Simulation Challenge

Generative Models and Monte Carlo Simulation

Simulation Challenge - Monte Carlo Analysis

Challenge Overview

Your Mission: Create a comprehensive Quarto document that simulates one or two investment strategies, analyzes the results, and demonstrates your ability to present counter-intuitive findings compellingly. Then render the document to HTML and deploy it via GitHub Pages from a new repository called "simulationChallenge."

A

AI Partnership Required

This challenge pushes boundaries intentionally. You'll tackle problems that normally require weeks of study, but with Cursor AI as your partner (and your brain keeping it honest), you can accomplish more than you thought possible.

The new reality: The four stages of competence are Ignorance \rightarrow Awareness \rightarrow Learning \rightarrow Mastery. AI lets us produce Mastery-level work while operating primarily in the Awareness stage. I focus on awareness training, you leverage AI for execution, and together we create outputs that used to require years of dedicated study.

The Investment Game

Original Game Strategy

Example 0.1. Imagine you are offered the following game and given a \$1,000 budget in a special account to play the game: I will flip a coin, and if it comes up heads, we increase your account's balance by 50%; if it comes up tails, we reduce your account's balance by 40%. We are not only doing this once, but we will do it once per year until you turn 55. When you turn 55, you will receive the balance in your account.

Generative DAG Model for the Investment Game

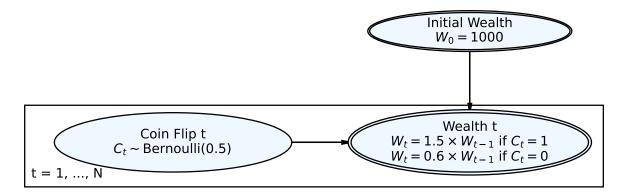


Figure 1: Generative DAG model for the investment game showing how wealth evolves over time through coin flips

Challenge Requirements

Minimum Requirements for Any Points on Challenge

- 1. **Create a Quarto Document:** Write a concise quarto markdown file that includes a narrative of what you are doing along with the requested code, results, and visualizations of your simulations.
- 2. Render to HTML: You must render the quarto markdown file to HTML.
- 3. **GitHub Repository:** The rendered HTML must be uploaded to a new GitHub repository called "simulationChallenge" in your Github account.
- 4. **GitHub Pages Setup:** The repository should be made the source of your github pages:
 - Go to your repository settings (click the "Settings" tab in your GitHub repository)
 - Scroll down to the "Pages" section in the left sidebar
 - Under "Source", select "Deploy from a branch"
 - Choose "main" branch and "/ (root)" folder
 - Click "Save"
 - Your site will be available at: https://[your-username].github.io/simulationChallenge/
 - Note: It may take a few minutes for the site to become available after enabling Pages

Grading Rubric

Questions to Answer for 75% Grade on Challenge

- 1. **Expected Value Analysis:** What is the "expected value" of your account balance after 1 coin flip for the original game?
- 2. **Expectation vs. Reality:** Is the expected value positive or negative? Do you expect your account to be worth more or less than \$1,000 based on this result?
- 3. **Single Simulation:** Run one simulation showing the dynamics of your account balance over time. Make an object-oriented matplotlib OR ggplot2 plot showing your simulated account balance over time (i.e. as you age). Comment on the results, are you happy?

Questions to Answer for 85% Grade on Challenge

4. **Multiple Simulations:** Run 100 simulations modelling the dynamics of your account balance over time. Make an object-oriented matplotlib OR ggplot2 plot showing a probability distribution of the 100 simulated account balance at age 55. Comment on the results, are you happy? Why or why not?

Questions to Answer for 95% Grade on Challenge

5. **Probability Analysis:** Based on the 100 simulations above, what is the probability that your account balance will be greater than \$1,000 at age 55?

Questions to Answer for 100% Grade on Challenge

6. **Strategy Comparison:** Run 100 simulations for the modified game strategy shown below in Example 0.2. What is the probability that your account balance will be greater than \$10,000 at age 55? Is this probability higher or lower than the probability in the original game?

Modified Game Strategy

Example 0.2. Imagine you are offered the following game and given a \$1,000 budget in a special account to play the game: I will flip a coin, and if it comes up heads, we increase your bet by 50%; if it comes up tails, we reduce your bet by 40%. You must bet exactly 50% of your current account balance on each flip, and this 50% is locked in for each round. We are not only doing this once, but we will do it once per year until you turn 55. When you turn 55, you will receive the balance in your account.

Technical Implementation Preferences

Setting Up Your Analysis

For R Users:

- Use tidyverse for data manipulation
- Use ggplot2 for visualizations
- Use set.seed() for reproducible results

For Python Users:

- Use numpy for numerical operations
- Use pandas for data manipulation
- Use matplotlib (object-oriented)
- Use np.random.seed() for reproducible results

Visualization Preferences

• **Professional Styling:** Use consistent colors, clear labels, readable fonts, and informative titles

Submission Checklist

| Minimum Requirements (Required for Any Points): | | | |
|---|---|--|--|
| | Quarto document created with clear narrative Document rendered to HTML successfully Repository "simulationChallenge" created HTML files uploaded to repository GitHub Pages enabled and working Site accessible at https://[your-username].github.io/simulationChallenge/ | | |
| 75% | Grade Requirements: | | |
| | Expected value calculations shown (Question 1) Expectation vs. reality analysis (Question 2) Single simulation with time series plot (Question 3) Clear interpretation of single simulation results | | |
| 85% | Grade Requirements: | | |
| | 100 simulations with distribution analysis (Question 4) | | |

| ☐ Probability distribution plot of final accomplex interpretation of multiple simulation | | | |
|--|-----------------|--|--|
| 95% Grade Requirements: | | | |
| □ Probability calculations for original strat□ Analysis of probability that balance > \$ | J , | | |
| 100% Grade Requirements: | | | |
| □ 100 simulations for modified strategy (Q □ Probability calculations for modified strategy □ Comparative analysis between both strategy □ Analysis of probability that balance > \$ | ategy tegies | | |
| Code Quality (All Grades): | | | |
| □ Reproducible results (seeds set) □ Clean, well-commented code □ Appropriate use of functions and loops □ Professional visualization styling | | | |

Resources

- Quarto Markdown: quarto.org/docs/authoring/markdown-basics.html
- Quarto Documentation: quarto.org/docs
- R for Data Science: r4ds.had.co.nz
- Python Data Science Handbook: jakevdp.github.io/PythonDataScienceHandbook

Getting Started Tips

i Navy SEALs Motto

"Slow is Smooth and Smooth is Fast"

Take your time to understand the simulation mechanics, plan your approach carefully, and execute with precision. Rushing through this challenge will only lead to errors and confusion.

- Browse Essential Simulation Concepts: This section will give you a good understanding of the concepts you need to know to complete the challenge.
- Start Simple: Begin with a single simulation to understand the mechanics
- Document Everything: Explain your reasoning and interpret your results

- Forgetting to Set Seeds: Always set random seeds for reproducible results
- Total time to complete: ~3-4 hours for the 100% grade
- Good luck, and remember simulation will steer you right even when intuition will steer you wrong!

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Important: Save Your Work Frequently!

Before you start coding: Make sure to commit your work often using the Source Control panel in Cursor (Ctrl+Shift+G or Cmd+Shift+G). This prevents the AI from overwriting your progress and ensures you don't lose your work.

Commit after each major step:

- After completing each simulation example
- After finishing each challenge question
- Before asking the AI for help with new code

How to commit:

- 1. Open Source Control panel (Ctrl+Shift+G)
- 2. Stage your changes (+ button)
- 3. Write a descriptive commit message
- 4. Click the checkmark to commit

Remember: Frequent commits are your safety net!

Essential Simulation Concepts

Before diving into the challenge, let's review the key simulation concepts you'll need. These examples will prepare you for the investment game analysis.

1. Simple Simulation: Coin Flip Game

Let's start with a basic coin flip simulation to understand the mechanics:

Generative DAG Model for the Simple Coin Flip Game

Key Difference from Investment Game: Unlike the investment game DAG (Figure 1) which models wealth evolution over multiple time periods with multiplicative changes, this simple coin flip DAG represents a single-period game with additive winnings. The investment game shows how wealth compounds over time ($W_t = 1.5 \times W_{t-1}$ or $W_t = 0.6 \times W_{t-1}$), while

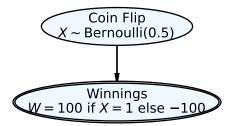


Figure 2: Generative DAG model for the simple coin flip game showing the relationship between coin flip outcome and winnings

this simple game shows fixed winnings (W=+100 or W=-100) based on a single coin flip outcome.

R

```
suppressPackageStartupMessages(library(tidyverse))

# Set seed for reproducibility
set.seed(123)

# Number of simulations
n_sims <- 10

# Create simulation data
sim_data <- tibble(
    sim_num = 1:n_sims,
    coin_flip = rbinom(n = n_sims, size = 1, prob = 0.5)
) %>%
    mutate(
        winnings = if_else(coin_flip == 1, 100, -100)
)

# Display results
sim_data
```

```
3
       3
                     -100
              0
4
       4
               1
                     100
5
       5
               1
                     100
6
       6
               0
                     -100
7
       7
               1
                     100
               1
8
       8
                     100
9
       9
               1
                     100
10
      10
                     -100
```

Python

```
import numpy as np
import pandas as pd
# Set seed for reproducibility
np.random.seed(123)
# Number of simulations
n_sims = 10
# Step 1: Draw coin flips (stochastic node)
X = np.random.binomial(n=1, p=0.5, size=n_sims)
# Step 2: Compute winnings (deterministic node)
W = np.where(X == 1, 100, -100)
# Combine into data frame
sim_data = pd.DataFrame({
    'sim_num': range(1, n_sims + 1),
    'coin_flip': X,
    'winnings': W
})
# Display results
sim_data
```

| | sim_num | coin_flip | winnings |
|---|---------|-----------|----------|
| 0 | 1 | 1 | 100 |
| 1 | 2 | 0 | -100 |
| 2 | 3 | 0 | -100 |
| 3 | 4 | 1 | 100 |

| 4 | 5 | 1 | 100 |
|---|----|---|------|
| 5 | 6 | 0 | -100 |
| 6 | 7 | 1 | 100 |
| 7 | 8 | 1 | 100 |
| 8 | 9 | 0 | -100 |
| 9 | 10 | 0 | -100 |

2. Time-Series Simulation: Account Balance Over Time

Now let's simulate how an account balance changes over multiple periods:

Generative DAG Model for Time-Series Account Balance

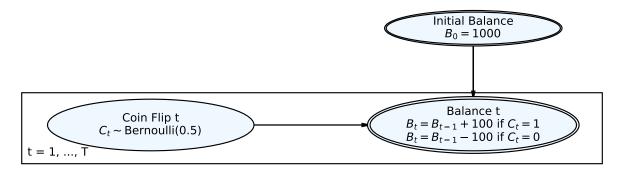


Figure 3: Generative DAG model for time-series account balance simulation showing how balance evolves sequentially over multiple periods

Key Difference from Simple Coin Flip Game: Unlike the simple coin flip DAG (Figure 2) which represents a single-period game, this time-series DAG models sequential balance evolution over multiple periods. Each period's balance depends on the previous period's balance plus the current coin flip outcome. The simple game shows independent winnings per flip, while this model shows cumulative balance changes where $B_t = B_{t-1} + \Delta_t$ and $\Delta_t = +100$ or -100 based on the coin flip.

R

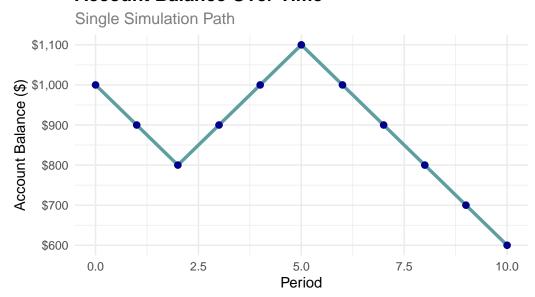
```
suppressPackageStartupMessages(library(tidyverse))
suppressPackageStartupMessages(library(ggplot2))

# Set seed for reproducibility
set.seed(456)
```

```
# Parameters
initial_balance <- 1000</pre>
n_periods <- 10
n_sims <- 1 # Start with one simulation</pre>
# Simulate one path
simulate_path <- function(initial, periods) {</pre>
  balance <- initial
  path <- numeric(periods + 1)</pre>
  path[1] <- initial</pre>
  for (i in 1:periods) {
    coin_flip \leftarrow rbinom(1, 1, 0.5)
    if (coin_flip == 1) {
      balance <- balance + 100
    } else {
      balance <- balance - 100
    }
   path[i + 1] <- balance</pre>
  }
  return(path)
# Run simulation
time_series_data <- tibble(</pre>
  period = 0:n_periods,
  balance = simulate_path(initial_balance, n_periods)
)
# Create time series plot
ggplot(time_series_data, aes(x = period, y = balance)) +
  geom_line(color = "cadetblue", linewidth = 1.2) +
  geom_point(color = "darkblue", size = 2) +
  labs(
    title = "Account Balance Over Time",
    subtitle = "Single Simulation Path",
    x = "Period",
    y = "Account Balance ($)",
    caption = "Heads: +$100$, Tails: -$100$"
  ) +
  scale_y_continuous(labels = scales::dollar_format()) +
```

```
theme_minimal() +
theme(
  plot.title = element_text(size = 14, face = "bold"),
  plot.subtitle = element_text(size = 12, color = "gray50")
)
```

Account Balance Over Time



Heads: +\$100\$, Tails: -\$100\$

Figure 4: R time-series simulation of account balance

```
# Show the data
time_series_data
```

```
# A tibble: 11 x 2
   period balance
             <dbl>
    <int>
 1
        0
              1000
 2
        1
               900
 3
        2
               800
4
        3
               900
5
        4
              1000
6
        5
              1100
7
        6
              1000
```

```
8 7 900
9 8 800
10 9 700
11 10 600
```

Python

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
# Set seed for reproducibility
np.random.seed(456)
# Parameters
initial_balance = 1000
n_{periods} = 10
n_sims = 1 # Start with one simulation
# Simulate one path
def simulate_path(initial, periods):
    balance = initial
    path = [initial]
    for i in range(periods):
        coin_flip = np.random.binomial(1, 0.5)
        if coin_flip == 1:
            balance = balance + 100 # $100 gain
        else:
            balance = balance - 100 # $100 loss
        path.append(balance)
    return path
# Run simulation
time_series_data = pd.DataFrame({
    'period': range(n_periods + 1),
    'balance': simulate_path(initial_balance, n_periods)
})
# Create time series plot
```

(0.0, 1540.0000000000000)

```
# Format y-axis as currency
ax.yaxis.set_major_formatter(plt.FuncFormatter(lambda x, p: f'${x:,.0f}'))
plt.tight_layout()
plt.show()
```

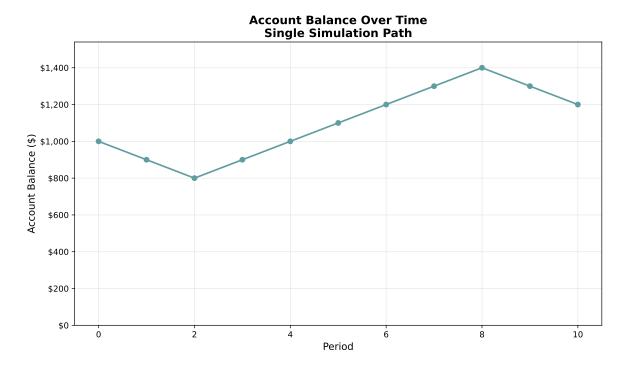


Figure 5: Python time-series simulation of account balance

```
# Show the data
print("Time Series Data:")
```

Time Series Data:

```
print(time_series_data)
```

| | period | balance |
|----|--------|---------|
| 0 | 0 | 1000 |
| 1 | 1 | 900 |
| 2 | 2 | 800 |
| 3 | 3 | 900 |
| 4 | 4 | 1000 |
| 5 | 5 | 1100 |
| 6 | 6 | 1200 |
| 7 | 7 | 1300 |
| 8 | 8 | 1400 |
| 9 | 9 | 1300 |
| 10 | 10 | 1200 |

3. Probability Distribution: Final Balance Distribution

Let's see what the distribution of final balances looks like across many simulations:

R

```
suppressPackageStartupMessages(library(tidyverse))
suppressPackageStartupMessages(library(ggplot2))

# Set seed for reproducibility
set.seed(789)

# Parameters
initial_balance <- 1000
n_periods <- 10
n_sims <- 100  # Multiple simulations

# Simulate multiple paths
simulate_final_balance <- function(initial, periods) {</pre>
```

```
balance <- initial
  for (i in 1:periods) {
    coin_flip <- rbinom(1, 1, 0.5)</pre>
    if (coin_flip == 1) {
     balance <- balance + 100 # $100 gain
    } else {
      balance <- balance - 100 # $100 loss
    }
  }
  return(balance)
# Run multiple simulations
final_balances <- replicate(n_sims, simulate_final_balance(initial_balance, n_periods))</pre>
# Create data frame
distribution_data <- tibble(</pre>
 sim_num = 1:n_sims,
 final_balance = final_balances
)
# Create histogram
ggplot(distribution_data, aes(x = final_balance)) +
  geom_histogram(bins = 20, fill = "plum", alpha = 0.8, color = "black") +
  geom_vline(xintercept = initial_balance, color = "red", linetype = "dashed", linewidth = 1
  labs(
   title = "Distribution of Final Account Balances",
   subtitle = paste("100 Simulations,", n_periods, "Periods Each"),
   x = "Final Balance ($)",
   y = "Frequency",
    caption = "Red line shows initial balance ($1,000)"
  scale_x_continuous(labels = scales::dollar_format()) +
  theme_minimal() +
  theme(
    plot.title = element_text(size = 14, face = "bold"),
   plot.subtitle = element_text(size = 12, color = "gray50")
```

Distribution of Final Account Balances

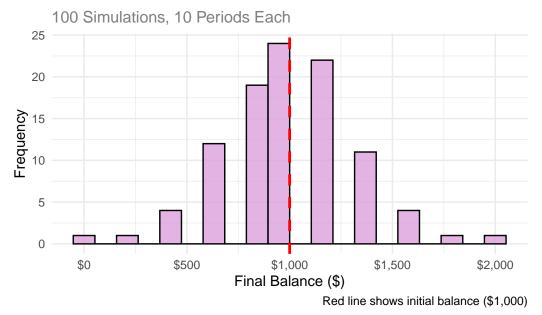


Figure 6: R probability distribution of final balances

```
# Summary statistics
summary_stats <- distribution_data %>%
summarise(
   mean_balance = mean(final_balance),
   median_balance = median(final_balance),
   prob_above_initial = mean(final_balance > initial_balance)
)
print("Summary Statistics:")
```

[1] "Summary Statistics:"

1002

1

0.39

1000

Python

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
# Set seed for reproducibility
np.random.seed(789)
# Parameters
initial balance = 1000
n_{periods} = 10
n_sims = 100 # Multiple simulations
# Simulate multiple paths
def simulate_final_balance(initial, periods):
    balance = initial
    for i in range(periods):
        coin_flip = np.random.binomial(1, 0.5)
        if coin_flip == 1:
            balance = balance + 100 # $100 gain
        else:
            balance = balance - 100 # $100 loss
    return balance
# Run multiple simulations
final_balances = [simulate_final_balance(initial_balance, n_periods) for _ in range(n_sims)]
# Create data frame
distribution_data = pd.DataFrame({
    'sim_num': range(1, n_sims + 1),
    'final_balance': final_balances
})
# Create histogram
fig, ax = plt.subplots(figsize=(10, 6))
ax.hist(distribution_data['final_balance'], bins=20, color='plum', alpha=0.8, edgecolor='bla
ax.axvline(initial_balance, color='red', linestyle='--', linewidth=2, label='Initial Balance
ax.set_title(f'Distribution of Final Account Balances\n100 Simulations, {n_periods} Periods I
             fontsize=14, fontweight='bold')
ax.set_xlabel('Final Balance ($)', fontsize=12)
ax.set_ylabel('Frequency', fontsize=12)
```

```
ax.legend()
ax.grid(True, alpha=0.3)

# Format x-axis as currency
ax.xaxis.set_major_formatter(plt.FuncFormatter(lambda x, p: f'${x:,.0f}'))

plt.tight_layout()
plt.show()
```


Figure 7: Python probability distribution of final balances

Final Balance (\$)

\$1,000

\$1,200

\$1,400

\$1,600

\$800

```
# Summary statistics
mean_balance = distribution_data['final_balance'].mean()
median_balance = distribution_data['final_balance'].median()
prob_above_initial = (distribution_data['final_balance'] > initial_balance).mean()
print("Summary Statistics:")
```

Summary Statistics:

\$200

\$400

\$600

```
print(f"Mean balance: ${mean_balance:,.2f}")
```

Mean balance: \$1,020.00

print(f"Median balance: \${median_balance:,.2f}")

Median balance: \$1,000.00

print(f"Probability above initial: {prob_above_initial:.3f}")

Probability above initial: 0.420