

H.W.

① Find grad ϕ , if $\phi = \log_e(x^2 + y^2 + z^2)$.

Ans. $\frac{2(x\hat{i} + y\hat{j} + z\hat{k})}{x^2 + y^2 + z^2}$

② Find the directional derivative of

$f = 2xy + z^2$ at $(1, -1, 3)$ in the direction of $\hat{i} + 2\hat{j} + 2\hat{k}$.

Ans. $\frac{14}{3}$

③ Find the directional derivative of

$\phi = 5x^2y - 5y^2z + \frac{5}{2}z^2x$ at $(1, 1, 1)$ in the direction of the line $\frac{x-1}{2} = \frac{y-3}{-2} = \frac{z}{1}$.

Ans. $\frac{35}{3}$

④ Find the directional derivative of ∇^2 where

$\nabla = xy^2\hat{i} + zy^2\hat{j} + xz^2\hat{k}$ at $(2, 0, 3)$ in the direction of the outward normal to the sphere $x^2 + y^2 + z^2 = 14$ at $(3, 2, 1)$.

Ans. $\frac{1404}{\sqrt{14}}$

[Note: $\nabla^2 = \nabla \cdot \nabla$]