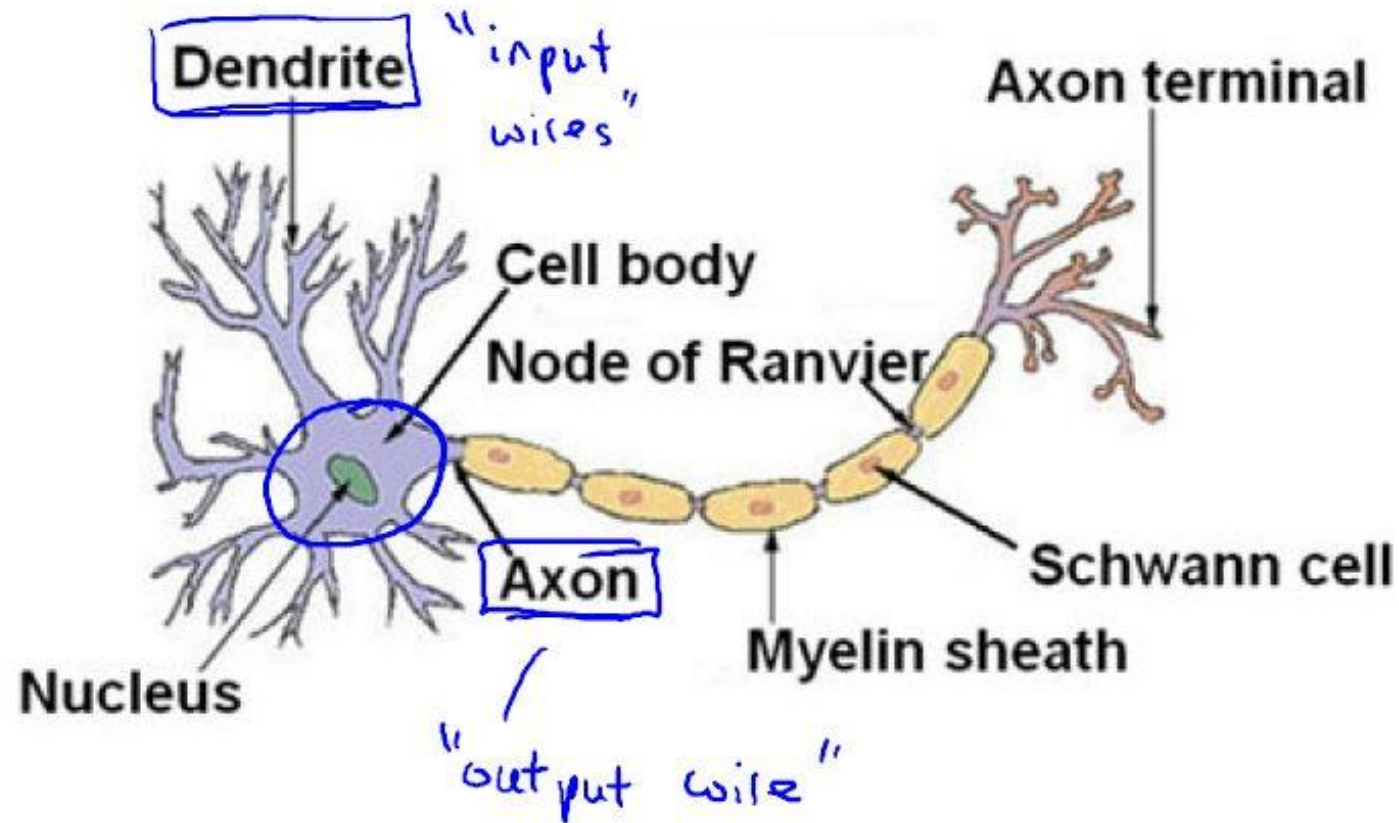
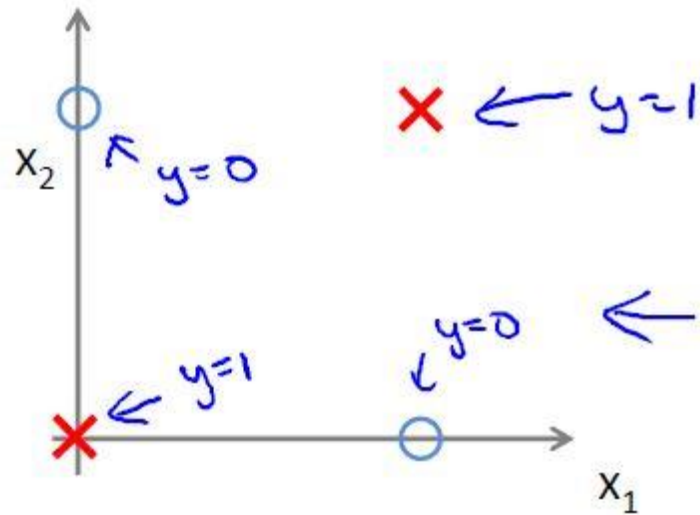


Neuron in the brain



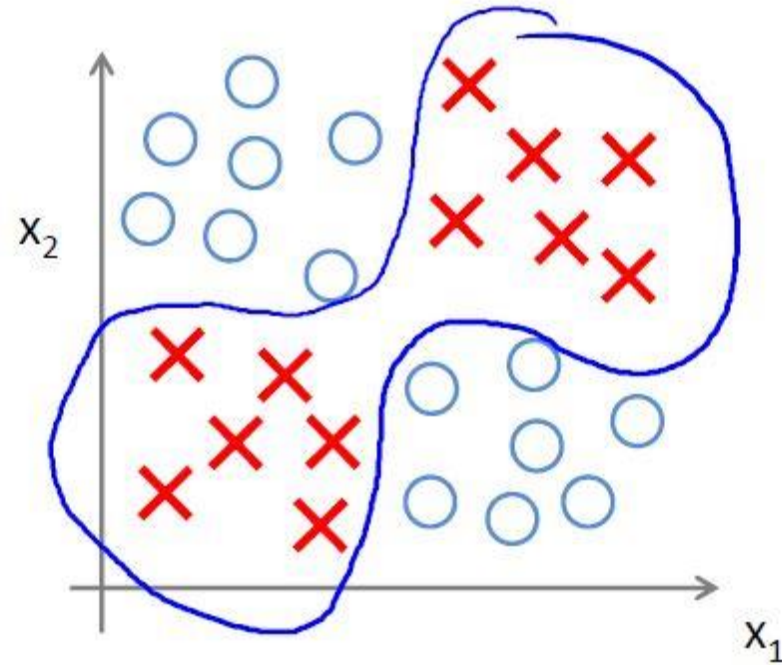
Non-linear classification example: XOR/XNOR

→ x_1, x_2 are binary (0 or 1).



$$y = \underline{x_1 \text{ XOR } x_2}$$

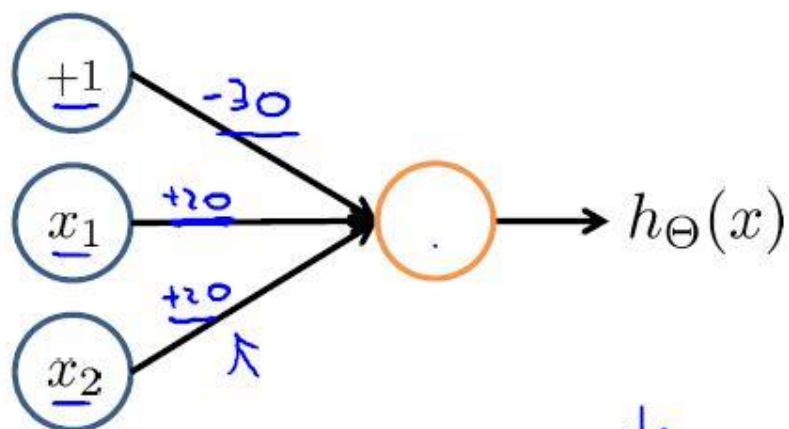
$$\begin{aligned} &\rightarrow \underline{x_1 \text{ XNOR } x_2} \leftarrow \\ &\rightarrow \underline{\text{NOT } (x_1 \text{ XOR } x_2)} \end{aligned}$$



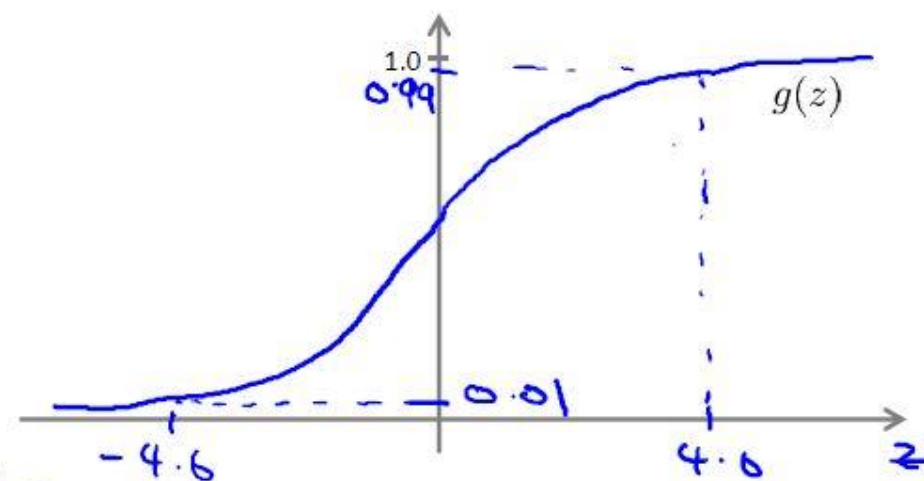
Simple example: AND

→ $x_1, x_2 \in \{0, 1\}$

→ $y = x_1 \text{ AND } x_2$



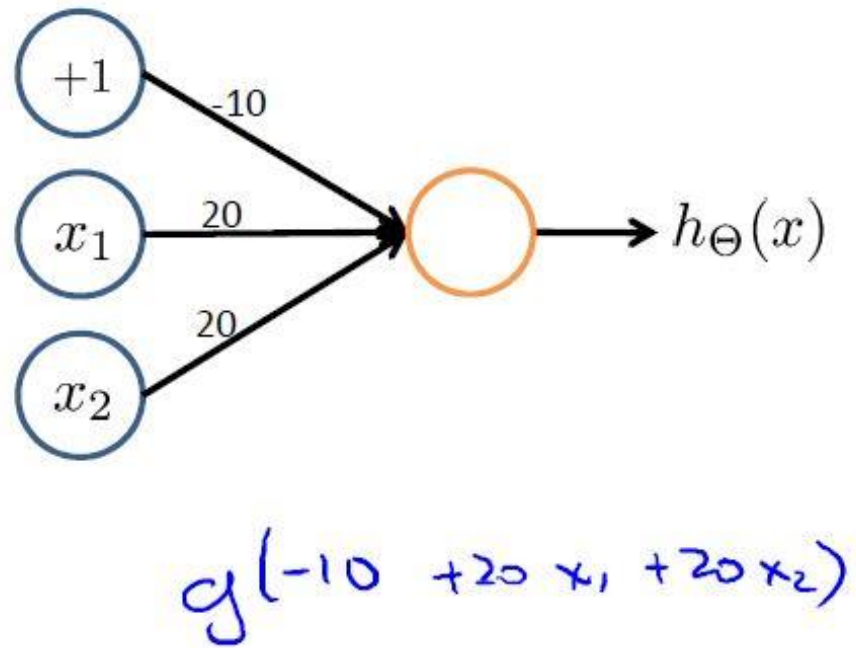
$$\rightarrow h_{\Theta}(x) = g\left(\underbrace{-30}_{\Theta_{1,0}^{(1)}} + \underbrace{20}_{\Theta_{1,1}^{(1)}}x_1 + \underbrace{20}_{\Theta_{1,2}^{(1)}}x_2\right)$$



x_1	x_2	$h_{\Theta}(x)$
0	0	$g(-30) \approx 0$
→ 0	1	$g(-10) \approx 0$
1	0	$g(-10) \approx 0$
→ 1	1	$g(10) \approx 1$

$h_{\Theta}(x) \approx x_1 \text{ AND } x_2$

Example: OR function



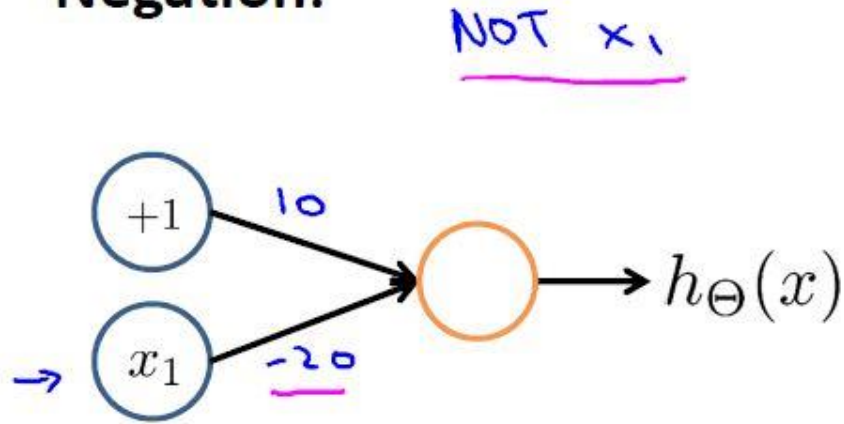
x_1	x_2	$h_{\Theta}(x)$
0	0	$g(-10) \approx 0$
0	1	$g(10) \approx 1$
1	0	≈ 1
1	1	≈ 1

$\rightarrow x_1$ AND x_2

$\rightarrow x_1$ OR x_2

$\{0,1\}$

Negation:

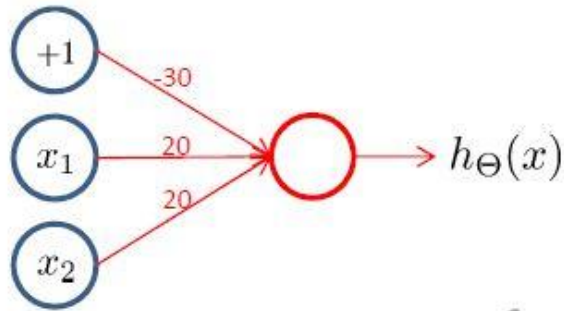
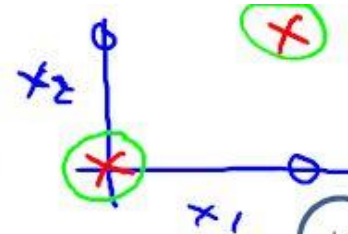


x_1	$h_{\Theta}(x)$
0	$g(10) \approx 1$
1	$g(-10) \approx 0$

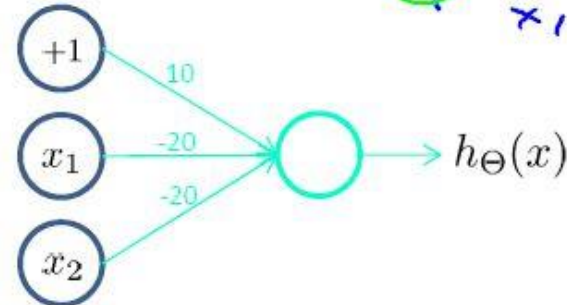
$$h_{\Theta}(x) = g(\underline{10 - 20x_1})$$

\rightarrow (NOT x_1) AND (NOT x_2)
(=1 if and only if
 $\rightarrow x_1 = x_2 = 0$)

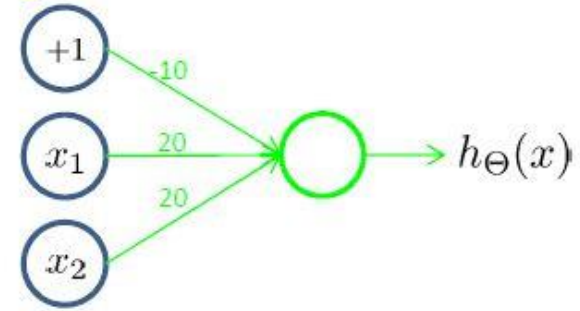
Putting it together: x_1 XNOR x_2



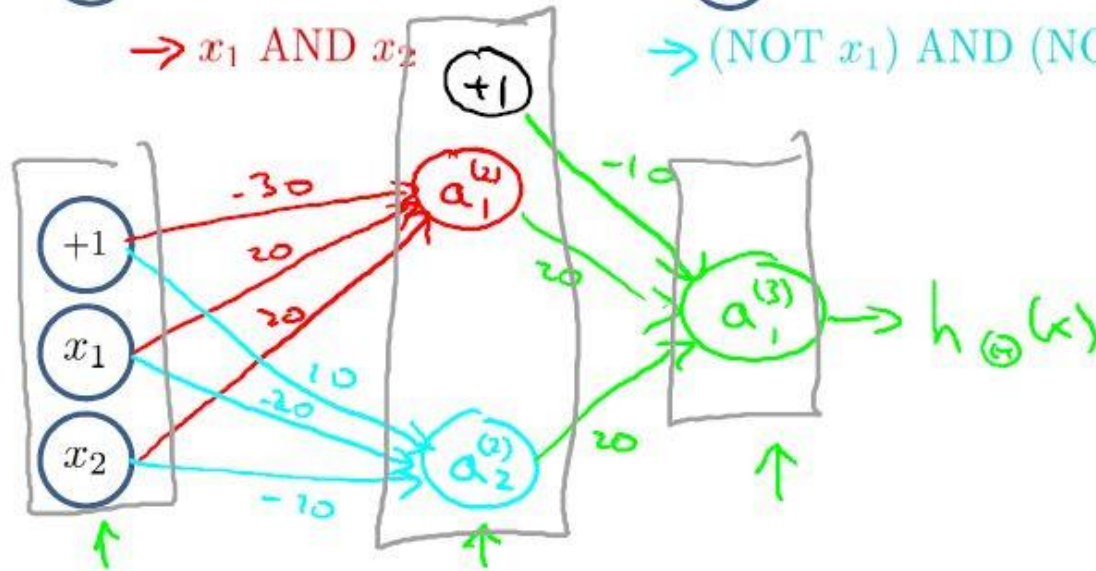
$\rightarrow x_1$ AND x_2



$\rightarrow (\text{NOT } x_1) \text{ AND } (\text{NOT } x_2)$

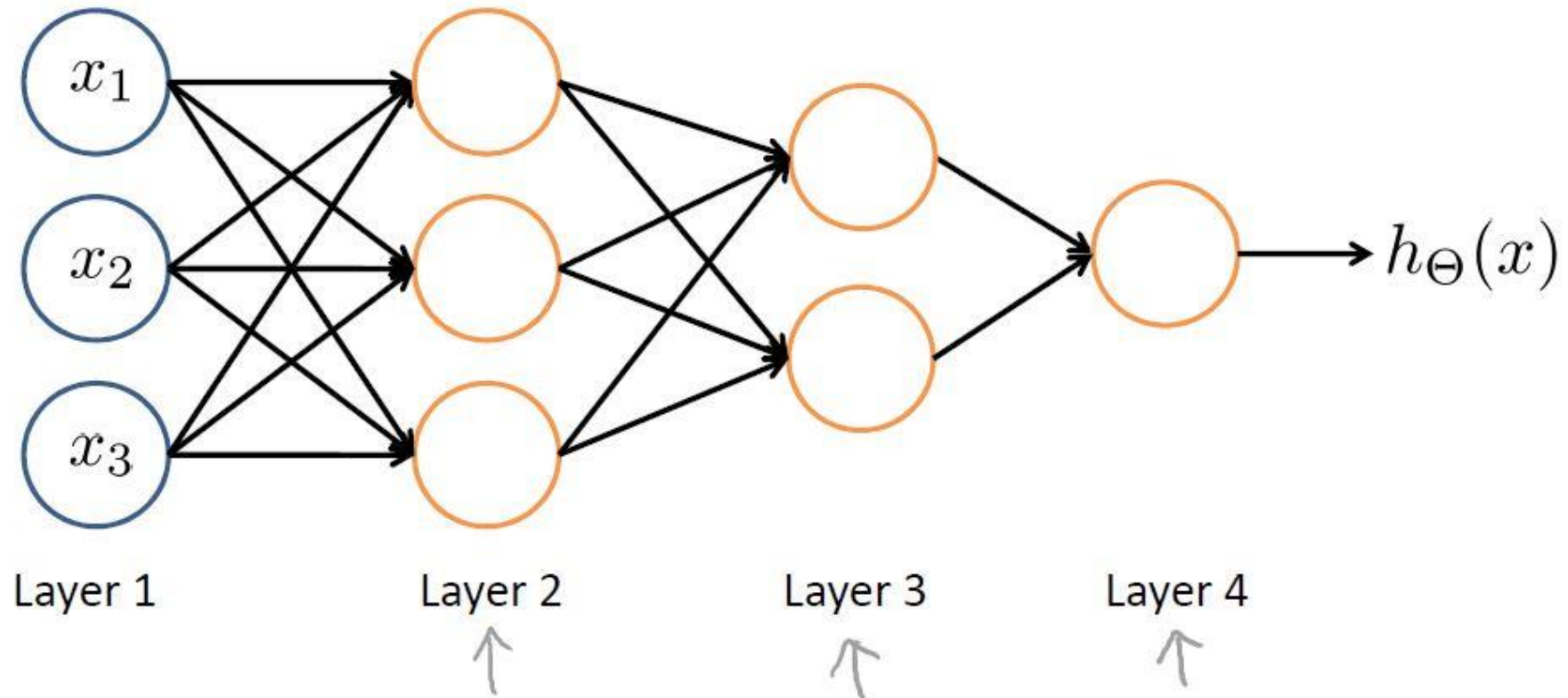


$\rightarrow x_1$ OR x_2



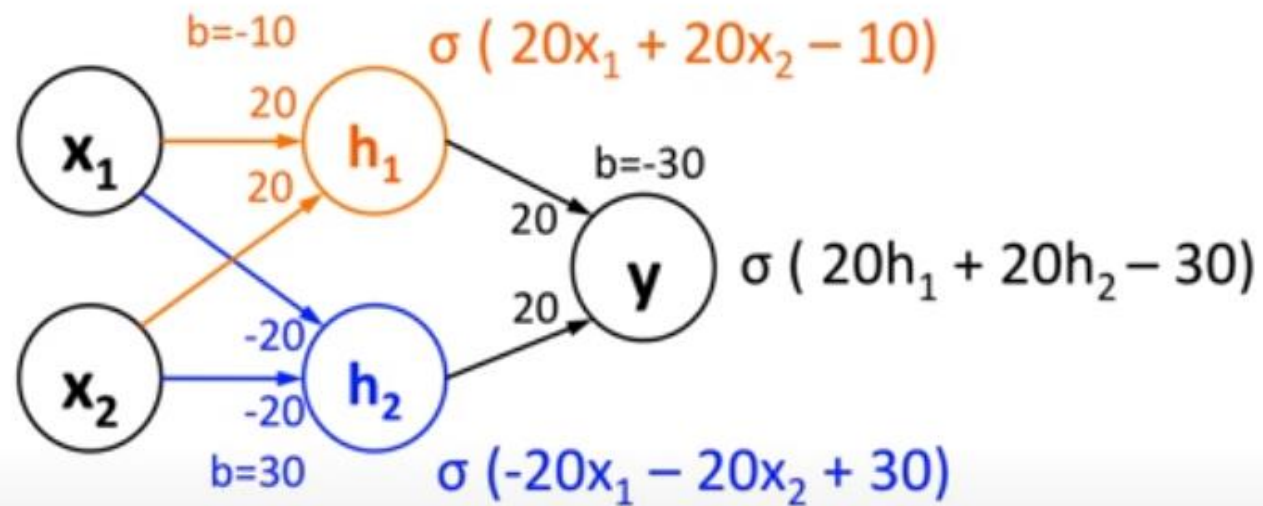
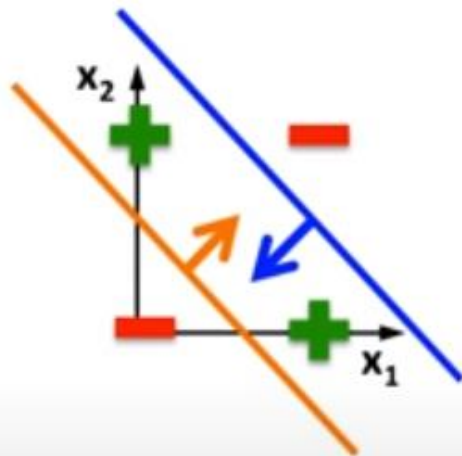
x_1	x_2	$a_1^{(2)}$	$a_2^{(2)}$	$h_{\Theta}(x)$
$\rightarrow 0$	0	0	1	1 \leftarrow
0	1	0	0	0
1	0	0	0	0
$\rightarrow 1$	1	1	0	1 \leftarrow

Neural Network intuition



Solving XOR with a Neural Net

Linear classifiers
cannot solve this



$$\sigma(20 \cdot 0 + 20 \cdot 0 - 10) \approx 0$$

$$\sigma(20 \cdot 1 + 20 \cdot 1 - 10) \approx 1$$

$$\sigma(20 \cdot 0 + 20 \cdot 1 - 10) \approx 1$$

$$\sigma(20 \cdot 1 + 20 \cdot 0 - 10) \approx 1$$

$$\sigma(-20 \cdot 0 - 20 \cdot 0 + 30) \approx 1$$

$$\sigma(-20 \cdot 1 - 20 \cdot 1 + 30) \approx 0$$

$$\sigma(-20 \cdot 0 - 20 \cdot 1 + 30) \approx 1$$

$$\sigma(-20 \cdot 1 - 20 \cdot 0 + 30) \approx 1$$

$$\sigma(20 \cdot 0 + 20 \cdot 1 - 30) \approx 0$$

$$\sigma(20 \cdot 1 + 20 \cdot 0 - 30) \approx 0$$

$$\sigma(20 \cdot 1 + 20 \cdot 1 - 30) \approx 1$$

$$\sigma(20 \cdot 1 + 20 \cdot 1 - 30) \approx 1$$