

BNF, the standard form

(* the start symbol: E; Follow(E) = { \$ } initially. *)

(* ε , the empty string; First(ε) = { ε } initially. *)

(* Terminal: { +, *, (, id }; First(+) = { + }, ... , initially. *)

(* NT: { E, E', T, T', F }; First: LHS, Follow: RHS. *)

$E \rightarrow TE'$

$E' \rightarrow +TE'$

$E' \rightarrow \varepsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT'$

$T' \rightarrow \varepsilon$

$F \rightarrow (E)$

$F \rightarrow \text{id}$

(* How ? Do ... until no change ! *)

(1)-(a) (* $A \rightarrow B$, $B \rightarrow C$, $C \rightarrow t$, First(A)=First(B)=First(C)=First(t)={t} *)

FIRST(E) = FIRST(T) = FIRST(F) = { (, id }

FIRST(E') = { +, ε }

FIRST(T') = { *, ε }

(1)-(b)

FOLLOW(E) = { \$ } \cup {) } = {) , \$ }

FOLLOW(E') = FOLLOW(E) = {) , \$ }

FOLLOW(T) = FIRST(E') = { +, ε } = { +, ε } - { ε } \cup FOLLOW(E)
= { + } \cup {) , \$ } = { +,) , \$ }

FOLLOW(T') = FOLLOW(T) = { +,) , \$ }

FOLLOW(F) = FIRST(T') = { *, ε } = { * ε } - { ε } \cup FOLLOW(T)
= { * } \cup { +,) , \$ } = { +, *,) , \$ }

(2)-(a) (* $A \rightarrow B$, $B \rightarrow C$, $C \rightarrow t$, First(t)=t, First(C) = First(t)={t},

First(B)=First(C), First(A)=First(B) *)

FIRST(F) = { (, id }

FIRST(T) = FIRST(F) = { (, id }

FIRST(E) = FIRST(T) = FIRST(F) = { (, id }

FIRST(E') = { +, ε }

FIRST(T') = { *, ε }

2-(b) the same as 1-(b).

(3)-(a)+(b) (* First, Follow, at the same time ! *)

Then, the predictive set for each production rule.

$\text{Predict}(A \rightarrow X_1 \cdots X_m) =$
 if $\lambda \in \text{First}(X_1 \cdots X_m)$
 $(\text{First}(X_1 \cdots X_m) - \lambda) \cup \text{Follow}(A)$
 else
 $(\text{First}(X_1 \cdots X_m))$

$E \rightarrow TE'$	$\text{PS}(E \rightarrow TE') = \text{FIRST}(TE') = \{ (, id \}$
$E' \rightarrow +TE'$	$\text{PS}(E' \rightarrow +TE') = \text{FIRST}\{ + TE' \} = \{ + \} !!$
$E' \rightarrow \varepsilon$	$\text{PS}(E' \rightarrow \varepsilon) = \text{FOLLOW}(E') = \{), \$ \} !!$
$T \rightarrow FT'$	$\text{PS}(T \rightarrow FT') = \text{FIRST}(FT') = \{ (, id \}$
$T' \rightarrow *FT'$	$\text{PS}(T' \rightarrow *FT') = \text{FIRST}(*FT') = \{ * \} !!!$
$T' \rightarrow \varepsilon$	$\text{PS}(T' \rightarrow \varepsilon) = \text{FOLLOW}(T') = \{ +,), \$ \} !!!$
$F \rightarrow (E)$	$\text{PS}(F \rightarrow (E)) = \text{FIRST}((E)) = \{ (\} !!!!$
$F \rightarrow id$	$\text{PS}(F \rightarrow id) = \text{FIRST}(id) = \{ id \} !!!!$

Finally, the parsing table based on the predictive set for each rule.

For each production $A \rightarrow \alpha$ of the grammar

For each terminal a in $\text{FIRST}(\alpha)$, add $A \rightarrow \alpha$ to $M[A, a]$.

If ε is in $\text{FIRST}(\alpha)$, add $A \rightarrow \alpha$ to $M[A, b]$ for each terminal b in $\text{FOLLOW}(A)$.

If ε is in $\text{FIRST}(\alpha)$ and $\$$ is in $\text{FOLLOW}(A)$, add $A \rightarrow \alpha$ to $M[A, \$]$.

LL(1) ??

LL(1) contains exactly those grammars that have disjoint predict sets for productions that share a common left-hand side