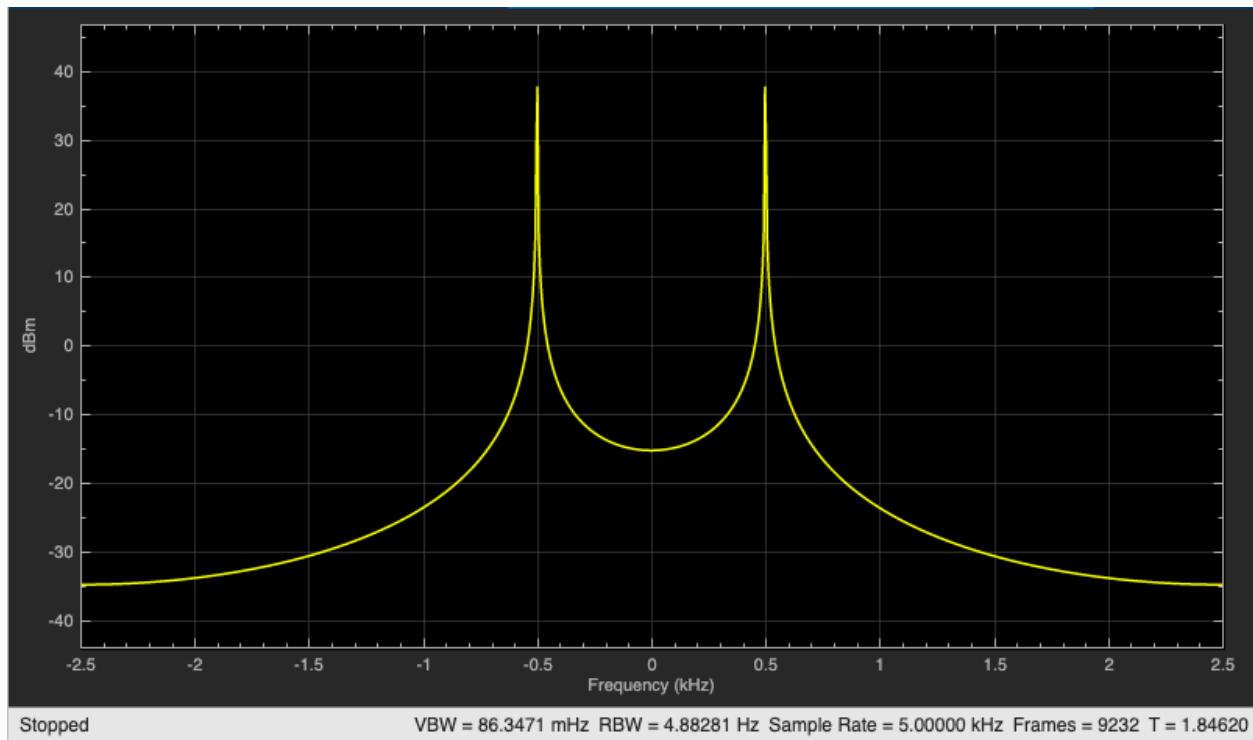


Fig5: Message Signal  $m(t)$  in Frequency Domain

In the freq-domain waveform for Modulated Signal  $S(F)$ :

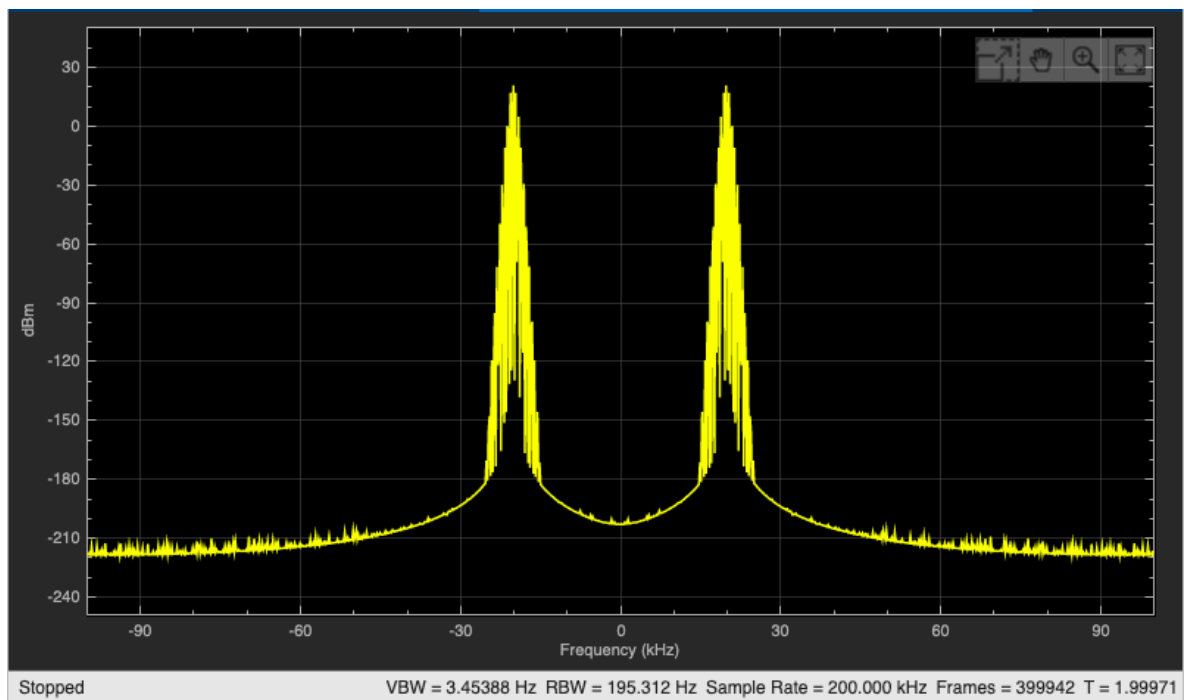


Fig6: Modulated Signal  $S(t)$  in Frequency Domain

3. Differentiate  $s(t)$  with respect to  $t$  and plot  $ds(t)/dt$ . Notice how this operation transforms an FM waveform into an AM waveform. **Write your observation and conclusions.** [by hand then use Simulink to observe your result].

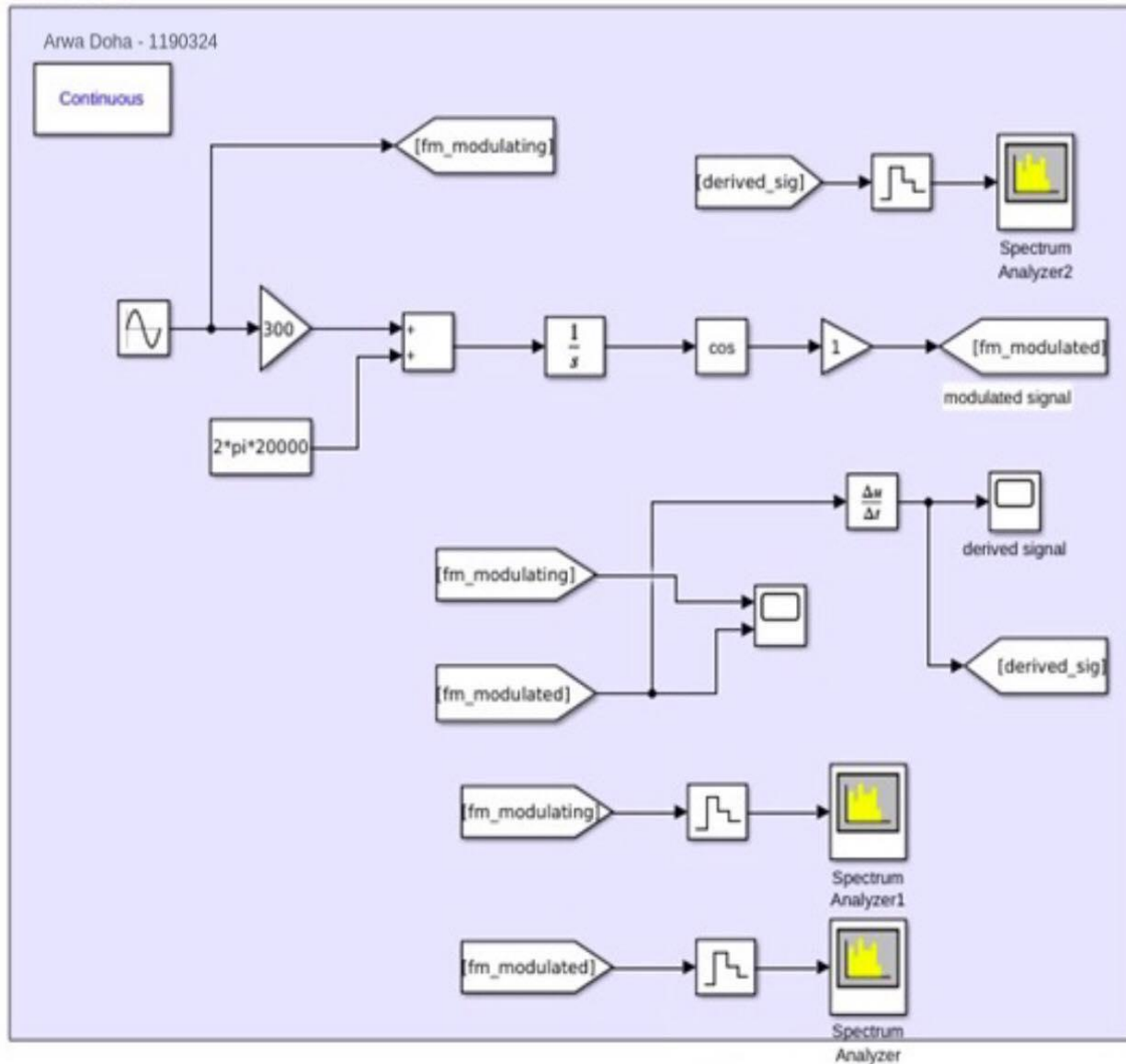


Fig8: Simulink block diagram of "FM to AM Transformation"

In the time-domain waveform for derived  $S(t)$  modulated signal:

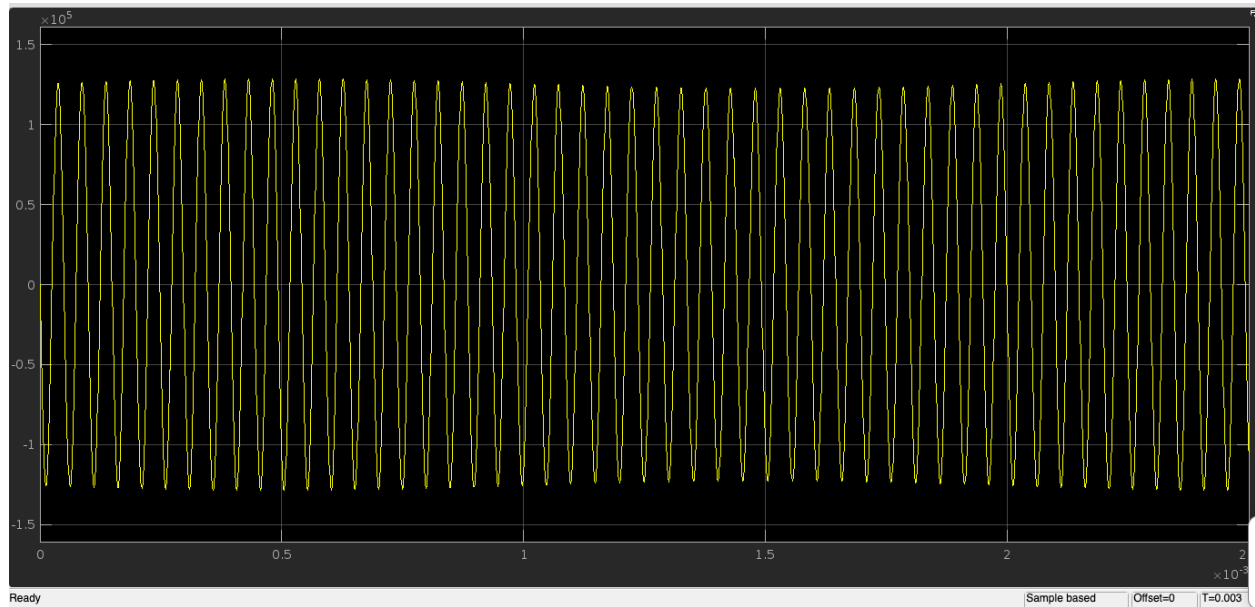


Fig9: Simulink block diagram in time domain of derived  $S(t)$

In the frequency-domain waveform for derived  $S(t)$  modulated signal:

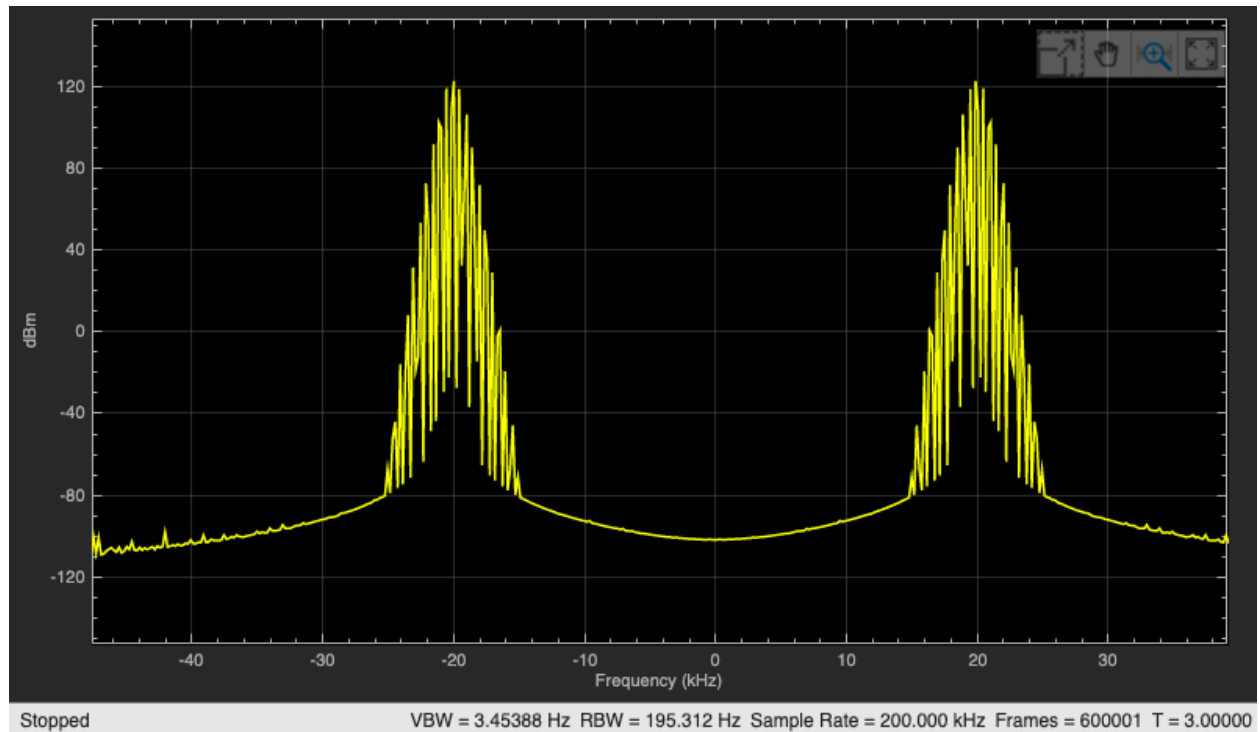


Fig10: Simulink block diagram in freq domain of derived  $S(t)$ .

### Analytical Solution by Hand: Differentiation of S(t)

Q3

$$S(t) = A_c \cos(2\pi f_c t + 2\pi k_f \int m(t) dt)$$

$$S(t) = A_c \cos(\underbrace{2\pi f_c t}_{\omega_c t} + \underbrace{2\pi k_f \int m(t) dt}_{\theta(t)})$$

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$$S(t) = A_c \cos(\omega_c t + \theta(t))$$

$$\frac{\partial S(t)}{\partial t} = -A_c \left( \omega_c + \frac{\partial \theta}{\partial t} \right) \sin(\omega_c t + \theta(t))$$

$$\theta(t) = 2\pi k_f \int m(t) dt \Rightarrow \frac{\partial \theta}{\partial t} = 2\pi k_f m(t)$$

$$\frac{\partial S(t)}{\partial t} = -A_c (\omega_c + 2\pi k_f m(t)) \sin(\omega_c t + \theta(t))$$

$$= A_c \omega_c [1 + 2\pi k_f m(t)] \sin(\omega_c t + \theta(t))$$

This is similar to the Normal AM

where  $S_{AM}(t) = A_c [1 + k_a m(t)] \cos(2\pi f_c t)$

Fig7: Differentiate s(t) by hand solution

### Observation & Result:

As observed in the waveform, when we differentiate S(t) (FM), we obtain a wave that looks like an AM waveform. As observed in the figures previously, deriving S(t) returns a negative sine wave, but if we overlook the negative sign in the calculations, we have a result =

$$A_c \omega_c \left[ 1 + \frac{2\pi k_f m(t)}{\omega_c} \sin(\omega_c t + \theta) \right]$$

Inside In this scenario, we multiply the carrier angular frequency ( $\omega_c$ ) by the carrier amplitude ( $A_c$ ), and within the parentheses, there is an addition of 1 to a sensitivity constant multiplied by the message signal ( $m(t)$ ).

The coefficient in this signal closely resembles that of Amplitude Modulation (AM), expressed as  $A_c [1 + K_a m(t)] \cos(\omega_c t)$ . When the Frequency Modulation (FM) modulation is differentiated with respect to time, it transforms into Amplitude Modulation.



4. Apply  $ds(t)/dt$  to an ideal envelope detector, subtract the dc term and show that the detector's output is linearly proportional to  $m(t)$ . Write your observation and conclusions. [by hand solution].

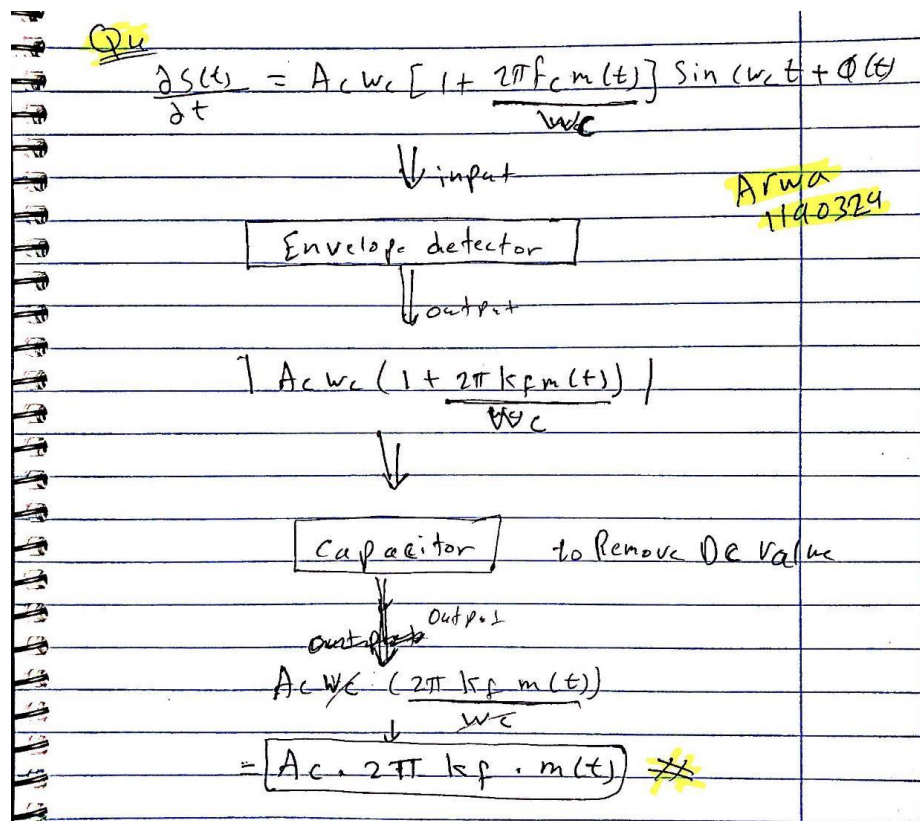


Fig11: Apply  $ds(t)/dt$  to an ideal envelope detector

## Observation & Result:

Applying the derivative of  $S(t)$  to an envelope detector yields an output representing the amplitude of the sine function, given by:

$$A_c w_c \left[ 1 + \frac{2\pi k_f m(t)}{w_c} \right]$$

When graphed, this results in a cosine wave elevated by the DC value  $A_c \cdot w_c$ . Subsequently passing this signal through a capacitor eliminates the DC component, resulting in an output of  $[A_c \cdot 2\pi \cdot k_f \cdot m(t)]$

Notably, this output is directly proportional to the message signal, with the amplitude of the message signal multiplied by  $[A_c \cdot 2\pi \cdot k_f]$ . Consequently, through this demodulation technique utilizing an envelope detector, the original message signal can be successfully recovered.



5. Extract message signal by using phase-locked loop (PLL).

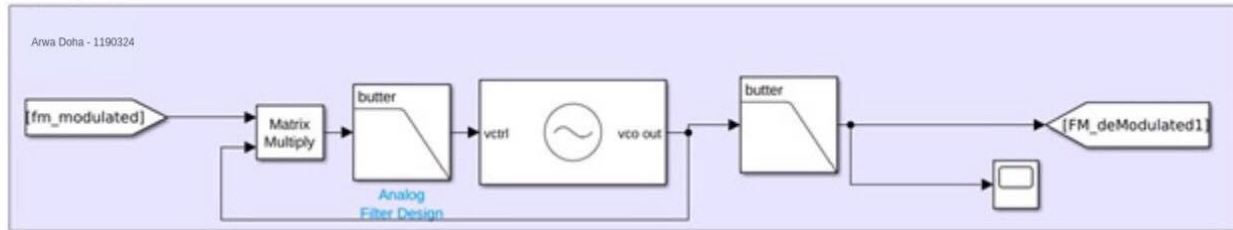


Fig12: Simulink block diagram of  $m(t)$  by using (PLL)

6. Extract the message signal by using the envelop detector.

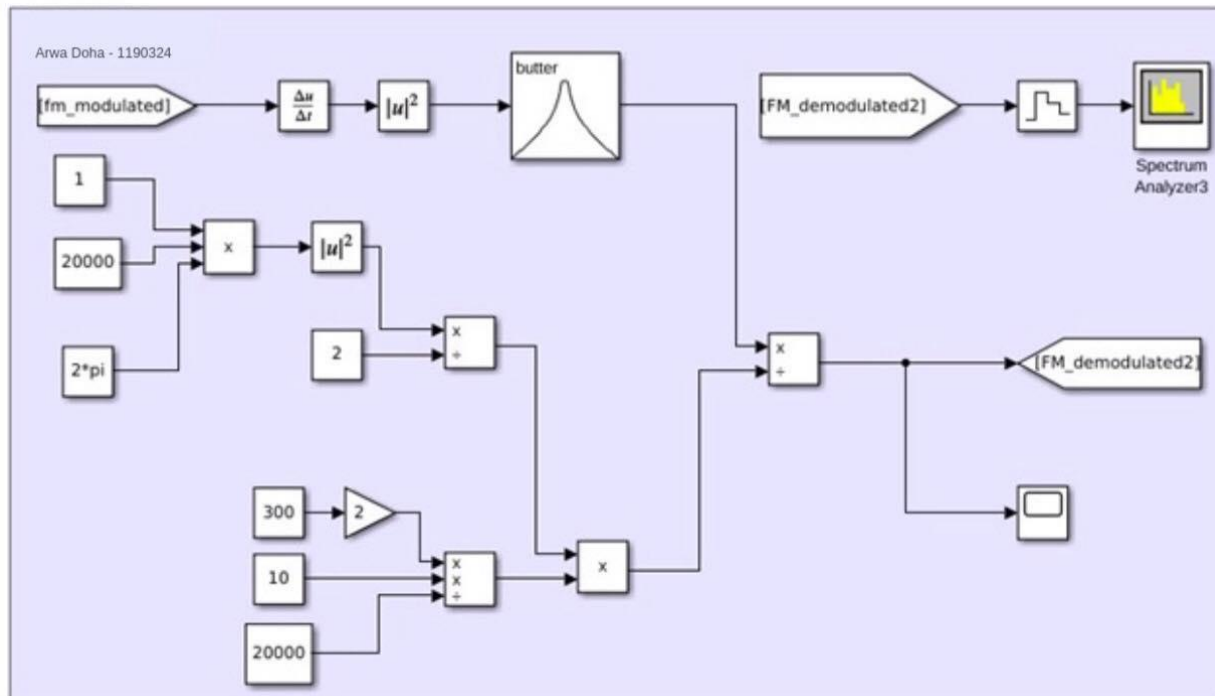
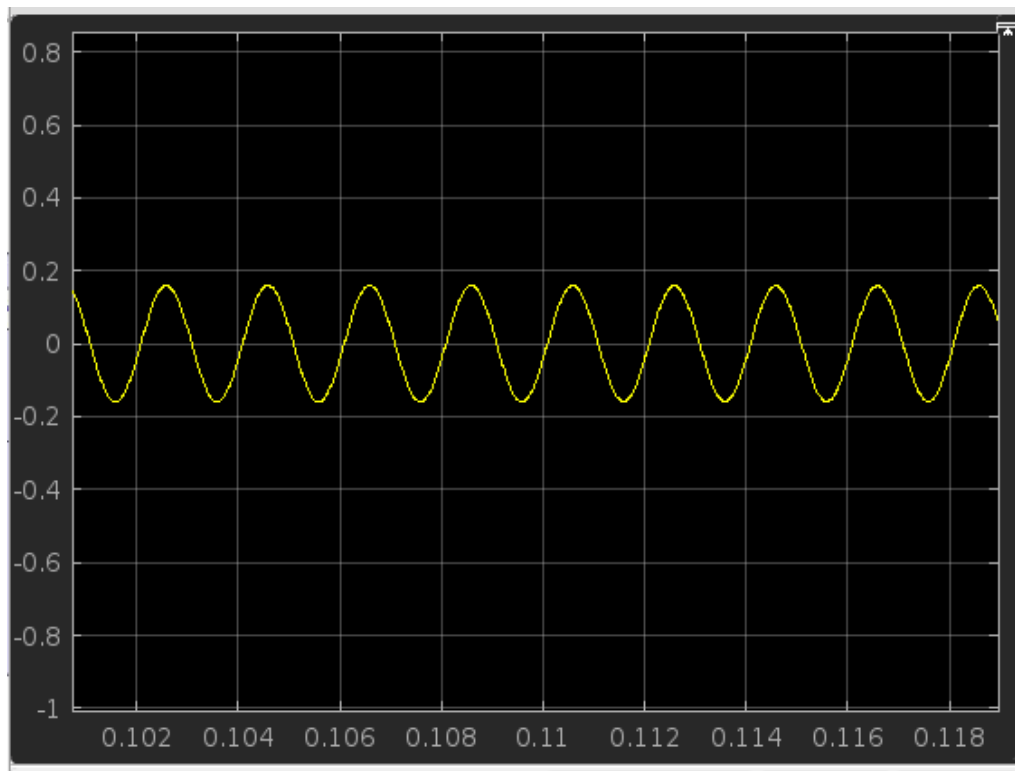


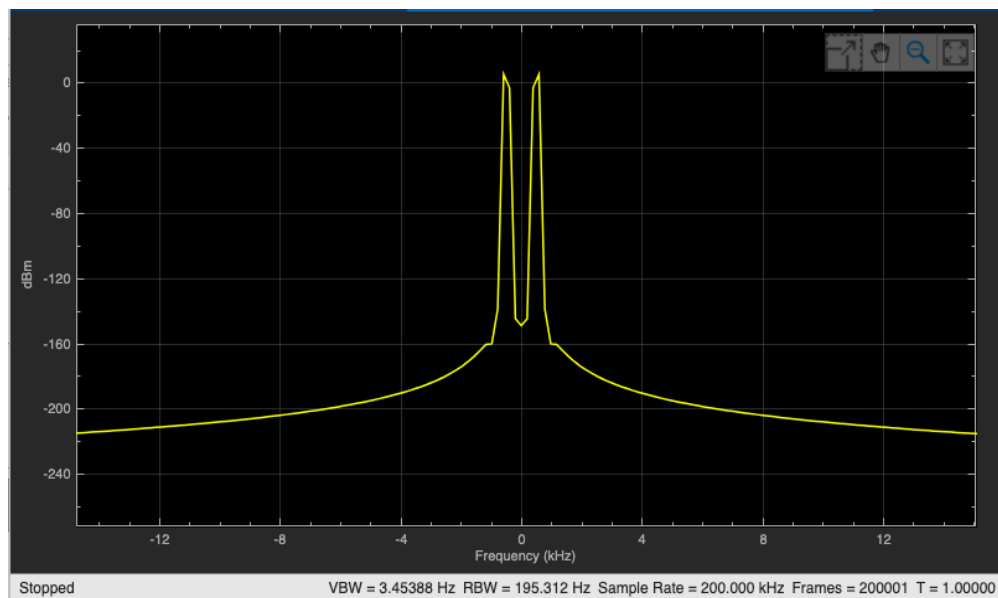
Fig13: Simulink block diagram of  $m(t)$  by envelop detector

Demodulated Signal in Time Domain (zoomed in when signal is stable)



*Fig13: Demodulated Signal in Time Domain*

Demodulated Signal in Frequency Domain (fm=500hz)



*Fig14: Demodulated Signal in Frequency Domain.*