

GREEDY ALGORITHMS

- (i) builds a solution step - by - step
- (ii) series of step / instruction used to solve a problem
- (iii) At each step → makes the choice that gives the highest immediate benefit
- (iv) locally optimum choice hoping to find global optimum
- (v) Used for optimisation problems.
- (vi) A problem can have many feasible solution but only 1 optimal solution
- (vii) Greedy is used for optimisation problems but does not give optimal solution always

QUESTION - FRACTIONAL KNAPSACK

Coding Exercise : Fractional Knapsack

Determine how to optimally fill a knapsack with a capacity of W kilograms using a list of N items, where each item is represented by a pair [profit, weight]. In the Fractional Knapsack problem, you can take fractions of items to maximize the total profit in the knapsack. (N will be greater than equal to 1)

Example 1:

Given arr[] = [[70, 10], [90, 20], [150, 30]]

$W = 25$

Expected output = 145

Example 2:

Given arr[] = [[70, 10], [90, 20], [150, 30]]

W= 45

Expected output = 242.5

CODE ↴

```
def fractionalKnapSack(W, arr, n):  
    arr.sort(reverse=True, key = lambda x :  
             x[0] / x[1])  
  
    remaining_weight = W  
    value = 0  
  
    for i in range(n):  
        if remaining_weight == 0:  
            break  
  
        weight = min(remaining_weight,  
                    arr[i][0])  
  
        remaining_weight -= weight  
        value += arr[i][0] / arr[i][1] *  
                 weight  
  
    return value
```

QUESTION: Non-Overlapping Intervals

Input : intervals = [[1,2], [2,3], [3,4], [1,3]]

Output : 1

Explanation : [1,3] can be removed and rest
of the interval are non-overlapping

Input : [[1,4], [2,5], [5,6], [3,4]]

Output : 2

CODE 7

```
def eraseOverlappingIntervals(intervals):
    intervals.sort(key = lambda x: x[1])
    # sort basis on end time

    res = 0
    end = float('-inf')

    for start, finish in intervals:
        if start >= end:
            end = finish
            # non-overlapping interval
        else:
            res += 1

    return res
```

QUESTION : 55. Jump Game

Example 1:

Input: nums = [2,3,1,1,4]

Output: true

Explanation: Jump 1 step from index 0 to 1, then 3 steps to the last index.

CODE

```
def canJump(nums):
    n = len(nums)
    max_index = 0
    for i in range(n):
        if i > max_index:
            return False
        max_index = max(max_index, i + nums[i])
    if max_index >= n - 1
        return True.
```

QUESTION : Minimum number of arrows to burst balloons

Input: points = [[10,16],[2,8],[1,6],[7,12]]

Output: 2

Explanation: The balloons can be burst by 2 arrows:

- Shoot an arrow at $x = 6$, bursting the balloons [2,8] and [1,6].
- Shoot an arrow at $x = 11$, bursting the balloons [10,16] and [7,12].

Similar to interval overlapping problem we discussed above,

In this case we arrow += 1 if we find a non-overlapping interval

CODE :

```
def findMinArrowShots(points):
    points.sort(key = lambda x : x[1])
    arrow = 0
    end = float('-inf')
    for start, finish in points:
        if start > end:
            # non-overlapping interval
            # found so increase arrow
            arrow += 1
            end = finish
    return arrow
```

QUESTION : Two city scheduling

Input: costs = [[10, 20], [30, 200], [400, 50], [30, 20]]
Output: 110 A B

Explanation:

The first person goes to city A for a cost of 10.
The second person goes to city A for a cost of 30.
The third person goes to city B for a cost of 50.
The fourth person goes to city B for a cost of 20.

There are $2N$ person and only maximum of n person can travel to a city

CODE :

```
def twoCitySchedCost(costs):
    cost.sort(key = lambda x : x[0] - x[-1])
    # this arranges the cost array in such
    # a manner that all low cost of A are
    # arranged before.

    total_cost = 0

    n = len(costs) // 2
    # and just n people to 'A' city

    for i in range(n):
        total_cost += costs[i][0]
    # now and rest to 'B'

    for i in range(n, 2*n):
        total_cost += costs[i][1]
```

return total_cost

QUESTION: Boats to save people.

Input: people = [1, 2], limit = 3

Output: 1

Explanation - 1 boat (1,2)

```
def numRescueBoats(people, limit):
```

```
    people.sort()  
    boats = 0
```

```
    lightest, heaviest = 0, len(people) - 1
```

```
    while lightest <= heaviest:
```

```
        boats += 1
```

```
        if people[lightest] + people[heaviest] <= limit
```

```
            lightest += 1
```

lightest person is included only
if condition is met true

```
        heaviest -= 1 # only heaviest person  
                      # is assigned boat is  
                      # limit is exceeded
```

```
    return boats
```

QUESTION - TASK SCHEDULER

Input: tasks = ['A', 'A', 'A', 'B', 'B', 'B'] , n=2

Output : 8

Explanation :

A, B, idle, A, B, idle, A, B

	\overbrace{AAABC}^{HF}	$\overbrace{AAABBBBC}^{HF \text{ HF}}_{\#=2}$
parts (P)	$HF - 1 \Rightarrow 3 - 1 = 2$	$HF - 1 \Rightarrow 3 - 1 = 2$
slot in Parts (S)	$P \times n$ (given)	$P \times [n - (\# - 1)]$
tasks to be placed	$5 - 3 \times 1$	$7 - 3 \times 2$
empty slots / idle	$S - T$	$S - T$

return empty_slots + len(tasks) if empty_slots > 0
 else len(tasks)

CODE :

```
def leastInterval(tasks, n):
    count = [0] * 26
    max_freq = 0
    number_max_freq = 0
    for task in tasks:
```

```

index = ord(task) - ord('A')
count[index] += 1

if max_freq < count[index]
    max_freq = count[index]
    number_max_freq = 1

if max_freq == count[index]
    number_max_freq += 1

parts = max_freq - 1
slots_per_part = n - (number_max_freq - 1)
total_slot_in_part = parts * slots_per_part
task_remaining = len(task) - max_freq * number_max_freq

idles = max(0, total_slot_in_part - task_remaining)

return len(tasks) + idles

```

QUESTION : LARGEST NUMBER

Input : [2, 10]

Output : 210

Input : [10, 5, 9]
 Output : 9510

CODE :

```
def largestNumber(nums):
    for i, n in enumerate(nums):
        nums[i] = str(n)

    def compare(n1, n2):
        if n1 + n2 > n2 + n1:
            return -1
        else:
            1

    nums = sorted(nums, key = cmp_to_key(compare))
    return str(int("".join(nums)))
```

QUESTION : 134. Gas Station.

There are n gas stations along a circular route, where the amount of gas at the i^{th} station is $\text{gas}[i]$.

You have a car with an unlimited gas tank and it costs $\text{cost}[i]$ of gas to travel from the i^{th} station to its next $(i + 1)^{\text{th}}$ station. You begin the journey with an empty tank at one of the gas stations.

Given two integer arrays gas and cost , return the starting gas station's index if you can travel around the circuit once in the clockwise direction, otherwise return -1 . If there exists a solution, it is guaranteed to be unique

Example 1:

Input: $\text{gas} = [1, 2, 3, 4, 5]$, $\text{cost} = [3, 4, 5, 1, 2]$

Output: 3

Explanation:

Start at station 3 (index 3) and fill up with 4 unit of gas. Your tank = $0 + 4 = 4$

Travel to station 4. Your tank = $4 - 1 + 5 = 8$

Travel to station 0. Your tank = $8 - 2 + 1 = 7$

Travel to station 1. Your tank = $7 - 3 + 2 = 6$

Travel to station 2. Your tank = $6 - 4 + 3 = 5$
Travel to station 3. The cost is 5. Your gas is just enough to travel back to station 3.
Therefore, return 3 as the starting index.

CODE :

```
def canComplete(gas, cost):
    if sum(gas) < sum(cost):
        return -1
    for i in range(len(gas)):
        total += gas[i] - cost[i]
        if total < 0:
            total = 0
            res = i + 1
    return res
```

QUESTION: JUMP GAME II

Input: nums = [2,3,1,1,4]

Output: 2

Explanation: The minimum number of jumps to reach the last index is 2. Jump 1 step from index 0 to 1, then 3 steps to the last index.

CODE :

```
def jump(nums):
    jumps = 0
    current_end = 0
    furthest = 0
```

```
for i in range(n-1): # we dont need to  
                      jump from the last  
                      element.
```

```
# always try to jump to farthest position
```

```
farthest = max(farthest, nums[i] + i)
```

```
if i == current_end:
```

```
    jump += 1
```

```
    current_end = farthest +
```

```
    if current_end >= n-1  
        break
```

```
return jumps
```

ARRAY QUESTIONS

QUESTION : Rotate Array

Input : nums = [1, 2, 3, 4, 5, 6, 7]
Output : [5, 6, 7, 1, 2, 3, 4]

Reverse the num array

[7, 6, 5, 4, 3, 2, 1,]

Now reverse the 2 sub array formed

[5, 6, 7, 1, 2, 3, 4]

(1) Reverse (2) Reverse (0, k-1)

Reverse (k, length-1)

CODE :

```
def rotate(nums):
    if len(nums) == 0:
        return 0
    k = k % len(nums)
    temp = nums[-k:] # create temp array
                      # of last k elements
    # now shift the front element to last
    for i in reversed(range(0, len(nums)-k)):
        nums[i+k] = nums[i]
    # now append the 'temp' array at the
    # beginning
    for i in range(len(temp)):
        nums[i] = temp[i]
```

2nd Way : More Code Intuitive

```

def rotate(nums):
    # define a reverse function to reverse the
    # nums

    def reverse(arr, start, end):
        while start < end:
            arr[start], arr[end] = arr[end],
            arr[start]
            start += 1
            end -= 1

        # reversing the whole array
        reverse(nums, 0, len(nums) - 1)

        # reversing the first k element
        reverse(nums, 0, k - 1)

        # reversing the rest k element
        reverse(nums, k, len(nums) - 1)

```

QUESTION : ISOMORPHIC STRINGS

Input: $s = 'egg'$ $t = 'add'$
 Output: true

CODE :

```
def isIsomorphic(s, t):
```

```

if len(s) != len(t):
    return False

s_hash, t_hash = {}, {}

for i in range(len(d)):
    char_s = s[i]
    char_t = t[i]

    if char_s not in s_hash:
        s_hash[char_s] = char_t

    if char_t not in t_hash:
        t_hash[char_t] = char_s

    if s_hash[char_s] != char_t or
       t_hash[char_t] != char_s:
        return False

return True

```

Question : 3. Longest Substring Without Repeating Characters

Input : $s = "abcabcbb"$

Output : 3

Explanation : 'abc' = 3

CODE :

```
def max_unique_length(s):
    maxlen = 0
    start = 0
    seen = {}
    for i in range(len(s)):
        char = s[i]
        if char in seen:
            start = max(start, seen[char] + 1)
        maxlen = max(maxlen, i - start + 1)
        seen[char] = i
    return maxlen
```

Question : 49. Group Anagrams

Input: strs = ["eat", "tea", "tan", "ate", "nat", "bat"]
Output: [["bat"], ["nat", "tan"], ["ate", "eat", "tea"]]

CODE

```
def group_anagrams(strs):
```

anagrams = {}

for string in strings:

 sorted_string = ''.join(sorted(string))

 if sorted_string in anagrams:

 anagram[sorted_string] += [string]

 else:

 anagrams[sorted_string] = [string]

return anagram.values()

Searching Algorithms

Questions

33. Search in a rotated array

CODE:

```
def search_rotated_sorted_array(nums, target):
```

```
# check if the array is empty
```

```
if not nums:
```

return -1

left, right = 0, len(nums) - 1

while left <= right :

 mid = (left + right) // 2

 if nums[mid] == target

 return mid

Check if the left half is sorted
if nums[left] < nums[mid] :

Check if the target is in the left half

if nums[left] <= target < nums[mid] :

 right = mid - 1 # check the
 left half

else :

 left = mid + 1 # check the
 right half

The right half is sorted

else :

if the target is in the right half

if nums[mid] < target <= nums
[right] :

 left = mid + 1 # check the
 right half

else :

 right = mid - 1 # check the

left half

return -1

34. Find First and Last Position of Elements in Sorted Array

Input = nums = [5, 7, 7, 8, 8, 10]
target = 8
Output = [3, 4]

CODE:

```
def search_for_range(array, target):  
    def search(nums, target, findstartIndex):  
        ans = -1  
        start = 0  
        end = len(nums) - 1  
  
        while start <= end :  
            mid = start + (end - start) // 2 # modified  
                                         version for finding min  
  
            if target < nums[mid] :  
                end = mid - 1  
  
            elif target > nums[mid] :  
                ...  
                ...
```

```

start = mid + 1

else :
    # target found
    ans = mid
    if findStartIndex :
        # if searching for start index
        continue searching left
        end = mid - 1

    else :
        # if searching for end index
        continue searching right
        start = mid + 1

return ans

# initialize ans array with default values
ans = [-1, -1]

# find the start index of the target
ans[0] = search (array, target, True)

if ans[0] != -1 :
    ans[1] = search (array, target, False)

return ans

```

74. Search a 2D Matrix

Input : $\begin{bmatrix} [1, 3, 5, 7], [10, 11, 16, 20], [23, 30, 34, 60] \end{bmatrix}$
target = 3

Output : True

We will consider the 2D matrix as 1D and apply the binary search, with some modification

We will convert 1D Index to 2D index on fly.

CODE:

```
def searchMatrix(self, matrix, target):  
    # Check if the matrix is empty  
    if not matrix or not matrix[0]:  
        return False  
  
    # Get the dimension of the matrix  
    row = m , column = n  
  
    m,n = len(matrix), len(matrix[0])  
  
    # Initialize pointers for binary search  
    # Treat the 2D matrix as a 1D sorted array  
  
    left, right = 0, m*n - 1  
  
    while left <= right:  
  
        mid = (left+right)//2  
  
        # Formula to convert 2D matrix to 1D  
        row, col = mid//n, mid % n  
  
        # Get the value of mid
```

value = matrix [row][col]

if value == target:
 return True

elif value < target:

 left = mid + 1

else:

 right = mid - 1

return False.