

Queue

Implementation of queue using array

LL

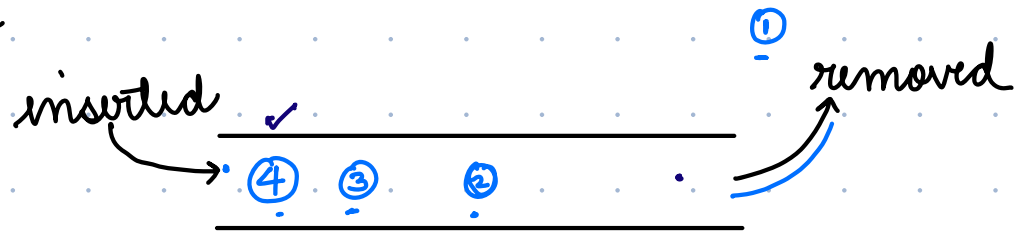
Stack

✓ Perfect Number Question

Double ended queue

Sliding window maximum

# Queue



linear data structure where element gets added from one end, but get removed from other end.

F I F O



Some real world examples —

1. Ticket counter
2. Toll plaza
3. Printer — Queue to print
4. Customer service

↳ First come first serve basis

## Functions :

add - Enqueue()  
remove - Dequeue()  
top - peek()  
size - size()



LL  
Array  
Stacks

# Arrays

size = 11

↓

27	26	35	5	6	7	15	16	17	25	26
0	1	2	3	4	5	6	7	8	9	10

↑

$f = \text{front} = -1$  = index of element which just got removed

$r = \text{rear} = -1$  = index of element which has just been added

enqueue (19)    dequeue ( )

enqueue (26)    enqueue (5)

enqueue (35)    enqueue (6)  
enqueue (7)

enqueue (15)

enqueue (16)

enqueue (17)

enqueue (25)

enqueue (26)

enqueue (27) ←

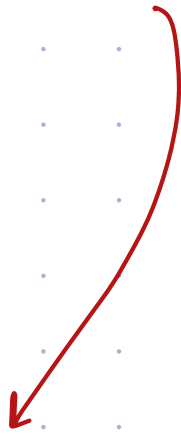
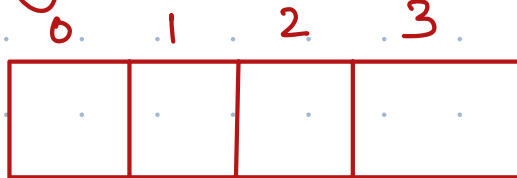
$f = f + 1$

$r = (r + 1) \% N$   
A[r] = x

peek

$f + 1$

How will you move?



$N = 4$

$x = 0$

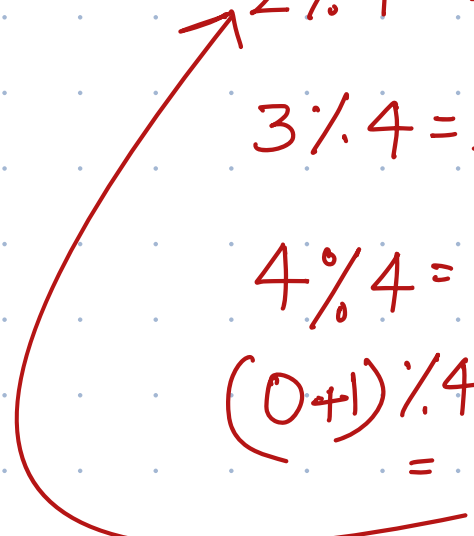
$$1 \% 4 = 1$$

$$2 \% 4 = 2$$

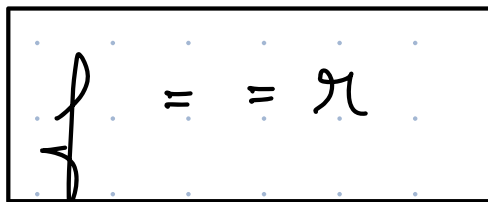
$$3 \% 4 = 3$$

$$4 \% 4 = 0$$

$$(0 + 1) \% 4 = 1$$



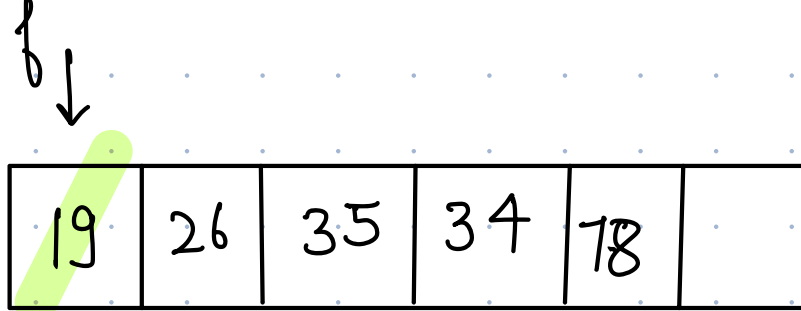
Circular way



← Queue being full



A small mistake



dequeue()

dequeue()

dequeue()

dequeue()

(N)

SZ

```
void enqueue (int x) {
    if (sz == N) { return; }

```

$r = (r + 1) \% N$

$A[r] = x$

$SZ++$

```
int dequeue () {
    if (sz == 0) {
        return -1;
    }

```

$f = (f + 1) \% N$

$int\ val = A[f]$

$SZ--$

return val;

}

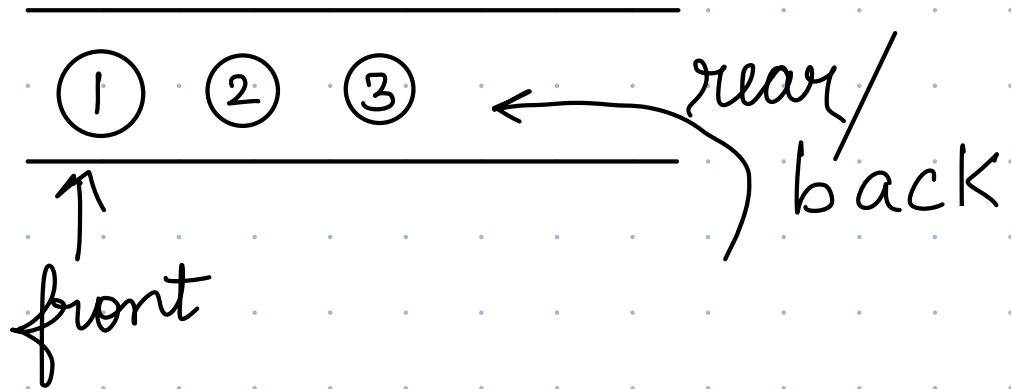
```

int peek() {
    if (sz == 0) { return -1; }
    int idx = (f + 1) % N
    return A[idx];
}

int size() {
    return sz;
}

```

TC  $\longrightarrow$



# linked list

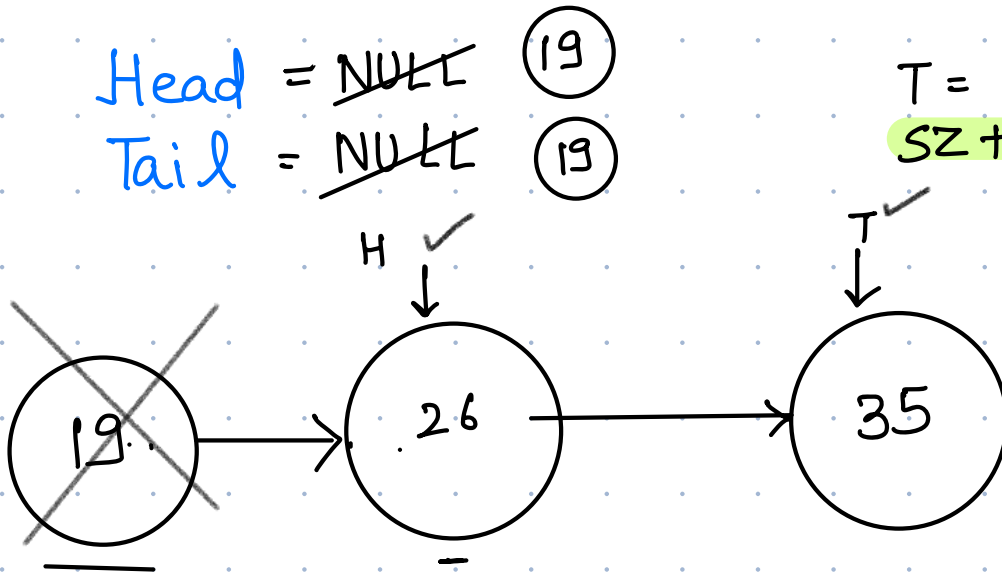
$O(1)$

Insert (addLast)

$T.Next = NE$

$T = T.Next$

$SZ++$



Removal (RemoveFirst)

$H = H.Next$

$SZ--$

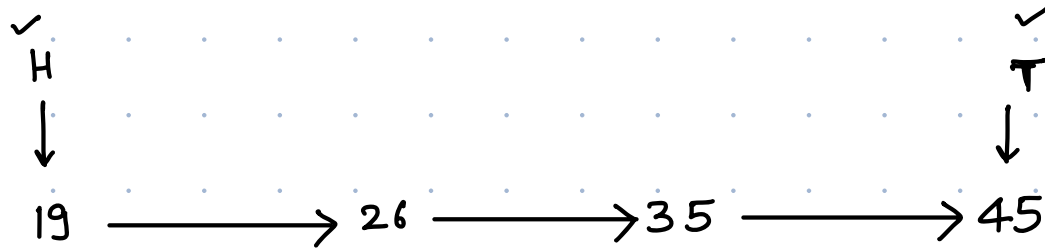
$O(1)$

Peek()

↳ Head

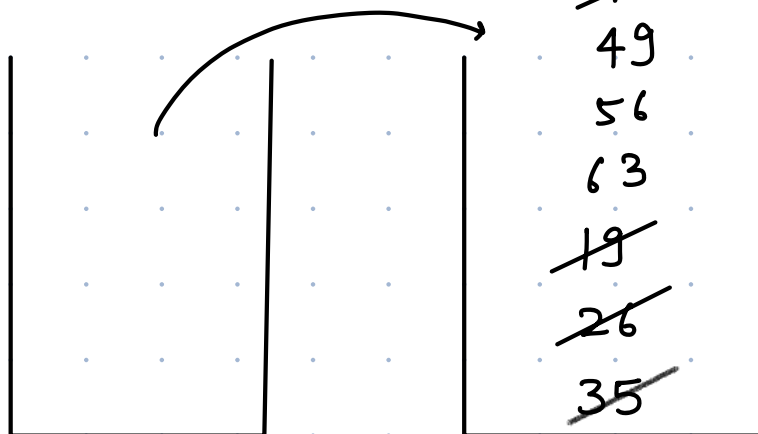
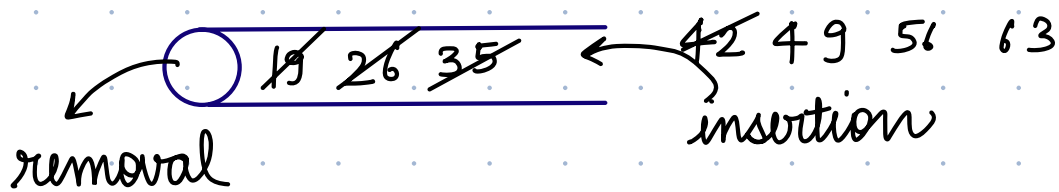
Size()

SZ



Singly L L

## Queues



enqueue  
stack

dequeue  
stack  
(Removal  
Order of queue)

19  
26  
35  
42  
49  
56  
63

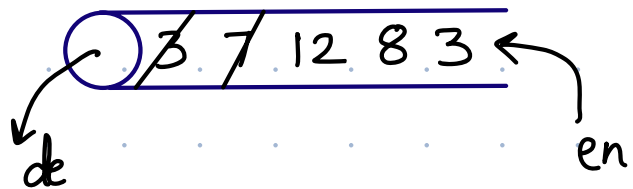


enqueue ( )  
 ↓  
 push into  
 enqueue Stack

dequeue ( )  
 dequeue Stack  
 ↙ ↘  
 sz == 0      sz != 0  
 1. empty  
   all enqueue  
   stack  
   and put it  
   into dequeue  
   stack  
 2. pop

Quiz :

en ( 3 )  
 en ( 7 )  
 en ( 12 )  
 deq ( )  
 deq ( )  
 en ( 8 )  
 en ( 3 )



12 8 3 ans

Quiz:

en(4)

deg

en(9)

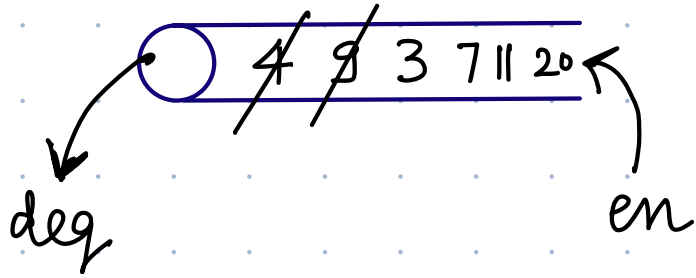
en(3)

en(7)

en(11)

en(20)

deg()

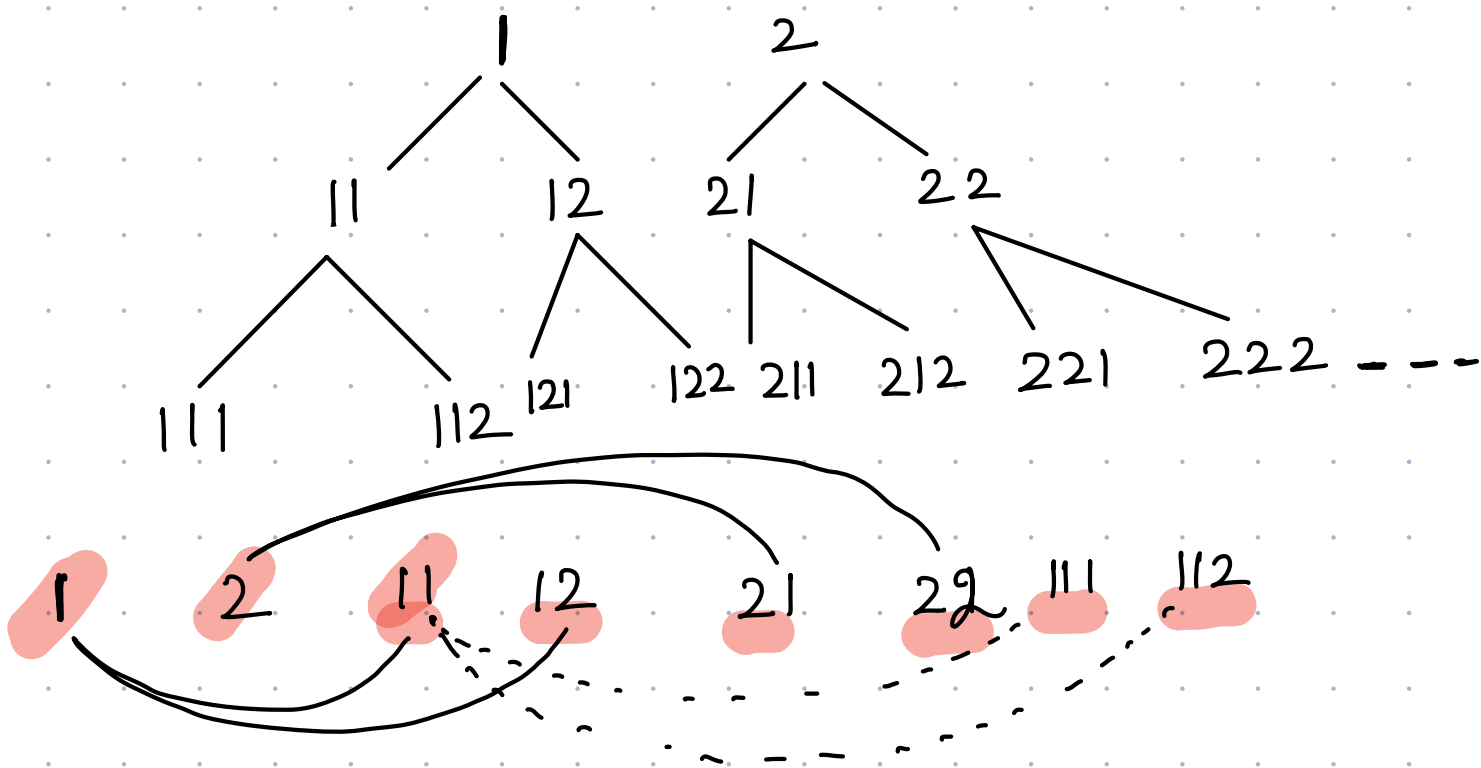


3 7 11 20

# Q Perfect Number

1 2 11 12 21 22 111 112 121 122 211 212 221

N  $\longrightarrow$  Nth number of series



~~1~~ ~~2~~ ~~11~~ ~~12~~ 21 22 111 112 121 122

$$\underline{12} \times 10 + 1 = 121$$

$$12 \times 10 + 2 = 122$$

TC:  $O(N)$

SC:  $O(N)$

```
int solve ( int N ) {  
    if ( N == 1 ) return 1;  
    if ( N == 2 ) return 2;  
    Queue < int > q;  
    q.enqueue(1)  
    q.enqueue(2)  
    i = 3;  
    while ( i <= N ) {  
        rem = q.dequeue()  
        a = rem * 10 + 1  
        b = rem * 10 + 2  
        if ( i == N ) { return a }  
        if ( i + 1 == N ) { return b }  
  
        q.add(a);  
        q.add(b);  
        i = i + 2;  
    }  
}
```

Dry Run:

N = 6

~~1~~ ~~2~~ 11 12

↑

~~l = 3~~ 5

a = ~~11~~ 21

b = ~~12~~ 22

ans

# Deque : Doubly Ended Queue

linear data structure

allows removal & insertion at both ends



6 important functions :

1) Insert at front

2) back

3) delete at front

4) delete at back

5) front

6) last

push-front ( )

push-back ( )

pop-front ( )

pop-back ( )

front ( )

back ( )

## Sliding Window Maximum

Q given an integer array A and a window K.

Find the maximum in all windows

$$A = \{ 10 \quad 1 \quad 9 \quad 3 \quad 7 \quad 6 \quad 5 \quad 11 \quad 8 \}, K = 4$$

$$\text{Ans} = 10 \quad 9 \quad 9 \quad 7 \quad 11 \quad 11$$

$$\left\{ \begin{array}{ccccc} & \overline{4} & 3 & \underline{\underline{2}} & 5 \\ \underline{1} & & & & \end{array} \right\} \quad K = 3$$

$$\text{Ans} \quad 4 \quad 4 \quad 5$$

# SLIDING WINDOW

K = 4

10 1 9 3 7 6 5 11 8

~~10~~ ~~1~~ ~~9~~ ~~3~~ ~~7~~ 11 8

Ans = 10 9 9 7 11 11

K = 4

1 8 5 6 7 4 2 0 3

~~1~~ ~~8~~ ~~5~~ ~~6~~ 7 4

ans 8 8 7 7 7 4

1) Solve first window

FIRST WINDOW

= TOP of DEQUE

2) Solve each window

$A[s-1] = \text{top of Deque}$   
remove

$A[e]$   
Deque

ans = TOP of DEQUE



```
void maxWindow (int[] A, int k) {
```

```
Deque<int> dq
```

```
// FIRST WINDOW
```

```
{  
    for (int i=0; i<k; i++) {  
        while (dq.size()>0 &&  
                A[i] > dq.back()) {  
            dq.pop-back();  
        }  
        dq.push-back(A[i])  
    }  
}
```

```
print (dq.front())
```

```
// Next windows
```

```
S = 1, e = k
```

```
N = A.length
```

```
while (e < N) {
```

```
// Handle S-1
```

```
if (A[S-1] == dq.front()) {
```

```
    dq.pop-front();
```

}

// Handle e

while ( dq.size() > 0  
    && A[e] > dq.back() ) {

    dq.pop-back();

}

    dq.push-back(A[e]);

// give the ans

    print(dq.front());

s++  
e++ }      move to next window

}

3

Every element — touched twice

going in } degree  
going out }

Tc:  $O(N)$

Sc:  $O(K)$