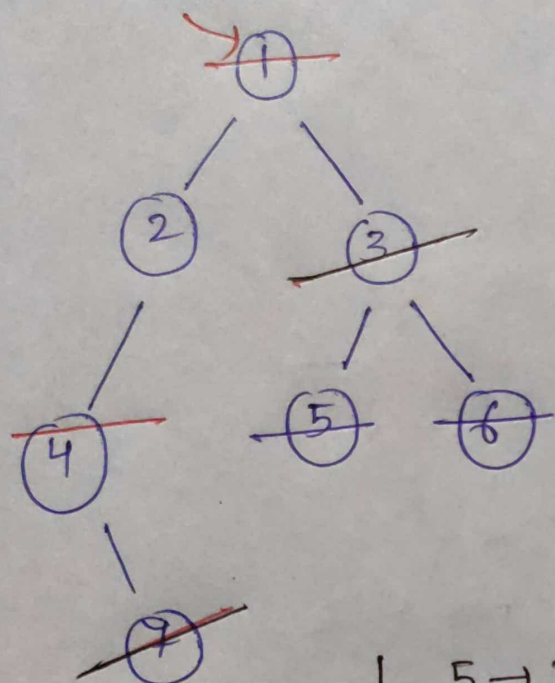


Min Time taken to Burn a Binary Tree from a node / leaf Node.



mode = 2

3 seconds

5 → 3
 2 → 1
 3 → 1
 4 → 2
 6 → 3
 7 → 4

Travel complete.

1
 2
 3
 4
 5
 6
 7

7
 6
 5
 4
 3
 2
 1

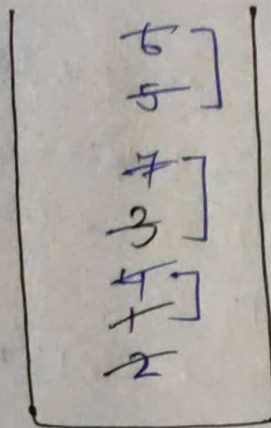
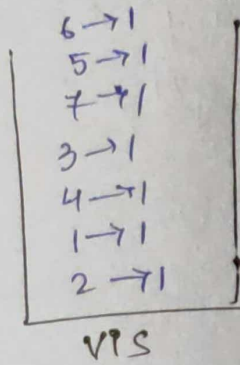
Queue.

Check 1 → left ✓
 → right ✓

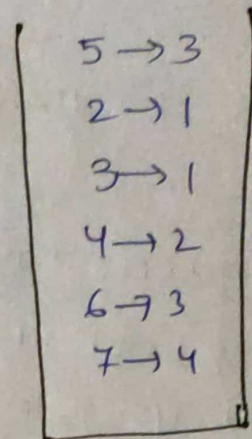
assign 2 → 1
parent

3 → 1
 put left, right in
 queue

time = 0



Queue



Parent Map

start from (node-2) mark as visited in vis ds.

check,

✓ ① mark 1 as visited.
put in queue

2

→ 2 has burnt someone so, update time to 1.

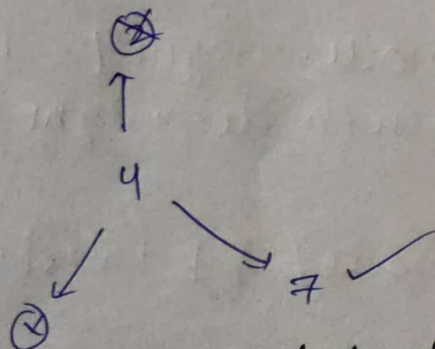
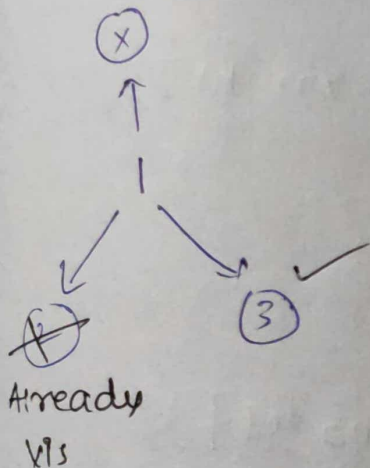
• pop 2 from queue.

check from

4
1

✓ ④ mark as vis, put in queue.

left ✓
right ✓
top ✓
} if exists mark as vis put in queue.



As they have burnt update time to 2.

Similarly, we can check for further iterations.

II Code:-

```
int findMaxDist (map < BinaryTree <int> * > & mpp,  
                BinaryTree <int> * target) {  
    queue < BinaryTree <int> * > q;  
    q.push(target);  
    map < BinaryTree <int> * , int> vis;  
    vis[target] = 1;  
    int maxi = 0;  
    while (!q.empty()) {  
        int sz = q.size();  
        int fl = 0;  
        for (int i = 0; i < sz; i++) {  
            auto node = q.front();  
            q.pop();  
            if (node->left && !vis[node->left]) {  
                fl = 1;  
                vis[node->left] = 1;  
                q.push(node->left);  
            }  
            if (node->right && !vis[node->right]) {  
                fl = 1;  
                vis[node->right] = 1;  
                q.push(node->right);  
            }  
            if (mpp[node] && !vis[mpp[node]]) {  
                fl = 1;  
                vis[mpp[node]] = 1;  
                q.push(mpp[node]);  
            }  
        }  
        if (fl) maxi++;  
    }  
    return maxi;  
}
```

```

BinaryTree <int> * bfsToMapParent (BinaryTree <int> * root,
map < BinaryTree <int> *, BinaryTree <int> * > &mpp,
int start) {

```

```

    queue < BinaryTree <int> * > q;

```

```

    q.push (root);

```

```

    BinaryTree <int> * res;

```

```

    while (! q.empty()) {

```

```

        BinaryTree <int> * node = q.front();

```

```

        if (node->data == start)

```

```

            res = node;    q.pop();

```

```

        if (node->left) mpp[node->left] = node;

```

```

        q.push (node->left);

```

```

        if (node->right) mpp[node->right] = node;

```

```

        q.push (node->right);

```

```

    }

```

```

}

```

```

return res;

```

```

}

```

```

int timeToBurnTree (BinaryTree <int> * root,
int start) {

```

```

    map < BinaryTree <int> *, BinaryTree <int> * >
    mpp;

```

```

    BinaryTree <int> * target = bfsToMapParents (root,
    mpp, start);

```

```

    int maxi = findMax (mpp, target);

```

```

    return maxi;

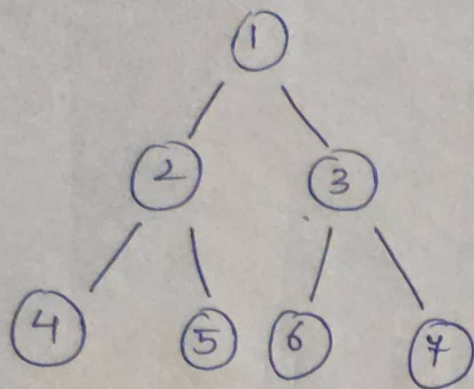
```

```

}

```


II Count Complete Tree Nodes:-



TC: $O(n)$

SC: $O(h)$

(If all levels are filled.)

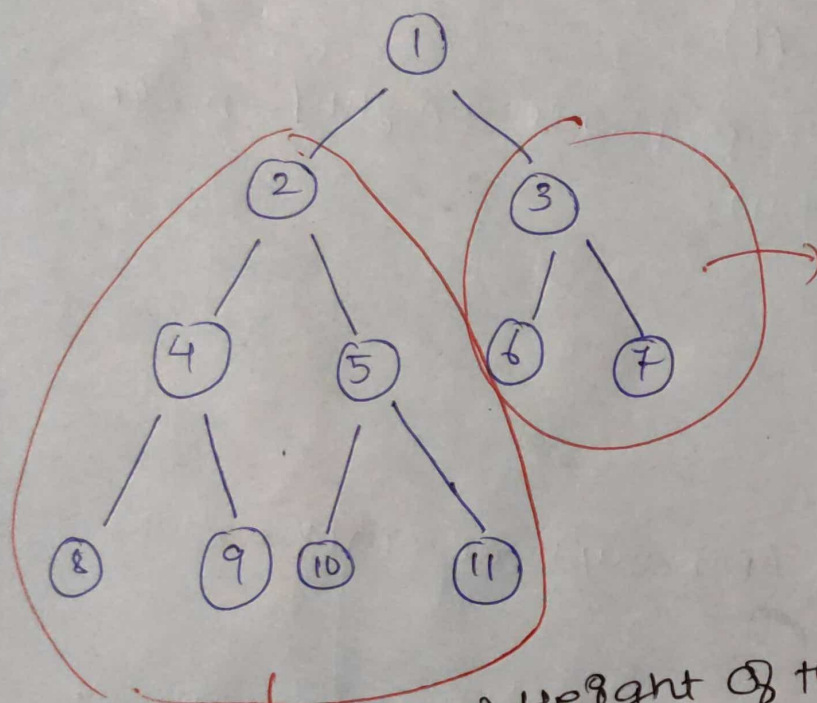
```

inorder (node, &cnt) {
  if (root == NULL)
    return;
  
```

cnt++;

inorder (node → left);

inorder (node → right);



$$1 + 4 + 3 = 11$$

$$2 - 1 = 3$$

Height of the right subtree.

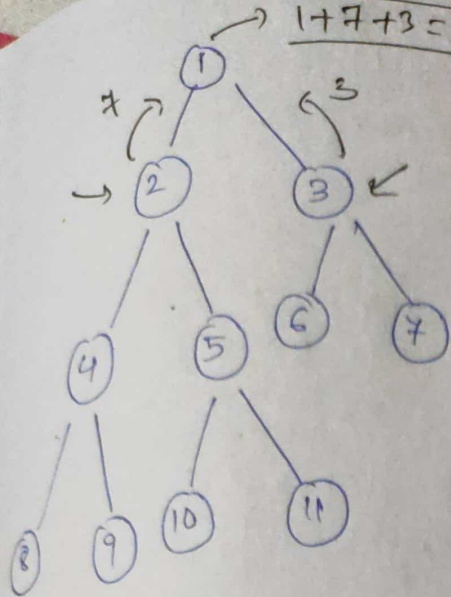
Height of the left subtree

$$3 - 1 = 4$$

$$1 + (\quad) + (\quad)$$

l.h.s

r.h.s



check from node-2

lh=3
rh=3 } both are of same height

that means it's a complete binary tree.

$$2^3 - 1 = 7$$

$$lh = 2$$

$$rh = 2$$

$$2^2 - 1 = 3$$

Code :-

```
int CountNodes(Tree Node *root) {
```

```
    if (root == NULL) return 0;
```

```
    int lh = findHeightLeft(root);
```

```
    int rh = findHeightRight(root);
```

```
    if (lh == rh) return (1 << lh) - 1;
```

```
    return 1 + countNodes(root->left) +  
           countNodes(root->right)
```

```
}
```

```
int findHeightLeft(Tree Node *node) {
```

```
    int height = 0;
```

```
    while (node) {
```

```
        height++;
```

```
        node = node->left;
```

```
    }  
    return height;
```

↓
similarly
for right

$$TC: O((\log N)^2)$$