

Web Mining Lab Assignment-5

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HITS Algorithm

```
In [ ]: !pip install networkx --upgrade
import networkx as nx
```

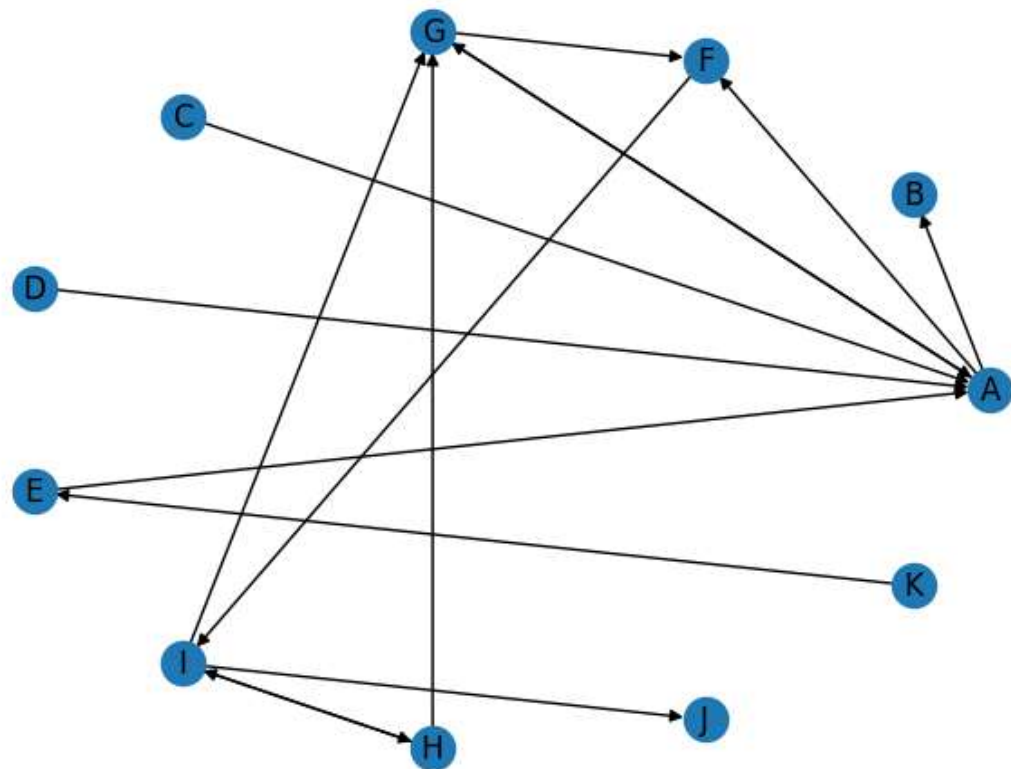
Requirement already satisfied: networkx in c:\users\ayuar\appdata\local\programs\python\python310\lib\site-packages (3.0)

```
In [ ]: import networkx as nx
import matplotlib.pyplot as plt

adj = [[0, 1, 0, 0, 0, 1, 1, 0, 0, 0, 0],
        [0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
        [1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
        [1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
        [1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
        [0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0],
        [1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0],
        [0, 0, 0, 0, 0, 0, 1, 0, 1, 0, 0],
        [0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 0],
        [0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
        [0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0]]

G = nx.DiGraph()
for i in range(len(adj)):
    for j in range(len(adj[i])):
        if adj[i][j] != 0:
            G.add_edge(i, j)
labels = {0: 'A', 1: 'B', 2: 'C', 3: 'D', 4: 'E', 5: 'F', 6: 'G', 7: 'H', 8: 'I', 9: 'J'}
for node in G.nodes:
    G.add_node(node, label=labels[node])
```

```
In [ ]: pos = nx.circular_layout(G)
nx.draw(G, pos, with_labels=True, labels={node: data["label"] for node, data in G.nodes(data=True)})
plt.show()
```



Using Custom Algorithm

```

In [ ]: num_vertices_1=11
num_iterations = 4
outbound_vertices_1 = [[] for _ in range(num_vertices_1)]
for i in range(num_vertices_1):
    for j in range(num_vertices_1):
        if adj[i][j] == 1:
            outbound_vertices_1[i].append(j)
outbound_vertices_1

```

```

Out[ ]: [[1, 5, 6], [], [0], [0], [0], [8], [0, 5], [6, 8], [6, 7, 9], [], [4]]

```

```

In [ ]: # Store the in-bound vertices for each vertex
inbound_vertices_1 = [[] for _ in range(num_vertices_1)]
for i in range(num_vertices_1):
    for j in range(num_vertices_1):
        if adj[j][i] == 1:
            inbound_vertices_1[i].append(j)
inbound_vertices_1

```

```

Out[ ]: [[2, 3, 4, 6], [0], [], [], [10], [0, 6], [0, 7, 8], [8], [5, 7], [8], []]

```

```

In [ ]: # We will initialize the `authority` and the `hub` scores.
authority_scores_1 = [1] * num_vertices_1
hub_scores_1 = [1] * num_vertices_1

```

```

In [ ]: # Initialize the authority and hub scores
authority_scores = dict.fromkeys(G.nodes(), 1.0)
hub_scores = dict.fromkeys(G.nodes(), 1.0)

# Iterate for the specified number of iterations

```

```

for i in range(num_iterations):
    # Store the old authority and hub scores
    old_authority_scores = authority_scores.copy()
    old_hub_scores = hub_scores.copy()

    # Update the authority and hub scores
    for node in G.nodes():
        inbound_vertices = G.predecessors(node)
        authority_scores[node] = sum([old_hub_scores[v] for v in inbound_vertices])
        outbound_vertices = G.successors(node)
        hub_scores[node] = sum([old_authority_scores[v] for v in outbound_vertices])

    # Normalize the authority and hub scores
    authority_norm = sum(authority_scores.values())
    hub_norm = sum(hub_scores.values())
    for node in G.nodes():
        authority_scores[node] /= authority_norm
        hub_scores[node] /= hub_norm
for node, authority_score in authority_scores.items():
    print(labels[node], ":", authority_score)

```

```

A : 0.16556291390728475
B : 0.10596026490066224
F : 0.17218543046357615
G : 0.271523178807947
C : 0.0
D : 0.0
E : 0.00662251655629139
I : 0.09271523178807947
H : 0.09271523178807949
J : 0.09271523178807949
K : 0.0

```

```

In [ ]: print("The Hub scores of the nodes using Networkx library : ")
        for node, hub_score in hub_scores.items():
            print(labels[node], ":", hub_score)

```

```

The Hub scores of the nodes using Networkx library :
A : 0.19428571428571428
B : 0.0
F : 0.04
G : 0.17142857142857143
C : 0.10285714285714284
D : 0.10285714285714284
E : 0.10285714285714284
I : 0.14857142857142858
H : 0.13142857142857145
J : 0.0
K : 0.005714285714285714

```

Using Inbuilt HITS Algorithm

```

In [ ]: hub_scores_networkx, authority_scores_networkx = nx.hits(G,max_iter=4, normalized =

```

```

In [ ]: # Print the Authority scores
        print("The Authority scores of the nodes using Networkx library : ")
        for k, v in authority_scores_networkx.items() :
            print(labels[k], " : ", v)

```

The Authority scores of the nodes using Networkx library :

```
A : 0.17083057489162345
B : 0.11135119658826395
F : 0.18087471475229738
G : 0.27107706702529233
C : 0.0
D : 0.0
E : 2.0432377644483274e-17
I : 0.08862214891417429
H : 0.08862214891417426
J : 0.08862214891417426
K : 0.0
```

```
In [ ]: # Print the Hub scores
print("The Hub scores of the nodes using Networkx library : ")
for k, v in hub_scores_networkx.items() :
    print(labels[k], " : ", v)
```

The Hub scores of the nodes using Networkx library :

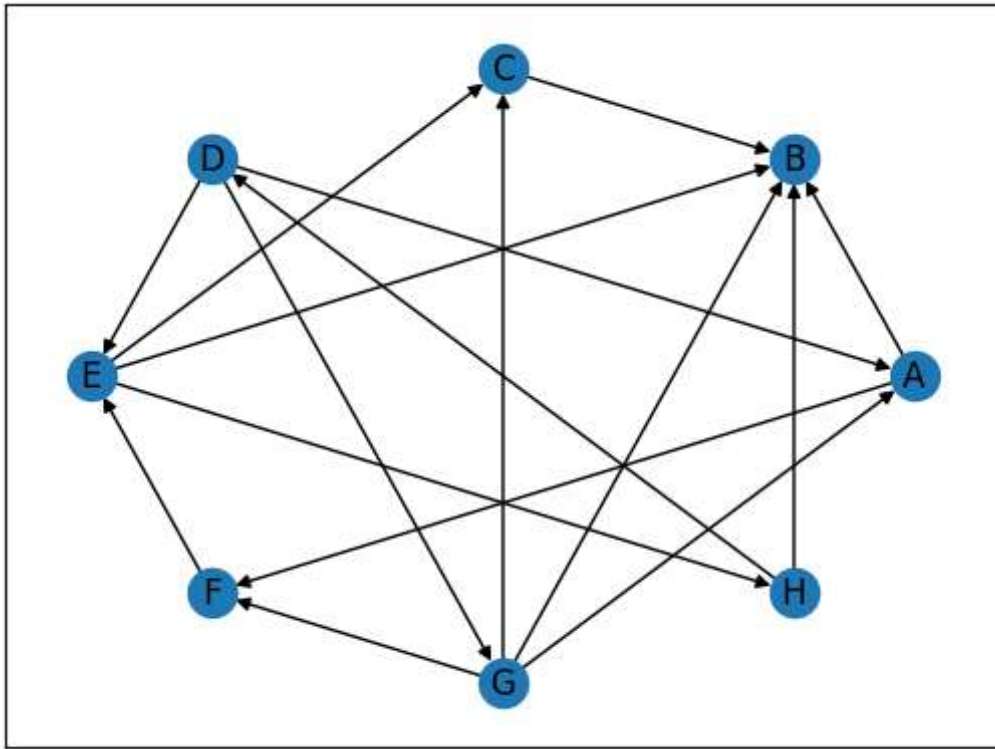
```
A : 0.24237021803296221
B : 0.0
F : 0.03813111305960052
G : 0.15132688980561315
C : 0.07350261808182357
D : 0.07350261808182357
E : 0.07350261808182357
I : 0.19289751895797694
H : 0.15476640589837648
J : 0.0
K : 8.791360981246017e-18
```

Comparing the Authority and Hub Scores for both the implementations they are very similar and are in the accepted criteria for error percentage so the results are verified

Page Rank

```
In [ ]: G1 = nx.DiGraph()
num_vertices=8
vertices_name1 = ['A', 'B', 'C', 'D', 'E', 'F', 'G', 'H']
G1.add_nodes_from(vertices_name1)
G1.add_edges_from([('A', 'B'), ('A', 'F'), ('C', 'B'), ('D', 'A'), ('D', 'E'), ('D', 'G'), ('E', 'F'), ('F', 'G'), ('G', 'H')])

nx.draw_networkx(G1, pos=nx.circular_layout(G1), arrows=True, with_labels=True)
plt.show()
```



Using Inbuilt Page Rank

```
In [ ]: pagerank=nx.pagerank(G1,alpha=0.85,max_iter=100)
print("The page ranks are as follows=\n")
pagerank
```

The page ranks are as follows=

```
Out[ ]: {'A': 0.08941499371129827,
        'B': 0.28120563198030324,
        'C': 0.10983011816321761,
        'D': 0.08864644387947536,
        'E': 0.1606990303925196,
        'F': 0.10229957241772619,
        'G': 0.07374454250177016,
        'H': 0.09415966695368949}
```

```
In [ ]: ## Sort the pages by their ranks
# page_ranks_networkx=dict(sorted(page_ranks_networkx.items(),key=Lambda item:item[1]))
# page_ranks_networkx
```

```
Out[ ]: {'B': 0.28120563198030324,
        'E': 0.1606990303925196,
        'C': 0.10983011816321761,
        'F': 0.10229957241772619,
        'H': 0.09415966695368949,
        'A': 0.08941499371129827,
        'D': 0.08864644387947536,
        'G': 0.07374454250177016}
```

Using Random Walk Algorithm

```
In [ ]: out_bound_vertices_count=[0 for _ in range(num_vertices)]
A=nx.adjacency_matrix(G1,nodelist=vertices_name1)
adj=A.todense()
for i in range(num_vertices):
```

```
    out_bound_vertices_count[i]=sum(adj[i])
out_bound_vertices_count
```

Out[]: [2, 0, 1, 3, 3, 1, 4, 2]

```
In [ ]: in_bound_vertices_list={}
        for i in range(num_vertices):
            in_bound_vertices_list[i]=[]
            for j in range(num_vertices):
                if adj[j][i]==1:
                    in_bound_vertices_list[i].append(j)
in_bound_vertices_list
```

Out[]: {0: [3, 6],
1: [0, 2, 4, 6, 7],
2: [4, 6],
3: [7],
4: [3, 5],
5: [0, 6],
6: [3],
7: [4]}

```
In [ ]: def pageRank(graph, vertices_names, in_bound_vertices_list, out_bound_vertices_count):
        # Number of vertices
        num_vertices = len(vertices_names)
        page_rank_manual={}
        page_rank = [(1/num_vertices) for _ in range(num_vertices)]
        epsilon = num_vertices * tolerance
        converged = False
        for i in range(max_iterations) :
            page_rank_old = page_rank[:]
            for j in range(num_vertices) :
                page_rank[j] = 0

                for k in in_bound_vertices_list[j] :
                    page_rank[j] += page_rank_old[k] / out_bound_vertices_count[k]
            error = sum([abs(page_rank[j] - page_rank_old[j]) for j in range(num_vertices)])
            if error < epsilon :
                converged = True
                break
        if converged :
            page_rank_manual = {}
            for i, pr in enumerate(page_rank) :
                page_rank_manual[vertices_names[i]] = pr
        return page_rank_manual
```

```
In [ ]: page_rank_manual = pageRank(G1,vertices_name1, in_bound_vertices_list, out_bound_vertices_count)
page_rank_manual
```

Out[]: {'A': 0.07291666666666666,
'B': 0.32291666666666663,
'C': 0.07291666666666666,
'D': 0.0625,
'E': 0.16666666666666666,
'F': 0.09375,
'G': 0.041666666666666664,
'H': 0.041666666666666664}

Sort the Values

```
In [ ]: page_rank_manual=dict(sorted(page_rank_manual.items(),key=lambda item:item[1],reverse=True),  
                                page_rank_manual)
```

```
Out[ ]: {'B': 0.32291666666666663,  
         'E': 0.16666666666666666,  
         'F': 0.09375,  
         'A': 0.07291666666666666,  
         'C': 0.07291666666666666,  
         'D': 0.0625,  
         'G': 0.04166666666666664,  
         'H': 0.04166666666666664}
```