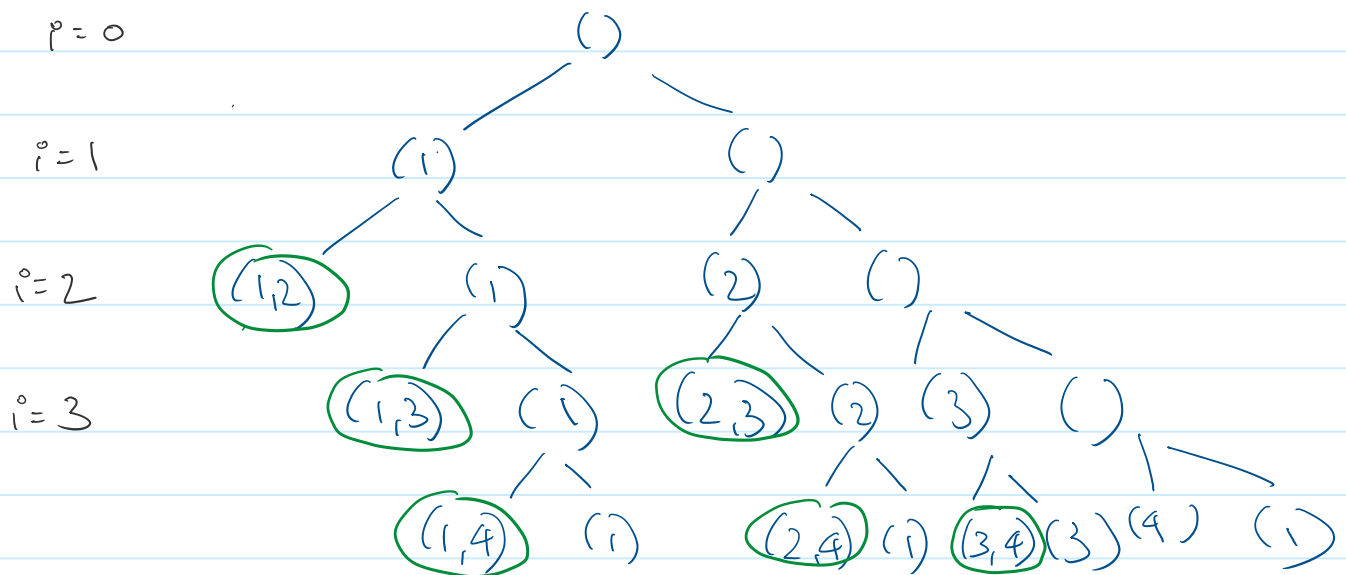


77. Combinations

- Given two integers, n and k , return all possible combinations of ' k ' numbers out of range $[1, n]$.

$n=4, k=2$ $[1, 2, 3, 4]$
 $[[1, 2], [1, 3], [1, 4], [2, 3], [2, 4], [3, 4]]$

// Brute force



Six combinations, max height of tree = k

Base: if ($i > n$) return
if ($k == 0$) ans.push();

- // Steps: - select a element i.e first element, at every position you have two options, either include in subset or ignore it.
- make recursive calls to find the combinations, as demonstrated in decision tree.

// Pseudocode :

```
helper(i, n, k, subset[], ans[]) {  
    if (i > n) {  
        if (k == 0) ans.push(subset);  
        return;  
    }  
    // base case
```

```
    subset.push(i); // include ith ele;  
    help(i+1, n, k-1, subset, ans);
```

```
    subset.pop(); // skip ith ele;  
    help(i+1, n, k, subset, ans);  
}
```

```
combinations(n, k) {  
    subset[];
```

T.C = Exponential

```
    ans[];
```

```
    help(1, n, k, subset, ans);  
    return ans;
```

S.C = Stack space + subset + ans

// Slight improvement:

- modify base case:

```
if (k == 0) ans.push(subset);  
return;
```

```
if (i > n) return;
```

```
if (k > n - i + 1) return;
```

#289. Game of life

- Given an board of size $m \times n$, each cell has a state

1 : live

0 : dead

1: will live if there are 2 or 3 live neighbours
else die.

0: with 3 live neighbours live
else die

// Brute force (using extra space)

- make a dummy matrix,
- start iterating the board, for each cell, check the all eight directions, and update the cell according to the conditions in the dummy matrix.
- after this, copy the dummy matrix in original board.

0	1	0		0	0	0
0	0	1		1	0	1
1	1	1	→	0	1	1
0	0	0		0	1	0

```

dum[i][j];
for(i=0 → m) {
  for(j=0 → n) {
    count no. of ones for
    current cell.
    if(a[i][j] == 1 & ones < 2)
      make dead;
    else if(a[i][j] == 1 & (ones == 2 || ones == 3))
      continue;
    else if(a[i][j] == 1 & ones > 3)
      make dead;
    else if(a[i][j] == 0 & ones == 3)
      make live;
    else continue;
  }
}

```

time complexity: $O(m \cdot n)$
space complexity: $O(m \cdot n)$

0	0	0
1	0	1
0	1	1
0	1	0

copy dum into original.

// Brute force (in-place solution)

observe possibilities:

original		new	map
0	→	0	0 - 0
1	→	0	1 - 0
0	→	1	2 - 1
1	→	1	3 - 1

0 ₀	1 ₁	0 ₀
0 ₂	0 ₀	1 ₃
1 ₁	1 ₃	1 ₃
0 ₀	0 ₂	0 ₀

// traverse and update the original
acc. to table above.

// change 3s and 2s according to table.

```

for (r = 0 → m) {
  for (c = 0 → n) {
    nei = countNeighbors(r, c);
    if (board[r][c] == 1) {
      if (nei == 2 || nei == 3) {
        board[r][c] = 1;
      }
      else if (nei == 3) {
        board[r][c] = 2;
      }
    }
  }
}

```

```

for (r = 0 → m) {
  for (c = 0 → n) {
    if (board[r][c] == 1) make 0;
    else if (board[r][c] == 3 or 2) make 1;
  }
}

```

```

countNeighbors(r, c) {
  neigh = 0;
  for (i = r - 1 → r + 1) {
    for (j = c - 1 → c + 1) {
      if ((i == r and j == c) || i < 0 || j < 0 || i == m || j == col):
        continue;
      if (board[i][j] == 1 || 3) neigh++;
    }
  }
  return neigh;
}

```

time complexity: $O(m \times n)$

space complexity: $O(1)$

#1499. Max Value of Equation

- Given an array of points, containing coordinates of 2D plane, points $[i] = [x_i, y_i]$ such that $(x_i < x_j)$ for $1 \leq i < j = \text{size}$.
- Also given integer k

- Return maximum value of eqn:

$$y_i + y_j + |x_i - x_j|, \quad |x_i - x_j| \leq k$$

$$[[1, 3], [2, 0], [5, 10], [6, -10]], \quad k=1$$

- satisfying points: $(1, 3)$ and $(2, 0)$
 $(5, 10)$ and $(6, -10)$

$$(1, 3) (2, 0): \quad 3 + 0 + |1 - 2| = 3 + 1 = 4 \quad \checkmark \text{Max Value}$$

$$(5, 10) (6, -10): \quad 10 + (-10) + |5 - 6| = 1$$

// Solution:

$$\boxed{x_0, y_0}, x_1, y_1, x_2, y_2, x_3, y_3 \quad (j)$$

$$\hookrightarrow x_1 - x_0 \quad (\text{as } x_1 > x_0)$$

eqn: $y_i + y_j + |x_i - x_j|$

$$y_i + y_j + x_j - x_i$$

we need to add (j) coordinate.

$$\boxed{(x_j + y_j) + (y_i - x_i)} \rightarrow \text{maximize this}$$

- implementing through priority_queue