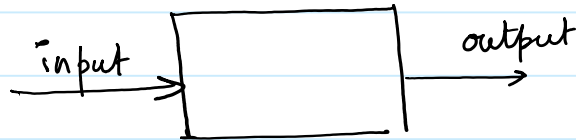
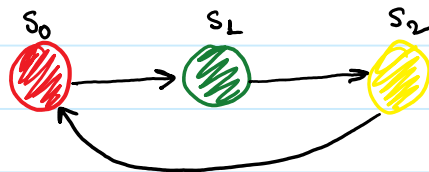


Systems



State: It says what is the current condition of the system.

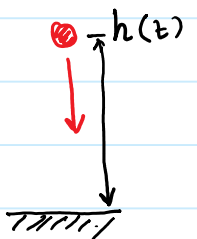


Finite state system: A system with finitely many states.

infinite state system:

The state is the height of the free falling ball.

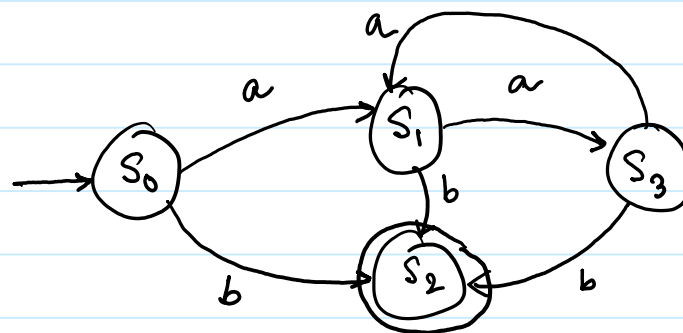
There are infinite possibilities.
3.1, 3.100029, ...



Finite state machines : denoted by $(Q, \Sigma, \delta, q_0, F)$

Q is the set of states.
 Σ " " " " action/input
 δ " " transition relation that dictates how one state moves to another upon applying an input

q_0 is the initial state.
 F is the final state(s).



$$Q = \{s_0, s_1, s_2, s_3\}, \quad \Sigma = \{a, b\}$$

$$q_0 = \{s_0\}, \quad F = \{s_2\}$$

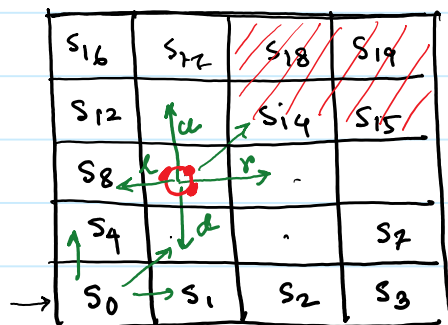
δ (current state, action) = next state

$$\begin{array}{l|l|l} \delta(s_0, a) = s_1 & \delta(s_1, a) = s_3 & \delta(s_2, a) = \phi \\ \delta(s_0, b) = s_2 & \delta(s_1, b) = s_2 & \delta(s_2, b) = \phi \end{array}$$

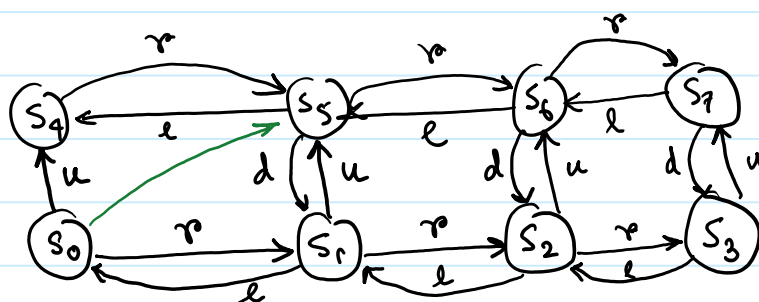
$$\delta(s_3, a) = s_1$$

$$\delta(s_3, b) = s_2$$

Robotics Path planning:



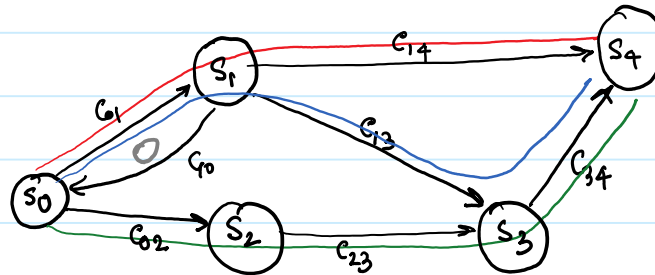
$$\begin{aligned} \checkmark \quad \mathcal{Q} &= \{s_0, \dots, s_{19}\} \\ q_0 &= s_0 \\ \checkmark \quad F &= \{s_{14}, s_{15}, s_{18}, s_{19}\} \end{aligned}$$



$$\begin{aligned} \delta(s_0, u) &= s_4 \\ \delta(s_0, r) &= s_1 \\ \delta(s_1, u) &= s_5 \\ \delta(s_1, r) &= s_2 \\ \delta(s_1, l) &= s_0 \end{aligned}$$

current		s ₀	s ₁	s ₂	s ₃
next	s ₀	X	l	X	X
	s ₁	r	X	l	X
	s ₂				
	s ₃				

Graphs and Network:



find the shortest ("least cost") path from one node to another.

Example: find path from s_0 to s_4

s_0 s_1 s_4

s_0 s_1 s_3 s_4

s_0 s_2 s_3 s_4

s_0 s_1 s_0 s_2 s_3 s_4

s_0 s_1 s_0 s_1 s_0 s_2 s_3 s_4

cost

$c_{01} + c_{14}$

$c_{01} + c_{13} + c_{34}$

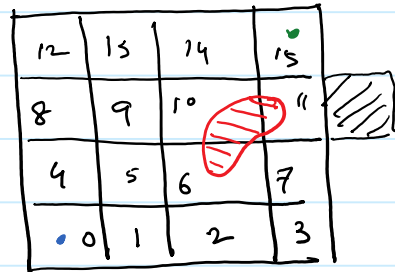
$c_{02} + c_{23} + c_{34}$

...

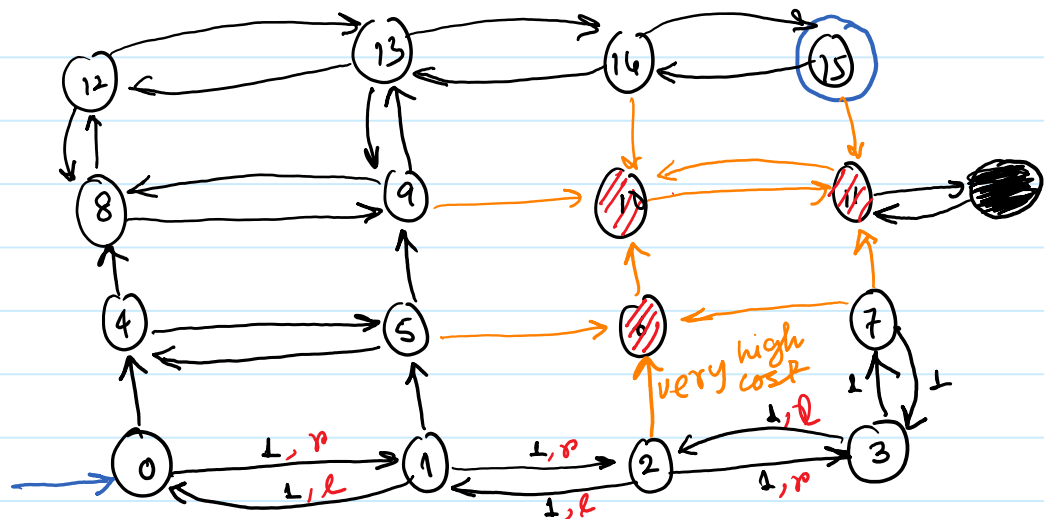
Dijkstra's algorithm for shortest path planning:

A^* is widely used for path planning in robotics.

Robotics path planning using Dijkstra's:

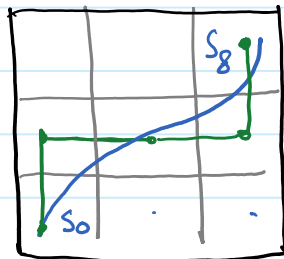
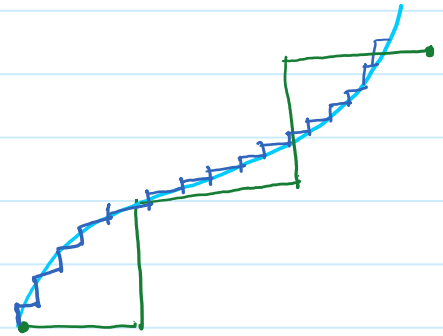
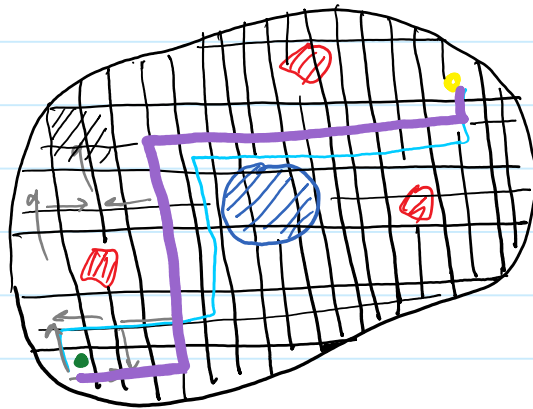


Step: find a FSM equivalent \rightarrow that gives the graph

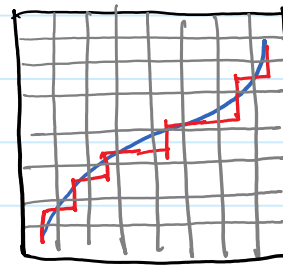


Find a path from s_0 to s_{15}

Problem:



this has only
9 states



this resolution gives
better path but it
has too many states



Computation and optimality trade-off:

Higher resolution \Rightarrow better path, but
high computation

lower resolution \Rightarrow coarser path, but
less time to
compute.

12	13	14	15
8	9	10	11
4	5	6	7
0	1	2	3

