

EXAMPLE 1

AGE	INCOME	STUDENT	CREDIT_RATING	BUYS_COMPUTER
<=30	High	No	Fair	No
<=30	High	No	Excellent	No
31...40	High	No	Fair	Yes
>40	Medium	No	Fair	Yes
>40	Low	Yes	Fair	Yes
>40	Low	Yes	Excellent	No
31...40	Low	Yes	Excellent	Yes
<=30	Medium	No	Fair	No
<=30	Low	Yes	Fair	Yes
>40	Medium	Yes	Fair	Yes
<=30	Medium	Yes	Excellent	Yes
31...40	Medium	No	Excellent	Yes
31...40	High	Yes	Fair	Yes
>40	Medium	No	Excellent	No

C1 : buys_computer = "yes"

C2 : buys_computer = "no"

Data sample X = (age ≤ 30, Income = medium, Student = yes Credit_rating = Fair)

A data sample is given to us here and we have to find whether the person buys a computer or no using Naive Bayesian classification. So first we calculate the probability of buys_computer. So the numbers of yes values divided upon total records that is 14 gives us the probability of buys_computer with yes and same with no.

$P(C_i) : P(\text{buys_computer} = \text{"yes"}) = 9/14 = 0.643$

$P(\text{buys_computer} = \text{"no"}) = 5/14 = 0.357$

The total number of records in the table are 14.

Compute $P(X|C_i)$ for each class

$$P(\text{age} = "<=30" \mid \text{buys_computer} = \text{"yes"}) = 2/9 = 0.222$$

$$P(\text{age} = "<= 30" \mid \text{buys_computer} = \text{"no"}) = 3/5 = 0.6$$

$$P(\text{income} = \text{"medium"} \mid \text{buys_computer} = \text{"yes"}) = 4/9 = 0.444$$
$$P(\text{income} = \text{"medium"} \mid \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$$

$$P(\text{student} = \text{"yes"} \mid \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$$

$$P(\text{student} = \text{"no"} \mid \text{buys_computer} = \text{"no"}) = 1/5 = 0.2$$

$$P(\text{credit_rating} = \text{"fair"} \mid \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$$
$$P(\text{credit_rating} = \text{"fair"} \mid \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$$

Multiplying all the probabilities with yes values and no values from above separately.

$P(X|C_i)$:

$$\begin{aligned} P(X|\text{buys_computer} = \text{"yes"}) \\ &= 0.222 \times 0.444 \times 0.667 \times 0.667 \\ &= 0.044 \end{aligned}$$

$$\begin{aligned} P(X|\text{buys_computer} = \text{"no"}) \\ &= 0.6 \times 0.4 \times 0.2 \times 0.4 \\ &= 0.019 \end{aligned}$$

Now, multiply these probabilities with the above calculated $P(C_i)$

$P(X|C_i) \cdot P(C_i)$:

$$\begin{aligned} P(X|\text{buys_computer} = \text{"yes"}) \cdot P(\text{buys_computer} = \text{"yes"}) &= \\ 0.044 \times 0.643 &= 0.028 \end{aligned}$$

$$\begin{aligned} P(X|\text{buys_computer} = \text{"no"}) \cdot P(\text{buys_computer} = \text{"no"}) &= \\ 0.019 \times 0.357 &= 0.007 \end{aligned}$$

The maximum value is 0.028.

Therefore, X belongs to class ("buys_computer = yes")