1 The Photon

1.1 constants

		$c = 2.998 \cdot 10^8 \left\lfloor \frac{\mathrm{m}}{\mathrm{s}} \right\rfloor$
$C\left[\frac{\mathrm{m}}{\mathrm{s}}\right]$	speed of light	$h = 6.626 \cdot 10^{-34} \left[\frac{\mathrm{m}^2 \mathrm{kg}}{\mathrm{s}} \right]$
$h\left[\frac{\mathrm{m}^2\mathrm{kg}}{\mathrm{s}}\right]$	planc's constant	$\hbar=rac{h}{2\pi}$
e [C]	electorn charge	211
m_e [kg]	electron mass	$e = 1.602 \cdot 10^{-19} \text{ [C]}$
$k_B \left[\frac{\mathrm{m}^2 \mathrm{kg}}{\mathrm{s}^2 \mathrm{K}} \right]$	bolzmann constant	$m_e = 9.109 \cdot 10^{-31} \text{ [kg]}$
$\epsilon_0 \left[\frac{\mathrm{F}}{\mathrm{m}} \right]$	vacuum permittivity	$k_B = 1.381 \cdot 10^{-23} \left[\frac{\text{m}^2 \text{ kg}}{\text{s}^2 \text{ K}} \right]$
λ [m]	Wavelength	9 954 10-12 [F]
$\nu \left[\frac{1}{s}\right]$	Frequency	$\epsilon_0 = 8.854 \cdot 10^{-12} \left[\frac{\mathrm{F}}{\mathrm{m}} \right]$
$\omega \left[\frac{\mathrm{rad}}{\mathrm{s}} \right]$	Radial frequency	$1 \text{ [eV]} = 1.602 \cdot 10^{-19} \text{ [J]}$
E [J]	Energy	$\lambda = \frac{c}{\nu}$ $\nu = \frac{c}{\lambda}$ $\omega = 2\pi\nu$
		$E = h \cdot \nu$

1.2 Photoelectric effect

V [V]	Voltage	
ϕ_0 [eV]	Work function	$h\nu - \phi_0 = \frac{1}{2}mv^2 = eV$
I [A]	Photo-current	2
$n \left[\text{m}^{-3} \right]$	Volume density of electrons	$V(\nu) = \frac{h}{e}\nu - \frac{\phi_0}{e}$
$A \left[m^2 \right]$	Area	I = nAve
$v\left[\frac{\mathrm{m}}{\mathrm{s}}\right]$	velocity of electrons	

1.3 Blackbody Radiation

$$L$$
 [m] length of blackbody cube k_i wave constants E_x Electric field in x-direction $\langle E \rangle$ Average Energy N Number of states D Density of states U Blackbody radiation U Power radiated

$$E_x(x,y,z) = E_{0x}\cos(k_x x)\sin(k_y y)\sin(k_z z)$$

$$k_x = n\frac{\pi}{L} \quad k_y = m\frac{\pi}{L} \quad k_z = l\frac{\pi}{L} \quad k = \sqrt{k_x^2 + k_y^2 + k_z^2}$$

$$N(k) = \frac{1}{3\pi^2}k^3L^3 \quad D(k) = \frac{k^2}{\pi^2}$$

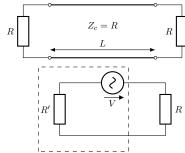
$$u(\omega) = \frac{\omega^2}{\pi^2c^3} \cdot \frac{\hbar\omega}{\exp\left(\frac{-\hbar\omega}{kT}\right) - 1}d\omega \quad u(\nu) = \frac{8\pi\hbar\nu^3}{c^3\left(\exp\left(\frac{\hbar\nu}{kT}\right) - 1\right)}d\nu$$

$$I(\omega) = c \cdot u(\omega)$$

Equipartition-Theorem: Each degree of Freedom has an energy of kT

1.4 Johnson-Noise

This is the noise created in a one-dimensional circuit (like a coax-cable).



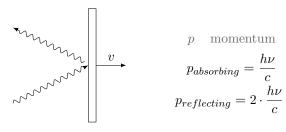
 $\langle V^2 \rangle$ Noise Voltage

Bandwidth

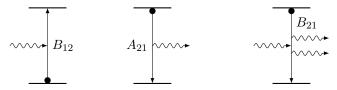
 $E = E_0 \cdot \sin(k_x \cdot x)$

 $\langle V^2 \rangle = 4R \cdot k_B T \cdot \Delta \nu$

1.5 Momentum of a photon



1.6 Absorption, spontaneous and stimulated emission



absorbtion spontaneous emission stimulated emission

 n_1 Number of electrons in the lower energy state

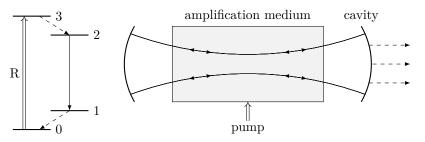
 n_2 Number of electrons in the higher energy state

$$\frac{dn_2}{dt} = \underbrace{n_1 \cdot u(\nu) \cdot B_{12}}_{\text{absorbtion}} - \underbrace{n_2 \cdot u(\nu) \cdot B_{21}}_{\text{stimulated emission}} - \underbrace{n_2 \cdot A_{21}}_{\text{spontaneous emission}}$$

$$\frac{n_2}{n_1} = e^{-\frac{h\nu}{k_BT}} = \frac{u(\nu)B_{12}}{u(\nu)B_{21} + A_{21}}$$

$$B_{21} = B_{12} = B \qquad A_{21} = \frac{8\pi h\nu^3}{c^3}$$

1.7 Laser-optical amplification



Electrons are excited from the ground state "0" to the level "3" by pumping through incoherent radiation. The electrons then fall onto a long-lived state n_2 (State "2") from level "3". The pumping can be done either optically by shining a strong incoherent light or by passing a current. It is also assumed that the lower state is quickly emptied by a fast process with lifetime τ_1 . As a result, the population in state "2" is:

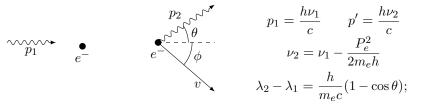
$$n_2 = \frac{R}{A_{21}}$$
 whereas $n_1 \approx 0$ because $A_{21} < \frac{1}{\tau_1}$

We have rherefore a population inversion between the two states. The likelihood of a stimulated emission process is larger than the one of absorbtion. If we enclose the system in an optical cavity, we can achieve self-sustained oscillation at the frequency ν .

2 Wave mechanics

	frequency	wavelength	momentum	energy
Particle		$\lambda_b = \frac{h}{p}$	p = mv	$E = \frac{1}{2}mv^2$
Wave	ω	$\lambda = \frac{2\pi c}{\omega}$	$p = \frac{\hbar\omega}{c}$	$E=\hbar\omega$

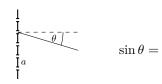
Compton Scattering



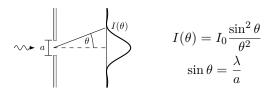
$$p_1 = \frac{h\nu_1}{c} \qquad p' = \frac{h\nu_2}{c}$$

$$\nu_2 = \nu_1 - \frac{P_e^2}{2m_e h}$$

2.2 Bragg diffraction



Single slit



Bohr-Sommerfeld equalization

Every single particle must satisfy the following equation. The quantized energy levels below relate to the hydrogen atom

$$\int_{length} p \cdot ds = n \cdot h \qquad n \in \mathbb{N}$$

$$p \qquad \text{Momentum of particle}$$

$$E_n \qquad \text{Energy of the nth state}$$

$$E_{ry} \qquad \text{Constant (energy)}$$

$$a_0 \qquad \text{Constant (Bohr-radius)}$$

$$F_{ry} = 13.6 \text{ [eV]}$$

$$a_0 = 5.292 \cdot 10^{-11} \text{ [m]}$$

Quantum Mechanics

Wave function

$$\psi(\vec{r},t) : \mathbb{R}^4 \to \mathbb{C} \qquad \iiint |\psi(\vec{r},t)|^2 d^3r = 1$$

 $\psi(\vec{r},t) = a\psi_1(\vec{r},t) + b\psi_2(\vec{r},t), \qquad |a|^2 + |b|^2 = 1$

The Schrödinger equation

$$V(x,t)$$
 potential m mass $\psi(x,t)$ 1-dimensional wave function

$$i\hbar \cdot \frac{\partial \psi(x,t)}{\partial t} = -\frac{\hbar^2}{2m} \cdot \frac{\partial^2 \psi(x,t)}{\partial x^2} + V(x,t)\psi(x,t)$$