Homework 1

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Loading the Relevant Libraries.

```
library(plyr)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:plyr':
##
       arrange, count, desc, failwith, id, mutate, rename, summarise,
##
##
       summarize
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library(glmnet)
## Loading required package: Matrix
## Loaded glmnet 4.1-3
library(mgcv)
## Loading required package: nlme
##
## Attaching package: 'nlme'
## The following object is masked from 'package:dplyr':
##
##
       collapse
## This is mgcv 1.8-38. For overview type 'help("mgcv-package")'.
library(Metrics)
library(fastDummies)
library(data.table)
```

```
##
## Attaching package: 'data.table'
## The following objects are masked from 'package:dplyr':
##
## between, first, last
```

Setting the Seed and Working Directory.

```
set.seed(1)
setwd('/Users/aryan/Desktop/MSBA_Spring_22/Machine Learning /Homework_1')
```

Loading the Dataset.

```
data("dji30ret", package = "rugarch")
head(dji30ret)
##
                                   AXP
                                                BA
                                                            BAC
                       AΑ
C
## 1987-03-16 -0.024466052 -0.006329135 -0.018158735 -0.007142888
                                                                0.00000000
## 1987-03-17 0.024466052 0.007905180 0.003919012 0.007142888
                                                                 0.00000000
0
              0.000000000 0.012519725 0.005201572 0.017637141
                                                                 0.03524593
## 1987-03-18
## 1987-03-19 0.020927520 0.001554002 -0.005201572
                                                    0.006968669
                                                                 0.02564243
## 1987-03-20 -0.002962965 -0.018809332 0.033336420 0.017212129 -0.00847462
## 1987-03-23 0.002962965 -0.004758137 -0.006325132 -0.003418807 0.01268516
0
##
                      CAT
                                 CVX
                                             DD
                                                         DIS
                                                                      GE
## 1987-03-16 -0.010810916 0.02030527
                                     0.00000000 -0.021713760 -0.00806456
## 1987-03-17
              0.002713706 0.03295191 0.03913300
                                                 0.035932009
                                                              0.02004075
## 1987-03-18 -0.013642776 0.02085080 0.02169282
                                                 0.000000000 -0.01197619
## 1987-03-19
              0.019048195 0.00000000 -0.01950224 -0.009456335
                                                              0.00000000
## 1987-03-20 0.010723963 0.01886848
                                     0.02378491
                                                 0.009456335
                                                              0.01988137
## 1987-03-23
              0.015873349 0.01698883
                                     0.02427560
                                                 0.020955365
                                                              0.02718614
##
                       GM
                                  HD
                                             HPQ
                                                          IBM
                                                                     INTC
## 1987-03-16 -0.011825128 -0.02105341 -0.01129956 -0.001693481 0.03077166
## 1987-03-17
              0.008685408
                           0.00000000
                                      0.04445176
                                                  0.016807118
                                                               0.05884050
## 1987-03-18 -0.003938564 0.08167803 -0.01754431 -0.005850414 0.01418463
## 1987-03-19
              0.005509656
                          0.01941809
                                      0.03264708
                                                  0.005016733
                                                               0.04138522
## 1987-03-20
              0.004698521 0.03774033
                                                  0.011196468 -0.01360565
                                      0.01698555
## 1987-03-23
              0.013964540 0.03636764 -0.01058211
                                                  0.007395268
                                                               0.00000000
##
                      JNJ
                                   JPM
                                              AIG
                                                            K0
                                                                        MCD
## 1987-03-16 -0.010810916 -0.012205906 0.000000000 -0.020408872 -0.012396853
## 1987-03-17
              0.007702220
                                                                0.018538121
## 1987-03-18 -0.008032172 -0.003472226 0.000000000 -0.002560821 -0.018538121
## 1987-03-19
              0.000000000 -0.001740644 0.000000000
                                                   0.020305266
                                                                0.002076844
## 1987-03-20
              0.013351333 -0.003490405 0.058738817
                                                   0.000000000
                                                                0.018500014
## 1987-03-23 0.018397365 0.010434877 0.018288124 0.012484557 0.032066876
```

```
MRK
##
                                                           PFE
                                                                        PG
                      MMM
                                             MSFT
## 1987-03-16 -0.006079046 0.013216051
                                       0.00000000 -0.005633818 -0.022663860
## 1987-03-17 0.021713760 0.034411998 0.04082199
                                                  0.005633818 0.011396135
## 1987-03-18 -0.003586376 0.000000000
                                       0.03922071
                                                   0.011173301 0.011267725
## 1987-03-19 0.020154802 -0.006362694
                                       0.03774033
                                                   0.005540180
                                                               0.011142177
## 1987-03-20
              0.026637360
                          0.025211419 -0.03774033
                                                   0.005509656
                                                               0.002766253
              0.011363759 -0.002076844
                                       0.00000000
                                                   0.005479466
                                                                0.010989122
## 1987-03-23
##
                        Τ
                                  UTX
                                                ٧Z
                                                           WMT
                                                                        X0
Μ
## 1987-03-16 -0.002528446 -0.002509412 -0.004590674 -0.019868203 -0.00597016
7
## 1987-03-17 0.000000000 0.010000083 0.001532567 0.009983444 0.02756080
## 1987-03-18 -0.002534856 -0.007490672 -0.013878403 -0.006644543 0.01158314
1
## 1987-03-19 0.005063302 0.002503130 0.006191970 0.003327790 -0.00577479
## 1987-03-20 0.017522351 0.000000000 0.006153866 0.022989518
                                                               0.00960622
## 1987-03-23 0.002478316 -0.005012542 0.009160369 0.022472856
                                                                0.02827709
```

Question 1

```
print(dim(dji30ret))
## [1] 5521
              30
print(summary(dji30ret))
##
          AA
                              AXP
                                                    BA
## Min.
           :-0.2745595
                                :-0.3034304
                                                     :-0.1938568
                         Min.
                                              Min.
##
   1st Qu.:-0.0114593
                         1st Qu.:-0.0109291
                                              1st Qu.:-0.0098007
## Median : 0.0000000
                         Median : 0.0000000
                                              Median : 0.0000000
                                : 0.0001687
##
          : 0.0001608
                                                   : 0.0003058
   Mean
                         Mean
                                              Mean
    3rd Qu.: 0.0116377
                         3rd Qu.: 0.0114812
                                              3rd Qu.: 0.0105709
          : 0.2087337
                                                    : 0.1439727
##
   Max.
                         Max.
                                : 0.1712035
                                              Max.
         BAC
                                                   CAT
##
                               C
   Min. :-0.3420588
                               :-0.3056056
                         Min.
                                                     :-0.244156
##
                                              Min.
    1st Qu.:-0.0093365
##
                         1st Qu.:-0.0111602
                                              1st Qu.:-0.010575
   Median : 0.0000000
                         Median : 0.0000000
                                              Median : 0.000000
##
##
   Mean
         : 0.0001149
                         Mean
                                : 0.0000796
                                              Mean
                                                   : 0.000378
    3rd Qu.: 0.0100293
                         3rd Qu.: 0.0116803
                                              3rd Qu.: 0.011141
          : 0.2698774
                              : 0.4572902
                                                    : 0.137371
##
    Max.
                         Max.
                                              Max.
##
        CVX
                               DD
                                                   DIS
##
                                :-0.2018984
    Min.
           :-0.1812526
                         Min.
                                              Min.
                                                     :-0.3426451
##
    1st Qu.:-0.0082829
                         1st Qu.:-0.0093255
                                              1st Qu.:-0.0102932
##
   Median : 0.0000000
                         Median : 0.0000000
                                              Median : 0.0000000
##
   Mean
         : 0.0004538
                         Mean
                                : 0.0001774
                                              Mean : 0.0002886
##
    3rd Qu.: 0.0095239
                         3rd Qu.: 0.0095836
                                              3rd Qu.: 0.0105821
   Max. : 0.1894765
                         Max. : 0.1086964
                                              Max. : 0.1756133
```

```
##
         GE
                               GΜ
                                                     HD
##
   Min.
           :-0.1947441
                         Min.
                                :-0.3727220
                                               Min.
                                                      :-0.3386365
    1st Qu.:-0.0083683
##
                         1st Qu.:-0.0119502
                                               1st Qu.:-0.0115889
##
   Median : 0.0000000
                         Median : 0.0000000
                                               Median : 0.0000000
##
    Mean
          : 0.0002751
                         Mean
                                :-0.0002715
                                               Mean
                                                    : 0.0006922
##
    3rd Qu.: 0.0093459
                         3rd Qu.: 0.0115692
                                               3rd Qu.: 0.0127656
##
    Max.
          : 0.1275967
                         Max. : 0.3009365
                                               Max. : 0.1315251
         HP0
                              IBM
##
                                                   INTC
##
    Min.
          :-0.2263815
                         Min.
                                :-0.268161
                                              Min.
                                                     :-0.2488610
##
    1st Qu.:-0.0125577
                         1st Qu.:-0.009243
                                              1st Qu.:-0.0139915
                         Median : 0.000000
                                              Median : 0.0000000
##
    Median : 0.0000000
##
   Mean
         : 0.0003792
                         Mean : 0.000249
                                              Mean
                                                     : 0.0005553
##
    3rd Qu.: 0.0135366
                         3rd Qu.: 0.009469
                                              3rd Qu.: 0.0158734
##
    Max.
          : 0.1591410
                         Max.
                               : 0.123635
                                              Max.
                                                     : 0.2265276
##
         ZNZ
                              JPM
                                                    AIG
##
    Min.
          :-0.2043813
                         Min.
                                :-0.3234769
                                               Min.
                                                      :-0.9362581
##
    1st Qu.:-0.0078036
                         1st Ou.:-0.0111299
                                               1st Ou.:-0.0089217
##
   Median : 0.0000000
                         Median : 0.0000000
                                               Median : 0.0000000
          : 0.0004993
                                : 0.0002586
##
    Mean
                         Mean
                                               Mean
                                                      :-0.0002978
##
    3rd Qu.: 0.0084695
                         3rd Qu.: 0.0111094
                                               3rd Qu.: 0.0094814
##
          : 0.1153126
                               : 0.2239172
                                               Max. : 0.3585320
    Max.
                         Max.
          K0
##
                              MCD
                                                    MMM
                                :-0.1827990
##
   Min.
           :-0.2828628
                         Min.
                                               Min.
                                                      :-0.2257926
##
    1st Qu.:-0.0080020
                         1st Qu.:-0.0093024
                                               1st Qu.:-0.0074074
    Median : 0.0000000
                         Median : 0.0000000
                                               Median : 0.0000000
##
    Mean
          : 0.0004333
                         Mean
                                : 0.0004514
                                               Mean : 0.0003322
##
    3rd Qu.: 0.0089027
                         3rd Qu.: 0.0099834
                                               3rd Qu.: 0.0082499
##
    Max.
          : 0.1791113
                         Max.
                                : 0.1030806
                                               Max. : 0.1049975
##
         MRK
                              MSFT
                                                   PFE
##
           :-0.3119154
                                :-0.379490
                                                     :-0.1892420
   Min.
                         Min.
                                              Min.
    1st Qu.:-0.0090772
##
                         1st Qu.:-0.010643
                                              1st Qu.:-0.0096386
    Median : 0.0000000
##
                         Median : 0.000000
                                              Median : 0.0000000
##
    Mean
           : 0.0003447
                         Mean
                                : 0.000787
                                              Mean
                                                     : 0.0003885
##
    3rd Qu.: 0.0100307
                         3rd Qu.: 0.012848
                                              3rd Qu.: 0.0107528
                         Max. : 0.178465
##
    Max.
          : 0.1224923
                                              Max.
                                                    : 0.0989399
                               Т
##
          PG
                                                    UTX
##
   Min.
          :-0.3598917
                         Min.
                                :-0.1352280
                                               Min.
                                                      :-0.3029024
##
    1st Qu.:-0.0074074
                         1st Qu.:-0.0087377
                                               1st Qu.:-0.0083770
##
    Median : 0.0000000
                         Median : 0.0000000
                                               Median : 0.0000000
##
    Mean
           : 0.0004917
                         Mean
                                : 0.0003364
                                               Mean
                                                     : 0.0004517
    3rd Qu.: 0.0085107
                         3rd Qu.: 0.0096619
                                               3rd Qu.: 0.0098064
##
    Max.
          : 0.1980376
                         Max.
                                : 0.1505242
                                               Max.
                                                     : 0.1278841
##
                                                    MOX
          ٧Z
                              WMT
##
   Min.
          :-0.1931448
                         Min. :-0.1249721
                                               Min.
                                                      :-0.2676996
    1st Qu.:-0.0087802
                         1st Qu.:-0.0100137
                                               1st Qu.:-0.0078818
##
##
   Median : 0.0000000
                         Median : 0.0000000
                                               Median : 0.0000000
##
   Mean
         : 0.0002848
                         Mean : 0.0004985
                                               Mean : 0.0004964
##
    3rd Qu.: 0.0089366
                         3rd Qu.: 0.0104713
                                               3rd Qu.: 0.0090419
    Max. : 0.1365130
                         Max. : 0.1146918
                                               Max. : 0.1653925
```

Question 2A

Question 2B

```
aa <- aa %>% bind_cols(data.frame(t(ldply(1:5, lag, x= (dji30ret$AA))))) #Add
ing lagged returns of AA using some R magic
aa <- na.omit(aa) #Removing NAs</pre>
head(aa)
##
                   Target
                                    X1
                                                 X2
                                                              X3
                                                                           Х
4
## 1987-03-23 0.002962965 -0.002962965 0.020927520 0.000000000 0.02446605
2
## 1987-03-24 0.017595762 0.002962965 -0.002962965 0.020927520 0.00000000
## 1987-03-25 0.005797118 0.017595762 0.002962965 -0.002962965 0.02092752
## 1987-03-26 -0.032308243 0.005797118 0.017595762 0.002962965 -0.00296296
## 1987-03-27 0.000000000 -0.032308243 0.005797118 0.017595762 0.00296296
## 1987-03-30 -0.024170361 0.000000000 -0.032308243 0.005797118 0.01759576
2
##
                       X5
## 1987-03-23 -0.024466052
## 1987-03-24 0.024466052
## 1987-03-25 0.000000000
## 1987-03-26 0.020927520
## 1987-03-27 -0.002962965
## 1987-03-30 0.002962965
```

Question 2B (continued)

```
print(summary(aa))
                                                 X2
##
                              X1
       Target
## Min.
          :-0.2745595
                               :-0.274560
                                                 :-0.2745595
                        Min.
                                            Min.
## 1st Qu.:-0.0114625
                        1st Qu.:-0.011463
                                            1st Qu.:-0.0114461
## Median : 0.0000000
                        Median : 0.000000
                                            Median : 0.0000000
## Mean
         : 0.0001576
                        Mean : 0.000149
                                                  : 0.0001552
                                            Mean
## 3rd Qu.: 0.0116305 3rd Qu.: 0.011618
                                            3rd Qu.: 0.0116305
```

```
Max. : 0.2087337
                       Max. : 0.208734
                                         Max. : 0.2087337
##
         X3
                            Χ4
                                                X5
         :-0.2745595
                            :-0.2745595
## Min.
                       Min.
                                          Min.
                                                 :-0.2745595
## 1st Qu.:-0.0114343
                       1st Qu.:-0.0114295
                                          1st Qu.:-0.0114343
## Median : 0.0000000
                       Median : 0.0000000
                                          Median : 0.0000000
                                          Mean : 0.0001733
## Mean
         : 0.0001697
                       Mean
                             : 0.0001807
## 3rd Qu.: 0.0116305
                       3rd Qu.: 0.0116378
                                           3rd Qu.: 0.0116305
## Max. : 0.2087337
                       Max. : 0.2087337
                                          Max. : 0.2087337
```

Question 2C

```
x <- model.matrix(Target~.,aa)[,-1]
y <- aa$Target
print(which(rownames(aa) %in% c("1987-03-23", "2002-12-31"))) #Finding out th
e indices for the relevant dates.
## [1] 1 3983
print(which(rownames(aa) %in% c("2003-01-01", "2009-02-03")))
## [1] 5516</pre>
```

As we can see, the range for the training data is from index 1 to index 3983, while the range for the testing data is from index 3984 to index 5516.

Question 2C (continued)

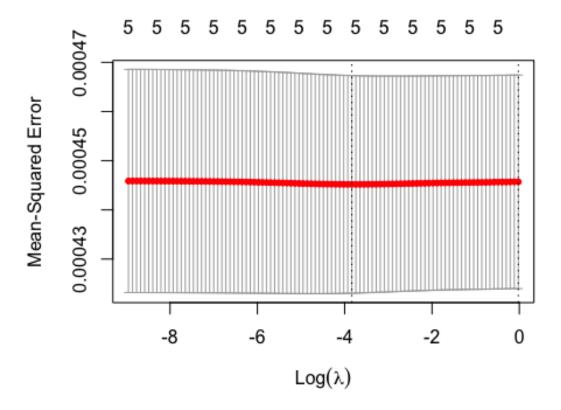
```
#Train-Test Split
x_train <- x[1:3983,]
x_test <- x[3984:5516,]
y_train <- y[1:3983]
y_test <- y[3984:5516]

#Initial Model Fit
grd <- 10 ^ seq( 10, -2, length = 100)
set.seed(1)
ridge_mod <- glmnet(x_train, y_train, alpha=0, lambda = grd, thresh = 1e-12)

#Cross-Validation
cv.out <- cv.glmnet(x_train, y_train, alpha = 0, nfolds=5)
plot(cv.out)</pre>
```

¹ For some reason, R didn't compile this block of code, so I had to take a screenshot.

Question 2C (continued)



Question 2C (continued)

```
bestlam <- cv.out$lambda.min
print(bestlam)
## [1] 0.02156627</pre>
```

The optimal lambda, in this case, is 0.02156627. Therefore, we will use this value when fitting our model.

Question 2C (continued)

```
#Fitting Model using Optimal Lambda
set.seed(1)
ridge_mod <- glmnet(x_train, y_train, alpha=0, lambda = bestlam)</pre>
print(summary(ridge_mod))
##
                               Mode
             Length Class
                               numeric
## a0
             1
                     -none-
## beta
             5
                     dgCMatrix S4
## df
             1
                     -none-
                               numeric
## dim
             2
                               numeric
                     -none-
## lambda
                     -none-
                               numeric
```

```
## dev.ratio 1
                     -none-
                               numeric
## nulldev 1
## npasses 1
## jerr 1
## call 5
                               numeric
                     -none-
                     -none-
                               numeric
                     -none-
                               numeric
                               logical
                     -none-
                               call
                     -none-
## nobs 1
                     -none-
                               numeric
```

Question 2D

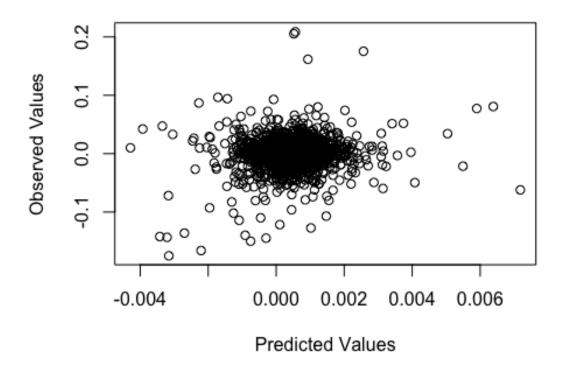
```
#Predicting Model
set.seed(1)
ridge_pred <- predict(ridge_mod, s = 0, newx = x_test)
print(mae(y_test, ridge_pred))
## [1] 0.01772329</pre>
```

As seen above, the MAE is 0.01772329.

Question 2D (continued)

```
plot(ridge_pred, y_test,xlab = "Predicted Values", ylab = "Observed Values")
```

² For some reason, R didn't compile this block of code, so I had to take a screenshot.



Conclusions: Even though it might seem like we have a very low mean absolute error, in the context of predicting daily stock returns, the model performs poorly. Essentially, an MAE of 0.0177 implies that our average ABSOLUTE error is 1.77%, and in a data set with a mean daily return of 0.0001576 (0.01576%), the error is quite substantial. In the world of finance, this could lead to huge losses, especially also in the presence of outliers (which are indeed present in our data set). This model is basically an autoregressive model, specifically an AR (5) model, which is rarely utilized in technical analysis to forecast future security prices. This is because we are implicitly assuming that the future will resemble the past, which can prove inaccurate under certain market conditions, such as financial crises, or the surge of 'meme-stocks'.

Furthermore, note that since the number of predictors is a lot lower than the number of observations, and that the relationship between the past 5 lagged returns and today's returns are almost always non-linear, a ridge regression will not perform well, which might explain why our model is performing poorly.

Question 3A

```
df_main <- data.frame(matrix(ncol = 7, nrow = 0))
for (i in colnames(dji30ret)){
   stock_df <- as.data.frame(dji30ret[[i]], row.names = row.names(dji30ret))
   stock_df <- stock_df %>% bind_cols(data.frame(t(ldply(1:5, lag, x= (dji30ret[,i])))))
```

```
stock df <- na.omit(stock df)</pre>
  stock df[7] <- i
  df_main <- rbind(df_main, stock_df)</pre>
colnames(df main) = c('Daily Returns', paste0("Lagged returns ", 1:5), 'Ticke
r_')
for (stock in 2:length(colnames(dji30ret))){
  df_main[stock+6] = dummy_cols(df_main$Ticker, remove_first_dummy = TRUE)[st
ock]
  colnames(df_main)[stock+6] = c(paste0(colnames(dji30ret)[stock],'_dummy'))}
head(df_main)
##
              Daily_Returns Lagged_returns_1 Lagged_returns_2 Lagged_returns_
3
## 1987-03-23
                0.002962965
                                 -0.002962965
                                                    0.020927520
                                                                      0.00000000
0
## 1987-03-24
                0.017595762
                                  0.002962965
                                                   -0.002962965
                                                                      0.02092752
0
## 1987-03-25
                0.005797118
                                  0.017595762
                                                    0.002962965
                                                                     -0.00296296
5
## 1987-03-26
               -0.032308243
                                  0.005797118
                                                    0.017595762
                                                                      0.00296296
## 1987-03-27
                0.000000000
                                 -0.032308243
                                                    0.005797118
                                                                      0.01759576
## 1987-03-30 -0.024170361
                                  0.000000000
                                                   -0.032308243
                                                                      0.00579711
8
##
              Lagged_returns_4 Lagged_returns_5 Ticker_ AXP_dummy BA_dummy
## 1987-03-23
                                     -0.024466052
                   0.024466052
                                                       AA
                                                                   0
## 1987-03-24
                   0.000000000
                                     0.024466052
                                                       AA
                                                                   0
                                                                            0
                                                                            0
## 1987-03-25
                   0.020927520
                                     0.000000000
                                                       AA
                                                                   0
                                                                            0
## 1987-03-26
                   -0.002962965
                                     0.020927520
                                                       AA
                                                                   0
                                                                            0
## 1987-03-27
                    0.002962965
                                     -0.002962965
                                                       AA
                                                                   0
## 1987-03-30
                   0.017595762
                                     0.002962965
                                                       AΑ
                                                                   0
                                                                            0
##
              BAC dummy C dummy CAT dummy CVX dummy DD dummy DIS dummy GE dum
my
## 1987-03-23
                       0
                               0
                                          0
                                                    0
                                                              0
                                                                        0
## 1987-03-24
                       0
                               0
                                          0
                                                    0
                                                              0
                                                                        0
0
## 1987-03-25
                       0
                               0
                                          0
                                                    0
                                                              0
                                                                        0
0
## 1987-03-26
                       0
                                                                        0
                               0
                                          0
                                                    0
                                                              0
0
## 1987-03-27
                       0
                                                                        0
                               0
                                          0
                                                    0
                                                              0
## 1987-03-30
                       0
                               0
                                          0
                                                    0
                                                              0
                                                                        0
0
              GM_dummy HD_dummy HPQ_dummy IBM_dummy INTC_dummy JNJ_dummy JPM_
```

dum	m) (
dum	1987-03-23	0	0	0	0		0	0
0	1907-03-23	0	ð	0	U		Ū	ð
-	1987-03-24	0	0	0	0		0	0
0	1307 03 24	O	O	O	Ü		O	O
	1987-03-25	0	0	0	0		0	0
0	1007-00-20	0	0	0	0		O	O
	1987-03-26	0	0	0	0		0	0
0	1307 03 20	ŭ	ŭ	ŭ	Ü		Ü	Ü
-	1987-03-27	0	0	0	0		0	0
0	130, 03 2,	ŭ	ŭ	· ·	Ū		Ü	Ü
	1987-03-30	0	0	0	0		0	0
0	1507 05 50	· ·	ŭ	· ·	·		Ü	Ü
##		AIG dummy	KO dummy	MCD_dummy	MMM dumm	v MRK dum	mv MSFT d	ummv
	1987-03-23	0	0	0)	<i>9</i>	0
	1987-03-24	0	0	0		9	0	0
	1987-03-25	0	0	0		9	0	0
	1987-03-26	0	0	0		9	0	0
	1987-03-27	0	0	0		9	0	0
	1987-03-30	0	0	0		9	0	Ø
##		PFE dummy	PG dummy	T_dummy U			WMT dummy	XOM dum
my		,		, .	,	,	,	
-	1987-03-23	0	0	0	0	0	0	
0								
##	1987-03-24	0	0	0	0	0	0	
0								
##	1987-03-25	0	0	0	0	0	0	
0								
##	1987-03-26	0	0	0	0	0	0	
0								
##	1987-03-27	0	0	0	0	0	0	
0								
##	1987-03-30	0	0	0	0	0	0	
0								
noint(summanu(df main))								
<pre>print(summary(df_main))</pre>								
##	Daily_Returns Lagged_returns_1 Lagged_returns_2							
##							_	
##	1st Qu.:-0.0095356							
##	Median : 0.0000000 Median : 0.0000000 Median : 0.0000000							
##	Mean : 0.0003194 Mean : 0.0003207 Mean : 0.0003238							
##	3rd Qu.: 0.0103353 3rd Qu.: 0.0103340 3rd Qu.: 0.0103346							
##	Max. : 0.4572902 Max. : 0.4572902 Max. : 0.4572902							
##	Lagged_returns_3 Lagged_returns_4 Lagged_returns_5							
##	Min. :-0.9362581 Min. :-0.9362581 Min. :-0.936258							
##								
##	Median : 0		_	0.000000	_	n : 0.000		
##	Mean : 6			0.000339		: 0.000		
##	3rd Qu.: 0			0.0103414		u.: 0.010		
			-					

```
##
                           Max. : 0.4572902
    Max. : 0.4572902
                                                 Max. : 0.457290
##
                                                                  BAC dummy
      Ticker
                           AXP dummy
                                               BA dummy
##
    Length:165480
                        Min.
                                :0.00000
                                            Min.
                                                    :0.00000
                                                               Min.
                                                                       :0.00000
    Class :character
##
                        1st Qu.:0.00000
                                            1st Qu.:0.00000
                                                               1st Qu.:0.00000
##
    Mode :character
                        Median :0.00000
                                            Median :0.00000
                                                               Median :0.00000
##
                        Mean
                                :0.03333
                                            Mean
                                                    :0.03333
                                                               Mean
                                                                       :0.03333
                                                                3rd Qu.:0.00000
##
                                            3rd Qu.:0.00000
                         3rd Qu.:0.00000
##
                        Max.
                                :1.00000
                                            Max.
                                                    :1.00000
                                                               Max.
                                                                       :1.00000
##
       C_dummy
                          CAT_dummy
                                             CVX_dummy
                                                                  DD_dummy
##
                                                                      :0.00000
    Min.
            :0.00000
                       Min.
                               :0.00000
                                           Min.
                                                   :0.00000
                                                              Min.
##
    1st Qu.:0.00000
                       1st Qu.:0.00000
                                           1st Qu.:0.00000
                                                               1st Qu.:0.00000
                       Median :0.00000
##
    Median :0.00000
                                           Median :0.00000
                                                               Median :0.00000
##
    Mean
            :0.03333
                       Mean
                               :0.03333
                                           Mean
                                                   :0.03333
                                                              Mean
                                                                      :0.03333
##
    3rd Qu.:0.00000
                       3rd Qu.:0.00000
                                           3rd Qu.:0.00000
                                                               3rd Qu.:0.00000
##
    Max.
            :1.00000
                       Max.
                               :1.00000
                                           Max.
                                                   :1.00000
                                                              Max.
                                                                      :1.00000
##
      DIS dummy
                           GE dummy
                                              GM dummy
                                                                  HD dummy
##
    Min.
            :0.00000
                       Min.
                               :0.00000
                                           Min.
                                                   :0.00000
                                                              Min.
                                                                      :0.00000
##
    1st Qu.:0.00000
                       1st Qu.:0.00000
                                           1st Qu.:0.00000
                                                               1st Qu.:0.00000
##
    Median :0.00000
                       Median :0.00000
                                           Median :0.00000
                                                               Median :0.00000
##
    Mean
                                                              Mean
            :0.03333
                       Mean
                               :0.03333
                                           Mean
                                                   :0.03333
                                                                      :0.03333
##
    3rd Qu.:0.00000
                       3rd Qu.:0.00000
                                           3rd Qu.:0.00000
                                                               3rd Qu.:0.00000
##
    Max.
            :1.00000
                       Max.
                               :1.00000
                                           Max.
                                                   :1.00000
                                                               Max.
                                                                      :1.00000
##
      HPQ_dummy
                          IBM_dummy
                                             INTC_dummy
                                                                 JNJ_dummy
##
            :0.00000
                               :0.00000
                                                   :0.00000
                                                                      :0.00000
    Min.
                       Min.
                                           Min.
                                                              Min.
##
    1st Qu.:0.00000
                       1st Qu.:0.00000
                                           1st Qu.:0.00000
                                                               1st Qu.:0.00000
##
    Median :0.00000
                       Median :0.00000
                                           Median :0.00000
                                                               Median :0.00000
##
    Mean
                       Mean
                                                              Mean
            :0.03333
                               :0.03333
                                           Mean
                                                   :0.03333
                                                                      :0.03333
##
    3rd Qu.:0.00000
                       3rd Qu.:0.00000
                                           3rd Qu.:0.00000
                                                               3rd Qu.:0.00000
##
    Max.
           :1.00000
                               :1.00000
                                                   :1.00000
                                                              Max.
                                                                      :1.00000
                       Max.
                                           Max.
##
      JPM dummy
                         AIG dummy
                                              KO dummy
                                                                MCD dummy
##
    Min.
            :0.00000
                               :0.00000
                                           Min.
                                                   :0.00000
                                                                      :0.00000
                       Min.
                                                              Min.
##
    1st Qu.:0.00000
                       1st Qu.:0.00000
                                           1st Qu.:0.00000
                                                               1st Qu.:0.00000
##
    Median :0.00000
                       Median :0.00000
                                           Median :0.00000
                                                              Median :0.00000
##
    Mean
           :0.03333
                       Mean
                               :0.03333
                                           Mean
                                                   :0.03333
                                                               Mean
                                                                      :0.03333
##
    3rd Qu.:0.00000
                       3rd Qu.:0.00000
                                           3rd Qu.:0.00000
                                                               3rd Qu.:0.00000
##
    Max.
            :1.00000
                               :1.00000
                                                   :1.00000
                                                                      :1.00000
                       Max.
                                           Max.
                                                              Max.
##
      MMM dummy
                         MRK_dummy
                                             MSFT dummy
                                                                 PFE_dummy
##
    Min.
            :0.00000
                               :0.00000
                                                   :0.00000
                                                                      :0.00000
                       Min.
                                           Min.
                                                              Min.
##
    1st Qu.:0.00000
                       1st Qu.:0.00000
                                           1st Qu.:0.00000
                                                               1st Qu.:0.00000
##
    Median :0.00000
                       Median :0.00000
                                           Median :0.00000
                                                              Median :0.00000
##
    Mean
           :0.03333
                               :0.03333
                                                   :0.03333
                                                              Mean
                       Mean
                                           Mean
                                                                      :0.03333
##
    3rd Qu.:0.00000
                       3rd Qu.:0.00000
                                           3rd Qu.:0.00000
                                                               3rd Qu.:0.00000
##
    Max.
           :1.00000
                       Max.
                               :1.00000
                                                   :1.00000
                                                              Max.
                                                                      :1.00000
##
       PG dummy
                           T dummy
                                             UTX dummy
                                                                  VZ dummy
##
                               :0.00000
           :0.00000
                                           Min.
                                                   :0.00000
                                                              Min.
                                                                      :0.00000
    Min.
                       Min.
##
    1st Qu.:0.00000
                       1st Qu.:0.00000
                                           1st Qu.:0.00000
                                                               1st Qu.:0.00000
##
    Median :0.00000
                       Median :0.00000
                                           Median :0.00000
                                                              Median :0.00000
##
    Mean
           :0.03333
                       Mean
                               :0.03333
                                           Mean
                                                   :0.03333
                                                              Mean
                                                                      :0.03333
##
    3rd Qu.:0.00000
                       3rd Qu.:0.00000
                                           3rd Qu.:0.00000
                                                               3rd Qu.:0.00000
    Max. :1.00000
                       Max. :1.00000
                                           Max. :1.00000
                                                              Max. :1.00000
```

```
##
     WMT dummy
                       XOM dummy
## Min.
          :0.00000
                     Min.
                            :0.00000
## 1st Qu.:0.00000
                     1st Qu.:0.00000
## Median :0.00000
                     Median :0.00000
## Mean
          :0.03333
                     Mean
                            :0.03333
## 3rd Qu.:0.00000
                     3rd Qu.:0.00000
## Max. :1.00000
                     Max. :1.00000
```

Question 3A (continued)

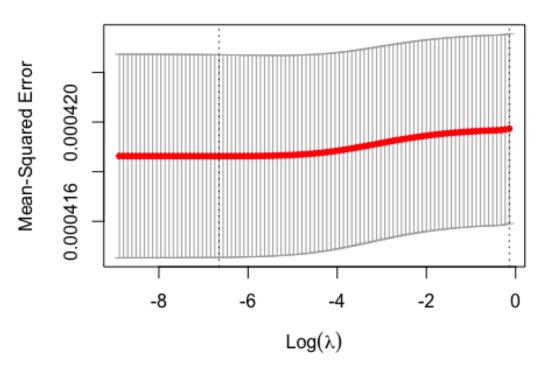
```
print(dim(df_main))
## [1] 165480 36
```

Question 3B

```
df_main <- setDT(df_main, keep.rownames = TRUE)[]</pre>
df_main$rn <- as.Date(df_main$rn, format= "%Y-%m-%d")
train <- subset(df_main, rn>= "1987-03-16" & rn <= "2002-12-31")
train <- subset(train, select = -c(Ticker_) ) #Don't need this column anymore
train <- subset(train, select = -c(rn) ) #Don't need this column anymore
test <- subset(df_main, rn>= "2003-01-01" & rn <= " 2009-02-03")
test <- subset(test, select = -c(Ticker_) ) #Don't need this column anymore
test <- subset(test, select = -c(rn)) #Don't need this column anymore
x_train <- model.matrix(Daily_Returns~.,train)[,-1] #Convert to numeric to avoid errors.</pre>
x_train <- x_train[, 1:5 ]
x_test <- model.matrix(Daily_Returns~.,test)[,-1]</pre>
x_test <- x_test[, 1:5]
y_train <- train[, 1]
y_train <- as.numeric(unlist(y_train)) #Convert to numeric to avoid errors.
y_test <- test[, 1]
y_test <- as.numeric(unlist(y_test))</pre>
grd <- 10 ^ seq( 10, -2, length = 100)
set.seed(1)
ridge_mod <- glmnet(x_train, y_train, alpha=0, lambda = grd)
cv.out <- cv.glmnet(x_train, y_train, alpha = 0, nfolds=5)</pre>
plot(cv.out)
3
```

³ For some reason, R didn't compile this block of code, so I had to take a screenshot.





Question 3B (continued)

```
bestlam <- cv.out$lambda.min
print(bestlam)
## [1] 0.001291421</pre>
```

Question 3B (continued)

```
grd <- 10 ^ seq( 10, -2, length = 100)
set.seed(1)
ridge_mod <- glmnet(x_train, y_train, alpha=0, lambda = bestlam)</pre>
print(summary(ridge_mod))
##
              Length Class
                                Mode
## a0
              1
                     -none-
                                numeric
## beta
              5
                     dgCMatrix S4
## df
              1
                      -none-
                                numeric
              2
## dim
                     -none-
                                numeric
## lambda
              1
                      -none-
                                numeric
## dev.ratio 1
                                numeric
                     -none-
## nulldev
              1
                      -none-
                                numeric
## npasses
              1
                      -none-
                                numeric
## jerr
              1
                      -none-
                                numeric
## offset
              1
                     -none-
                                logical
```

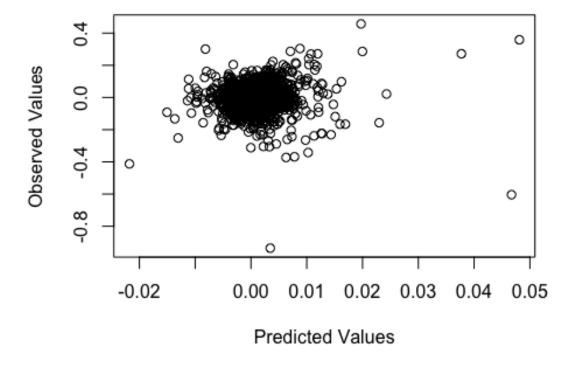
```
## call 5 -none- call
## nobs 1 -none- numeric
```

Question 3C

```
set.seed(1)
ridge_pred <- predict(ridge_mod, s = 0, newx = x_test)
print(mae(y_test, ridge_pred))
## [1] 0.0127123</pre>
```

Question 3C (continued)

```
plot(ridge_pred, y_test,xlab = "Predicted Values", ylab = "Observed Values")
4
```



Conclusions: Compared to our previous model, we notice that this model performs better in terms of MAE, with a lower MAE of 0.0127. One reasonable explanation for a lower MAE could be that we have more observations. Also note that the mean daily average return for

⁴ For some reason, R didn't compile this block of code, so I had to take a screenshot.

this data set is 0.0003194, which is 0.03194%, and since our average ABSOLUTE error is 1.27%, this model is still a very poor model (although still better than the previous model). This is because the number of observations is a lot higher than the number of predictors and the relationship between the past 5 lagged returns and daily returns is again almost never linear, so a ridge regression is not a viable choice at the end of the day.

Question 3D

Yes. We can include the dummy variables in our data set as possible features that could help us predict the daily returns. This will increase the number of predictors and add complexity to our model, which theoretically should reduce bias and improve the error. On a more intuitive level, the stock ticker (stock name) should contain at some level of information about the company, which can lead to better fit of the model. Moreover, we could also include interactions between dummy variables to capture industry-wide trends (e.g. interact all technology stocks), which may add robustness to the model.