

Merge Sort :

- Merge sort is a divide and conquer algorithm, it divides the given array into equal parts and then merges the 2 sorted parts.
- There are two functions:
 1. `merge()` : This function merges two halves of the array, assuming both parts are sorted.
 2. `mergeSort()` : This function divides the array into 2 parts ($low \rightarrow mid$, $mid+1 \rightarrow high$)

// Algorithm & Pseudocode :

• Algorithm :

function 1 : `mergeSort(arr[], low, high)` :

- first divide the array into two parts, divide the array's range into two halves.

eg: range $\rightarrow 0$ to 4 ,
first half = $\frac{0+4}{2} = 0 \rightarrow 2$

second half = $3 \rightarrow 4$

// range : $low \rightarrow high$: $mid = (low+high)/2$
1st half : $low \rightarrow mid$
2nd half : $mid+1 \rightarrow high$

- divide the array by making recursive call:
 - \rightarrow `mergeSort(arr, low, mid)` // 1st half
 - \rightarrow `mergeSort(arr, mid+1, high)` // 2nd half.

- base case: if ($low \geq high$) return;

// Pseudocode:

```
mergeSort(arr[], low, high) {  
    if (low >= high)           // base case  
        return;  
    int mid = (low + high) / 2; // find mid  
  
    mergeSort(arr, low, mid);  // left half  
    mergeSort(arr, mid + 1, high); // right half  
  
    merge(arr, low, mid, high);  
}
```

• merge(arr[], low, mid, high):

- use a temp array to store the elements of the two sorted array after merging.
- use two pointers : one at low
(left)
other at mid + 1.
(right)
- using while loop ($\text{left} \leq \text{mid} \ \&\& \ \text{right} \leq \text{high}$), select the minimum from the left & right element and insert it in temp array.
- left-out elements will be copied as it is.
- transfer elements from temp to range low to high, in original array.

```
merge(arr, low, mid, high) {  
    temp[];  
    left = low;  
    right = mid + 1;  
    while (left <= mid && right <= high) {
```

```
while (left <= mid && right <= high) {  
    if (arr[left] < arr[right]) {  
        temp.add(arr[left]);  
    }
```

```

    left++;
}
else {
    temp.add(arr[right]);
    right++;
}
}

while (left <= mid) {
    temp.add(arr[left]);
    left++;
}

while (right <= high) {
    temp.add(arr[right]);
    right++;
}

for (i = low → high) {
    arr[i] = temp[i - low];
}
}

```

<p>time complexity : $O(n \log n)$</p> <p>space complexity : $O(n)$</p>
