

A - Find the number that appear once and others twice
 $\text{arr}[] = \{1, 1, 2, 3, 3, 4, 4\}$

Brute:

$n = \text{arr.size}();$ (Sorted assumption)

int maxi = arr[n-1];

int visi[maxi+1] = {0};

```
for (int i=0; i<n; i++)  
    visi[arr[i]]++;
```

}

```
for (int i=0; i<=maxi; i++)  
    if (visi[i] == 1)  
        cout << i  
        break;
```

}

if not sorted then find
 $\text{maxi} = \text{arr}[0];$
for ($i = 0$ to n) {
 if ($\text{A}[i] > \text{maxi}$) {
 maxi = A[i]
 }
}

T.C $\rightarrow O(N+N)$

S.C $\rightarrow O(N)$

Optimal: for sorted & other appear twice only

```
for (i=0; i<n-1; i+=2)  
    if (A[i] != A[i+1]) {  
        cout << A[i];  
    }  
}
```

T.C $\rightarrow O(n)$

S.C $\rightarrow O(1)$

// if single element is last
cout << A[n-1]

Best Sol is XOR Method

XOR:
~~then bind~~
~~Σ~~
~~axi);~~
~~i]~~

```

int XOR = 0;
for(i = 0 → n) {
    XOR = XOR ^ A[i];
}
cout << XOR
    
```

$T \cdot C \rightsquigarrow O(n)$
 $S \cdot C \rightsquigarrow O(1)$

Q- Longest Subarray with sum k
 $\text{arr}[] = \{1, 2, 3, 1, 1, 1, 1, 4, 2, 3\}$ $k=3$

Generate all subarray
 $(i \rightarrow j)$

$A[] = \{ \overset{i}{1}, \overset{j}{2}, \overset{k}{3}, 1, 1, 1, 1, 4, 2, 3 \}$

Brute:

```

int lcn=0;
for(i = 0; i < n; i++) {
    for(j = i; j < n; j++) {
        sum = 0;
        for(k = i → j) {
            sum = sum + A[k];
        }
        if(sum == k) lcn = max(lcn; j - i + 1);
    }
}
print(lcn)
    
```

$T \cdot C \rightsquigarrow O(n^3)$
 $S \cdot C \rightsquigarrow O(1)$

we can optimize it by

```

for(i = 0 → n) {
    sum = 0;
    for(j = 0 → n) {
        sum = sum + A[j];
    }
    if(sum == k) lcn = max(lcn, j - i + 1);
}
    
```

$T \cdot C \rightsquigarrow O(n^2)$
 $S \cdot C \rightsquigarrow O(1)$

Note: Any time you deal with sum use

long long

especially when:

- prefix sum
- Sliding window
- Subarray sum
- constraint have to $\leq 10^9$ etc.

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Optimal:

```
int longestSub(int A[], int n, long long k) {
```

```
    int left = 0, right = 0;
```

```
    long long sum = A[0];
```

```
    int maxlen = 0;
```

```
    while (right < n) {
```

```
        while (left <= right && sum > k) {
```

```
            sum = sum - A[left];
```

```
            left++;
```

```
}
```

```
        if (sum == k) {
```

```
            int len = right - left + 1;
```

shrink if sum > k

```
            if (len > maxlen) {
```

```
                maxlen = len;
```

```
}
```

```
}
```

```
        right++;
```

```
        if (right < n) {
```

```
            sum = sum + A[right];
```

```
}
```

```
}
```

```
    return maxlen;
```

```
}
```

Move right pointer

$\{1, 2, 3, 1, 1, 1, 1, 3, 3\}$
 $\uparrow \uparrow \uparrow \uparrow \uparrow \uparrow \uparrow \uparrow$
 $\uparrow \uparrow \uparrow \uparrow \uparrow \uparrow \uparrow \uparrow$ $k=6$

Sum = 1 3 4 7 6 7

5 6 7

4 7 6 9

3 7 6

$len = 6$

Note: See the better soln from striver bcz it is also a optimal
soln for problem where sum k (positive + negative)

3.2 Medium level

Q- Two Sum problem

$$\text{arr[]} = \{2, 6, 5, 8, 11\}$$

target = 14

(i) Ans is YES/NO
for possible target

$$A = \{2, 6, 5, 8, 11\}$$

$$n = \text{Size of}(A) / \text{Size of}(A[0]);$$

target = 14;

(ii) return index
of both element

Brute:

bool found = false;

```
for (i=0; i < n; i++) {
    for (j = i+1; j < n; j++) {
        if (A[i] + A[j] == target) {
            found = true;
            break;
        }
    }
}
```

T.C $\sim O(n^2)$
S.C $\sim O(1)$

if (found) break;

}

```
if (found) cout << "YES";
else cout << "NO";
```

~~use hashing~~

Better:

```

string read(int n, vector<int> book, int target) {
    map<int, int> mpp;
    for(int i = 0; i < n; i++) {
        int a = book[i];
        int more = target - a;
        if(mpp.find(more) != mpp.end()) {
            return "YES"; // for index
        }
        mpp[a] = i;
    }
    return "No";
}

```

T.C $\rightarrow O(N \log N)$
S.C $\rightarrow O(N)$

here book \rightarrow array given

Optimal: ^{2 pointers}

first sort the array (Quicksort)

$$A = \{2, 5, 6, 8, 11\}$$

\uparrow left \uparrow right

ONLY for 1st variety,
optimal exist

```

string read(int n, vector<int> book, int target) {
    int left = 0, right = n - 1;
    sort(book.begin(), book.end());
    while(left < right) {
        int sum = book[left] + book[right];
        if(sum == target) return "YES";
        else if(sum < target) left++;
        else right--;
    }
    return "No";
}

```

T.C $\rightarrow O(N \log N) + O(N)$
S.C $\rightarrow O(1)$

Q. Sort an array of 0's, 1's and 2's
arr[] = {0, 1, 2, 0, 1, 2, 1, 2, 0, 0, 0, 1}

Brute: use any of sorting technique like Merge sort

Note: here are only three distinct value

and Quick sort ignores property

and interviewer expect you to

exploit constraints • use merge sort

T.C $\sim O(N \log N)$

S.C $\sim O(N)$

Better: $cnt_0 = 0, cnt_1 = 0, cnt_2 = 0$

for($i = 0 \rightarrow n$)

if ($arr[i] == 0$) cnt_0++

else if ($arr[i] == 1$) cnt_1++

else cnt_2++

}

int idx = 0;

while (cnt_0)

$arr[idx++] = 0$;

}

else

use (cnt_0--)

while (cnt_1)

$arr[idx++] = 1$;

}

while (cnt_2)

$arr[idx++] = 2$;

}

T.C $\sim O(N)$

S.C $\sim O(1)$

for($i = 0 \rightarrow n$)

$cout \ll arr[i] \ll " "$;

Optimal: Dutch National Flag algorithm
 $A = [0, 1, 2, 0, 1, 2, 1, 0, 2, 0, 0, 0, 1]$
 ↑ mid ↑ high

$[0 \dots low-1] \rightsquigarrow 0's$
 $[low \dots mid-1] \rightsquigarrow 1's$
 $[high+1, n-1] \rightsquigarrow 2's$

0 low-1 low mid-1 mid high high+1 n-1
 0 0 * 0 0 0 1 1 1 1 1 2 2 2 2

↓
unsorted
0 1 1 2

$(a[mid] == 0) \{$
 swap ($a[low], a[mid]$);
 $low++, mid++$

$(a[mid] == 1) \{$
 $mid++;$
 $\}$

$(a[mid] == 2) \{$
 swap ($a[mid], a[high]$);
 $high--;$

See code of this from github / GPT

Q- Majority element ($> \frac{n}{2}$ times)

$$A = [2 2 3 3 1 2 2]$$

Brute:

```
for(i=0→n)
    cnt = 0;
```

```
for(j=0→n)
```

```
if(A[j] == A[i])
```

```
cnt++;
```

}

```
if(cnt > n/2) return arr[i];
```

}

T.C → O(N²)

S.C → O(1)

Better:

```
int maxi = A[0];
```

```
for(i=1→n){
```

```
if(A[i] > maxi) maxi = A[i];
```

}

also use
hashing
for better
soln

```
int visi[maxi+1] = {0};
```

T.C → O(N)

S.C → O(N)

```
for(i=0→n){
```

```
visi[A[i]]++;
```

}

target = n/2;

```
for(i=0; i ≤ maxi; i++) {
```

```
if(visi[i] > target){
```

```
cout << i
```

```
break;
```

}

}

Optimal: Moore's voting algorithm

```
int majElem(vector<int> v) {
    int cnt = 0;
    int cl;
    for(int i = 0; i < v.size(); i++) {
        if(cnt == 0) {
            cnt = 1;
            cl = v[i];
        }
        else if(v[i] == cl) {
            cnt++;
        }
        else {
            cnt--;
        }
    }
    int cnt1 = 0;
    for(int i = 0; i < v.size(); i++) {
        if(v[i] == cl) cnt1++;
    }
    if(cnt1 > v.size() / 2) {
        return cl;
    }
    return -1;
}
```

T.C ~ O(N)

S.C ~ O(1)

O- Maximum Subarray Sum

$A[] = \{-2, -3, 4, -1, -2, 1, 5, -3\}$

ANSWER

Note: For the Brute soln just copy paste the brute soln of longest subarray with sum K - only remove the "if" part and rest same

$\begin{bmatrix} \leftarrow & \leftarrow & \leftarrow & \leftarrow & \leftarrow & \leftarrow & \downarrow \\ -2, -3, 4, -1, -2, 1, 5, -3 \end{bmatrix}$

Optimal: Kadane's Algorithm

maxi = -2 ~~4~~ 7

Sum = 0 -2 4
-2 0 3
0 1 2
2 ~~4~~
~~4~~

long long maxSubSum(int arr[], int n){

long long Sum = 0, maxi = LONG_MIN;
for (int i=0; i < n; i++) {

Sum = Sum + arr[i];

if (Sum > maxi) {

maxi = Sum;

}

if (Sum < 0) {

Sum = 0;

}

}

return maxi;

}

Note: if all elements in array are -ve and you need to find and compute maxi to be a -ve value, also answer a cmp subarray bcz it has sum = 0 which is greater than -

Q- Best Time to buy & Sell Stocks
arr[] ~ [7, 1, 5, 3, 6, 4]

Do it later

min = arr[0]; profit = 0;
for (i = 1 to n) {
 cost = arr[i] - min;
 profit = max(profit, cost);
 min = min(min, arr[i]);
}

T.C $\rightarrow O(N)$
S.C $\rightarrow O(1)$

Q- Rearrange array elements by sign

arr[] = {3, 1, -2, -5, 2, -4}

Output {3, -2, 1, -5, 2, -4}

order ↴
(+, -, +, -, +, -)
OR
(-, +, -, +, -, +)

there will always be equal positive & equal negative

Note: order of occurrence
will be same even
in output

Ex: input \rightarrow 3, 1, -2, -4
output \rightarrow 3, -2, 1, -4

Brute:

```
int p=0, q=0  
int pos[n];  
int neg[n];
```

T.C $\rightarrow O(2N)$
S.C $\rightarrow O(N)$

Step 1:
for (i = 0 to n) {
 if (arr[i] > 0) {

inserting
positive | negative
separately

pos[p] = arr[i];

p++;

}

else {

neg[q] = arr[i];

q++;

}

}

```

int i=0, j=0, k=0;
while(i < p && j < q) {
    arr[k++] = pos[i++];
    arr[k++] = neg[j++];
}

```

optimal: we know that all positive are at even index (0, 2, 4, ...)
 all negative are at odd index (1, 3, 5, ...)

We iterate and check element and place on its respective index

```

n = nums.size();
vector<int> ans;
int posIndex = 0, negIndex = 1;
for (int i = 0; i < n; i++) {
    if (nums[i] < 0) {
        ans[negIndex] = nums[i];
        negIndex = negIndex + 2;
    } else {
        ans[posIndex] = nums[i];
        posIndex += 2;
    }
}
return ans;

```

Variety 1 is done where we have equal negative and positive element

Variety 2: almost same like 1 but if both are not equal, after inserting alternately. Insert the rest in any order
we can't use optimal soln now

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int p=0, q=0
int pos[n]; neg[n]

Brute: Step 1 will remain same

collect all positive & negative (till pos == neg)
don't collect all at once because
we still can apply the same for
(pos == neg) case.

arr[] = { -1, 2, 3, 4, -3, 1 }

for(i=0; i<2; i++) {

// collect

- - -

}

i=0, j=0, k=0

while(i < p && j < q) {

arr[k++] = pos[i++];

arr[k++] = neg[j++];

}

index = 4;
for remaining element

for(i=2; i < p; i++) {

arr[index] = pos[i];

index++;

}

Worst $O(N/2)$

T.C $\rightarrow O(N) + O(\min(p, q)) + O(\text{left over})$

$\sim O(2N)$

S.C $\sim O(N)$

Q- Next Permutation

$$A[] = \{3, 1, 2\}$$

Output: {3, 2, 1}

1	2	3
1	3	2
2	1	3
2	3	1
3	1	2
3	2	1

Brute:

- a) Generate all permutation (in sorted order)
- b) Linear search to find given permutation
- c) Return next index

it will be a lot of time taking

Note: in C++ STL we have funcn for next permutation

```
next_permutation(A.begin(), A.end());
return A;
```

Optimal:

idx = -1;

for(i = n-2; i >= 0; i--) {

if(a[i] < a[i+1]) {

idx = i;

break;

}

→ find longest prefix match

if(idx == -1) {

reverse(A.begin(), A.end());

for(i = n-1; i >= 0; i--) {

if(a[i] > a[idx]) {

swap(a[i], a[idx]);

}

→ find > a[idx] but the smallest one so that you can stay close

}

rev(a, idx+1, n-1);

T.C. O(n)
S.C. O(1)
+ space

everything on the right should be smaller

0 - Leaders in an array
 $A[] = [10, 22, 12, 3, 0, 6]$
 output $\rightarrow \{22, 12, 1\}$

observation:
 last element will
 always be the
 leader

Brute:

```
vector<int> leaders;
for (i = 0 → n) {
  bool isLeader = true;
  for (j = i + 1 → n) {
    if (A[j] >= A[i]) {
      isLeader = false;
      break;
    }
  }
}
```

T.C $\rightarrow O(n^2)$

S.C $\rightarrow O(N)$

```
if (isLeader) {
  leaders.push_back(A[i]);
}
```

Optimal:

```
vector<int> ans;
int maxi = INT_MIN;
for (int i = n - 1; i ≥ 0; i--) {
  if (a[i] > maxi) {
    ans.push_back(a[i]);
  }
  maxi = max(maxi, a[i]);
}
```

idea: Start from last of current
 1) Stay at any index
 2) find maxi element
 from right
 3) if current > maxi → needs

T.C $\rightarrow O(N)$

S.C $\rightarrow O(1)$

extra
 space

Q. Longest Consecutive Sequence

$\text{arr}[] = \{102, 4, 100, 1, 101, 3, 2, 1, 1\}$

Output \rightarrow ~~102, 2, 3, 4~~ 4 ($\& n=4$) {1, 2, 3, 4}

Brute:

```
longest = 1;
for(i = 0; i < n; i++) {
    m = arr[i];
    cnt = 1;
    while(ls(arr, m+1) == true) {
        m = m + 1;
        cnt = cnt + 1;
    }
}
```

T.C $\rightarrow O(n^2)$
S.C $\rightarrow O(1)$

Better:

```
sort(nums.begin(), nums.end());
int n = nums.size();
int lastSmaller = INT_MIN;
int cnt = 0;
int longest = 1;
for(int i = 0; i < n; i++) {
    if(nums[i] - 1 == lastSmaller) {
        cnt = cnt + 1;
        lastSmaller = nums[i];
    } else if(lastSmaller != nums[i]) {
        cnt = 1;
        lastSmaller = nums[i];
    }
    longest = max(longest, cnt);
}
return longest;
```

T.C $\rightarrow O(N \log N + N)$

```

Optimal:
int longest = 1;
unordered_set<int> st;
for(int i = 0; i < n; i++) {
    st.insert(a[i]);
}
for (auto it : st) {
    if (st.find(it - 1) == st.end()) {
        int cnt = 1;
        int x = it;
        while (st.find(x + 1) != st.end()) {
            x = x + 1;
            cnt++;
        }
        longest = max(longest, cnt);
    }
}
return longest;

```

$$T.C \sim O(3N)$$

$$S.C \sim O(N)$$

Q- Set Matrix zeros

$(n \times m)$

row column

1	1	1	1
1	0	0	1
1	1	0	1
1	1	1	1

Whenever you find a zero.
make its complete
row & column to
zero

Output

1	0	0	1
0	0	0	0
0	0	0	0
1	0	0	1

Note: To traverse in a 2D array
you need Min T.C $\sim O(n^2)$
so you cannot make it
less than n^2

```

Brute:
for(int i=0; i<n; i++) {
    for(int j=0; j<mid; j++) {
        if (arr[i][j] == 0) {
            markRow(i);
            markCol(j);
        }
    }
}

```

```

markRow(i) {
    for(j=0; j<m; j++) {
        if (arr[i][j] == 0) {
            arr[i][j] = -1;
        }
    }
}

markCol(j) {
    for(i=0; i<n; i++) {
        if (arr[i][j] == 0) {
            arr[i][j] = -1;
        }
    }
}

```

```

for(i=0 → n) {
    for(j=0 → m) {
        if (arr[i][j] == -1) {
            arr[i][j] = 0;
        }
    }
}

```

T.C $\rightarrow O(n \times m \times (n+m)) + O(n \times m)$
S.C $\rightarrow O(1)$

Better

```

col[m] = {0}, row[n] = {0};
for(i=0 → n) {
    for(j=0 → m) {
        if (arr[i][j] == 0) {
            row[i] = 1;
            col[j] = 1;
        }
    }
}

```

T.C $\rightarrow O(n \times m) + O(n \times m)$
S.C $\rightarrow O(n + O(m))$

```

for(i=0 → n) {
    for(j=0 → m) {
        if (row[i] || col[j]) {
            arr[i][j] = 0;
        }
    }
}

```

for optimal one we
you just need to check
space bcz time is
already optimised

Note: Watch optimal from Striver bcz it asked directly in
interviews many times

(a) Rotate Matrix / Image by 90° ($n \times n$)

$$\begin{matrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \\ 13 & 14 & 15 & 16 \end{matrix} \xrightarrow{\text{rotate}} \begin{matrix} 13 & 9 & 5 & 1 \\ 14 & 10 & 6 & 2 \\ 15 & 11 & 7 & 3 \\ 10 & 12 & 8 & 4 \end{matrix}$$

Brute:

i	j	$\xrightarrow{\quad (n-1)-i \quad}$
{1}	{0}	$\rightarrow \{0\}\{3\}$
{0}	{1}	$\rightarrow \{1\}\{2\}$
{0}	{2}	$\rightarrow \{2\}\{3\}$
{0}	{3}	$\rightarrow \{3\}\{2\}$

initially at finally at
1st row \rightarrow last column
2nd row \rightarrow 2nd last column
3rd row \rightarrow 2nd column
4th row \rightarrow 1st column

i	j	$\xrightarrow{\quad (n-1)-i \quad}$
{1}	{0}	$\rightarrow \{0\}\{2\}$
{1}	{1}	$\rightarrow \{1\}\{2\}$
{1}	{2}	$\rightarrow \{2\}\{2\}$
{1}	{3}	$\rightarrow \{3\}\{2\}$

ans[n][n]:
for($i=0 \rightarrow n$) {
 for($j=0 \rightarrow n$) {
 ans[j][n-1-i] = matrix[i][j];
 }
}

T.C $\rightarrow O(n^2)$
S.E $\rightarrow O(n^2)$

Optimal: Take transpose \rightarrow reverse all row

How to take transpose:

matrix: 1) The diagonal will stay same even after doing transpose

2) The upper & lower triangular element swap

$$\begin{matrix} \{0\}\{1\} \rightarrow \{1\}\{0\} & \{1\}\{2\} \rightarrow \{2\}\{1\} \\ \{0\}\{2\} \rightarrow \{2\}\{0\} & \{1\}\{3\} \rightarrow \{3\}\{1\} \\ \{0\}\{3\} \rightarrow \{3\}\{0\} & \{2\}\{3\} \rightarrow \{3\}\{2\} \end{matrix}$$

$$\{i\}\{j\} \rightarrow \{j\}\{i\}$$

Observation: first column becomes the first row but in a reverse order

Second column becomes the second row but in a reverse order

this is what we call
Transpose \rightarrow change column to row or vice versa

```

for(i = 0 → n-1) {
    for(j = i+1 → n) {
        swap(a[i][j] > a[j][i]);
    }
}

```

$T \cdot C \rightarrow O(n^2)$
 $S \cdot C \rightarrow O(1)$

```

for(i = 0 → n) {
    reverse(a[i].begin(), a[i].end());
}

```

Q- Spiral matrix

1	2	3	4	5	6
20	21	22	23	24	7
19	32	33	34	25	8
18	31	36	35	26	9
17	30	29	28	27	10
16	15	14	13	12	11

- it has only one solution
- interviewer will ask this to test your implementation and how clean you can write the code

top = 0 bottom = 5
 left = 0 right = 5

right → bottom → left → top

watch the code from [github/striver](#)

$a[] []$

↑ left/right
 ↓ top/bottom

whatever is constant
 but it there and
 another one will
 always be ;

Q- Number of subarrays with sum k
 $\text{arr} = \{1, 2, 3, -3, 1, 1, 1, 4, 2, -3\}$ $k=3$

Brute : Generate all subarray and check for which sum = k

```
cnt = 0;
for(i=0 → n)
```

Sum = 0;

```
for(j=i → n){
```

sum = sum + arr[j];

```
if(sum == k){
```

cnt++;

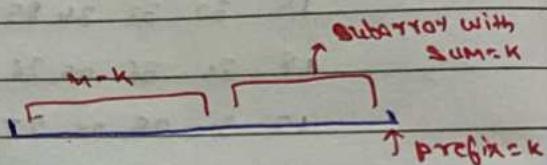
}

}

T.C $\rightsquigarrow O(n^2)$

S.C $\rightsquigarrow O(1)$

Optimal : Using prefix sum



No. of $m-k$ = No. of subarray with k

HashMap (presum, cnt)
 ↑ ↓
 Key Value

$mpp[0] = 1;$

int presum = 0, cnt = 0;

for (i=0 → n){

 presum = presum + arr[i];

 int remove = presum - k;

 cnt = cnt + mpp[remove];

 mpp[presum] = mpp[presum] + 1;

}

return cnt;

T.C $\rightsquigarrow O(n \log n)$

S.C $\rightsquigarrow O(n)$