

# ARRAYS - I

Start doing dry run,  
start using pen and  
paper while solving  
DSA problems. Trust  
me half of your  
problems will be  
solved.

Try this !!



Good  
Morning

## Agenda

01. Space complexity
02. Arrays Introduction
03. Reverse Array
04. Rotate Array
05. Dynamic Array

Space complexity  $\rightarrow$  Max space used at any point of time during the execution of algorithm

Space complexity is also measured by Big(O)

\* function (int N) {

    int x; // 4B

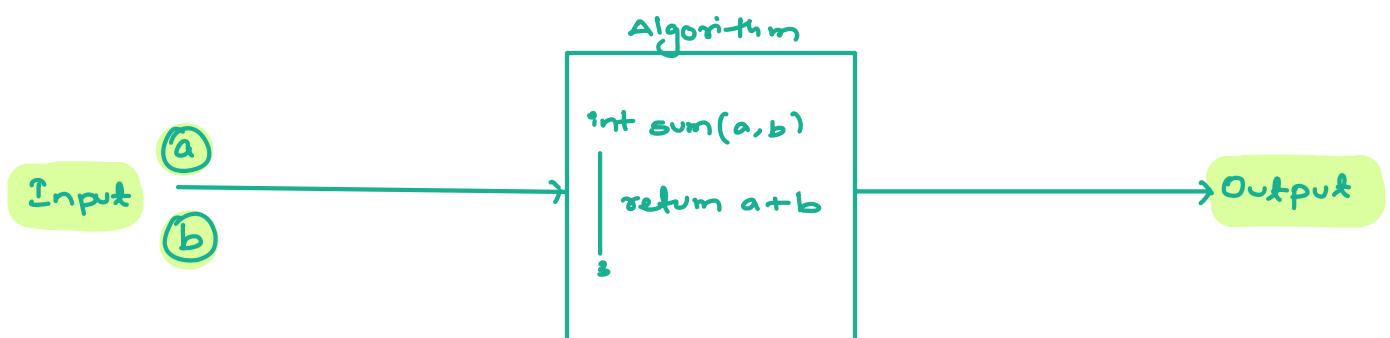
$$\text{Space} = 4 + 4 + 8$$

    int y; // 4B

- 16 bytes

    long z; // 8B

SC: O(1)  $\rightarrow$  independent of input



Obs 1  $\rightarrow$  space complexity is the extra space taken by algorithm.

Input space  $\times$

Output space  $\times$

func (int N)

int x; // 4B

$$\text{Space} = 4 + 4 + 8 + 4N$$

int y; // 4B

$$= 16B + 4 * N$$

long z; // 8B

SC: O(N)

int [] arr = new int [N]; // 4N

3

\* func (int N, int M)

int x = N // 4B

$$\text{Space} = 4 + 4 + 8 + 4N + 8N^2$$

int y = x \* 2 // 4B

$$= 16 + 4N + 8N^2$$

long z = x + y // 8B

SC: O(N<sup>2</sup>)

int [] arr = new int [N] // 4 \* N

long [][] l = new long [N][N] // 8N<sup>2</sup>

2

```

int max (int [] arr, int N)
{
    int ans = 0
    for (int i = 0; i < N; i++)
    {
        if (arr[i] > ans)
        {
            ans = arr[i];
        }
    }
    return ans;
}

```

TC : O(N)

SC : O(1)

```

int[] max (int [] arr, int N)
{
    int ans = 0 // 4B
    for (int i = 0; i < N; i++)
    {
        if (arr[i] > ans)
        {
            ans = arr[i];
        }
    }
    int [] A = new int [1];
    A[0] = max;
    return A;
}

```

Space = 8B

SC : O(1)

## Arrays

- Collection of data of some data type
- Contiguous memory location
- Ordered linear data structure
- Memory is predefined (size is fixed)

`int arr[n];`

$n$  = size of array

arr = name of the array

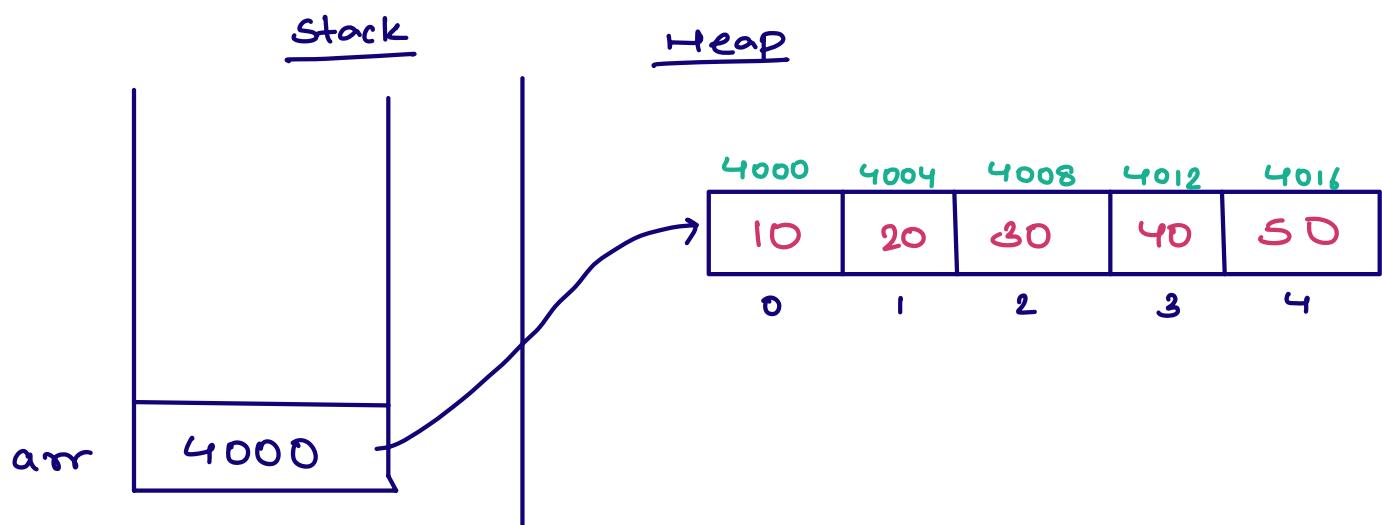
`int` = type of data this array is going to store

`int [ ] arr = new int [5]`

10	20	30	40	50
0	1	2	3	4

$\text{arr}[0] = 10$

$\text{arr}[n-1] = 50$



$$\begin{aligned}
 \text{arr}[0] &= 4000 + 0 \text{ integers} \\
 &= 4000 + 0 * 4 \\
 &= 4000 \longrightarrow 10
 \end{aligned}$$

$$\begin{aligned}
 \text{arr}[3] &= 4000 + 3 \text{ integers} \\
 &= 4000 + 3 * 4B \\
 &= 4000 + 12B \\
 &= 4012 \longrightarrow 40
 \end{aligned}$$

To fetch value = base address + index \* size of datatype

point all elements in array

```

void print_array ( int [ ] A , int n ) {
    for ( int i = 0 ; i < n ; i ++ ) {
        print ( A [ i ] );
    }
}
  
```

size of array

Tc: O(n)  
 Sc: O(1)

Accessing elements inside Array → O(1)

$$A[5] = \{5, -4, 8, 9, 10\}$$

0 1 2 3 4

element	id <sub>2</sub>
1	0
2	1
3	2
4	3
5	4

sum of 1<sup>st</sup> & 5<sup>th</sup> element

$$A[0] + A[4]$$

7:57 AM → 8:07 AM + 1 more min

Q Given an array of size N. Reverse the entire array

$$N = 5$$

$$A[] = \{10, 20, 30, 40, 50\}$$

0 1 2 3 4

$$\text{Output} = A[] = \{50, 40, 30, 20, 10\}$$

0 1 2 3 4

Brute force Approach = Take extra memory of array size & fill that array traversing from last

TC: O(n) SC: O(1)

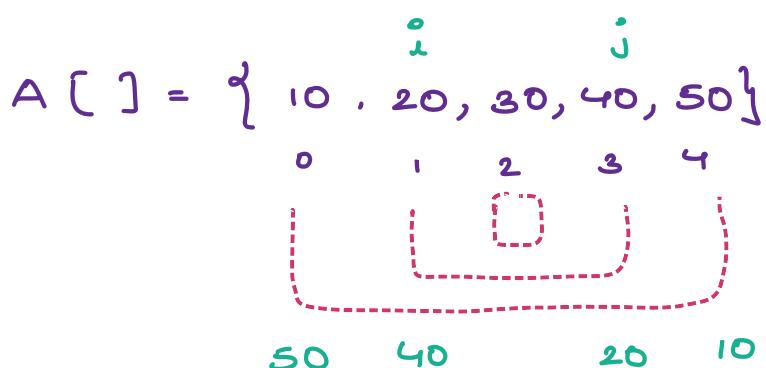
```

int [] reverse ( int [ ] arr ) {
    int [ ] ans = new int [n]; int j=0
    for ( i=n-1; i ≥ 0; i-- ) {
        ans [j] = arr [i];
        j++;
    }
    return ans;
}

```

TC: O(N)  
SC: O(1)

\* Without taking extra memory

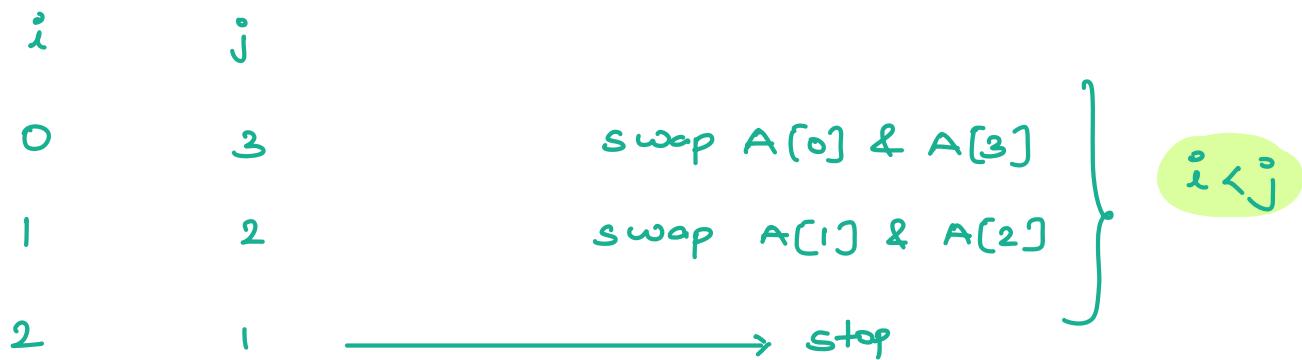


i	j	
0	4	swap $A[0]$ & $A[4]$
1	3	swap $A[1]$ & $A[3]$
2	2	stop

$i < j$

$A[ ] = \{ 10, 20, 30, 40 \}$

40 30 20 10



void reverse (int [] ar) {

```
int i = 0
int j = n - 1
while (i < j) {
    int t = A[i] ✓
    A[i] = A[j]
    A[j] = t
    i++; j--;
```

TC: O(n)  
SC: O(1)

Q Given an array, st, e . Reverse the array from st to e .

```
void reverseRange (int [] arr, int s, int e) {
```

```
    int i = s
    int j = e
    while (i < j) {
        int t = A[i] ✓
        A[i] = A[j]
        A[j] = t
        i++; j--;
    }
}
```

TC: O(n)  
SC: O(1)

### \* Rotate array

Q Given an array of size N. Rotate the array from right to left/anticlockwise K times.

A [] = 

1	2	3	4	5	6
0	1	2	3	4	5

      K=3

K=1 

6	1	2	3	4	5
0	1	2	3	4	5

K=2 

5	6	1	2	3	4
0	1	2	3	4	5

$k=3$

4	5	6	1	2	3
0	1	2	3	4	5

$k=4$

3	4	5	6	1	2
0	1	2	3	4	5

Brute force  $\rightarrow$  Pick the last element, move it in the front & move <sup>rest of</sup> <sub>^</sub> elements on the RHS  
 $k$  times

```
void rotate ( int [] A, int k )
```

```
for ( i=0 ; i < k ; i++ ) {
```

$n \rightarrow$  size of array

```
    int last = A [n-1]
```

```
    for ( j=n-2 ; j ≥ 0 ; j-- ) {
```

$Tc : O(k * n)$

```
        A [j+1] = A [j];
```

$Sc : O(1)$

```
    }
```

```
    A [0] = last;
```

}

3

$j$	$\downarrow$						$\downarrow$	
$A[ ] =$		5	6	1	2	3	4	

0 1 2 3 4 5

$k=2$

$n=6$

$i=0 \quad 0 < 2$   
 $+ \quad 1 < 2$   
 $2 \quad 2 < 2 \times$

$$\text{last} = A[5] = 5 \quad A[j+1] = A[j]$$

$j=4$	$4 \geq 0$	$A[4+1] = A[4]$
3	$3 \geq 0$	$A[3+1] = A[3]$
2	$2 \geq 0$	$A[2+1] = A[2]$
1	$1 \geq 0$	$A[1+1] = A[1]$
0	$0 \geq 0$	$A[0+1] = A[0]$

### Observation

$A[ ] =$	10 20 30 40 50 60 70 80 90	$k=3$
	0 1 2 3 4 5 6 7 8	

Reverse	$A[ ] =$	90 80 70 60 50 40 30 20 10
$A[ ]$		0 1 2 3 4 5 6 7 8

Reverse	$A[ ] =$	70 80 90 60 50 40 30 20 10
blue		0 1 2 3 4 5 6 7 8

Reverse	$A[ ] =$	70 80 90 10 20 30 40 50 60
green		0 1 2 3 4 5 6 7 8

$A[ ] =$	70 80 90 10 20 30 40 50 60
	0 1 2 3 4 5 6 7 8

```
void rotate ( int [ ] A, int K ) {
```

```
    K = K % n
```

```
    if ( K == 0 ) return ;
```

```
reverseRange ( A, 0, n - 1 )
```

Tc : O(n)

```
reverseRange ( A, 0, K - 1 )
```

Sc : O(1)

```
reverseRange ( A, K, n - 1 )
```

3

A [ ] = { 1, 2, 3, 4 }

K = 0 { 1, 2, 3, 4 }

K = 1 { 4, 1, 2, 3 }

K = 9 → 1

K = 2 { 3, 4, 1, 2 }

K = 10 → 2

K = 3 { 2, 3, 4, 1 }

K = 7 → 3

K = 4 { 1, 2, 3, 4 }

K = 9 % 4 → 1

K = 5 { 4, 1, 2, 3 }

K = 10 % 4 → 2

K = 6 { 3, 4, 1, 2 }

K = 7 % 4 → 3

K = 7 { 2, 3, 4, 1 }

K = 8 { 1, 2, 3, 4 }

K = 9 { 4, 1, 2, 3 }

\* Dynamic Arrays → Automatic resizing

Drawback of normal Arrays → fixed size

- Strength → Accessing of elements is  $O(1)$
- Resize itself whenever elements are increased

Weakness → Adding elements

1	2	3	...	
0	1	2	3	4

$$Lf = 0.7$$

$$0.7 * 5 \\ = 3.5$$



1	2	3	4					
0	1	2	3	4	5	6	7	8

$$0.7 \approx 10 \\ = 7 \text{ elements}$$

TC to add elements ⇒ Amortized  $O(1)$

Average  $O(1)$

Please don't  
miss it.

Next class → prefix array → When?

How?

Problem based Prefix array