

time

Each thread is incharge of "depth" number of sums. Then one thread (P3) is in charge of adding up the partial sums. the pre task foreach thread is the initial set of the result variable

reduce (int, max) - Yes. It would find the max element in 3.2) cach section of the array then compare He max for each section against each other to find the whole max

reduce & std: string, concact> - yes, He also would concact each section then concast each section together, it would maintain proper order

reduce < float, sum > - yes, code is templeted, and int is similar to float & would work the same way

reduce (float, max> - yes, similar to reduce kint, max>

$$(i=1)$$
 $\rightarrow (i=1)$ $\rightarrow (i=2)$ $\rightarrow (i=3)$ $\rightarrow \dots \rightarrow (i=n)$

all tasks are dependent on He i-1 iteration. This is because to calculate pr[i], you need pr[i-1]

width=1 CP = n+1 work=n+1

parallel version

Similar to the reduce function, the array will be split into smaller chunks and prefix sum will be computed then the last sum of each chunck is added into the next chunk

Dos 1	0012345	Pr 0 0 1 3 6 10 5	9 10	pr 0 6 13 21 30 40 51	ar 12 13 14 15 16	pr 0 12 25 39 54 70 87	do partial prefix sum for each chunck of the data in this case 3 chunks. He offset is the largest partial sum of that chunk. This is step 1
		1 /	1		. 1	1 2	

thread 3 offset = 87

	offset=15	offset=51	OFFSE	Mark Hall from
Pass 2	error = 0 pr fin 0 0 1 3 6 10 15	error = 15 pr fin 0 15 6 21 13 28 21 36 30 45 40 55 51 66	error = $51+15=66$ pr fin 0 66 12 78 25 91 39 105 59 120 70 136 87 153	Now add all the offsets from the previous chunks to each member of the partial sum the sum of the offsets is the error. This sumation is independent and can be threaded similar to slep 1. This is step 2 and final Step
			1	

mergesort (arr) if len (arr) =1: return arr

> left = left half of arr right = right half of arr

left = mergesort (left) right = mergesort (right) return merge (left, right)

merge (left, right)

result = empty array

while left is not emply

and right is not emply:

if left[0] \(\) right[0]:

result t= left[0]

result += risht [0]
rem risht[0]

if left is not empty
result to left

if right is not empty
result to right

return result

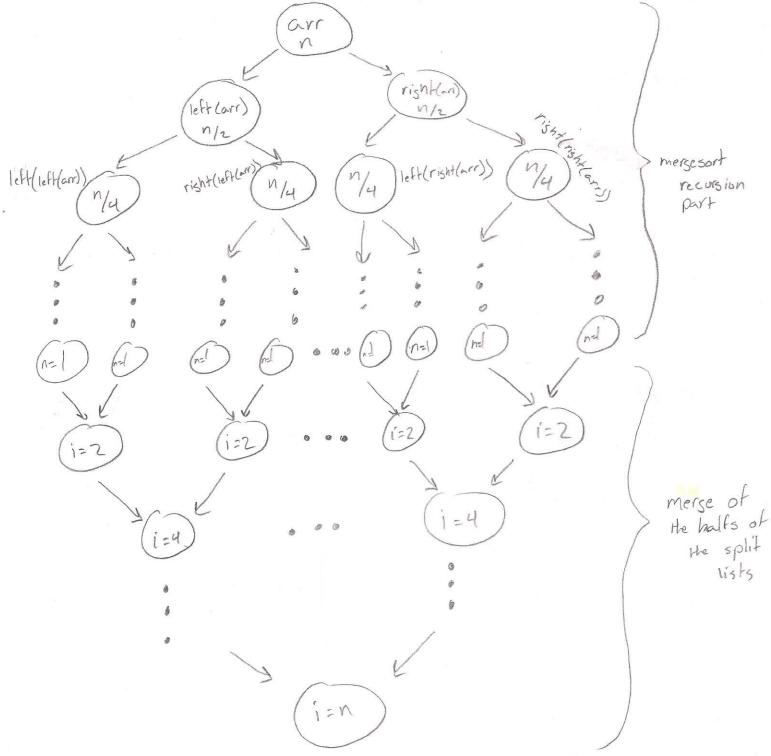
an array of size 1 is sorted

split into 2 parts

sort both left right parts
recursively
merse the two parts in order

go through both left tright sides and place the saller of the first element into the result array

place the rest of the elements from either list into the result array



He first half of the dependency tree is the recursive part of mercesort() function it splits the array into 2 sobarrays. Then these subarrays are sorted and mersed in the second half of the dependency graph. The merse part of the dependency graph takes more time to compute

work = 3n-2 $CP = 2\log_2(n) + 1$ width = 1

PILI	N 2	513		[i-2]	I i - 4	Control State of Stat	i=n	
P2	n z	77	1					
P3 1		54		[i=2]		2 - 1		
P4		21.3				999		
p5]		4 8	0	122	1=4	1		
P6								
P7]				122				
PS			1	e	•	. Jerston de grande de la companya d		
The acceptance of the state of	17 as a triminant and contact on before its absenced in California.	and graph comment accounts the condition field of the condition of the con	3	P	•			
1		time	9	0	0			

Diamond shape? If we don't have any penalty for spawning threads, then each recursive call would spawn 2 threads: one for each half of its current thread. There is very little "work" happening ofter than the creation of the threads. That is why the boars here are thin. When the marger of two subarrays happen, one thread will handle it but because it has to go through 2 sub arrays, the time taken to sort will double as the recursion stack collapses to the end condition is in

To make the code more parallel, I would remove some of the initial recursion so there is little dependency athe bigining of the run. For example with a Pot 4, He fist 2 "layers" of the shart chart I dependency graph will be sone. Then the processor mergesorts the 4 halves of the array. At the end a thread sorts the 2 halves that are left.

```
1
 2 // PLEASE COMPILE WITH g++ reduce_par.cpp -lpthread
 4 #include <memory>
 5 #include <iostream>
 6 #include <vector>
 7 #include <thread>
 8 #include <cassert>
 9 #include <string>
10 // #include <numeric>
11 // #include <execution>
12 #include <parallel/numeric>
13
14 template <typename T>
15 T sum(T a, T b) {
    return a + b;
16
17 }
18
19 template <typename T>
20 T max(T a, T b) {
21
    return a > b ? a : b;
22 }
23
24 // template <typename T, typename = std::enable_if_t<std::is_same_v<T,
   std::string>>>
25 template <typename T, typename = std::enable_if_t<std::is_same<T,
   std::string>::value>>
26 constexpr auto concact = sum<T>;
27
28 // Code from the assignment. The last parameter is needed
29 // because F is a type, even though it can be modified to only
30 // have 2 parameters, I belive this is easier on the head
31 template <typename T, typename F>
32 T reduce_sin(T* array, size_t n, F op) {
33
    T result = array[0];
34
    for (int i=1; i < n; ++i)
35
       result = op(result, array[i]);
36
    return result;
37 }
38
39 // I do not want to deal with promises or futures, so Im doing this.
40 /// Partially reduces the array from [start, end) and places it in
41 /// result.
42 /// @note The *result variable does not have a race condidtion as it
            is only being written by one thread.
43 ///
44 template <typename T, typename F>
45 void partial_reduce(T* start, T* end, T* result, F op) {
46
     *result = reduce_sin(start, std::distance(start, end), op);
47 }
48
49 /// Parallel reduce
50 template <typename T, typename F>
51 T reduce_par (T* array, size_t n, size_t p, F op) {
52
    // create nessicary structures
53
    std::unique_ptr<T[]> data{ new T[p] };
54
    std::vector<std::thread> threads{ };
55
56
    // calculate parallelism
57
     size_t depth = n / p;
58
     T* start = array;
```

```
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                                            reduce_par.cpp
  59
       T* end = array + depth;
  60
  61
       // the actual parallel code
  62
       for (size_t i = 0; i ; ++i) {
  63
         // The <T, F> is needed because partial_reduce is a templated function so
     we need
        // to thread the <T, F> version of the function
  64
  65
         threads.emplace_back(partial_reduce<T, F>, start, end, &data[i], op);
        start = end;
  66
  67
         end += depth;
  68
       }
  69
  70
      // the last one (this thread will do it so we dont spin on waiting for them
    to join)
  71
      partial_reduce(start, array + n, &data[p - 1], op);
  72
  73
      // wait for them to finish
  74
       for (auto& t : threads)
 75
        t.join();
 76
  77
      // final sum
  78
       return reduce_sin(data.get(), p, op);
  79 }
 80
  81
  82 // options:
  83 // 1: reduce<int, sum>
  84 // 2: reduce<int, max>
  85 // 3: reduce<std::string, concact>
  86 // 4: reduce<float, sum>
  87 // 5: reduce<float, max>
  88 #define OPTION 1
  89 | #define MAX 500'000'007
  90 // @warning, the only one that doesnt really work very well is option 4.
    Adding up
  91 // more than 1mil values gives you two different answers and I'm mostly
     certains its
  92 // because of FP arithmetic
  93
  94
  95 #if OPTION == 1
 96
       #define NUMERIC
 97
              NUM TYPE = int;
 98
       template <typename T> constexpr auto op_t = sum<T>;
 99 #elif OPTION == 2
100
      #define NUMERIC
101
      using
              NUM_TYPE = int;
102
       template <typename T> constexpr auto op_t = max<T>;
103 #elif OPTION == 3
104
      template <typename T> constexpr auto op_t = concact<T>;
105 \# elif OPTION == 4
106
       #define NUMERIC
107
              NUM_TYPE = float;
108
      template <typename T> constexpr auto op_t = sum<T>;
109 #elif OPTION == 5
110
      #define NUMERIC
111
      using
               NUM_TYPE = float;
112
       template <typename T> constexpr auto op_t = max<T>;
113 #else
114
       #error "[E] Valid option not chosen"
```

```
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                                            reduce_par.cpp
115 #endif
116
117
118 int main() {
119
120 #ifdef NUMERIC
121
122
       constexpr unsigned long long LG_NUM = MAX;
123
       std::vector<NUM_TYPE> data{};
124
       data.push_back(3); // this is a "valid" dummy data for max
125
126
       for (unsigned long long i = 1; i < LG_NUM + 1; ++i) {
127
         data.push_back(1); // sums of ones
128
       }
129
130 #else
131
       char temp[2] = \{ ' \ 0', ' \ \};
132
133
       std::vector<std::string> data{};
134
      for (int j = 0; j < 3; ++j) {
         for (unsigned long long i = 0; i < 26; ++i) {
135
136
           // 97-122
137
           temp[0] = i + 97;
138
           data.emplace_back(temp);
139
         }
140
       }
141
142 #endif
143
144
       auto op = op_t<decltype(data)::value_type>;
145
146
      auto begin1 = std::chrono::high_resolution_clock::now(); //// AHHHHHHH
147
       auto accum1 = reduce_sin(data.data(), data.size(), op);
148
       auto end1
                   = std::chrono::high_resolution_clock::now(); //// AHHHHHHH
149
150
       std::chrono::duration<double, std::milli> elapse1{ end1 - begin1 };
151
       std::cout << "Serial: " << elapse1.count() << std::endl;</pre>
152
153
      auto begin2 = std::chrono::high_resolution_clock::now(); //// AHHHHHHH
154
      auto accum2 = reduce_par(data.data(), data.size(), 8, op);
155
                   = std::chrono::high_resolution_clock::now(); //// AHHHHHHH
       auto end2
156
157
       std::chrono::duration<double, std::milli> elapse2{ end2 - begin2 };
       std::cout << "Parallel: " << elapse2.count() << std::endl;</pre>
158
159
160
       // Turns out that neither gnu g++ or clang++ supports the parallelism TS,
    kms
161
      // https://youtu.be/Mcjrc2uxbKI?t=571 MSVC ahead of the game *slow claps*
162
       // nvm: https://godbolt.org/z/TCGaze The internet video lies
163
       // auto begin3 = std::chrono::high_resolution_clock::now();
164
       // double result = std::reduce(std::execution::par, sum.begin(),
     sum.end());
165
      // auto end3 = std::chrono::high_resolution_clock::now();
166
167
      // std::chrono::duration<double, std::milli> elapse3{ end3 - begin3 };
168
      // std::cout << "STL: " << elapse3.count();</pre>
169
170
       // hehe https://gcc.gnu.org/onlinedocs/libstdc++/manual/parallel_mode.html
```

// after seeing the results, another lie. Why does the docs lie?????

// Serial: 1512.65

171

172

2/10/2019 reduce_par.cpp

```
173
    // Parallel: 351.756
174
     // GNU: 1562.03
175
    // The sum is: 50000010
176 // #if OPTION == 1
177 // auto begin4 = std::chrono::high_resolution_clock::now();
178 // double accum4 = __gnu_parallel::accumulate(data.begin(), data.end(), 0);
179 // auto end4 = std::chrono::high_resolution_clock::now();
180
181 // std::chrono::duration<double, std::milli> elapse4{ end4 - begin4 };
182 // std::cout << "GNU: " << elapse4.count() << std::endl;
183 // #endif
184
185
     if (accum1 == accum2)
186
      std::cout << "The result is: " << accum1 << std::endl;</pre>
187
     else
      std::cout << "The result were different, you screwed up..." << std::endl
   << accum1 << " " << accum2 << std::endl;
189 }
```