

# DnA: Homework 4

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## Part One

1)

a)  $R = ABC$

i) The functional dependencies are :

- $AB \rightarrow C$
- $BC \rightarrow A$
- $AC \rightarrow B$

This is a minimal cover already.

ii) Since  $AB$ ,  $BC$  and  $AC$  are all candidate keys for  $R$ , it is in BCNF form.

Hence the strongest normal form not violating these attributes is BCNF

iii) No conversion as it is already in BCNF.

b)  $R = ABCD$

i) The functional dependencies are :

- $B \rightarrow D$
- $AB \rightarrow C$
- $BC \rightarrow A$
- $AC \rightarrow B$

This is a minimal cover already.

ii)  $R$  is not in BCNF, 3NF or 2NF as there exists a partial dependency

$B \rightarrow D$  since  $B$  is a subset of candidate key  $AB$ . Hence strongest normal not violating these attributes in 1NF.

iii) BCNF Decomposition - Decompose into 2 relations  $R_1$  and  $R_2$  :

- $R_1 = ABC$
- $R_2 = BD$

c)  $R = ABCEG$

i) The functional dependencies are :

- $E \rightarrow G$
- $AB \rightarrow C$
- $BC \rightarrow A$
- $AC \rightarrow B$

This is a minimal cover already.

ii) R is not in BCNF, 3NF or 2NF as there exists a partial dependency  $E \rightarrow G$  since E is a subset of candidate key ABE. Hence strongest normal form not violating these attributes is 1NF.

iii) BCNF Decomposition - Decompose into 3 relations R1, R2 and R3 :

- $R1 = ABC$
- $R2 = ABE$
- $R3 = EG$

d)  $R = DCEGH$

i) The functional dependencies are :

- $E \rightarrow G$

This is a minimal cover already.

ii) R is not in BCNF, 3NF or 2NF as there exists a partial dependency  $E \rightarrow G$  since E is a subset of candidate key DCEH. Hence the strongest normal form not violating these attributes is 1NF.

iii) BCNF Decomposition - Decompose into 2 relations R1 and R2 :

- $R1 = DCEH$
- $R2 = EG$

e)  $R = ACEH$

i) The relation does not have any functional dependencies.

This is a minimal cover already.

ii) Since there are no valid FDs, the only candidate key is ACEH itself and it is already in BCNF form. Hence the strongest normal form not violating these attributes is BCNF

iii) No conversion as it is already in BCNF form.

2)

a) The decomposition is not dependency preserving : The functional dependencies,  $AB \rightarrow C$ ,  $AC \rightarrow B$  and  $BC \rightarrow A$  are not preserved.

The decomposition is not lossless join.

b) The decomposition is not dependency preserving : The functional dependencies,  $B \rightarrow D$  and  $E \rightarrow G$  are not preserved.

The decomposition is lossless join : If we first join ABC and ACDE it is lossless as their intersection AC is a key of ABCDE. Now if we join ABCDE with ADG it is lossless as their intersection is AD and AD  $\rightarrow$  ADG.

## Part Two

Table : PURCHASES

<u>Customer_ID</u>	<u>Order_ID</u>	<u>Product_ID</u>	Cust_Name	Product_Name	Phn_Nos	Day	Discount
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Convert the relational table to a) 1NF b) 2NF c) 3NF

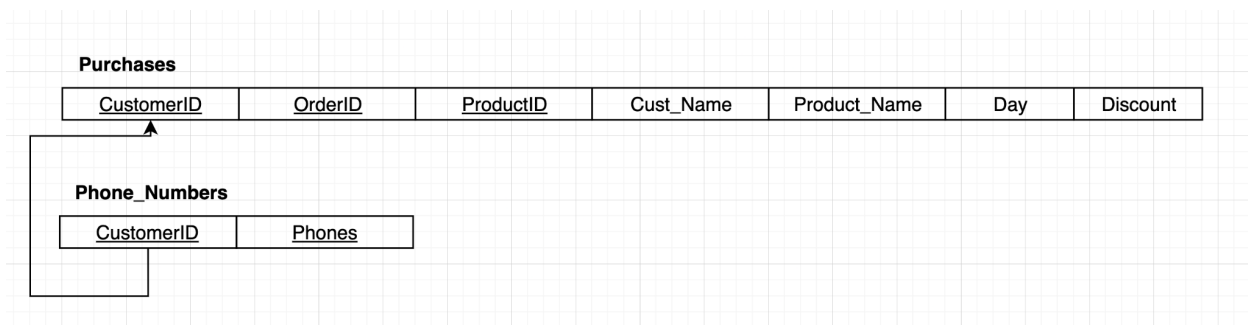
Information about the table :

1. Composite Key is Customer\_ID + Order\_ID + Product\_ID
2. Phn\_Nos is a multi-valued attribute.
3. Day  $\rightarrow$  Discount
4. Customer\_ID  $\rightarrow$  Cust\_Name
5. Product\_ID  $\rightarrow$  Product\_Name
6. Order\_ID  $\rightarrow$  Day

### Table after 1NF:

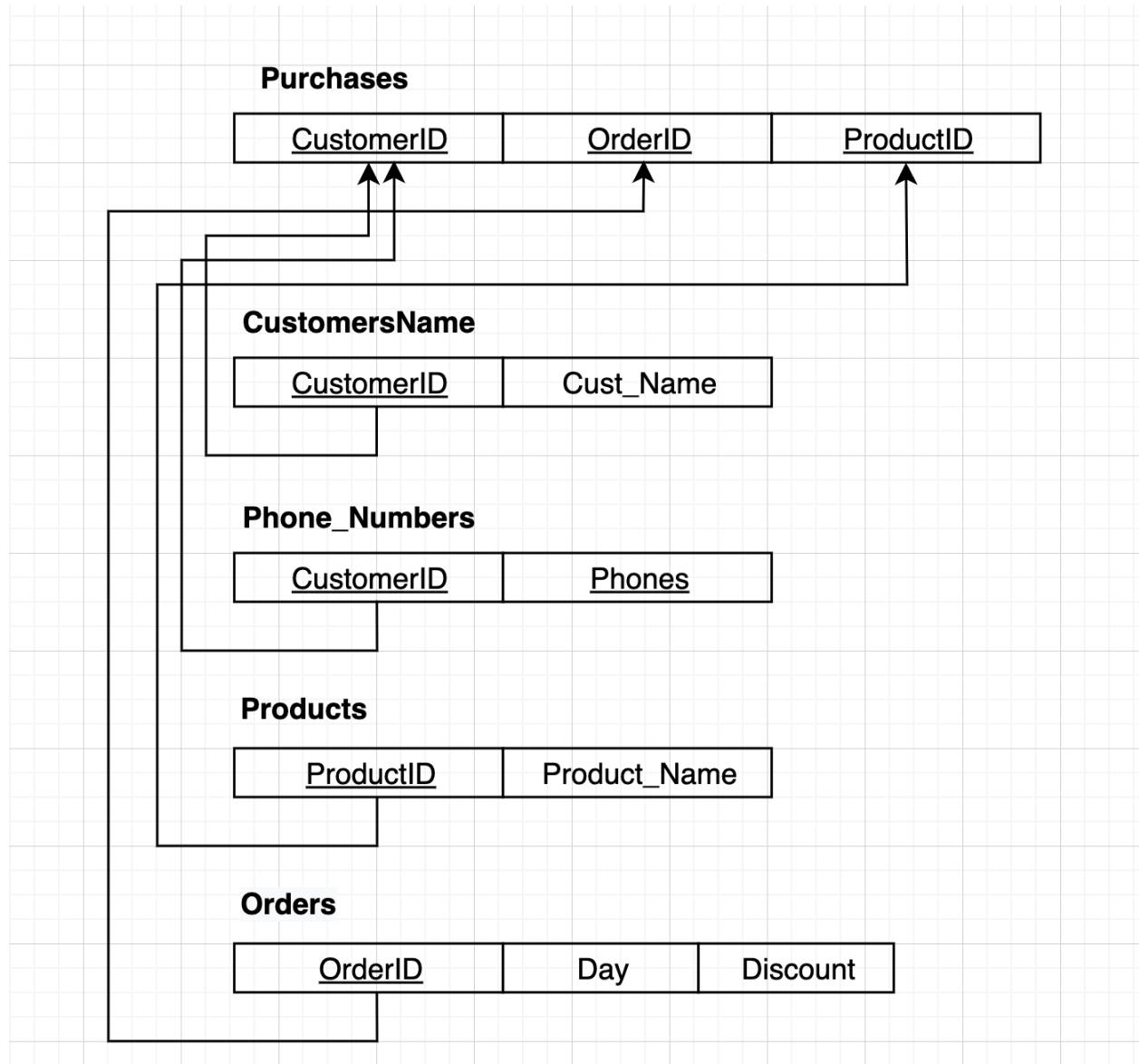
Made a separate relation. The primary key of this is the customerID combined with Phones.

CustomerID is included because Phones is functionally dependent on it.



### Table after 2NF:

Made three more relations CustomersName, Products, and Orders. These are formed since Cust\_Name is dependent on CustomerID, Product Name is dependent on ProductID, and Day is dependent on OrderID while Discount is dependent on Day.



### Table after 3NF:

Made one more relation DiscountA since Orders showed transitive behaviour. Day is dependent on OrderID while Discount is dependent on Day. Orders was also modified.

